

## CODE

## COMMENTARY

**Table 22.7.4.1(a)—Threshold torsion for solid cross sections**

Type of member	$T_{th}$	
Nonprestressed member	$0.083 \lambda \sqrt{f'_c} \left( \frac{A_{cp}^2}{p_{cp}} \right)$	(a)
Prestressed member	$0.083 \lambda \sqrt{f'_c} \left( \frac{A_{cp}^2}{p_{cp}} \right) \sqrt{1 + \frac{f_{pc}}{0.33 \lambda \sqrt{f'_c}}}$	(b)
Nonprestressed member subjected to axial force	$0.083 \lambda \sqrt{f'_c} \left( \frac{A_{cp}^2}{p_{cp}} \right) \sqrt{1 + \frac{N_u}{0.33 A_g \lambda \sqrt{f'_c}}}$	(c)

**Table 22.7.4.1(b)—Threshold torsion for hollow cross sections**

Type of member	$T_{th}$	
Nonprestressed member	$0.083 \lambda \sqrt{f'_c} \left( \frac{A_g^2}{p_{cp}} \right)$	(a)
Prestressed member	$0.083 \lambda \sqrt{f'_c} \left( \frac{A_g^2}{p_{cp}} \right) \sqrt{1 + \frac{f_{pc}}{0.33 \lambda \sqrt{f'_c}}}$	(b)
Nonprestressed member subjected to axial force	$0.083 \lambda \sqrt{f'_c} \left( \frac{A_g^2}{p_{cp}} \right) \sqrt{1 + \frac{N_u}{0.33 A_g \lambda \sqrt{f'_c}}}$	(c)

**22.7.5 Cracking torsion**

**22.7.5.1** Cracking torsion  $T_{cr}$  shall be calculated in accordance with Table 22.7.5.1 for solid and hollow cross sections, where  $N_u$  is positive for compression and negative for tension.

**Table 22.7.5.1—Cracking torsion**

Type of member	$T_{cr}$	
Nonprestressed member	$0.33 \lambda \sqrt{f'_c} \left( \frac{A_{cp}^2}{p_{cp}} \right)$	(a)
Prestressed member	$0.33 \lambda \sqrt{f'_c} \left( \frac{A_{cp}^2}{p_{cp}} \right) \sqrt{1 + \frac{f_{pc}}{0.33 \lambda \sqrt{f'_c}}}$	(b)
Nonprestressed member subjected to axial force	$0.33 \lambda \sqrt{f'_c} \left( \frac{A_{cp}^2}{p_{cp}} \right) \sqrt{1 + \frac{N_u}{0.33 A_g \lambda \sqrt{f'_c}}}$	(c)

sections with large voids. For a straight-line interaction, a torsional moment of  $T_{th}$  would cause a reduction in the inclined cracking shear of approximately 25 percent, which was considered to be significant. Therefore, the expressions for solid sections are modified by the factor  $(A_g/A_{cp})^2$  to develop the expressions for hollow sections. Tests of solid and hollow beams (Hsu 1968) indicate that the cracking torsional moment of a hollow section is approximately  $(A_g/A_{cp})$  times the cracking torsional moment of a solid section with the same outside dimensions. An additional multiplier of  $(A_g/A_{cp})$  reflects the transition from the circular interaction between the inclined cracking loads in shear and torsion for solid members, to the approximately linear interaction for thin-walled hollow sections.

**R22.7.5 Cracking torsion**

The cracking torsional moment under pure torsion,  $T_{cr}$ , is derived by replacing the actual section with an equivalent thin-walled tube with a wall thickness  $t$  prior to cracking of  $0.75 A_{cp}/p_{cp}$  and an area enclosed by the wall centerline  $A_o$  equal to  $2 A_{cp}/3$ . Cracking is assumed to occur when the principal tensile stress reaches  $0.33 \lambda \sqrt{f'_c}$ . The stress at cracking,  $0.33 \lambda \sqrt{f'_c}$ , has purposely been taken as a lower bound value. In a nonprestressed beam loaded with torsion alone, the principal tensile stress is equated to the torsional shear stress,  $\tau = T/(2 A_o t)$ . Thus, cracking occurs when  $\tau$  reaches  $0.33 \lambda \sqrt{f'_c}$ , giving the cracking torsional moment  $T_{cr}$  as defined by expression (a) in Table 22.7.5.1.

For prestressed members, the torsional cracking load is increased by the prestress given by expression (b) in Table 22.7.5.1. A Mohr's Circle analysis based on average stresses indicates the torsional moment required to cause a principal tensile stress equal to  $0.33 \lambda \sqrt{f'_c}$  is  $\sqrt{1 + f_{pc}/(0.33 \lambda \sqrt{f'_c})}$  times the corresponding torsional cracking moment in a nonprestressed beam. A similar modification is made in expression (c) in Table 22.7.5.1 for members subjected to axial force and torsion.

If the factored torsional moment exceeds  $\phi T_{cr}$  in a statically indeterminate structure, a maximum factored torsional moment equal to  $\phi T_{cr}$  may be assumed to occur at critical sections near the faces of the supports. This limit has been