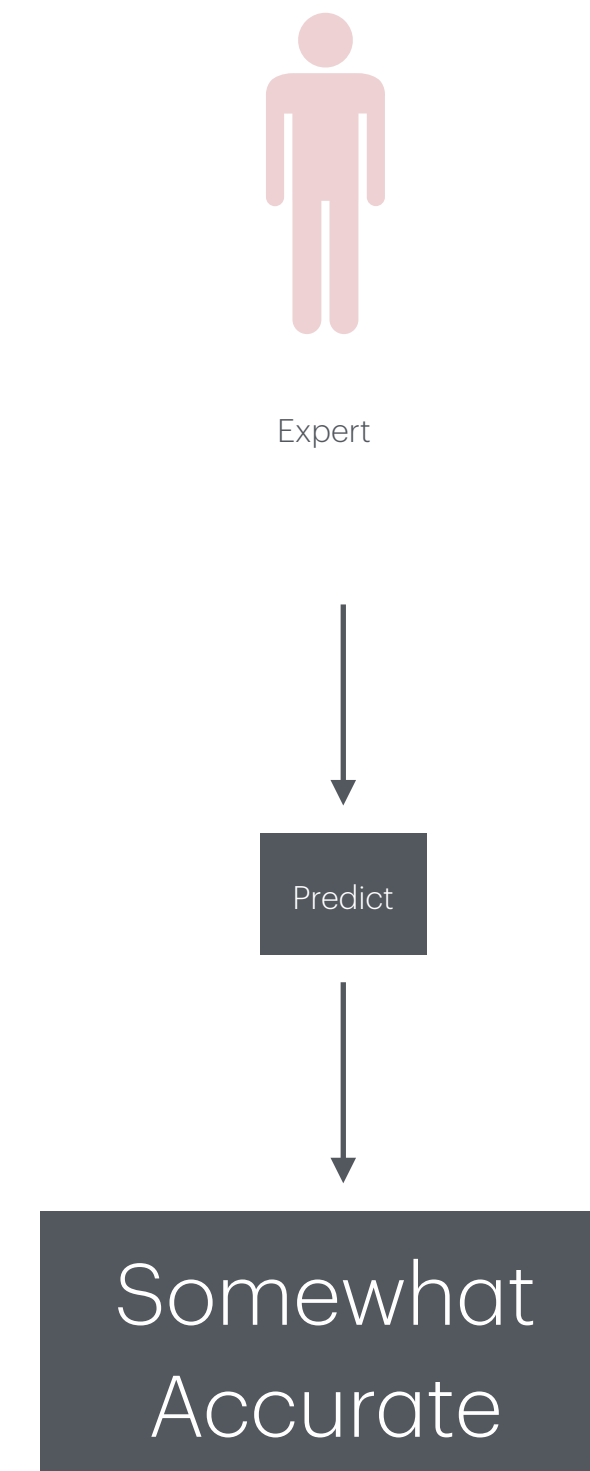
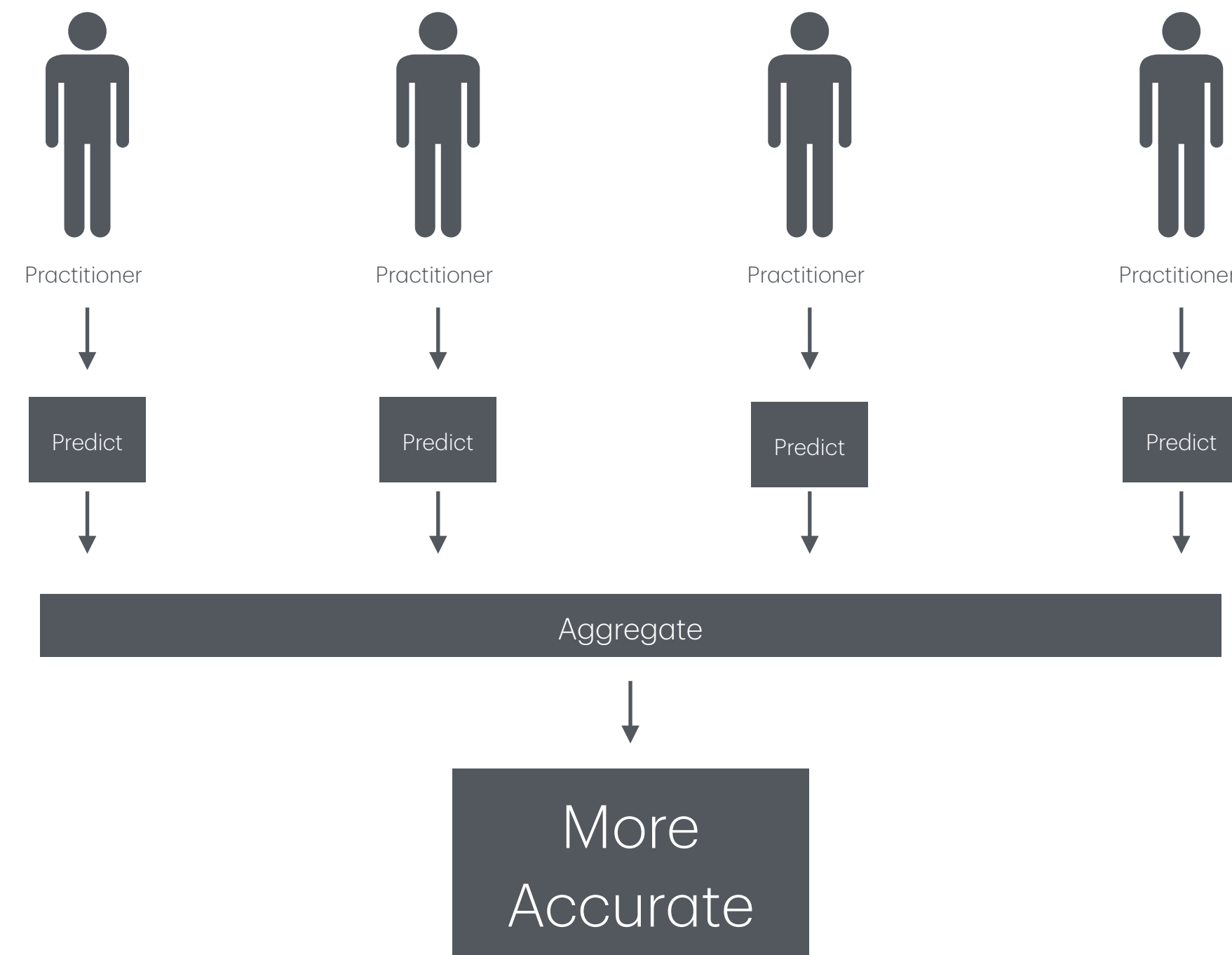
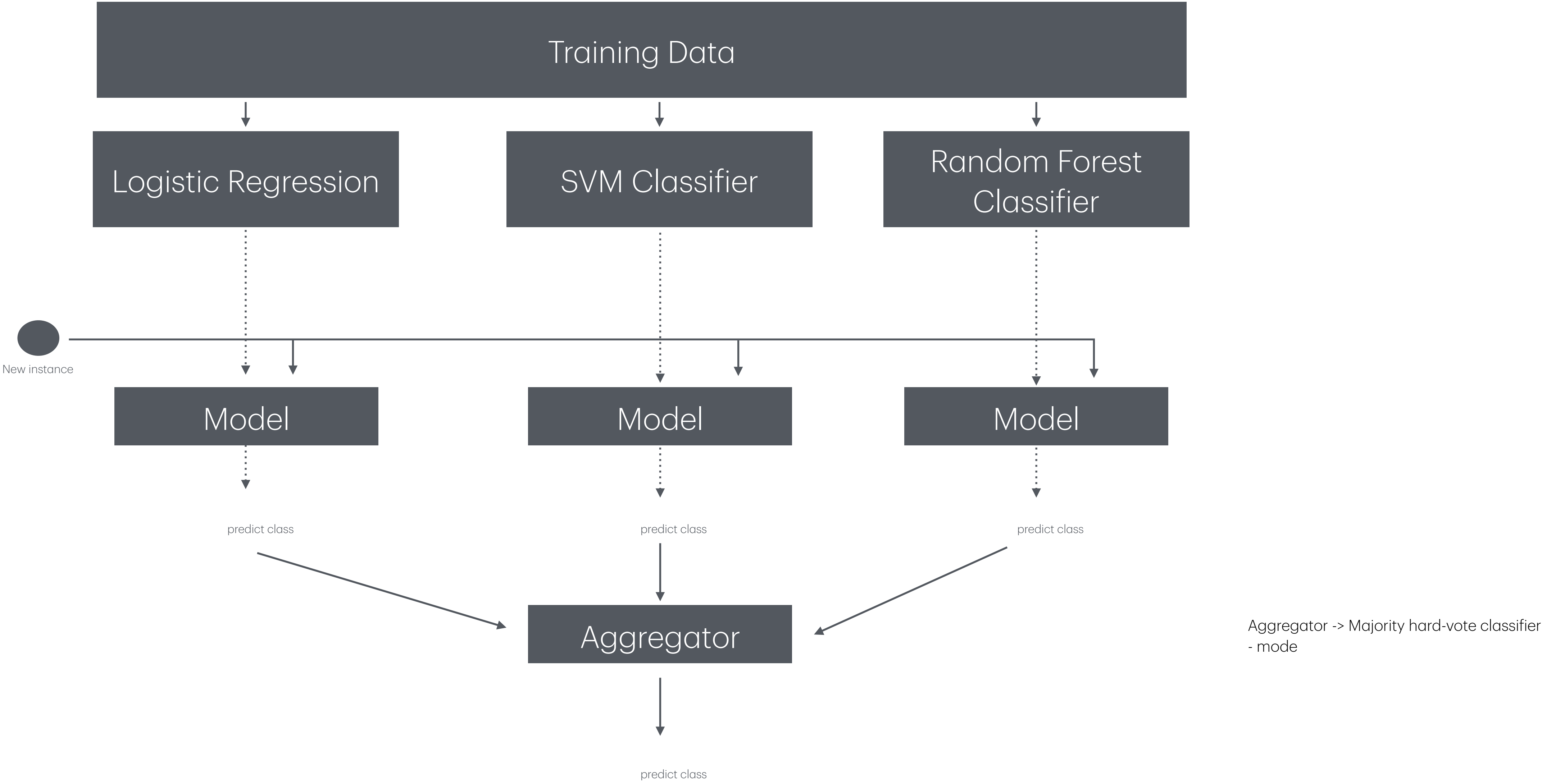


