$$1. \int u \, \mathrm{d}v = uv - \int v \, \mathrm{d}u$$

**2.** 
$$\int u^n du = \frac{u^{n+1}}{n+1} + C, \quad n \neq -1$$

$$3. \int \frac{1}{u} \, \mathrm{d}u = \ln|u| + C$$

$$4. \int e^u \, \mathrm{d} u = e^u + C$$

$$5. \int a^u \, \mathrm{d}u = \frac{a^u}{\ln a} + C$$

$$\mathbf{6.} \int \sin u \, \mathrm{d}u = -\cos u + C$$

7. 
$$\int \cos u \, \mathrm{d}u = \sin u + C$$

8. 
$$\int \sec^2 u \, \mathrm{d}u = \tan u + C$$

$$9. \int \csc^2 u \, \mathrm{d}u = -\cot u + C$$

$$\mathbf{10.} \quad \int \sec u \tan u \, \mathrm{d}u = \sec u + C$$

11. 
$$\int \csc u \cot u \, du = -\csc u + C$$

$$103. \int \sinh u \, \mathrm{d}u = \cosh u + C$$

$$104. \int \cosh u \, \mathrm{d}u = \sinh u + C$$

$$I_{12} = \int \tan u \, du$$

$$= \int \frac{\sin u}{\cos u} \, du$$
Let  $v = \cos u \longrightarrow dv = -\sin u \, du \longrightarrow -dv = \sin u \, du$ 

$$= -\int \frac{1}{v} \, dv$$

$$= -\ln|v| + C$$
Reverse the substitution

 $=-\ln|\cos u|+C$ 

$$I_{13} = \int \cot u \, du$$
$$= \int \frac{\cos u}{\sin u} \, du$$

Let  $v = \sin u \longrightarrow dv = \cos u du$ 

$$= \int \frac{1}{\nu} \, \mathrm{d}\nu$$
$$= \ln|\nu| + C$$

$$=\ln|\sin u|+C$$

$$I_{14} = \int \sec u \, du$$

$$= \int \sec u \cdot \frac{\sec u + \tan u}{\sec u + \tan u} \, du$$

$$= \int \frac{\sec^2 u + \sec u \cdot \tan u}{\sec u + \tan u} \, du$$

Let  $v = \sec u + \tan u \longrightarrow dv = \sec^2 u + \sec u \tan u du$ 

$$= \int \frac{\mathrm{d}v}{v}$$
$$= \ln|v| + C$$

$$=\ln|\sec u + \tan u| + C$$

$$\begin{split} I_{15} &= \int \csc u \, \mathrm{d}u \\ &= \int \csc u \cdot \frac{\csc u - \cot u}{\csc u - \cot u} \, \mathrm{d}u \\ &= \int \frac{\csc^2 u - \csc u \cdot \cot u}{\csc u - \cot u} \, \mathrm{d}u \end{split}$$

Let  $v = \csc u - \cot u \longrightarrow dv = \csc^2 u - \csc u \cot u du$ 

$$= \int \frac{\mathrm{d}v}{v}$$
$$= \ln|v| + C$$

$$=\ln|\csc u - \cot u| + C$$

$$I_{16} = \int \frac{1}{\sqrt{a^2 - u^2}} du$$
Let  $\sin \theta = \frac{u}{a}$ ,  $\cos \theta = \frac{\sqrt{a^2 - u^2}}{a}$   $\longrightarrow \tan \theta = \frac{u}{\sqrt{a^2 - u^2}}$  and so  $u = a \sin \theta$   $\longrightarrow du = a \cos \theta d\theta$  
$$= \int \frac{a \cos \theta}{a \cos \theta} d\theta$$
$$= \int 1 d\theta$$
$$= \theta + C$$

