



# Do current data prefer a nonminimally coupled inflaton?

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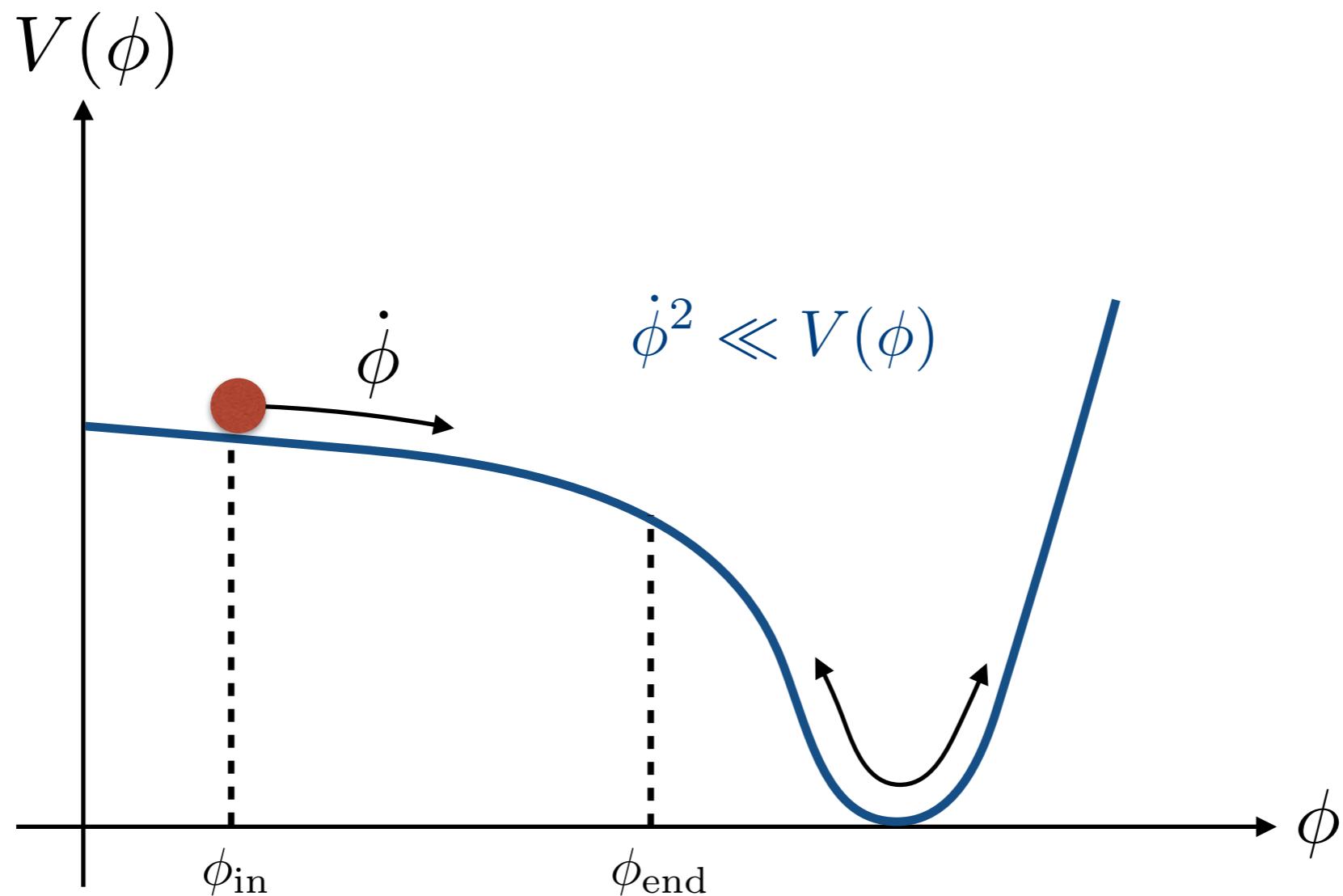
L. Boubekeur, E. Giusarma, O. Mena and HR,

arXiv:1502.05193 [astro-ph.CO].  
Phys. Rev. D 91 (2015) 103004.

# Outline

1. Single-field slow-roll inflation: generalities and status.
2. Motivation.
3. The model.
4. Results.
5. Future constraints.
6. Conclusions.

# Simplest picture: Single-field slow-roll inflation



A. Linde '82

$$S = \int d^4x \sqrt{-g} \left[ \frac{M_{\text{pl}}^2}{2} \mathcal{R} - \frac{1}{2} g^{\mu\nu} \partial_\mu \phi \partial_\nu \phi - U(\phi) \right]$$

Minimal coupling

# The observables

$$\Delta_s^2(k) \equiv \frac{k^3}{2\pi^2} P_\zeta(k) = \left. \frac{1}{8\pi^2} \frac{H^2}{\epsilon} \right|_{k=aH}$$

Primordial scalar power spectrum

$$\Delta_t^2(k) = \left. \frac{2}{\pi^2} \frac{H^2}{M_{\text{pl}}^2} \right|_{k=aH}$$

Primordial tensor power spectrum

Tensor-to-scalar ratio

Primordial tilt

$$r \equiv \frac{\Delta_t^2}{\Delta_s^2} = 16\epsilon$$

$$n_s - 1 \equiv \frac{d \ln \Delta_s^2}{d \ln k} = -2\epsilon - \eta$$

And others:  $n_t \equiv \frac{d \ln \Delta_t^2}{d \ln k}$ ,  $\alpha_s \equiv \frac{d n_s}{d \ln k}$ ,  $\beta_s \equiv \frac{d \alpha_s}{d \ln k}$ , ...

# Single field Slow-Roll inflation

- Single-field SR inflation is favoured:

Observables	Prediction	Exp. Value	
Fluctuations Amplitude	$\Delta_s^2 = \frac{H_\star^2}{8\pi^2 M_{\text{pl}}^2 \epsilon_\star}$	$2.2 \times 10^{-9}$	OK
Tensor-to-scalar ratio	$r = 16\epsilon_\star$	$r < 0.11$ (95% CL)	✗
Tilt	$n_s = 1 + 2\eta_\star - 6\epsilon_\star$	$n_s = 0.9655 \pm 0.0062$	OK
Non-Gaussianity	~ Gaussian. $[O(\epsilon, \eta)]$	Compatible with 0.	OK
Isocurvature	No	$\lesssim$ few %	OK

- Alternatives are less elegant<sup>†</sup> and are in bad shape: too much non-Gaussianity, isocurvature modes, etc.

<sup>†</sup>**elegant:** (of a scientific theory or solution to a problem) pleasingly ingenious and simple: *the grand unified theory is compact and elegant in mathematical terms.* The Oxford dictionary.