Ensemble



Hard Classifier



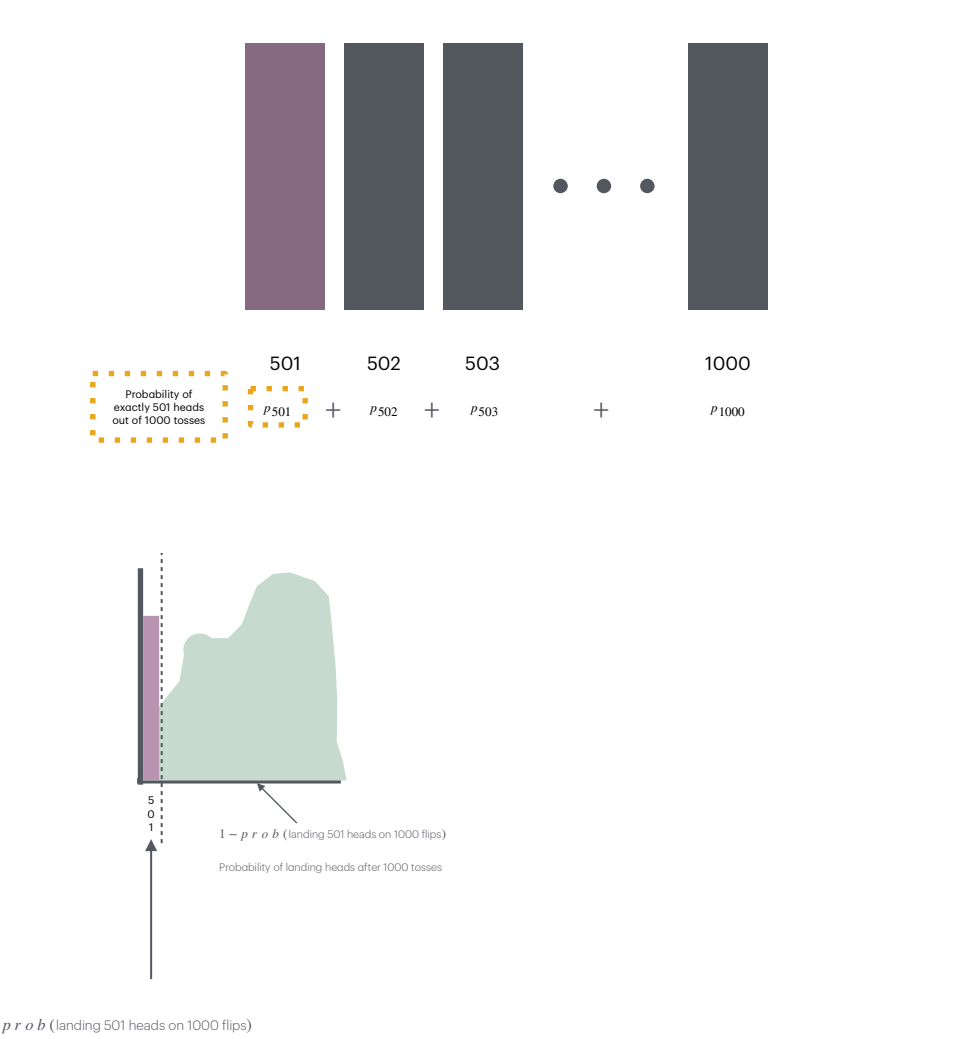
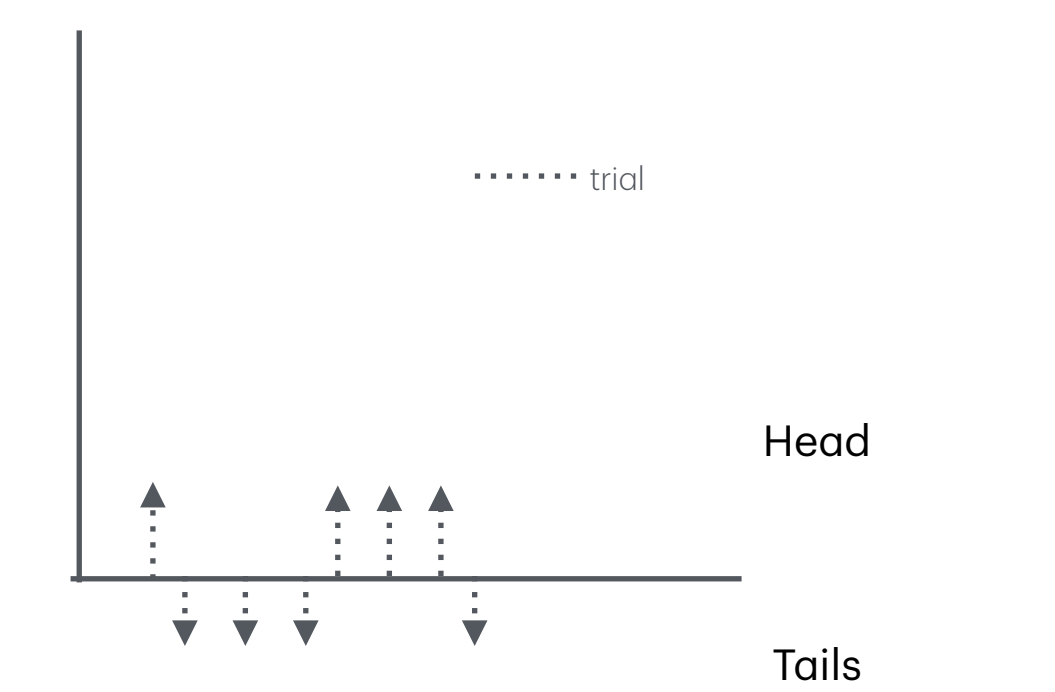
Law Large Numbers

In probability and statistics, a Bernoulli process is a finite or infinite sequence of binary random variables, so it is a discrete-time stochastic process that takes only two values, canonically 0 and 1. The component Bernoulli variables X_i are identically distributed and independent. Prosaically, a Bernoulli process is a repeated coin flipping, possibly with an unfair coin. Every variable X_i in the sequence is associated with a Bernoulli trial or experiment.