Reverse the substitution of u, where  $\sin \theta = \frac{u}{a} \longrightarrow \theta = \arcsin \frac{u}{a}$   $= \arcsin \frac{u}{a} + C$ 

$$\int \frac{1}{\sqrt{a^2 - u^2}} \, \mathrm{d}u = \arcsin \frac{u}{a} + C$$

$$I_{17} = \int \frac{1}{a^2 + u^2} du$$

$$\text{Let} v = \frac{u}{a} \longrightarrow av = u \longrightarrow a dv = du$$

$$= \int \frac{a}{a^2 + (av)^2} dv$$

$$= \int \frac{a}{a^2 (1 + v^2)} dv$$

$$= \frac{1}{a} \int \frac{1}{1 + v^2} dv$$

$$= \frac{1}{a} \arctan v$$

$$=\frac{1}{a}\arctan\frac{u}{a}+C$$

$$\int \frac{1}{a^2 + u^2} \, \mathrm{d}u = \frac{1}{a} \arctan \frac{u}{a} + C$$

$$I_{18} = \int \frac{1}{u\sqrt{u^2 - a^2}} \, \mathrm{d}u$$

Let 
$$\sin \theta = \frac{\sqrt{u^2 - a^2}}{u}$$
,  $\cos \theta = \frac{a}{u}$   $\longrightarrow \tan \theta = \frac{\sqrt{u^2 - a^2}}{a}$   $u$   $\theta$  and so  $u = a \sec \theta$   $\longrightarrow$   $du = a \sec \theta \tan \theta d\theta$   $\sqrt{u^2 - a^2}$ 

and 
$$\sqrt{u^2 - a^2} = a \tan \theta$$

$$I_{18} = \int \frac{a \sec \theta \tan \theta}{a \sec \theta \cdot a \tan \theta} d\theta$$
$$= \int \frac{1}{a} d\theta$$
$$= \frac{1}{a} \theta + C$$

Reverse the substitution, where  $u = a \sec \theta \longrightarrow \theta = \operatorname{arcsec} \frac{u}{a}$ 

$$=\frac{1}{a}\operatorname{arcsec}\frac{u}{a}+C$$

$$\int \frac{1}{u\sqrt{u^2-a^2}} du = \frac{1}{a} \operatorname{arcsec} \frac{u}{a} + C$$

$$I_{19} = \int \frac{1}{a^2 - u^2} du$$
$$= \int \frac{A}{a + u} + \frac{B}{a - u} du$$

Where 
$$A(a-u) + B(a+u) = 1$$
  $\longrightarrow$   $A+B = \frac{1}{a}$  and  $B-A=0$   
 $\longrightarrow$   $B=A$   $\longrightarrow$   $2A = \frac{1}{a}$   $\longrightarrow$   $A = \frac{1}{2a}$   $\longrightarrow$   $B = \frac{1}{2a}$   

$$= \int \frac{\frac{1}{2a}}{a+u} + \frac{\frac{-1}{2a}}{a-u} du$$

$$= \frac{1}{2a} \cdot \int \frac{1}{a+u} + \frac{1}{a-u} du$$

Rearranging so u preceeds a for aesthetic reasons

$$= \frac{1}{2a} \cdot \int \frac{1}{u+a} - \frac{1}{u-a} du$$

$$= \frac{1}{2a} \left( \ln|u+a| - \ln|u-a| \right) + C$$

$$= \frac{1}{2a} \cdot \ln\left| \frac{u+a}{u-a} \right| + C$$

$$\int \frac{1}{a^2 - u^2} du = \frac{1}{2a} \ln \left| \frac{u + a}{u - a} \right| + C$$

$$I_{20} = \int \frac{1}{u^2 - a^2} du$$
$$= \int \frac{A}{u - a} + \frac{B}{u + a} du$$