# Minimally coupled Chaotic inflation:

$$V(\phi) = \frac{1}{2}m^2\phi^2$$

- $\epsilon(\phi) = \eta(\phi) = 2 \left( \frac{M_{\text{pl}}}{\phi} \right)^2 \longleftrightarrow \phi_{\text{end}} = \sqrt{2}M_{\text{pl}}$
  - $N = \int_{\phi_{\text{cmb}}}^{\sqrt{2}M_{\text{pl}}} \frac{\phi}{2M_{\text{pl}}^2} d\phi = -60 \longleftrightarrow \phi_{\text{cmb}} \sim 15M_{\text{pl}}$
  - $r = 16\epsilon_* \simeq 0.13$
  - $n_s = 1 - 2\epsilon_* - \eta_* \simeq 0.96$
- Super-Planckian values!
- 

# Motivation

- It is usually assumed that a term of the form  $\xi \mathcal{R} \phi^2$  vanishes.
- Since the inflaton is coupled to light degrees of freedom (during reheating),

$$\mathcal{L}_{\text{reheating}} \simeq \lambda \phi^2 / 4! + y_\psi \phi \bar{\psi} \psi + \lambda_\chi \chi^2 \phi^2 + \dots$$

the RGE of  $\xi$  is nontrivial. One can make it vanish at some scale, but it will be nonzero at some point because of its running:

$$\beta_\xi = \frac{\xi - \frac{1}{6}}{(4\pi)^2} [\lambda + \lambda_\xi + 4y_\psi^2 + \dots]$$

- What about nonminimally scenarios?:

- D. S. Salopek, J. R. Bond and J. M. Bardeen, PRD 40, 1753 (1989).
- T. Futamase and K. i. Maeda, PRD 39 (1989) 399.
- R. Fakir and W. G. Unruh, PRD 41, 1783 (1990).
- D. I. Kaiser, PRD 52, 4295 (1995), [astro-ph/9408044].
- E. Komatsu and T. Futamase, PRD 59, 064029 (1999).
- M. P. Hertzberg, JHEP 1011, 023 (2010).
- N. Okada, M. U. Rehman and Q. Shafi, PRD 82 (2010) 043502.
- A. Linde, M. Noorbala and A. Westphal, JCAP 1103, 013 (2011).
- D. I. Kaiser and E. I. Sfakianakis, PRL 112 (2014) 1, 011302.
- T. Chiba and K. Kohri, PTEP 2015, no. 2, 023E01.
- C. Pallis and Q. Shafi, JCAP 1503, no. 03, 023 (2015).
- S. Tsujikawa, J. Ohashi, S. Kuroyanagi and A. De Felice, PRD 88 (2013) 2, 023529.

## Nonminimally coupled Chaotic inflation:

$$S = \int d^4x \sqrt{-g} \left[ \frac{M_{\text{pl}}^2}{2} \mathcal{R} + \frac{\xi}{2} \mathcal{R} \phi^2 - \frac{1}{2} g^{\mu\nu} \partial_\mu \phi \partial_\nu \phi - U(\phi) \right]$$

Performing a conformal (Weyl) transformation:

$$g_{\mu\nu}^E = \Omega(\phi) g_{\mu\nu} \quad \text{where} \quad \Omega(\phi) \equiv 1 + \frac{\xi \phi^2}{M_{\text{pl}}^2}$$

We recast the action in canonical form:

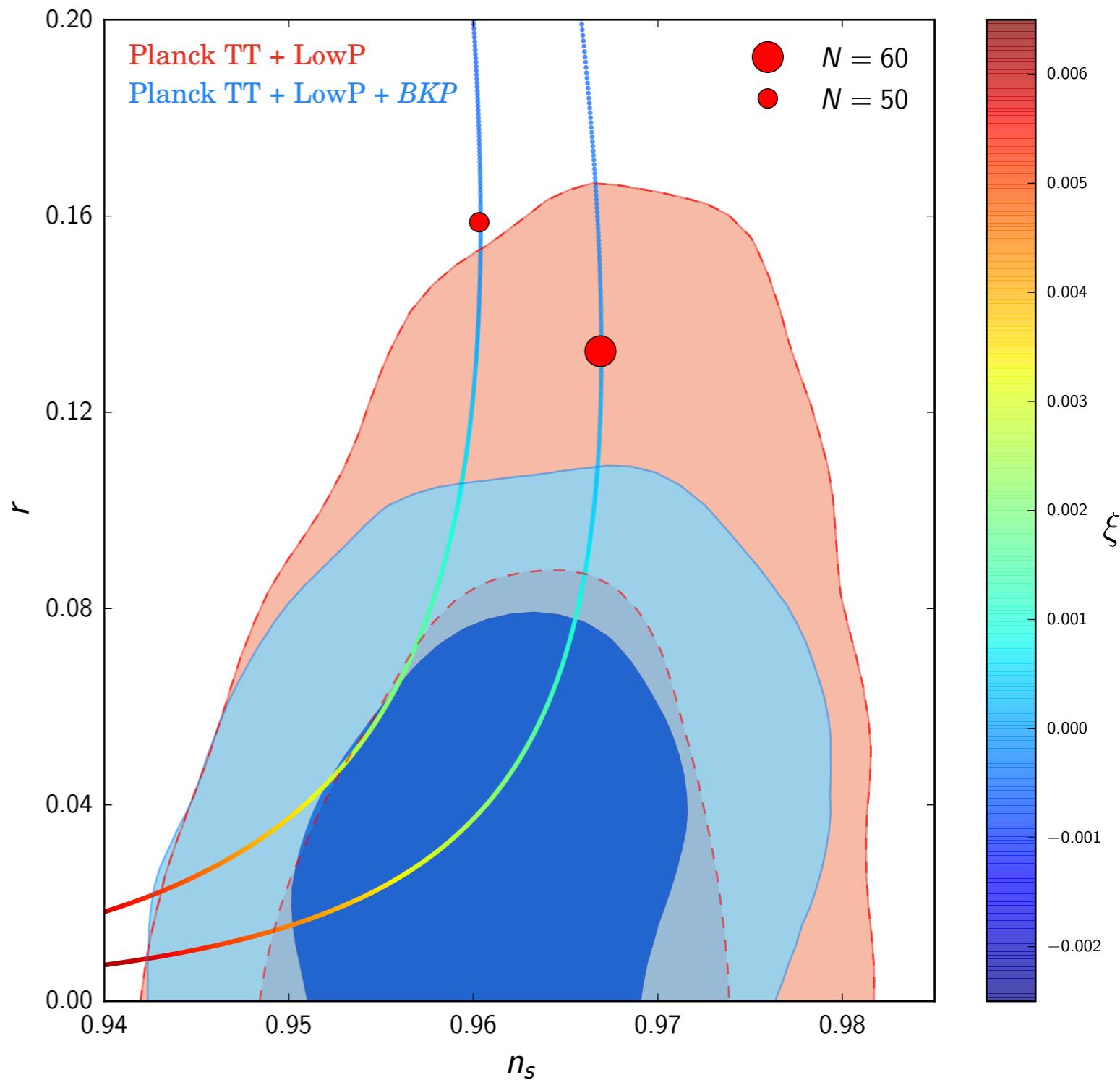
$$S = \int d^4x \sqrt{-g_E} \left[ \frac{M_{\text{pl}}^2}{2} \mathcal{R}_E - \frac{1}{2} g_E^{\mu\nu} \partial_\mu \varphi \partial_\nu \varphi - V[\phi(\varphi)] \right]$$

Where the potential is now:

$$V[\phi(\varphi)] = \frac{U(\phi)}{\Omega^2(\phi)} \quad \xrightarrow{\hspace{1cm}} \quad U(\phi) = \frac{1}{2} m^2 \phi^2$$

# Results

- $\Lambda$ CDM Cosmology +  $\xi \neq 0$ .
- Planck '15 TT measurements (BKP=BICEP2/KECK + Planck).
- We perform a MCMC analysis using COSMOMC.

