

(b) What is the running time complexity of your function? Justify.

The time complexity of my particular solution is  $O(\log N)$  this is because on each recursive call the size of the problem gets cut in half, as an example given with starting at 63 on the second pass, this becomes  $31 + 1$  extra multiplication, on the second pass its only  $15 + 1$ extra multiplication, and then its just  $7 + 1$ extra multiplication ect... On each consecutive recursive the problem has been cut in roughly half. Thus we can conclude that the time complexity is  $O(\log n)$ .

(c) Give a number of multiplications used by your function to calculate x 63.

Starting at 63 we have

$63 \rightarrow 31*2 + 1$  extra multiplication of the base  $\rightarrow 15*2 + 1 \rightarrow 7*2 + 1 \rightarrow 3*2 + 1 \rightarrow 1*2 + 1 \rightarrow 0*2 + 1$ .

adding all the odd 1 gets us 6

each multiplication is repeated on the higher step so we get that we have 12 multiplications.