Where 
$$A(u+a) + B(u-a) = 1$$
  $\longrightarrow$   $A+B=0$  and  $A-B=\frac{1}{a}$   $\longrightarrow$   $B=-A$   $\longrightarrow$   $2A=\frac{1}{a}$   $\longrightarrow$   $A=\frac{1}{2a}$   $\longrightarrow$   $B=-\frac{1}{2a}$ 

$$= \int \frac{\frac{1}{2a}}{u-a} + \frac{-\frac{1}{2a}}{u+a} du$$

$$= \frac{1}{2a} \cdot \int \frac{1}{u-a} - \frac{1}{u+a} du$$

$$= \frac{1}{2a} \left( \ln|u-a| - \ln|u+a| + C \right)$$

$$= \frac{1}{2a} \cdot \ln\left| \frac{u-a}{u+a} \right| + C$$

$$\int \frac{1}{u^2 - a^2} \, \mathrm{d}u = \frac{1}{2a} \ln \left| \frac{u - a}{u + a} \right| + C$$

$$I_{21} = \int \sqrt{a^2 + u^2} \, du$$
Let  $\sin \theta = \frac{u}{\sqrt{a^2 + u^2}}$ ,  $\cos \theta = \frac{a}{\sqrt{a^2 + u^2}}$   $\longrightarrow \tan \theta = \frac{u}{a}$  and so  $u = a \tan \theta$   $\longrightarrow du = a \sec \theta \tan \theta \, d\theta$  and  $\sqrt{u^2 + a^2} = a \sec \theta$ 

$$= a \sec \theta \, a \sec^2 \theta \, d\theta$$

$$= a^2 \int \sec^3 \theta \, d\theta$$
Apply integal identity  $(71)$ :
$$\int \sec^3 u \, du = \frac{1}{2} \sec u \tan u + \frac{1}{2} \ln|\sec u + \tan u| + C$$

$$= a^2 \left( \frac{1}{2} \sec \theta + \tan \theta + \frac{1}{2} \ln|\sec \theta| + \tan \theta \right) + C \right)$$

$$\int \sec^3 u \, du = \frac{1}{2} \sec u \tan u + \frac{1}{2} \ln|\sec u + \tan u| + C$$

$$= a^2 \left( \frac{1}{2} \sec \theta \tan \theta + \frac{1}{2} \ln|\sec \theta + \tan \theta| + C \right)$$

$$= \frac{a^2}{2} \frac{\sqrt{u^2 + a^2}}{a} \cdot \frac{u}{a} + \frac{a^2}{2} \ln \left| \frac{\sqrt{u^2 + a^2}}{a} + \frac{u}{a} \right| + C$$

$$= \frac{u}{2} \sqrt{u^2 + a^2} + \frac{a^2}{2} \ln \left| \frac{u + \sqrt{u^2 + a^2}}{a} \right| + C$$

$$= \frac{u}{2} \sqrt{u^2 + a^2} + \frac{a^2}{2} \ln \left| u + \sqrt{u^2 + a^2} \right| - \frac{a^2}{2} \ln|a| + C$$

$$= \frac{u}{2} \sqrt{u^2 + a^2} + \frac{a^2}{2} \ln \left| u + \sqrt{u^2 + a^2} \right| + C$$

(21) 
$$\int \sqrt{a^2 + u^2} \, du = \frac{u}{2} \sqrt{u^2 + a^2} + \frac{a^2}{2} \ln \left| u + \sqrt{u^2 - a^2} \right| + C$$

$$\begin{split} I_{63} &= \int \sin^2 u \, \mathrm{d}u \\ &= \int \frac{1 - \cos 2u}{2} \, \mathrm{d}u \\ &= \frac{1}{2} \cdot \int 1 - \cos 2u \, \mathrm{d}u \\ &= \frac{1}{2} \cdot \left( u - \frac{1}{2} \sin 2u \right) + C \\ &= \frac{1}{2} u - \frac{1}{4} \sin 2u + C \end{split}$$