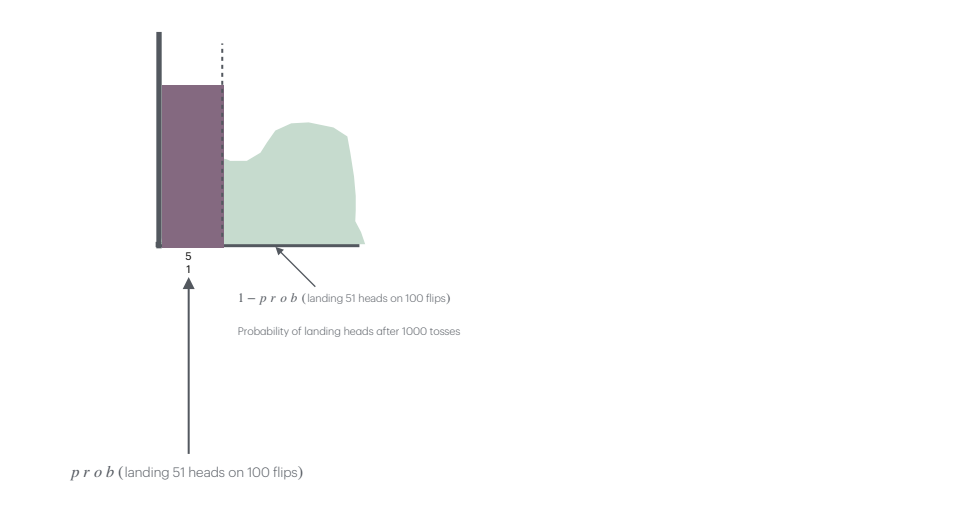
Wikipedia

Features

Head=1	Tails =0
--------	----------

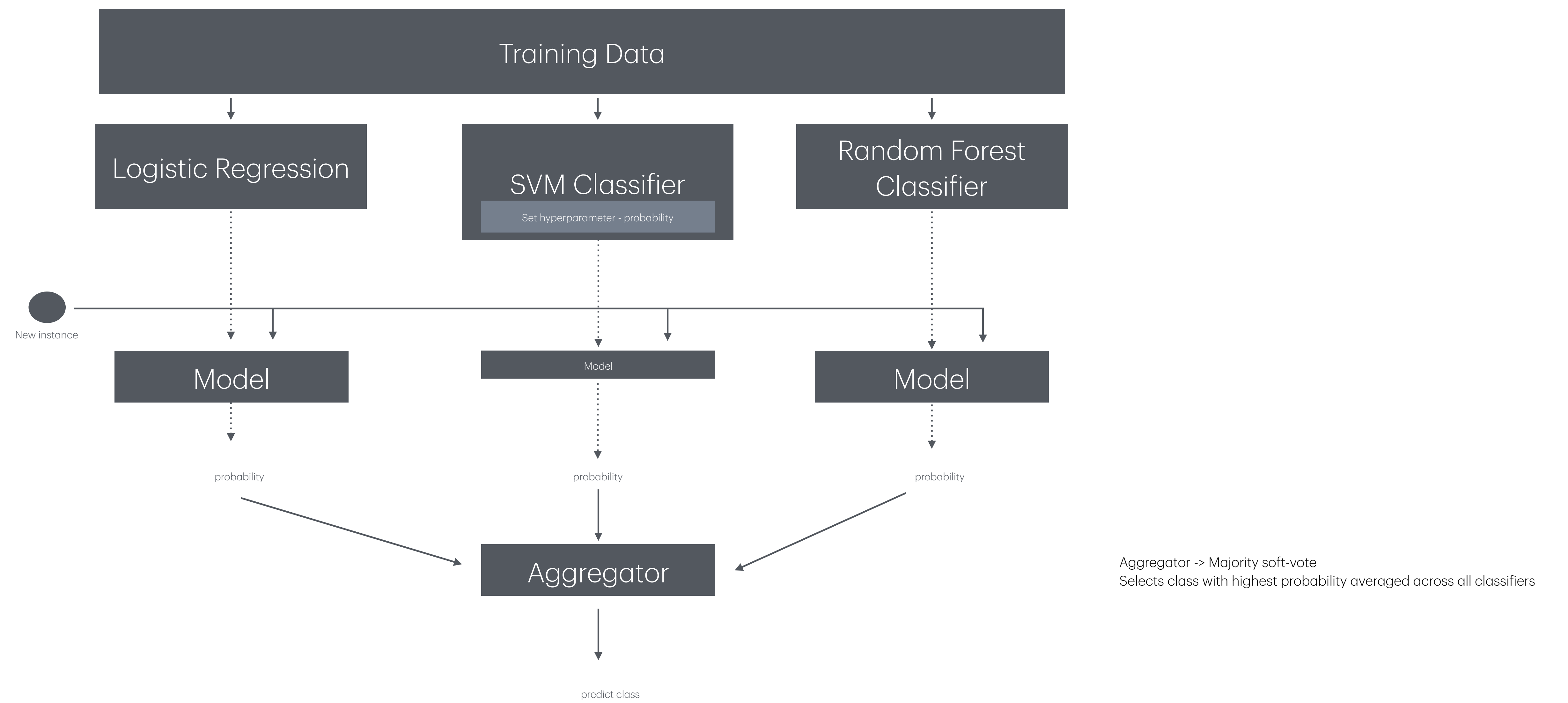


Larger rv distribution



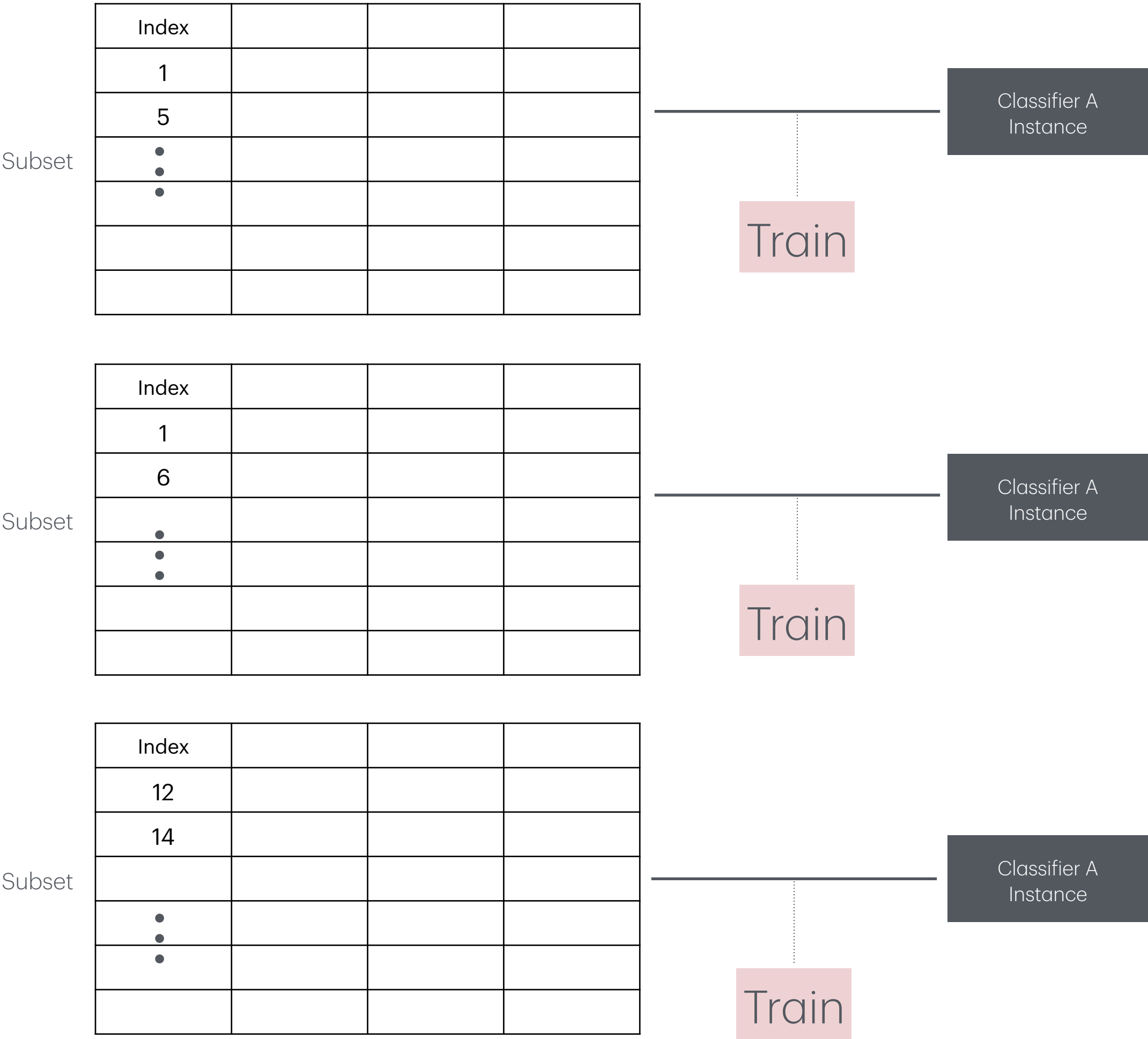
Smaller rv distribution

Soft Classifier



Bagging

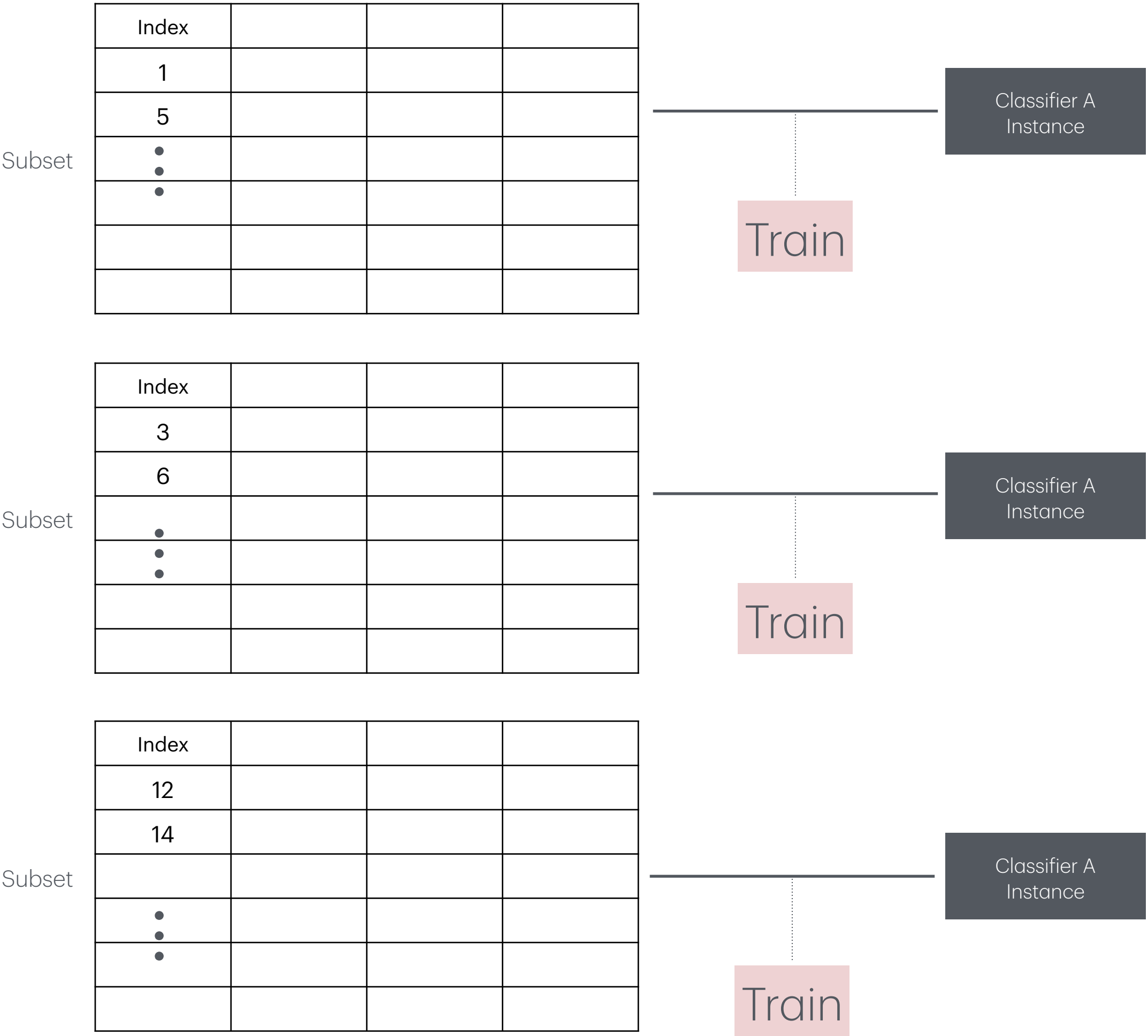