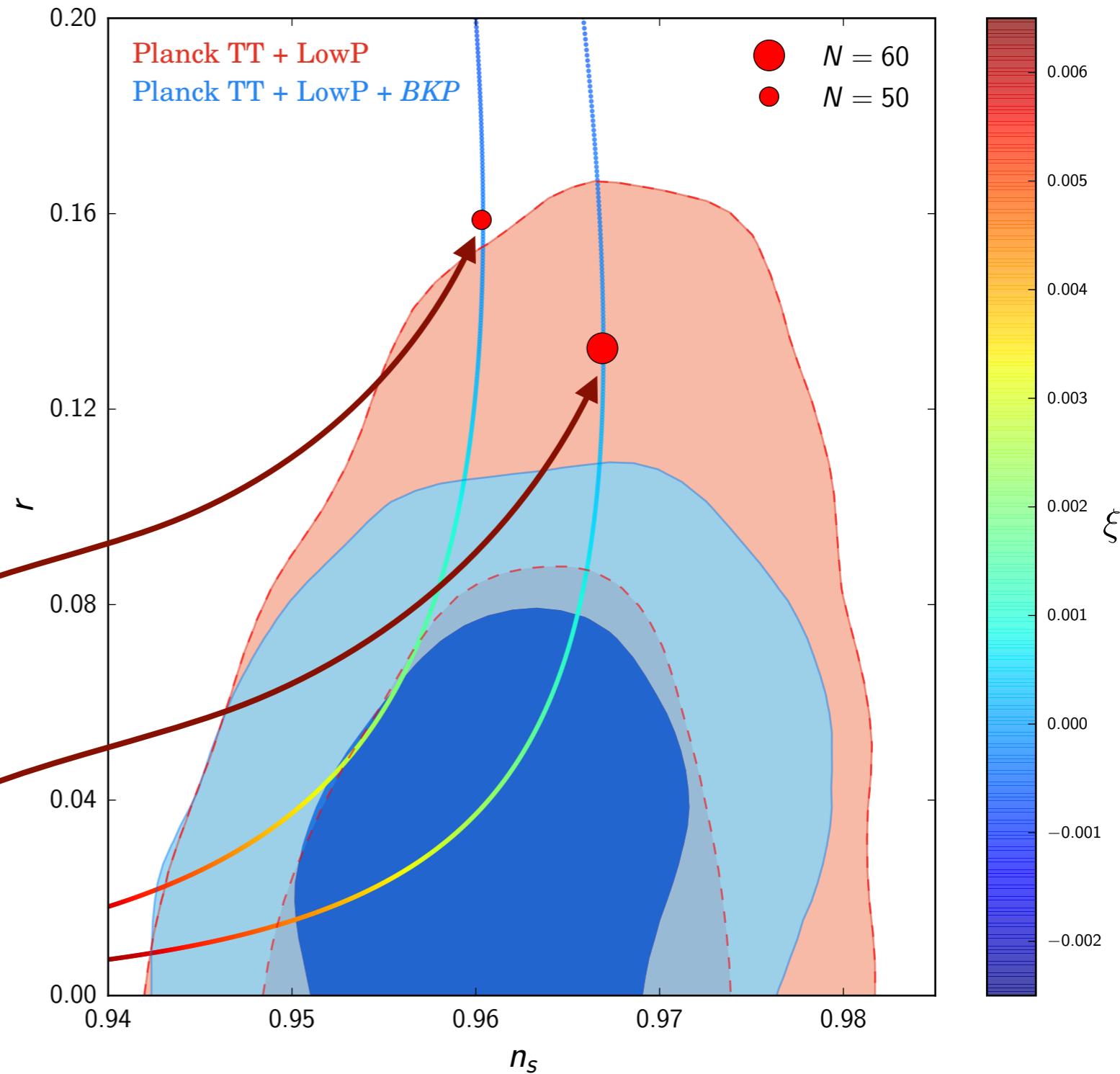


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Ruled out at more than 99% C.L.

Disfavoured at 95% C.L.



# Results

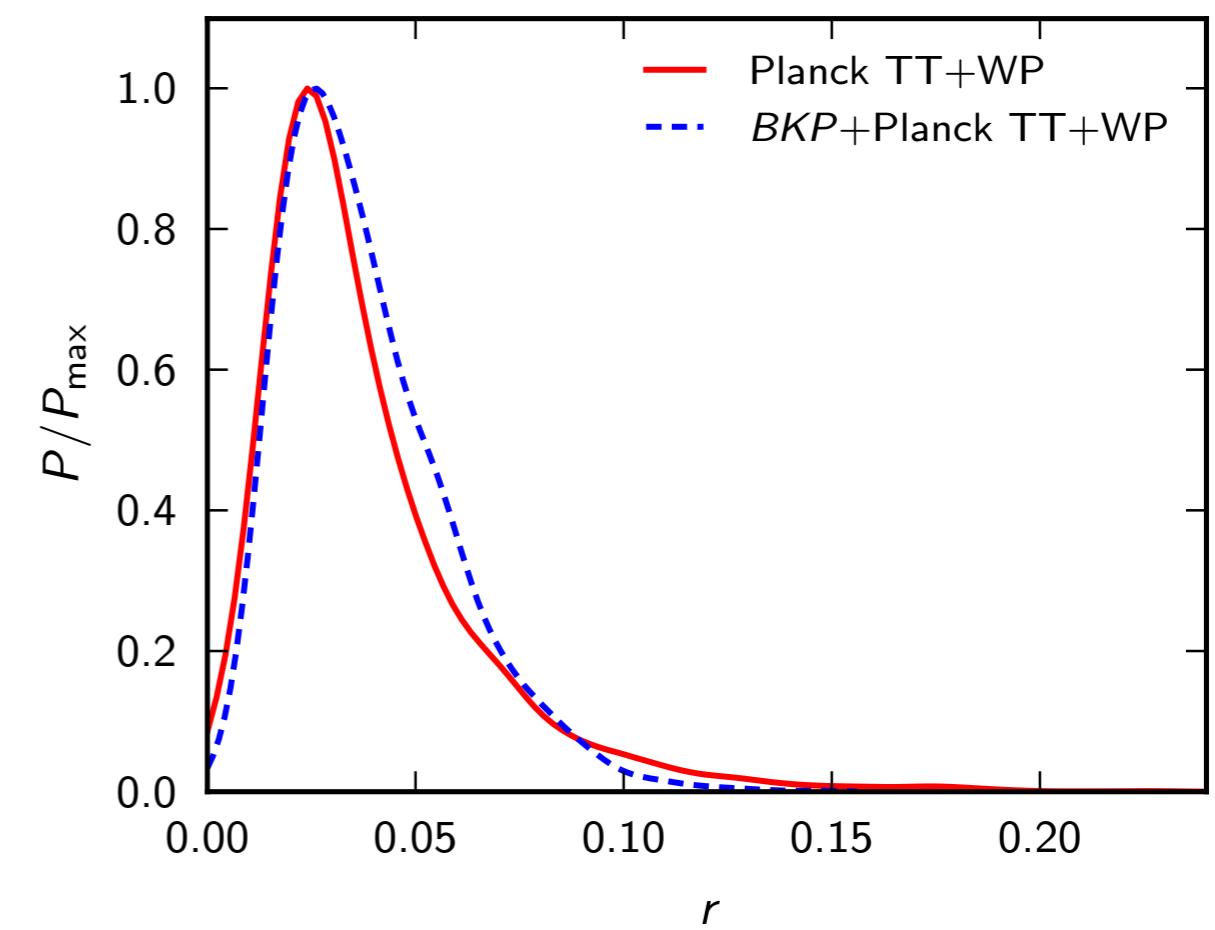
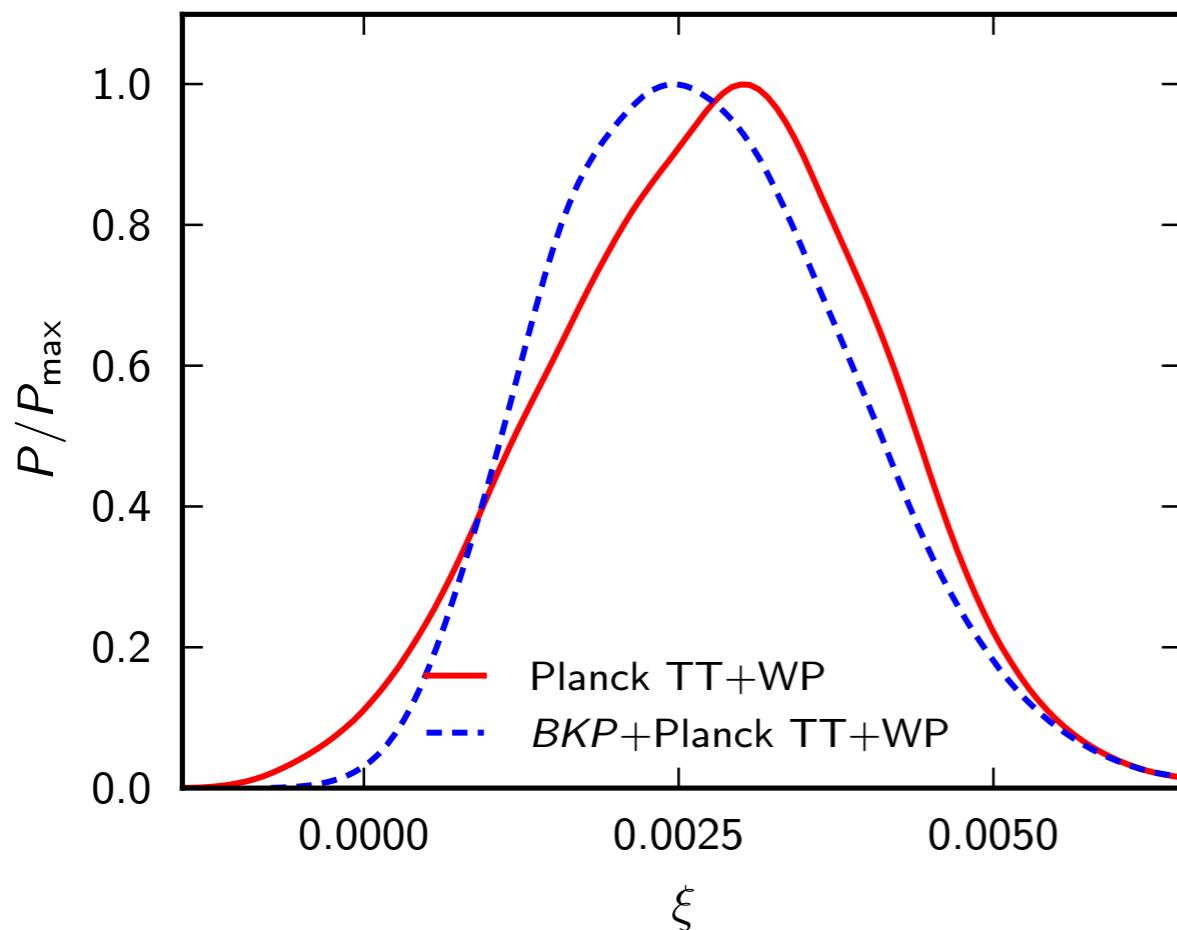
95% C.L. constraints:

	Planck TT+WP		BK+Planck TT+WP	
$N$	60	50	60	50
$\xi$	$0.0028^{+0.0023}_{-0.0025}$	$0.0024^{+0.0023}_{-0.0023}$	$0.0027^{+0.0023}_{-0.0022}$	$0.0027^{+0.0020}_{-0.0019}$
$n_s$	$0.958^{+0.010}_{-0.011}$	$0.954^{+0.007}_{-0.009}$	$0.958^{+0.009}_{-0.011}$	$0.953^{+0.007}_{-0.009}$
$r$	$0.038^{+0.051}_{-0.031}$	$0.063^{+0.056}_{-0.048}$	$0.038^{+0.039}_{-0.030}$	$0.053^{+0.038}_{-0.037}$
$\alpha \equiv dn_s / d \ln k$	$-0.0005^{+0.0001}_{-0.0001}$	$-0.0007^{+0.0001}_{-0.0001}$	$-0.0005^{+0.0001}_{-0.0001}$	$-0.0007^{+0.0001}_{-0.0001}$

- A nonvanishing coupling is preferred in this context.
- A nonvanishing  $r$  is also favoured.

# Results

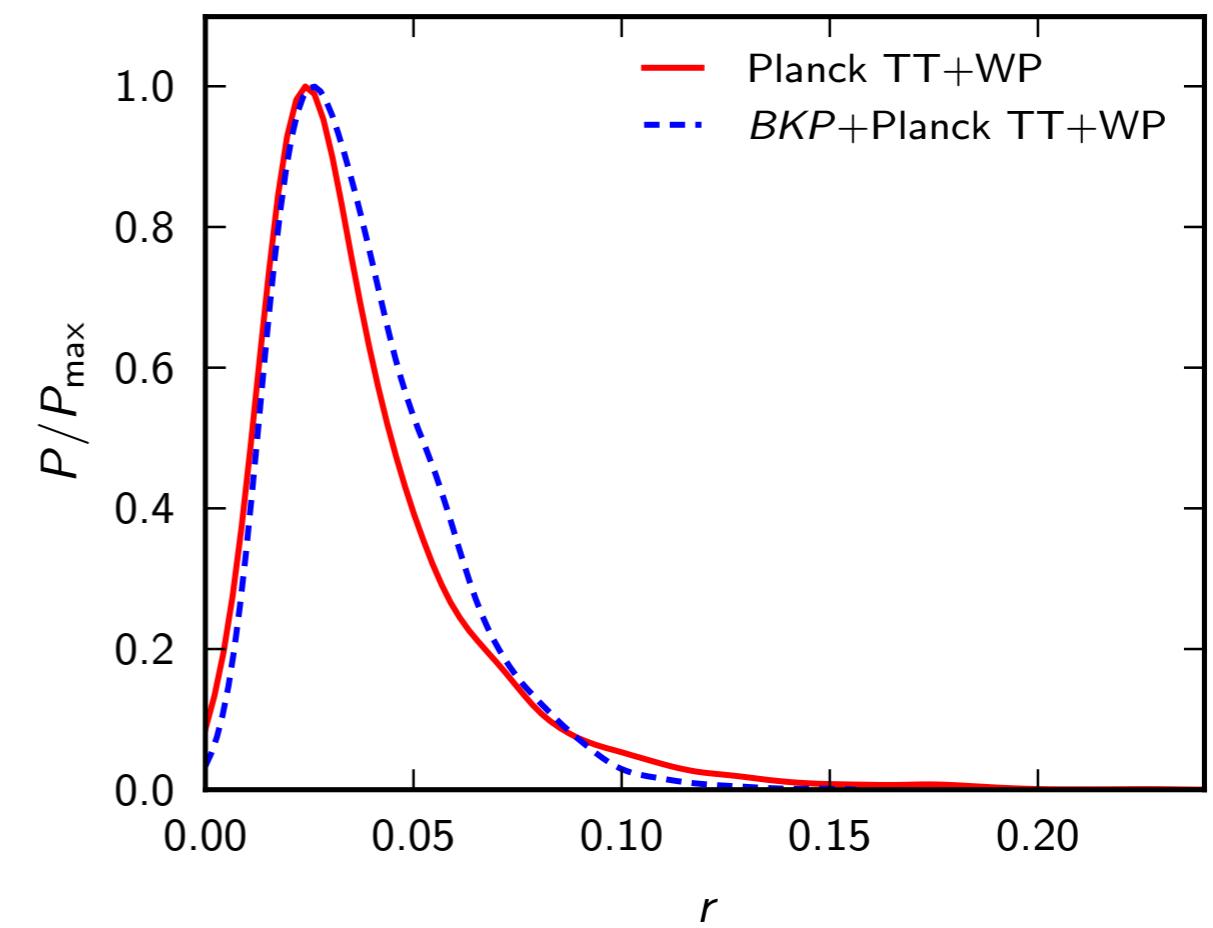
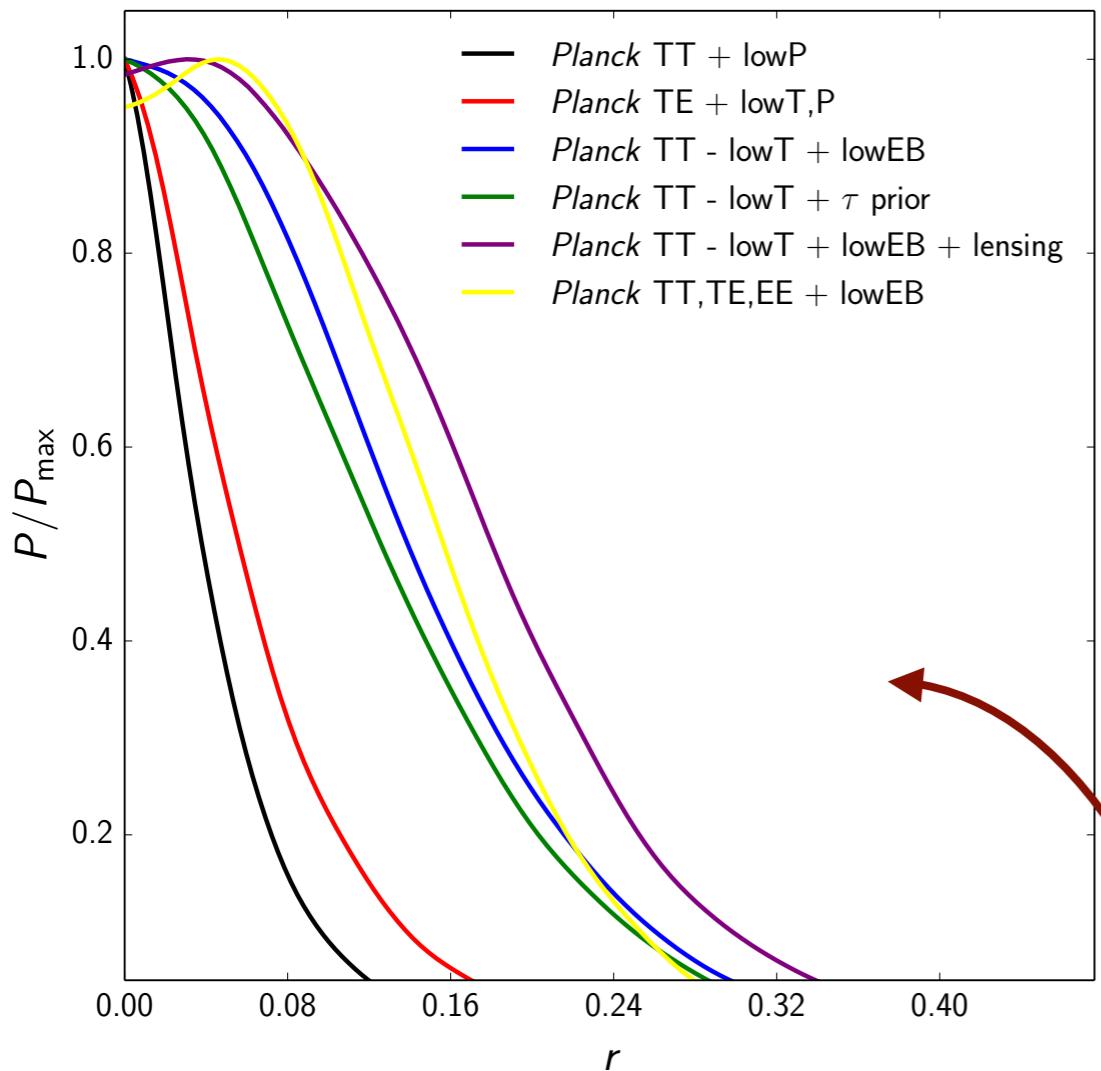
One-dimensional posterior probability distributions.



- Slight preference for nonzero  $\xi$  and  $r$ .

# Results

One-dimensional posterior probability distributions.



Planck '15 ( $\xi = 0$ )

# Results

We compare the  $\chi^2$ -statistics for both models:

$$\Delta\chi^2 = \chi^2[\xi = 0] - \chi^2[\xi \neq 0]$$

Considering a distribution with one degree of freedom ( $\xi$ ):

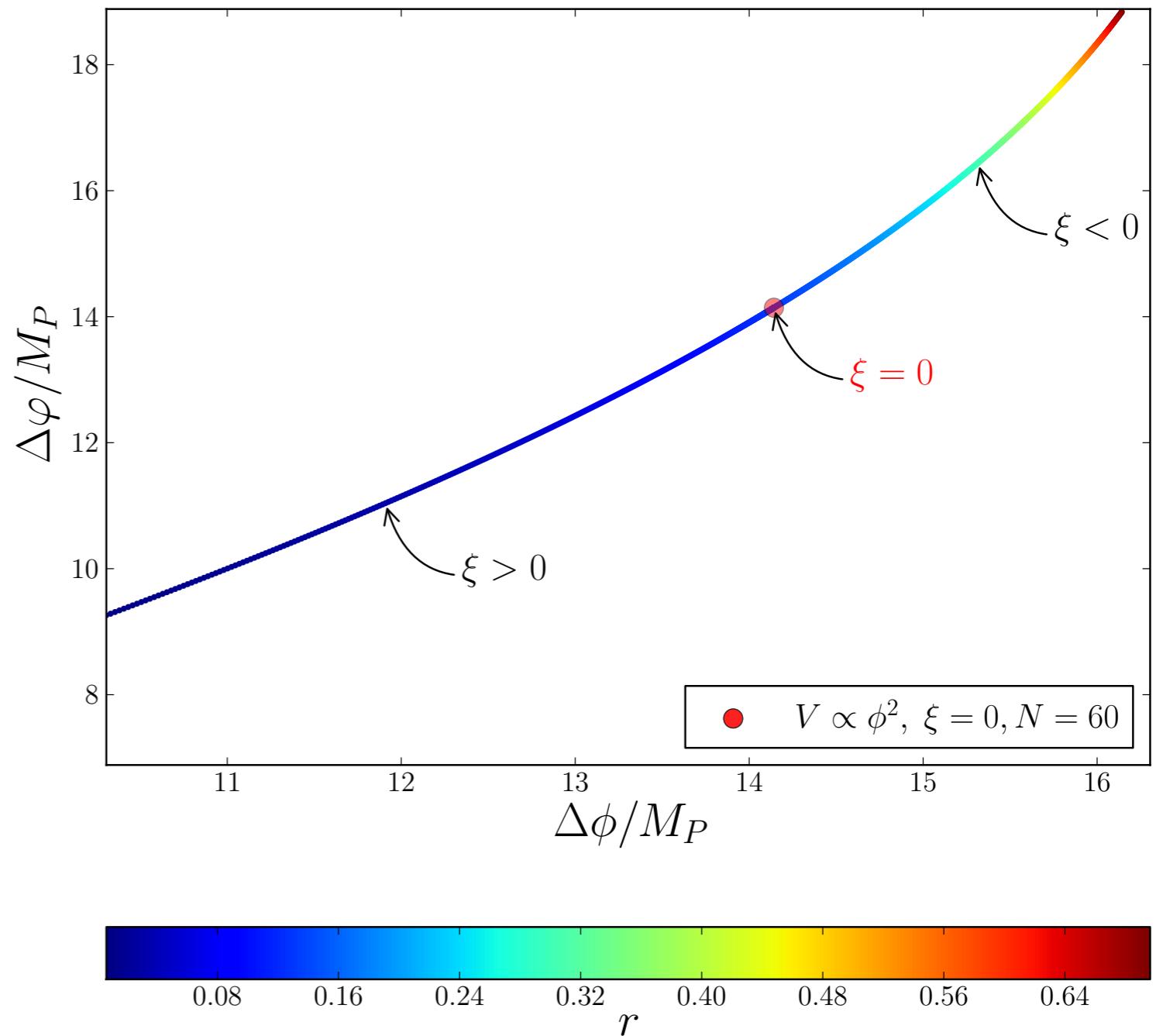
	Planck TT+WP	BK+Planck TT+WP
$\Delta\chi^2$	6	10
$p$ -value	0.014	0.0016
Statistical Significance	Significant	Very significant