$$I_{64} = \int \cos^2 u \, du$$

$$= \int \frac{1 + \cos 2u}{2} \, du$$

$$= \frac{1}{2} \cdot \int 1 + \cos 2u \, du$$

$$= \frac{1}{2} \cdot \left( u + \frac{1}{2} \sin 2u \right) + C$$

$$= \frac{1}{2}u + \frac{1}{4} \sin 2u + C$$

$$I_{65} = \int \tan^2 u \, \mathrm{d}u$$

Rewrite using trigonometric identity  $\tan^2 u = \sec^2 u - 1$ 

$$= \int \sec^2 u - 1 \, \mathrm{d}u$$
$$= \tan u - u + C$$

$$I_{66} = \int \cot^2 u \, \mathrm{d}u$$

Rewrite using trigonometric identity  $\tan^2 u = \csc^2 u - 1$ 

$$= \int \csc^2 u - 1 \, \mathrm{d}u$$
$$= -\cot u - u + C$$

$$\int \cot^2 u \, du = -\cot u - u + C$$

$$I_{67} = \int \sin^3 u \, du$$

$$= \int (1 - \cos^2 u) \sin u \, du$$

$$= \int \sin u \, du - \int \cos^2 u \sin u \, du$$

Let  $v = \cos u \longrightarrow dv = -\sin u \, du$ 

$$= \int v^2 dv - \cos u$$
$$= \frac{1}{3}v^3 - \cos u + C$$

Reverse the substitution

$$= \frac{1}{3}\cos^3 u - \cos u + C$$

(which we could leave right there)

$$= \left(\frac{1}{3}\cos^2 u - 1\right)\cos u + C$$

$$= \left(\frac{1}{3}(1 - \sin^2 u) - 1\right)\cos u + C$$

$$= -\frac{1}{3}(2 + \sin^2 u)\cos u + C$$

$$I_{68} = \int \cos^3 u \, du$$

$$= \int (1 - \sin^2 u) \cos u \, du$$

$$= \int \cos u \, du - \int \sin^2 u \cos u \, du$$

$$\text{Let } v = \sin u \longrightarrow dv = \cos u \, du$$

$$= \sin u - \int v^2 \, dv$$

Reverse the substitution

$$=\sin u - \frac{1}{3}\sin^3 u + C$$

 $=\sin u - \frac{1}{2}v^3 + C$ 

(which we could leave right there)

$$= \left(1 - \frac{1}{3}\sin^2 u\right)\sin u + C$$

$$= \left(1 - \frac{1}{3}(1 - \cos^2 u)\right)\sin u + C$$

$$= \frac{1}{3}\left(2 + \cos^2 u\right)\sin u + C$$

$$\int \cos^3 u \, du = \frac{1}{3} (2 + \cos^2 u) \sin u + C$$

$$I_{69} = \int \tan^3 u \, du$$

$$= \int (\sec^2 u - 1) \tan u \, du$$

$$= \int (\sec^2 u \tan u) \, du - \int \tan u \, du$$

$$\text{Let } v = \tan u \longrightarrow dv = \sec^2 u \, du$$

$$= \int v \, dv - \ln|\sec u|$$

$$= \frac{1}{2}v^2 - \ln|\sec u| + C$$

$$\text{Reverse the substitution}$$

$$= \frac{1}{2} \tan^2 u - \ln|\sec u| + C$$

(which we could leave right there)

 $= \frac{1}{2} \tan^2 u + \ln|\cos u| + C$ 

$$\int \tan^3 u \, du = \frac{1}{2} \tan^2 u + \ln|\cos u| + C$$

$$I_{70} = \int \cot^3 u \, du$$

$$= \int (\csc^2 u - 1) \cot u \, du$$

$$= \int (\csc^2 u \cot u) \, du - \int \cot u \, du$$

$$\text{Let } v = \cot u \longrightarrow dv = -\csc^2 u \, du$$

$$= -\int v \, dv - \ln|\sin u|$$

$$= -\frac{1}{2}v^2 - \ln|\sin u| + C$$
Reverse the substitution
$$= -\frac{1}{2}\cot^2 u - \ln|\sin u| + C$$
(which we could leave right there)