Index			
0			
1			
2			
3			
4			
5			
6			
7			
8			
9			
10			
11			
12			
13			
14			
15			



Sampling replacement. Indices can be reused by differing subsets

Pasting

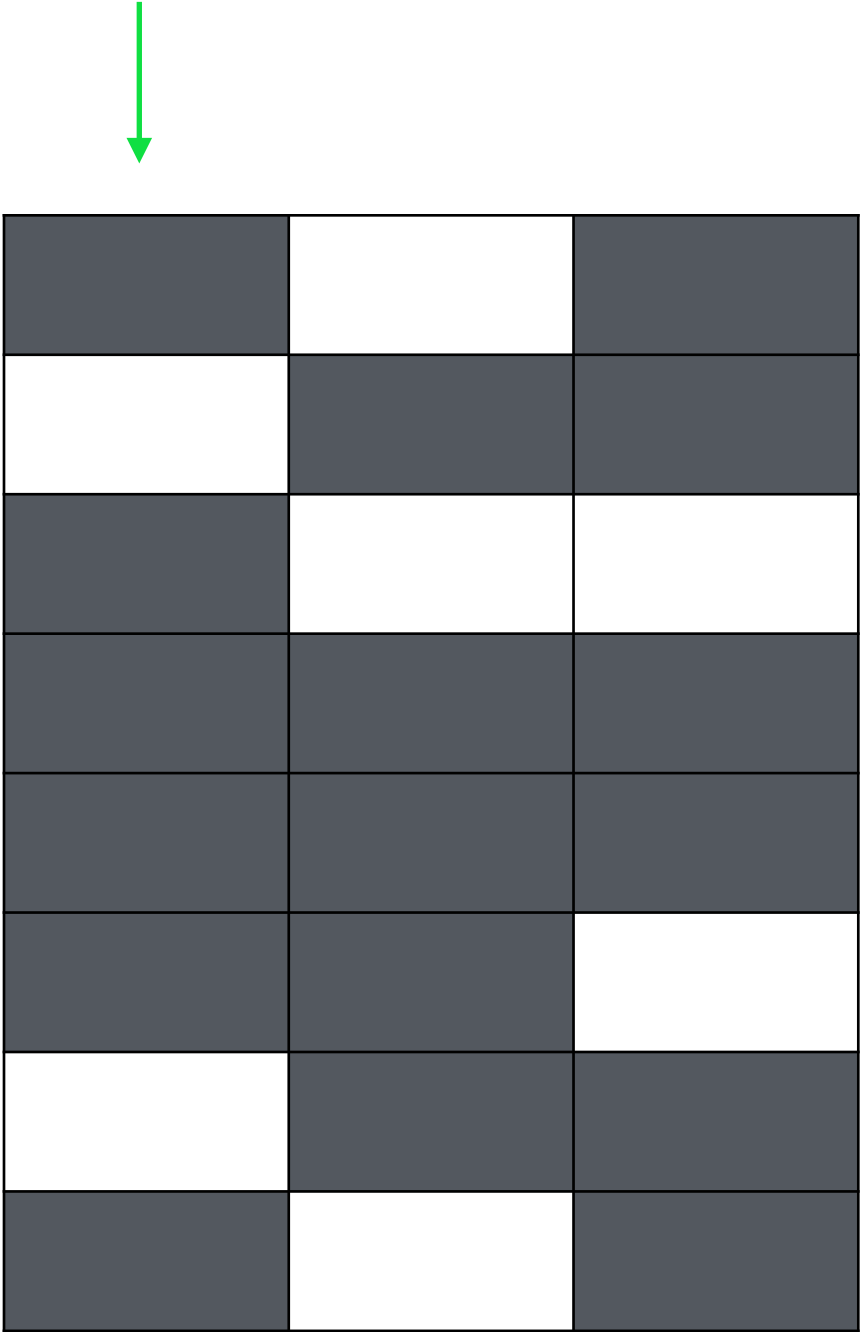
Index			
0			
1			
2			
3			
4			
5			
6			
7			
8			
9			
10			
11			
12			
13			
14			
15			



