

## CODE

where  $\beta_{dns}$  shall be the ratio of maximum factored sustained axial load to maximum factored axial load associated with the same load combination and  $I$  in Eq. (6.6.4.4c) is calculated according to Table 6.6.3.1.1(b) for columns and walls.

**6.6.4.5 Moment magnification method: Nonsway frames**

**6.6.4.5.1** The factored moment used for design of columns and walls,  $M_c$ , shall be the first-order factored moment  $M_2$  amplified for the effects of member curvature.

$$M_c = \delta M_2 \quad (6.6.4.5.1)$$

**6.6.4.5.2** Magnification factor  $\delta$  shall be calculated by:

$$\delta = \frac{C_m}{1 - \frac{P_u}{0.75P_c}} \geq 1.0 \quad (6.6.4.5.2)$$

**6.6.4.5.3**  $C_m$  shall be in accordance with (a) or (b):

(a) For columns without transverse loads applied between supports

$$C_m = 0.6 - 0.4 \frac{M_1}{M_2} \quad (6.6.4.5.3a)$$

where  $M_1/M_2$  is negative if the column is bent in single curvature, and positive if bent in double curvature.  $M_1$  corresponds to the end moment with the lesser absolute value.

(b) For columns with transverse loads applied between supports.

$$C_m = 1.0 \quad (6.6.4.5.3b)$$

## COMMENTARY

simplification, it can be assumed that  $\beta_{dns} = 0.6$ . In this case, Eq. (6.6.4.4a) becomes  $(EI)_{eff} = 0.25E_cI_g$ .

In reinforced concrete columns subject to sustained loads, creep transfers some of the load from the concrete to the longitudinal reinforcement, increasing the reinforcement stresses. In the case of lightly reinforced columns, this load transfer may cause the compression reinforcement to yield prematurely, resulting in a loss in the effective  $EI$ . Accordingly, both the concrete and longitudinal reinforcement terms in Eq. (6.6.4.4b) are reduced to account for creep.

**R6.6.4.5 Moment magnification method: Nonsway frames**

**R6.6.4.5.2** The 0.75 factor in Eq. (6.6.4.5.2) is the stiffness reduction factor  $\phi_K$ , which is based on the probability of understrength of a single isolated slender column. Studies reported in Mirza et al. (1987) indicate that the stiffness reduction factor  $\phi_K$  and the cross-sectional strength reduction  $\phi$  factors do not have the same values. These studies suggest the stiffness reduction factor  $\phi_K$  for an isolated column should be 0.75 for both tied and spiral columns. In the case of a multistory frame, the column and frame deflections depend on the average concrete strength, which is higher than the strength of the concrete in the critical single understrength column. For this reason, the value of  $\phi_K$  implicit in  $I$  values in 6.6.3.1.1 is 0.875.

**R6.6.4.5.3** The factor  $C_m$  is a correction factor relating the actual moment diagram to an equivalent uniform moment diagram. The derivation of the moment magnifier assumes that the maximum moment is at or near midheight of the column. If the maximum moment occurs at one end of the column, design should be based on an equivalent uniform moment  $C_m M_2$  that leads to the same maximum moment at or near midheight of the column when magnified (MacGregor et al. 1970).

The sign convention for  $M_1/M_2$  has been updated to follow the right hand rule convention; hence,  $M_1/M_2$  is negative if bent in single curvature and positive if bent in double curvature. This reflects a sign convention change from the 2011 Code.

In the case of columns that are subjected to transverse loading between supports, it is possible that the maximum moment will occur at a section away from the end of the member. If this occurs, the value of the largest calculated moment occurring anywhere along the member should be used for the value of  $M_2$  in Eq. (6.6.4.5.1).  $C_m$  is to be taken as 1.0 for this case.