

MINISTÉRIO DA EDUCAÇÃO  
UNIVERSIDADE FEDERAL DO PIAUÍ  
CAMPUS SENADOR HELVÍDIO NUNES DE BARROS  
CHEFIA DO CURSO DE SISTEMA DE INFORMAÇÃO

Profa.: Aline Moraes

Disciplina: Cálculo I

3ª Atividade Avaliativa

Aluno: *Fleto Jose Rodrigues Salgueiro*

$$\begin{aligned} 1- \quad y &= x^3 - 3x + 4 \\ y &= 3x^2 - 3 \\ y &= 3 \cdot 2^2 - 3 \\ y &= 3 \cdot 4 - 3 \\ y &= 9 \end{aligned}$$

$$2-a) \frac{d}{dx} (3x^2 - 5x + 2)$$

$$\frac{d}{dx} (3x^2) - \frac{d}{dx} (5x) + \frac{d}{dx} (2);$$

$$\frac{d}{dx} (3x^2) = 6x \Rightarrow \frac{d}{dx} (5x) = 5 \Rightarrow \frac{d}{dx} (2) = 0;$$

$$6x - 5$$

$$b) \frac{d}{dx} \left( \frac{x^2 + 1}{2x + 3} \right)$$

$$\frac{\frac{d}{dx} (x^2 + 1)(2x + 3) - \frac{d}{dx} (2x + 3)(x^2 + 1)}{(2x + 3)^2};$$

$$\frac{d}{dx} (x^2 + 1) = 2x \Rightarrow \frac{d}{dx} (2x + 3) = 2$$

$$\frac{2x(2x + 3) - 2(x^2 + 1)}{(2x + 3)^2};$$

$$\frac{2x^2 + 6x - 2}{(2x + 3)^2}$$

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$$2-c) \frac{d}{dx} ((4x^2 + 13x) \cdot (\tan(x) - 4))$$

$$\frac{d}{dx} (4x^2 + 13x)(\tan(x) - 4) + \frac{d}{dx} (\tan(x) - 4)(4x^2 + 13x);$$

$$\frac{d}{dx} (4x^2 + 13x) = 8x + 13 \Rightarrow \frac{d}{dx} (\tan(x) - 4) = \sec^2(x);$$

$$(8x + 13)(\tan(x) - 4) + \sec^2(x)(4x^2 + 13x)$$

$$d) \frac{d}{dx} (\ln(x^2 + 2x + 5))$$

$$\frac{1}{x^2 + 2x + 5} \frac{d}{dx} (x^2 + 2x + 5);$$

$$\frac{d}{dx} (x^2 + 2x + 5) = 2x + 2;$$

$$\frac{1}{x^2 + 2x + 5} (2x + 2);$$

$$\frac{2x + 2}{x^2 + 2x + 5}$$

$$e) \frac{d}{dx} (\sec(x) e^{3x})$$

$$\frac{d}{dx} (\sec(x) e^{3x}) + \frac{d}{dx} (e^{3x}) \sec(x);$$

$$\frac{d}{dx} (\sec(x)) = \sec(x) \tan(x) \Rightarrow \frac{d}{dx} (e^{3x}) = e^{3x} \cdot 3;$$

$$\sec(x) \tan(x) e^{3x} + e^{3x} \cdot 3 \sec(x)$$

3-  $f'''(x) = 2 \sin x + 3 \cos x - x^3$  Aluno: Hecto José Rodrigues Salgueiros

$$2 \sin(x) + 3 \cos(x) - x^3 = 2 \cos(x) - 3 \sin(x) - 3x^2;$$

$$2 \cos(x) - 3 \sin(x) - 3x^2 = -2 \sin(x) - 3 \cos(x) - 6x;$$

$$-2 \sin(x) - 3 \cos(x) - 6x \Rightarrow -2 \cos(x) - (-3 \sin(x)) - 6;$$

$$-2 \cos(x) + 3 \sin(x) - 6$$

$$4- S(t) = 2t^4 + 5t^2 + 2$$

$$S(5) = 2 \cdot 5^4 + 5 \cdot 5^2 + 2;$$

$$S(5) = 2 \cdot 5^4 + 5^3 + 2;$$

$$S(5) = 1250 + 125 + 2;$$

$$S(5) = 1377$$

$$5- a) \lim_{x \rightarrow 0} \frac{e^{\sin(x)} - 1}{\ln(x+1)}$$

$$\lim_{x \rightarrow 0} \left( \frac{e^{\sin(x)} \cos(x)}{\frac{1}{x+1}} \right);$$

$$\lim_{x \rightarrow 0} \frac{e^{\sin(0)} \cos(0)}{\frac{1}{0+1}} = 1$$

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$$5-b) \lim_{x \rightarrow 1} \left( \frac{\ln(x)}{\sin(\pi x)} \right)$$

Para  $\lim_{x \rightarrow a} \left( \frac{f(x)}{g(x)} \right)$ , se  $\lim_{x \rightarrow a} \left( \frac{f(x)}{g(x)} \right) = \frac{0}{0}$ , então  $\lim_{x \rightarrow a} \left( \frac{f(x)}{g(x)} \right) = \lim_{x \rightarrow a} \left( \frac{f'(x)}{g'(x)} \right)$ ;

$$\lim_{x \rightarrow 1} \left( \frac{(\ln(x))'}{(\sin(\pi x))'} \right);$$

$$(\ln(x))' = \frac{1}{x} \Rightarrow (\sin(\pi x))' = \cos(\pi x) \pi;$$

$$\lim_{x \rightarrow 1} \left( \frac{\frac{1}{x}}{\cos(\pi x) \pi} \right) \Rightarrow \left( \frac{\frac{1}{1}}{\cos(\pi \cdot 1) \pi} \right) = \underline{\underline{-\frac{1}{\pi}}}$$

$$c) \lim_{x \rightarrow -3} \left( \frac{36 - 4x^2}{2x^2 + 7x + 3} \right)$$

$$\lim_{x \rightarrow -3} \left( \frac{-8x}{4x + 7} \right);$$

$$\lim_{x \rightarrow -3} \left( \frac{-8(-3)}{4(-3) + 7} \right);$$

$$\lim_{x \rightarrow -3} -\frac{24}{5}$$

$$d) \lim_{x \rightarrow 2} \left( \frac{1 - 2/x}{x^2 - 4} \right)$$

$$\lim_{x \rightarrow 2} \left( \frac{\frac{2}{x^2}}{\frac{2}{2x}} \right) \Rightarrow \left( \frac{2^{2/2}}{2 \cdot 2} \right) = \underline{\underline{\frac{1}{8}}}$$