Sampling without replacement. Indices in red are not able to be fetched after usage

Random Patches

- Sampling both
- Training instances
 - Features



Classifier A



Random Subspaces

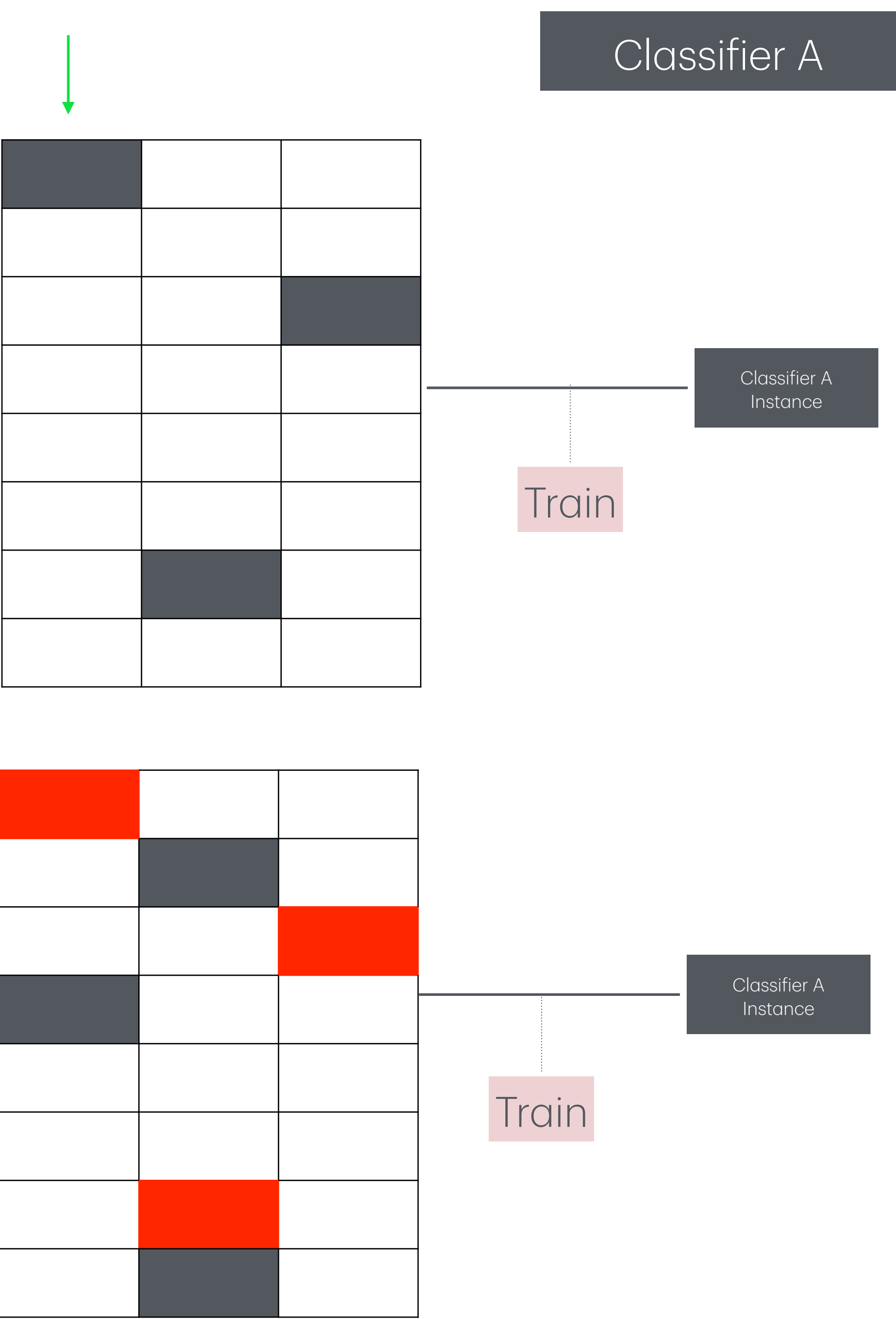
Sampling
- Features



Random Subspaces (Pasting)

Sampling
- Features

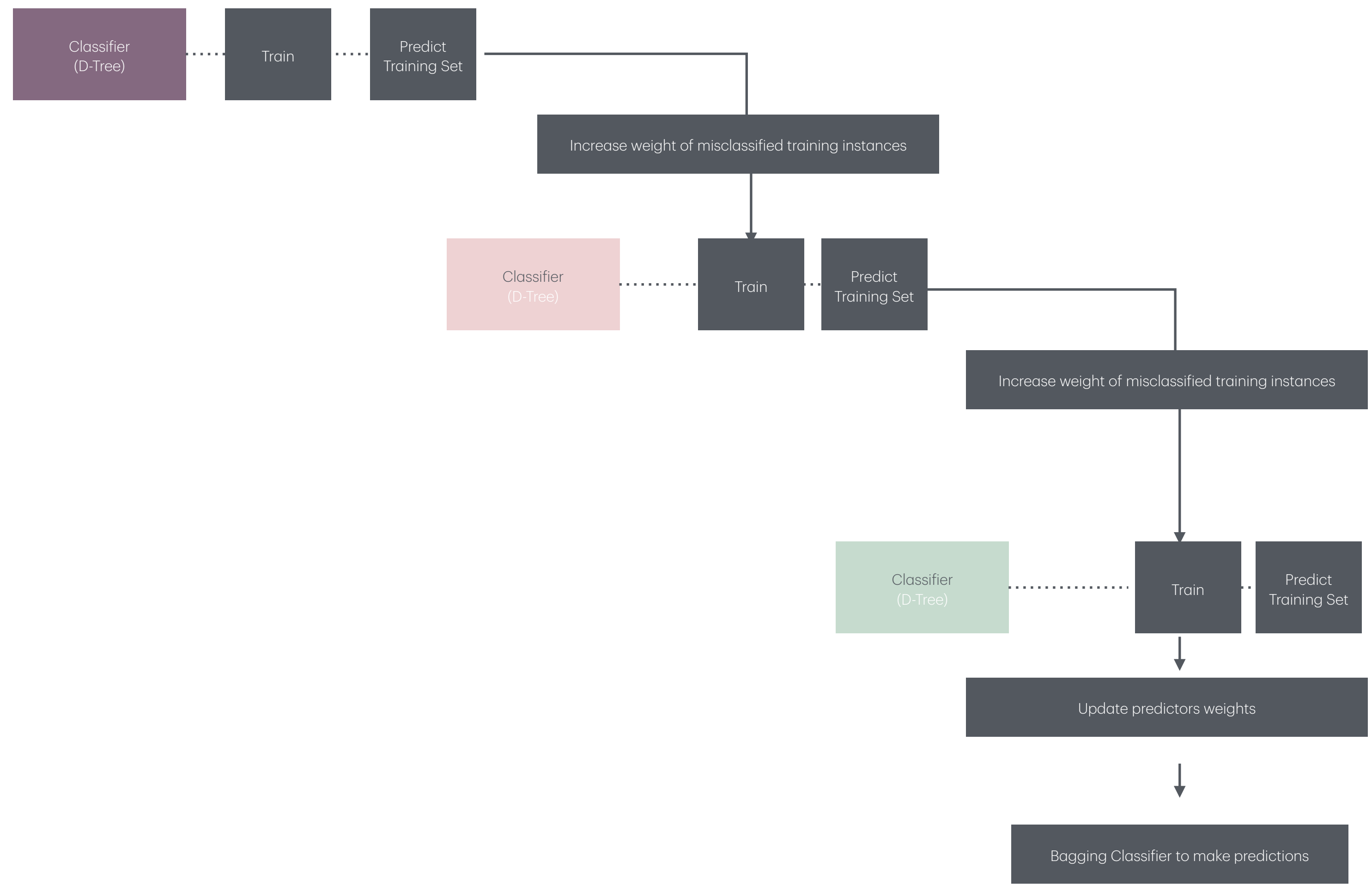
Sampling without replacement. Indices in red are not able to be fetched after usage