- The nonminimally coupled scenario is favoured (with respect to the minimal one) at 99% of confidence level.

# Results

$$\left(\frac{d\varphi}{d\phi}\right)^2 = \frac{1}{\Omega} + \frac{3}{2}M_P^2 \left(\frac{\Omega'}{\Omega}\right)^2$$

- The excursion of the nonminimally coupled inflaton is bit smaller but still super-Planckian.
- Large  $r$  correlates with large excursions as dictated by the Lyth bound.



# Future constraints

- We can construct a combination of first order slow-roll observables:

$$n_s - 1 + \frac{r}{4} = -20\xi,$$

- This combination vanishes for  $\xi = 0$ , in the context of the chaotic scenario.
- Future observations from PIXIE, Euclid, COrE, and PRISM are targeting

$$\sigma_r = \sigma_{n_s-1} = 10^{-3}$$



$$\sigma_\xi \leq 10^{-4}$$

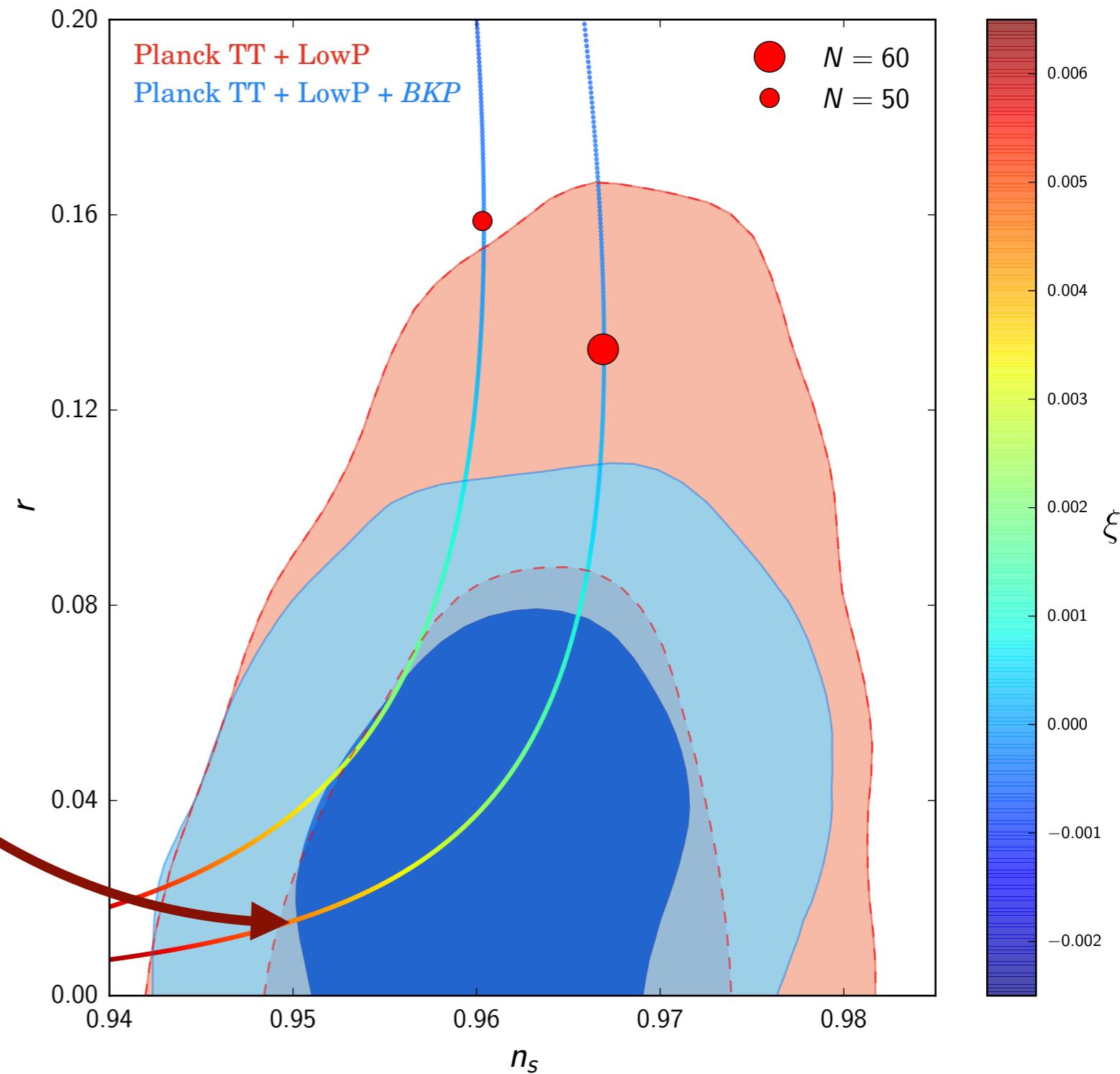
- Combined with future accurate measurements of  $n_s$ , this might rule-out this model due to its nontrivial correlation with  $r$ .