 $= -\frac{1}{2}\cot^2 u - \ln|\sin u| + C$ 

$$\int \cot^3 u \, du = -\frac{1}{2} \cot^2 u - \ln|\sin u| + C$$

$$I_{71} = \int \sec^3 u \, du$$

$$Integrate \text{ by parts} \begin{cases} (\sec u)' = \sec u \tan u \\ \sec^2 u = (\tan u)' \end{cases}$$

$$= (\sec u)(\tan u) - \int (\sec u \tan u)(\tan u) \, du$$

$$= \sec u \tan u - \int \sec u \tan^2 du$$

$$= \sec u \tan u - \int \sec u(\sec^2 u - 1) \, du$$

$$= \sec u \tan u - \int \sec^3 u \, du + \int \sec u \, du$$

$$2 \int \sec^3 u \, du = \sec u \tan u + \int \sec u \, du$$

$$\int \sec^3 u \, du = \frac{1}{2} \sec u \tan u + \frac{1}{2} \int \sec u \, du$$

$$= \frac{1}{2} \sec u \tan u + \frac{1}{2} \ln|\sec u + \tan u| + C$$

$$I_{72} = \int \csc^3 u \, du$$

$$Integrate \text{ by parts} \begin{cases} (\csc u)' = -\csc u \cot u \\ \csc^2 u = (-\cot u)' \end{cases}$$

$$= (\csc u)(-\cot u) - \int (-\csc u \cot u)(-\cot u) \, du$$

$$= -\csc u \cot u - \int \csc u \cot^2 du$$

$$= -\csc u \cot u - \int \csc u (\csc^2 u - 1) \, du$$

$$= -\csc u \cot u - \int \csc^3 u \, du + \int \csc u \, du$$

$$2 \int \csc^3 u \, du = -\csc u \cot u + \int \csc u \, du$$

$$\int \csc^3 u \, du = -\frac{1}{2} \csc u \cot u + \frac{1}{2} \int \csc u \, du$$

$$= \frac{1}{2} \csc u \cot u + \frac{1}{2} \ln|\csc u - \cot u| + C$$

$$I_{73} = \int \sin^n u \, \mathrm{d}u$$
Integrate by

Integrate by parts 
$$\begin{cases} (\sin^{n-1} u)' &= (n-1)\sin^{n-2} u \cos u \\ \sin u &= (-\cos u)' \end{cases}$$
$$= (\sin^{n-1} u)(-\cos u) - \int ((n-1)\sin^{n-2} u \cos u)(-\cos u) du$$
$$= -\sin^{n-1} u \cos u + (n-1) \int \sin^{n-2} u \cos^2 u du$$
$$= -\sin^{n-1} u \cos u + (n-1) \int \sin^{n-2} u (1-\sin^2 u) du$$
$$= -\sin^{n-1} u \cos u + (n-1) \left( \int \sin^{n-2} u du - \int \sin^n u du \right)$$

$$1 + (n-1) \int \sin^n u \, du = -\sin^{n-1} u \, \cos u + (n-1) \int \sin^{n-2} u \, du$$
$$\int \sin^n u \, du = -\frac{1}{n} \sin^{n-1} u \, \cos u + \frac{(n-1)}{n} \int \sin^{n-2} u \, du$$

$$\int \sin^{n} u \ du = -\frac{1}{n} \sin^{n-1} u \cos u + \frac{n-1}{n} \int \sin^{n-2} u \ du \ (73)$$

$$I_{74} = \int \cos^n u \, \mathrm{d}u$$

Integrate by parts 
$$\begin{cases} (\cos^{n-1} u)' &= -(n-1)\cos^{n-2} u \sin u \\ \cos u &= (\sin u)' \end{cases}$$
$$= (\cos^{n-1} u)(\sin u) - \int (-(n-1)\cos^{n-2} u \sin u)(\sin u) du$$
$$= \cos^{n-1} u \sin u + (n-1) \int \cos^{n-2} u \sin^2 u du$$
$$= \cos^{n-1} u \sin u + (n-1) \int \cos^{n-2} u (1 - \cos^2 u) du$$
$$= \cos^{n-1} u \sin u + (n-1) \left( \int \cos^{n-2} u du - \int \cos^n u du \right)$$