Feature Importance

Quick method to find feature importance

Boosting AdaBoost



AdaBoost Weights

$$w_{all} = \frac{1}{m}$$

X	Y	W
		w_r11
		w_r12
		w_r13
		w_r14

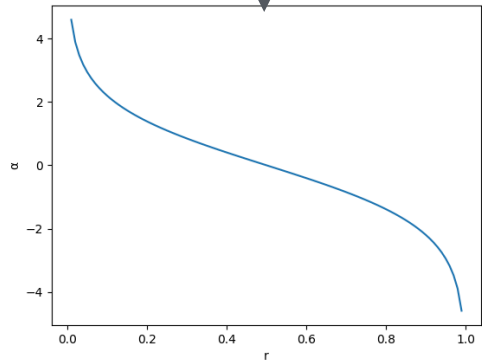
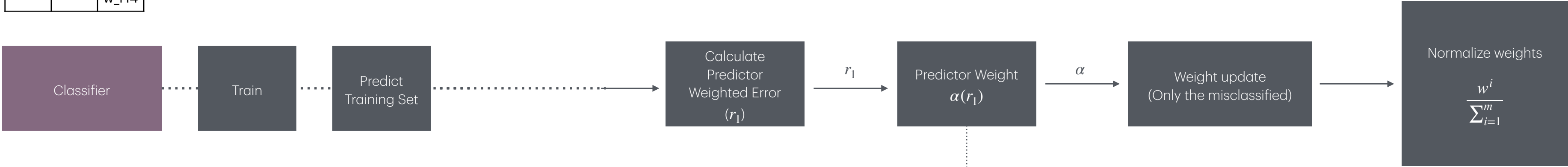
X	Y ₋	Y	W
			w_r11
			w_r12
			w_r13
			w_r14

$$r_1 = \frac{\sum_{i=1}^m w^i \cdot (Y = Y_-)}{\sum_{i=1}^m w^i}$$

$$r_1 = \frac{w^{i=2} + w^{i=4}}{w^{i=1} + w^{i=2} + w^{i=3} + w^{i=4}}$$

X	Y ₋	Y	W
			w_r11
			w_r12 * exp(a)
			w_r13
			w_r14 * exp(a)

X	Y ₋	Y	W
			w_r11
			w_r12
			w_r13
			w_r14



X	Y	W
		w_r11
		w_r12
		w_r13
		w_r14

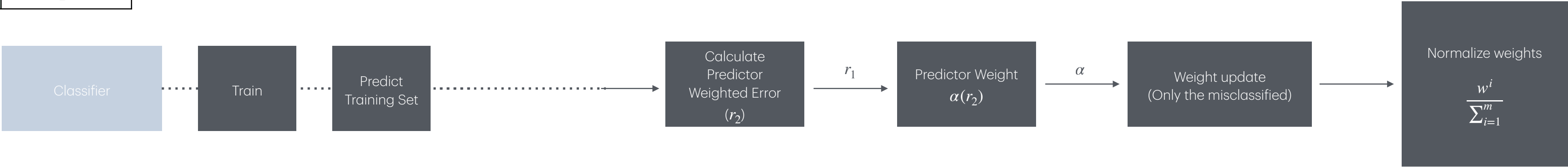
X	Y ₋	Y	W
			w_r11
			w_r12
			w_r13
			w_r14

$$r_2 = \frac{\sum_{i=1}^m w^i \cdot (Y = Y_-)}{\sum_{i=1}^m w^i}$$

$$r_1 = \frac{w^{i=2}}{w^{i=1} + w^{i=2} + w^{i=3} + w^{i=4}}$$

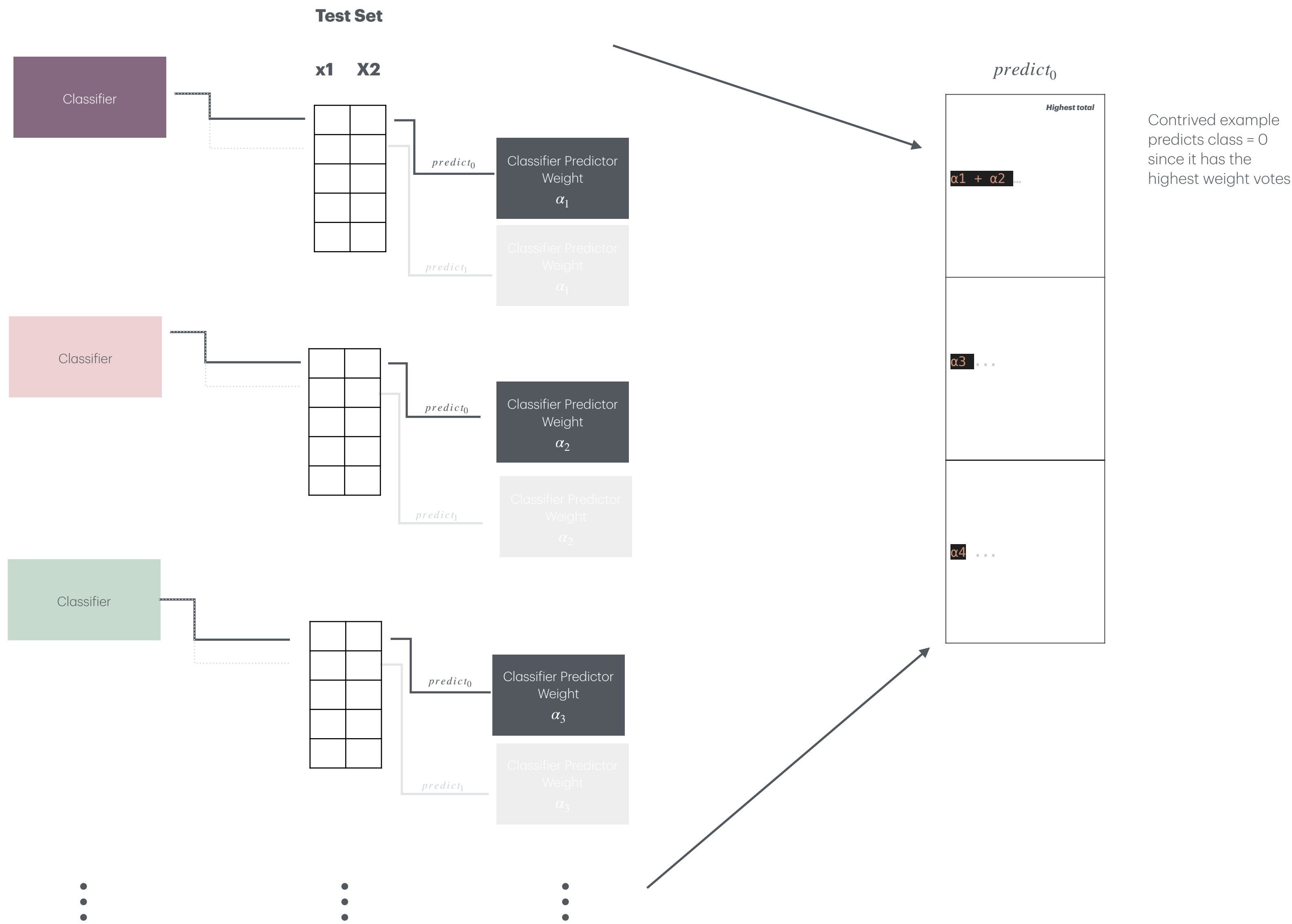
X	Y ₋	Y	W
			w_r11
			w_r12 * exp(a)
			w_r13
			w_r14