# Future constraints

In this scenario,

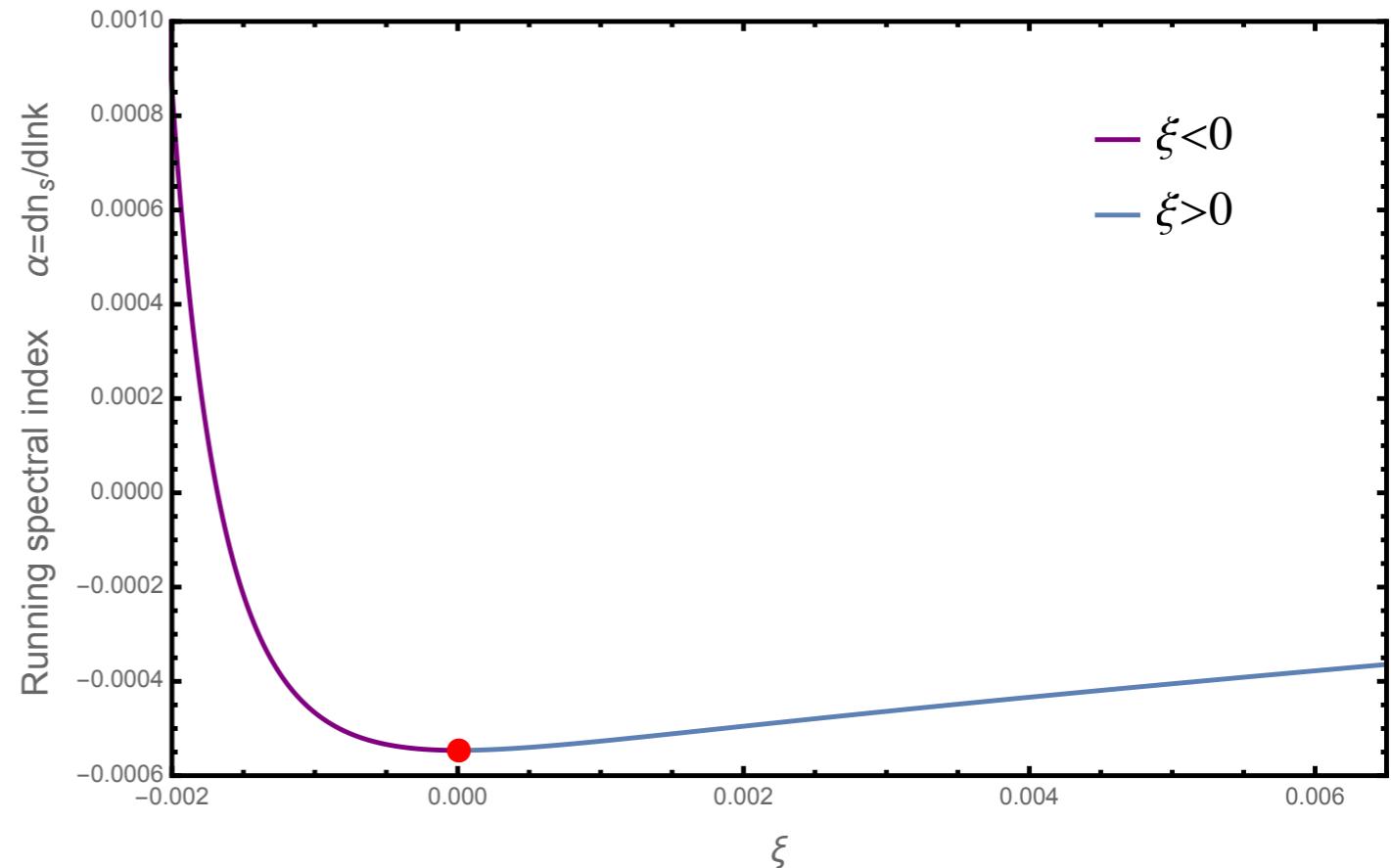
$n_s < 0.96$  for  $r < 0.03$

is potentially falsifiable.



# Future constraints

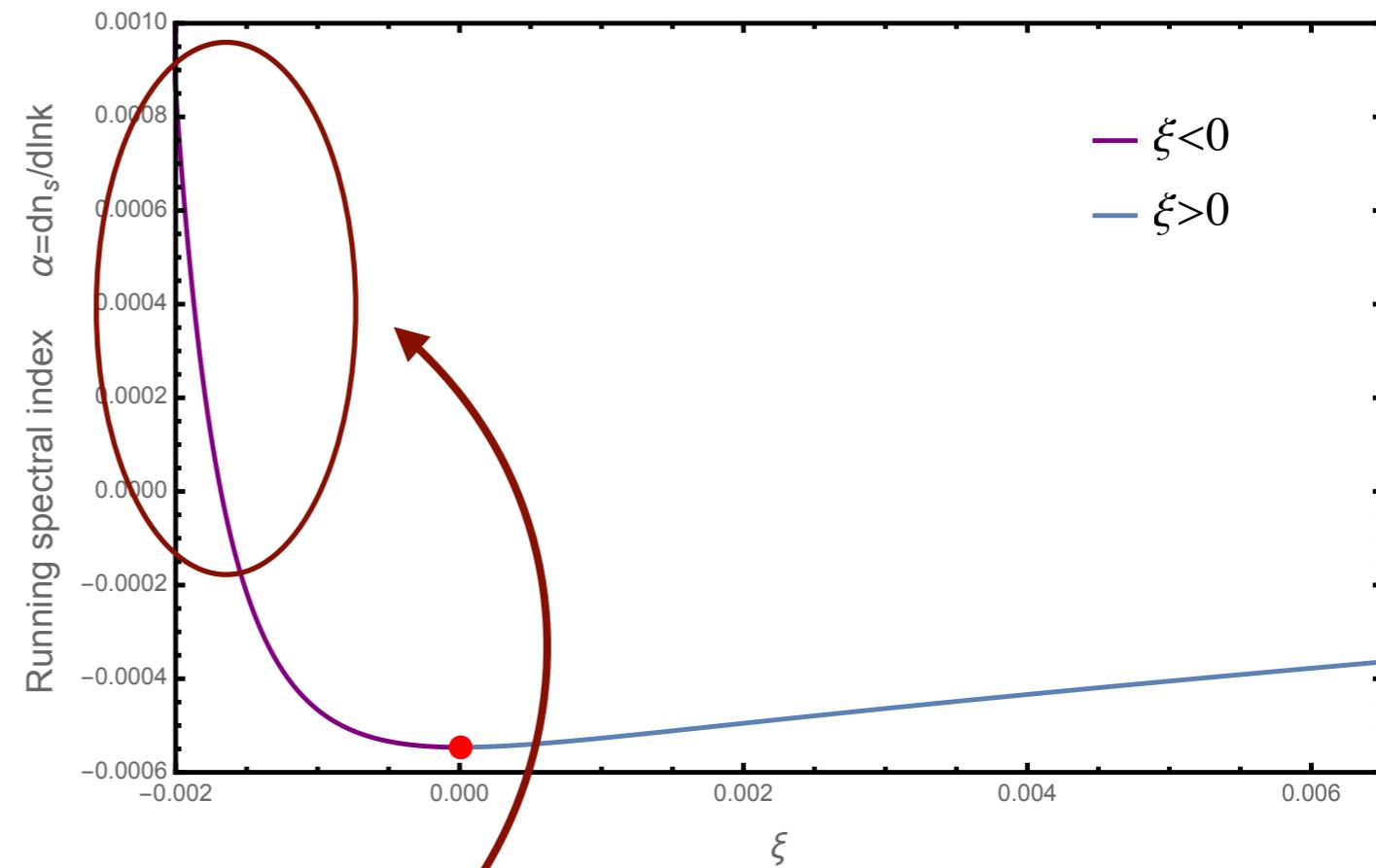
- Negative coupling gives significant running (and higher  $r$  ).
- The running is a good discriminator.
- Future constraints might falsify this model.