$$1 + (n-1) \int \cos^n u \, du = \cos^{n-1} u \sin u + (n-1) \int \cos^{n-2} u \, du$$
$$\int \cos^n u \, du = \frac{1}{n} \cos^{n-1} u \sin u + \frac{(n-1)}{n} \int \cos^{n-2} u \, du$$

(74) 
$$\int \cos^n u \ du = \frac{1}{n} \cos^{n-1} u \sin u + \frac{n-1}{n} \int \cos^{n-2} u \ du$$

$$I_{75} = \int \tan^n u \, du$$

$$= \int \tan^{n-2} u \tan^2 u \, du$$

$$= \int \tan^{n-2} u (\sec^2 u - 1) \, du$$

$$= \int \tan^{n-2} u \sec^2 u \, du - \int \tan^{n-2} u \, du$$

$$Let \quad v = \tan u \quad \longrightarrow \quad dv = \sec^2 u \, du$$

$$= \int v^{n-2} u \, dv - \int \tan^{n-2} u$$

$$= \frac{1}{n-1} v^{n-1} - \int \tan^{n-2} u$$

$$= \frac{1}{n-1} \tan^{n-1} u - \int \tan^{n-2} u$$

$$I_{76} = \int \cot^n u \, du$$

$$= \int \cot^{n-2} u \cot^2 u \, du$$

$$= \int \cot^{n-2} u (\csc^2 u - 1) \, du$$

$$= \int \cot^{n-2} u \csc^2 u \, du - \int \cot^{n-2} u \, du$$

$$\text{Let } v = \cot u \longrightarrow dv = -\csc^2 u \, du$$

$$= -\int v^{n-2} u \, dv - \int \cot^{n-2} u$$

$$= \frac{-1}{n-1} v^{n-1} - \int \cot^{n-2} u$$

$$= \frac{-1}{n-1} \cot^{n-1} u - \int \cot^{n-2} u$$

$$I_{77} = \int \sec^{n} u \, du$$

$$Integrate by parts \begin{cases} \sec^{2} u = (\tan u)' \\ (\sec^{n-2} u)' = (n-2)\sec^{n-3} u \sec u \tan u \end{cases}$$

$$= (\tan u) \left(\sec^{n-2} u\right) - \int (\tan u) \left((n-2)\sec^{n-3} u \sec u \tan u\right) du$$

$$= \tan u \sec^{n-2} u - (n-2) \int \sec^{n-2} \tan^{2} u \, du$$

$$= \tan u \sec^{n-2} u - (n-2) \int \sec^{n-2} (\sec^{2} u - 1) \, du$$

$$= \tan u \sec^{n-2} u - (n-2) \left(\int \sec^{n} u \, du - \int \sec^{n-2} du\right)$$

$$(1 + (n-2)) \int \sec^{n} u \, du = \tan u \sec^{n-2} u - (n-2) \int \sec^{n-2} du$$

$$\int \sec^{n} u \ du = \frac{1}{n-1} \tan u \sec^{n-2} u + \frac{n-2}{n-1} \int \sec^{n-2} u \ du \ (77)$$