X	Y ₋	Y	W
			w_r11
			w_r12
			w_r13
			w_r14

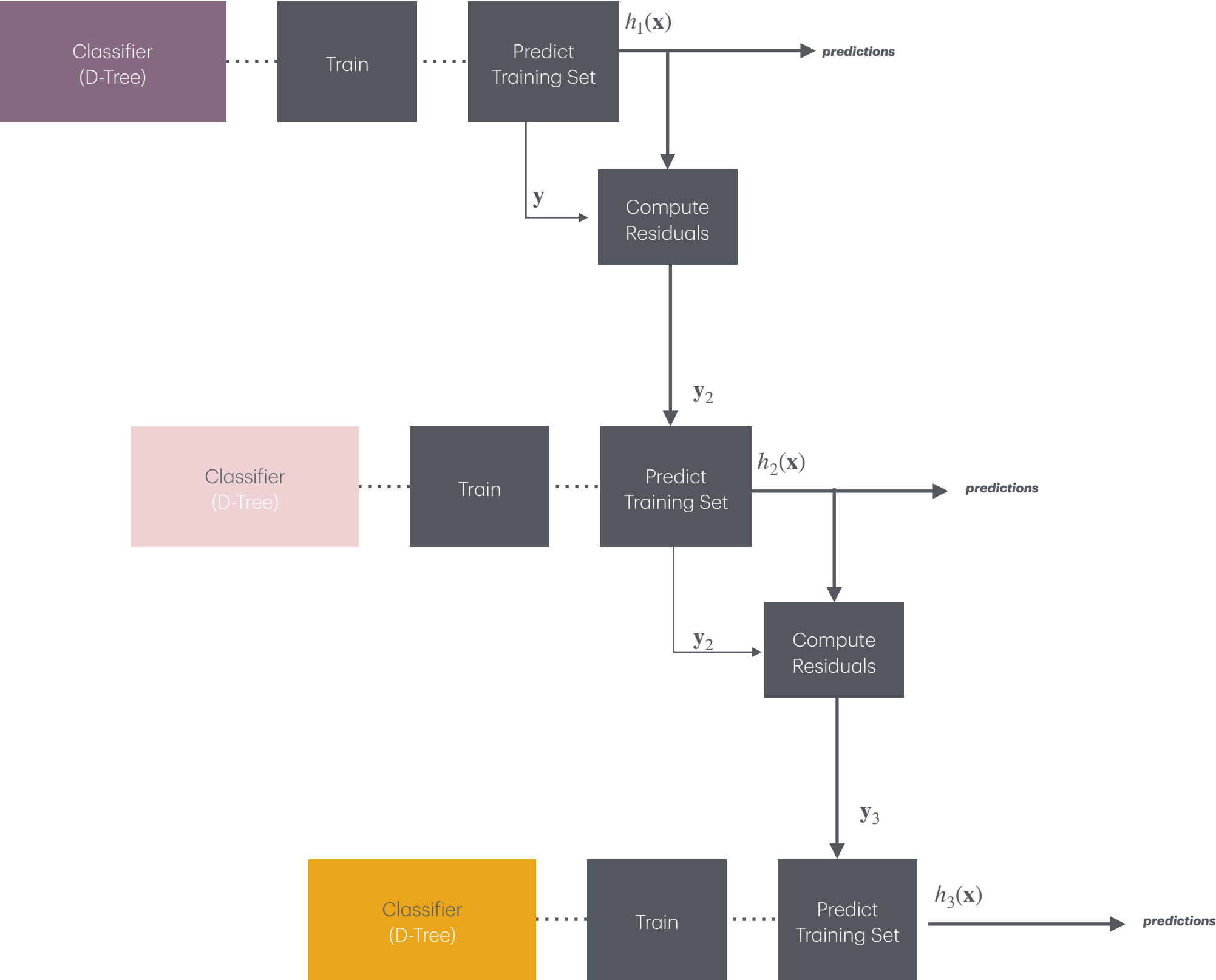


⋮

Predictions AdaBoost

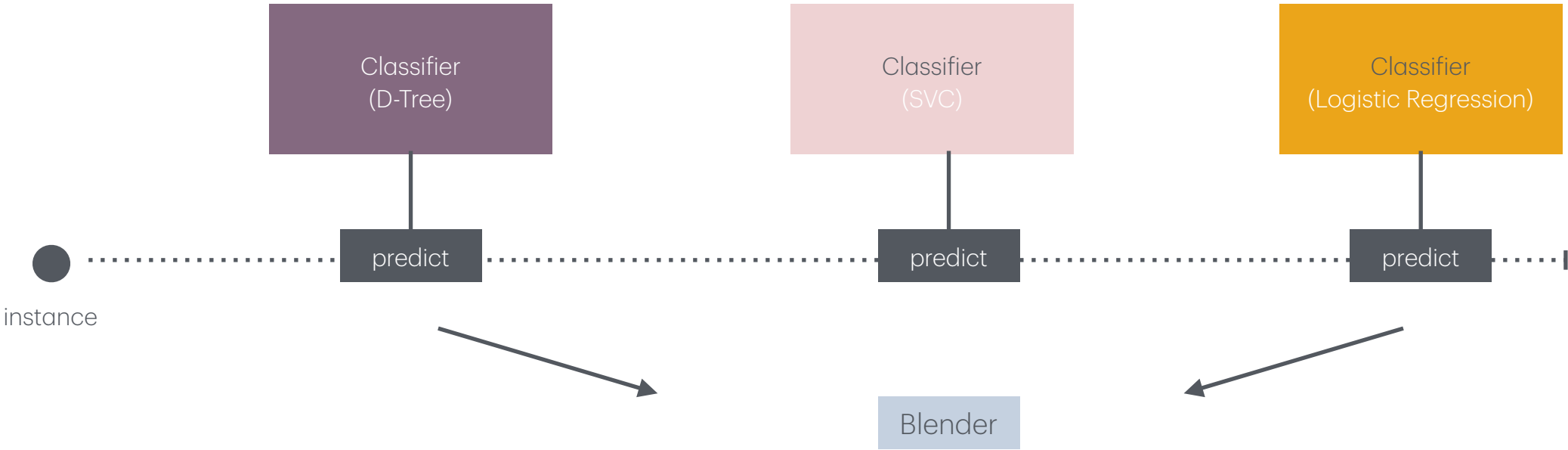


Gradient Boosting AdaBoost

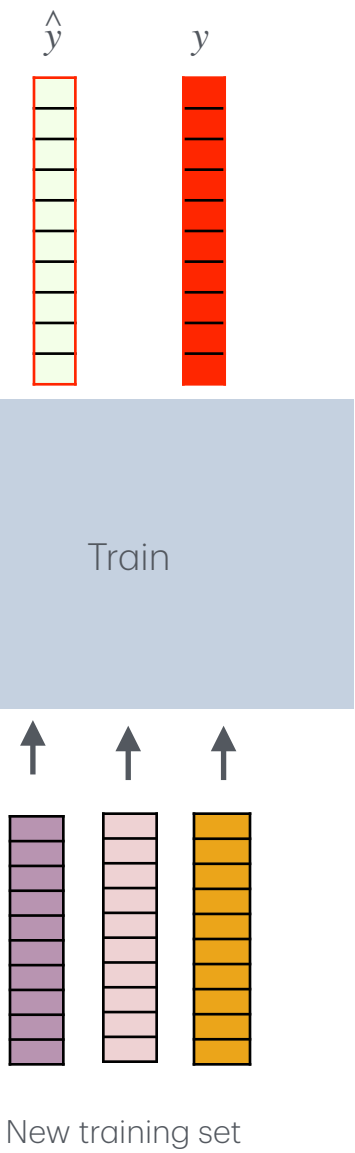
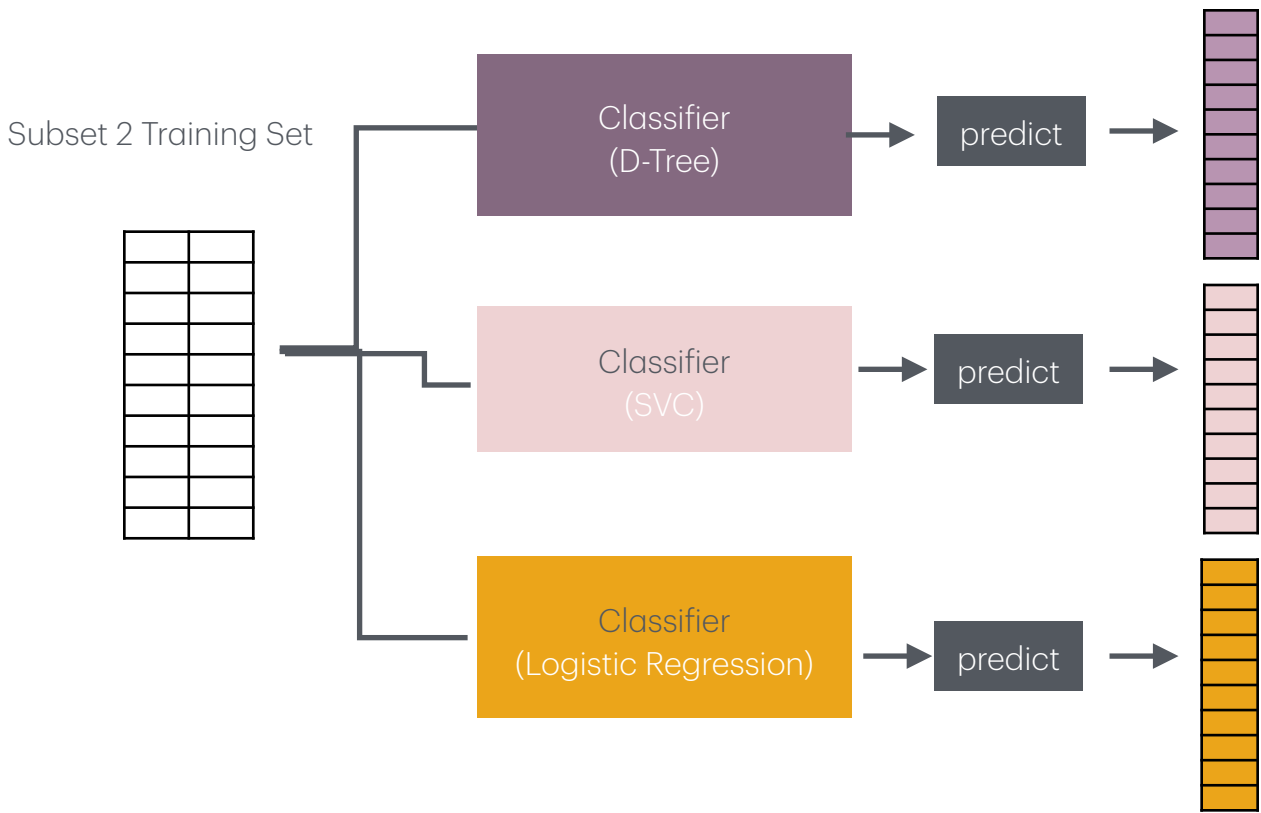
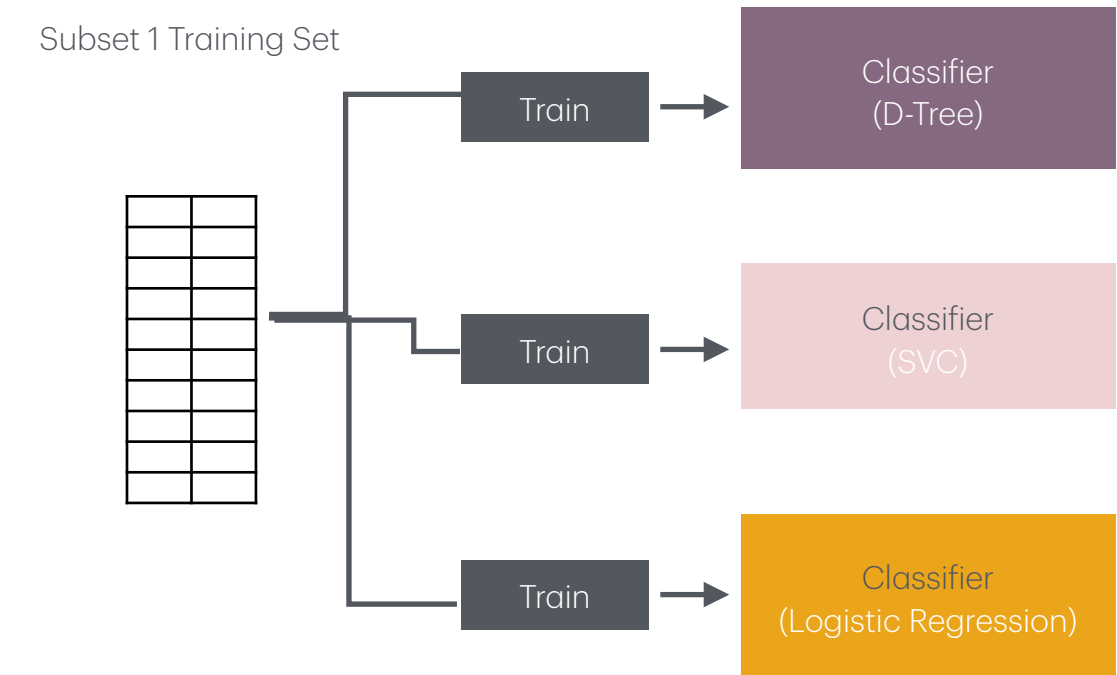


Stacking

Train a model to perform aggregation



Layer 1:
Models trained on Subset 1



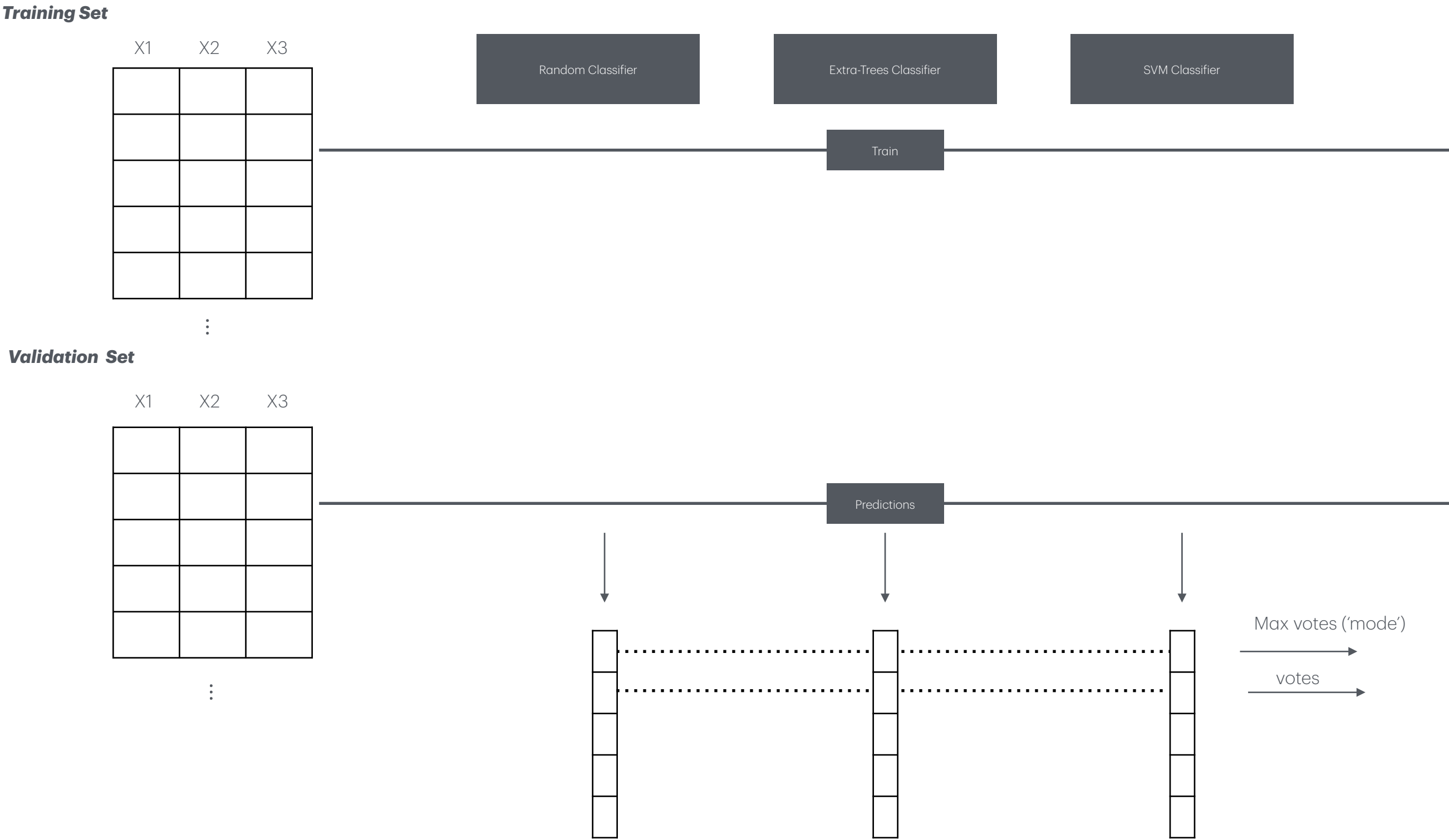
Layer 2:

Models trained on Subset 2
predictions

Blender learns to predict target
values given first layer predictions

Learning from the aggregate rather
than learning from scratch

Example 8 : Hard Voting



Example 8 : Soft Voting

Training Set

X1	X2	X3
⋮		

Random Classifier

Extra-Trees Classifier

SVM Classifier

Train

Validation Set

X1	X2	X3
⋮		

Predictions

0.9																			

0.2																			

K1																			K10
0.4																			

Average individual probabilities

K1																			K10
0.5									9.8										

Max = predicted class
 $\xrightarrow{\max k} k_{(max)}$