# Future constraints

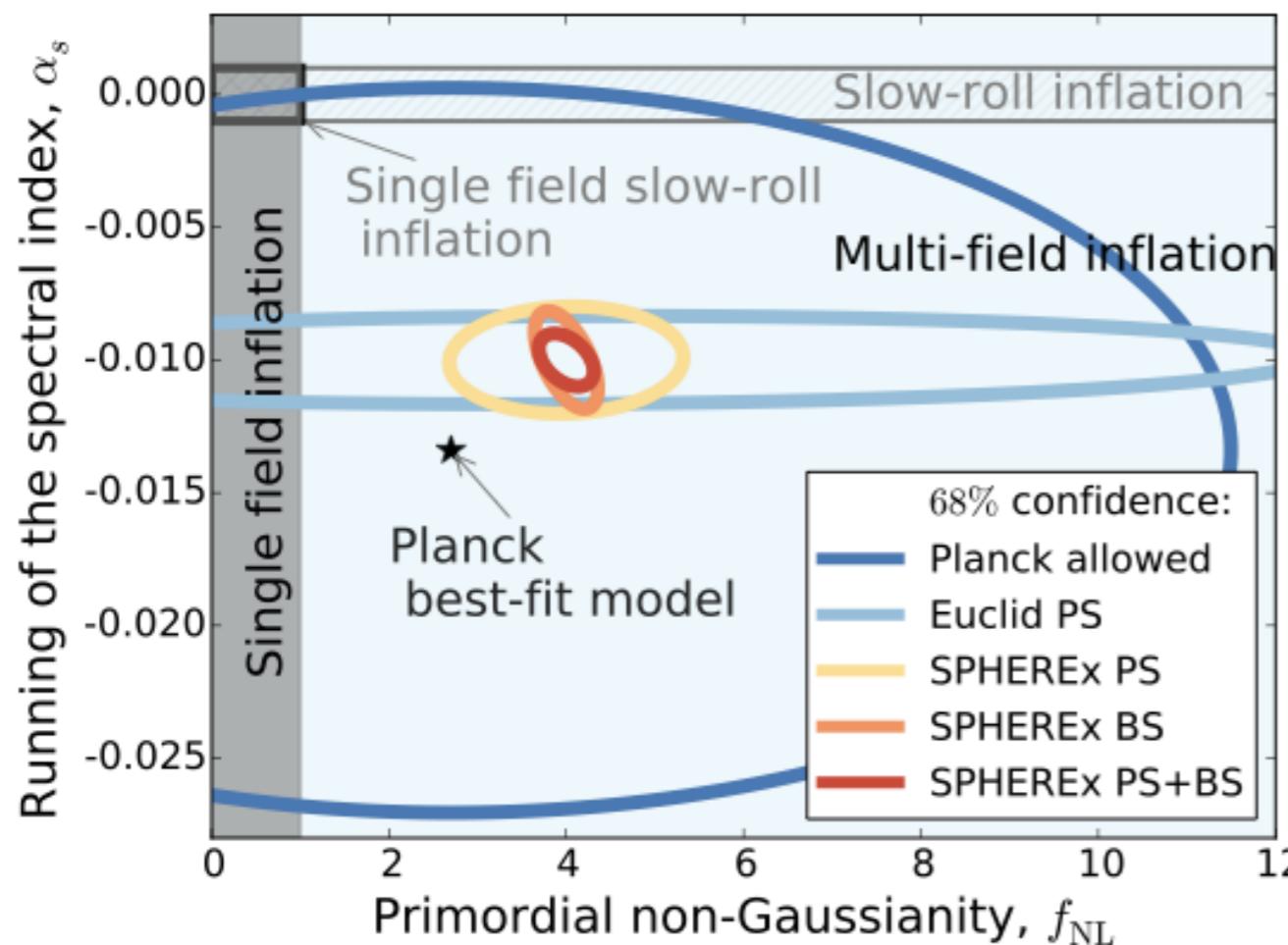
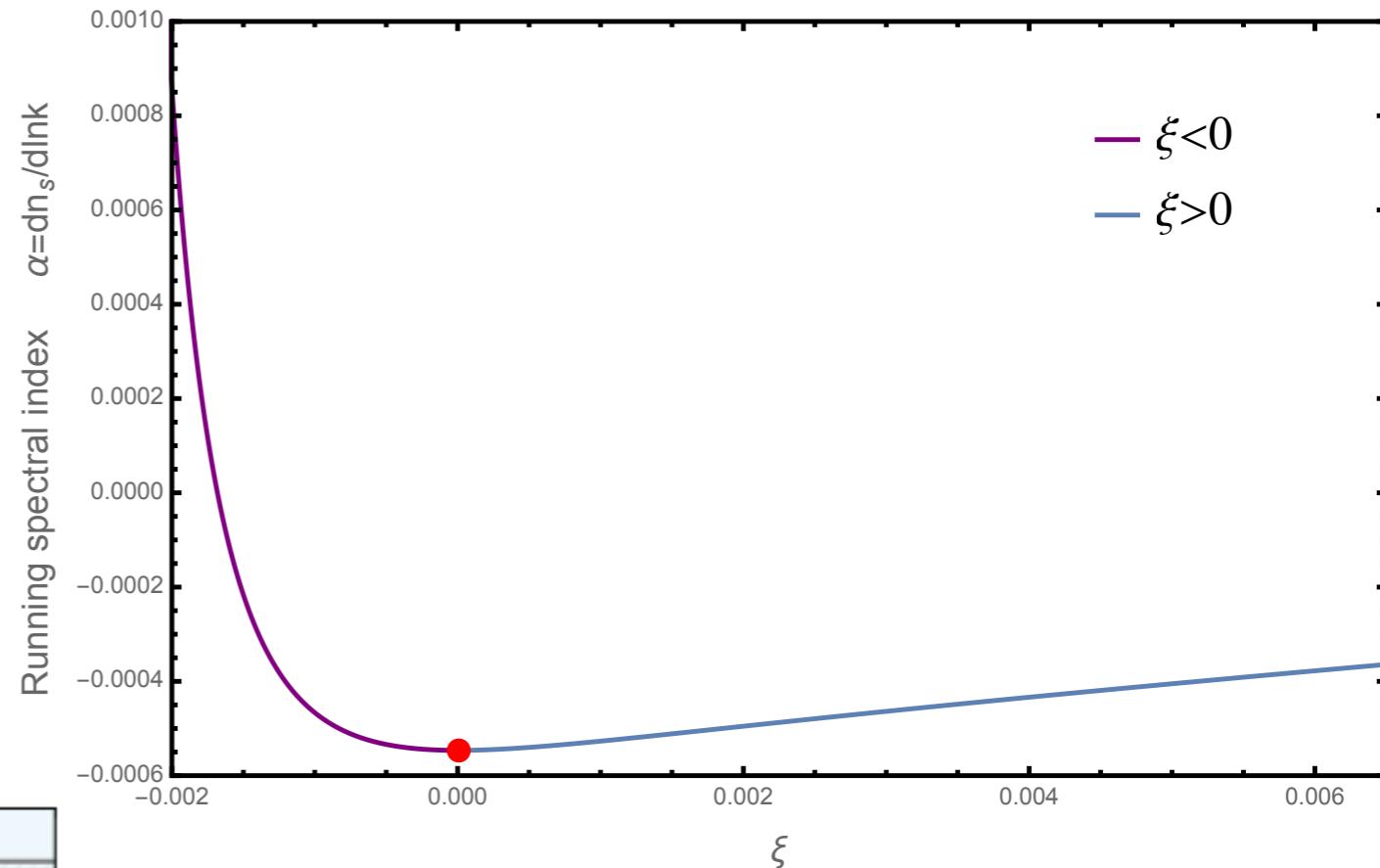
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Compatible with  
Planck '15, but  
 $r > 0.2$



# Future constraints

- Negative coupling gives significant running (and higher  $r$ ).
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**SPHEREx (Caltech)**  
 (Spectrophotometer for the History of Universe, Epoch of Reionization and Ices Explorer)

$$\sigma_{\alpha_s} \approx 0.00065$$

# Conclusions

- The answer is YES!
  - Current data have a preference for a nonminimally coupled  $\phi^2$  scenario.
- With the introduction of a nonminimal coupling, the preferred value of  $r$  is nonzero.
- Next round of observations might rule-out this scenario
  - Better measurements of  $n_s$  and  $r$  by, e.g., PIXIE, Euclid, COrE, and PRISM.
  - Better measurements of  $\alpha_s$  by, e.g., SPHEREx.
- More futuristic observations (like 21 cm Cosmology) will certainly answer this question.

Thank you!