 $\int \sec^{n} u \, du = \frac{1}{n-1} \tan u \, \sec^{n-2} u - \frac{n-2}{n-1} \int \sec^{n-2} du$ 

$$I_{82} = \int u \sin u \, du$$
Integrate by parts 
$$\begin{cases} (u)' = 1 \\ \sin u = (-\cos u)' \end{cases}$$

$$= (u)(-\cos u) - \int (1)(-\cos u) \, du$$

$$= \int \cos u \, du - u \cos u$$

$$= \sin u - u \cos u$$

$$I_{83} = \int u \cos u \, du$$
Integrate by parts 
$$\begin{cases} (u)' = 1 \\ \cos u = (\sin u)' \end{cases}$$

$$= (u)(\sin u) - \int (1)(\sin u) \, du$$

$$= u \sin u - (-\cos u)$$

$$= \cos u + u \sin u$$

$$I_{92} = \int u \arctan u \, \mathrm{d}u$$

Integrate by parts 
$$\begin{cases} u = \left(\frac{1}{2}u^2\right)' \\ (\arctan u)' = \frac{1}{1+u^2} \end{cases}$$
$$= \left(\frac{1}{2}u^2\right)(\arctan u) - \int \left(\frac{1}{2}u^2\right)\left(\frac{1}{1+u^2}\right) du$$
$$= \frac{u^2}{2}\arctan u - \frac{1}{2}\int \frac{u^2+1-1}{1+u^2} du$$
$$= \frac{u^2}{2}\arctan u - \frac{1}{2}\int 1 - \frac{1}{1+u^2} du$$
$$= \frac{u^2}{2}\arctan u - \frac{1}{2}(u - \arctan u) + C$$
$$= \frac{u^2+1}{2}\arctan u - \frac{u}{2} + C$$

$$I_{96} = \int ue^{au} du$$
Integrate by parts 
$$\begin{cases} (u)' = 1 \\ e^{au} = \left(\frac{e^{au}}{a}\right)' \end{cases}$$

$$= (u)\left(\frac{e^{au}}{a}\right) - \int (1)\left(\frac{e^{au}}{a}\right) du$$

$$= \frac{1}{a}ue^{au} - \frac{1}{a}\int e^{au} du$$

$$= \frac{1}{a}ue^{au} - \frac{1}{a^2}e^{au} + C$$

$$= \left(\frac{1}{a}u - \frac{1}{a^2}\right)e^{au} + C$$
Simplify
$$= \frac{1}{a^2}(au - 1)e^{au} + C$$

$$I_{97} = \int u^n e^{au} du$$
Integrate by parts 
$$\begin{cases} (u^n)' = n \cdot u^{n-1} \\ e^{au} = \left(\frac{e^{au}}{a}\right)' \end{cases}$$

$$= (u^n) \left(\frac{e^{au}}{a}\right) - \int (n \cdot u^{n-1}) \left(\frac{e^{au}}{a}\right) du$$

$$= \frac{1}{a} u^n e^{au} - \frac{n}{a} \int u^{n-1} e^{au} du$$

$$I_{100} = \int \ln u \, du$$
Integrate by parts 
$$\begin{cases} 1 = (u)' \\ (\ln u)' = \frac{1}{u} \end{cases}$$

$$= (u)(\ln u) - \int (u)(\frac{1}{u}) \, du$$

$$= u \ln u - \int 1 \, du$$

$$= u \ln u - u + C$$

$$I_{102} = \int \frac{1}{u \ln u} du$$
Let  $v = \ln u \longrightarrow dv = \frac{1}{u} du$ 

$$= \int \frac{1}{v} dv$$

$$= \ln v + C$$

$$=\ln|\ln u|$$

20: 
$$\frac{1}{u^2 - a^2}$$

21: 
$$\sqrt{a^2+u^2}$$

63: 
$$\sin^2 u$$

64: 
$$\cos^2 u$$

16: 
$$\frac{1}{\sqrt{a^2-u^2}}$$

65: 
$$\tan^2 u$$

17: 
$$\frac{1}{a^2 + u^2}$$

66: 
$$\cot^2 u$$

18: 
$$\frac{1}{u\sqrt{u^2-a^2}}$$

71: 
$$\sec^3 u$$

102: 
$$\frac{1}{u \ln u}$$

19: 
$$\frac{1}{a^2 - u^2}$$

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