

Fordelinger:

$$\mu \leftarrow \bar{x}_{\cdot} = \frac{1}{n} \sum_{i=1}^n x_i \sim N(\mu, \frac{\sigma^2}{n})$$

$$\mu_i \leftarrow \bar{x}_{i\cdot} \sim N(\mu_i, \frac{\sigma^2}{n})$$

$$\mu \leftarrow \bar{x}_{\cdot\cdot} = \frac{S_{\cdot}}{n_{\cdot}} \sim N(\mu, \frac{\sigma^2}{n_{\cdot}})$$

$$\sigma^2 \leftarrow s^2 = \frac{1}{n-1} \sum_{i=1}^n (x_i - \bar{x}_{\cdot})^2 = \frac{1}{n-1} SSD = \frac{1}{n-1} (USS - \frac{S^2}{n}) \sim \sigma^2 \chi^2(f)/f$$

$$\sigma_i^2 \leftarrow s_{(i)}^2 = \frac{1}{n_i-1} \sum_{j=1}^{n_i} (x_{ij} - \bar{x}_{i\cdot})^2 \sim \sigma_i^2 \chi^2(f_{(i)})/f_{(i)} = (n_i-1)/n_i - 1$$

$$\sigma_{02}^2 \sim N(\alpha(\frac{1}{n}) + \frac{t_0^{-n}}{SSD_t} \sigma^2)$$

$$t \sim t(f_1) = t(n-1)$$

$$-2 \ln Q(x) = f_1 \ln(s_1^2) - \sum_{i=1}^k f_{(i)} \ln s_{(i)}^2 \sim \chi^2(k-1)$$

$$Ba = \frac{-2 \ln Q(x)}{C} \sim \chi^2(k-1)$$

$$\alpha \leftarrow \hat{\alpha} = \bar{x}_{\cdot} - \bar{\beta} \bar{t}_{\cdot} \sim N(\alpha, \sigma^2(\frac{1}{n} + \frac{\bar{t}_{\cdot}^2}{SSD_t}))$$

$$\alpha_i \leftarrow \hat{\alpha}_i = \bar{x}_{i\cdot} - \bar{\beta} \bar{t}_{i\cdot} \sim N(\alpha_i, \sigma_i^2(\frac{1}{n_i} + \frac{\bar{t}_{i\cdot}^2}{SSD_{ti}}))$$

$$\beta \leftarrow \hat{\beta} = \frac{SPD_{xt}}{SSD_t} \sim N(\beta, \frac{\sigma^2}{SSD_t})$$

$$\beta_i \leftarrow \hat{\beta}_i = \frac{SPD_{xt}}{SSD_t} \sim N(\beta_i, \frac{\sigma_i^2}{SSD_{ti}})$$

$$\hat{\alpha} + \hat{\beta} t \sim N(\alpha + \beta t, \sigma^2(\frac{1}{n} + \frac{(t - \bar{t}_{\cdot})^2}{SSD_t}))$$

Formler

$$S_x = \sum_{i=1}^n x_i$$

$$S_t = \sum_{i=1}^n t_i$$

$$USS_x = \sum_{i=1}^n x_i^2$$

$$USS_t = \sum_{i=1}^n t_i^2$$

$$SSD_x = \sum_{i=1}^n (x_i - \bar{x}.)^2$$

$$SSD_t = \sum_{i=1}^n (t_i - \bar{t}.)^2$$

$$SP_{xt} = \sum_{i=1}^n x_i t_i$$

$$SPD_{xt} = \sum_{i=1}^n (x_i - \bar{x}.)(t_i - \bar{t}.)$$

$$\hat{\sigma}^2 = \frac{1}{n-2} \sum_{i=1}^n \{x_i - (\hat{\alpha} + \hat{\beta}t_i)\}^2$$

$$C = 1 + \frac{1}{3(k-1)} \left[\left(\sum_{i=1}^k \frac{1}{f(i)} \right) - \frac{1}{f_1} \right]$$

$$SSD_2 = SSD_{02} - SSD_1$$

Konfidensintervaller:

Binomialfordelinger Hvis: $M_b : X \sim b(n, \pi)$, er 95% konfidensintervallet for π

$$\pi_- = \frac{1}{n + 1.96^2} \left[x + \frac{1.96^2}{2} - 1.96 \sqrt{\frac{x(n-x)}{n} + \frac{1.96^2}{4}} \right]$$

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$$\pi_+ = \frac{1}{n + 1.96^2} \left[x + \frac{1.96^2}{2} + 1.96 \sqrt{\frac{x(n-x)}{n} + \frac{1.96^2}{4}} \right]$$

$$C_{0.95}(x) = \{\pi_0 | H_0 : \pi = \pi_0 \text{ forkastes ikke med niveau } 0.05 \text{ test}\} = [\pi_-, \pi_+]$$

Normalfordelt observationrække med ukendt varians: 95% for σ^2

$$\left[\frac{(n-1)s^2}{\chi_{1-\frac{\alpha}{2}}^2(n-1)}, \frac{(n-1)s^2}{\chi_{\frac{\alpha}{2}}^2(n-1)} \right]$$

Pobs test

Binomialfordeling:

Test for $H_{0\pi} := \pi_1 = \dots = \pi_n = x$

$$-2\ln Q(x) = 2 \sum_{i=1}^n x_i \ln\left(\frac{x_i}{e_1}\right) \sim \chi^2(k-1-d), \text{ k er observationsrækker, d er frie variabler}$$

p_{obs} test

$$p_{obs} = 1 - F_{\chi^2(k-1-d)}(-2\ln Q(x))$$

En normalt fordelte observationsrækker

Test af ens varians:

$$F = \frac{s_{tæller}^2}{s_{nævner}^2}$$
$$p_{obs} = \begin{cases} 2F_{F(f_{(tæller)}, f_{(nævner)})}\left(\frac{s_{(tæller)}^2}{s_{(nævner)}^2}\right) & \text{hvis } \frac{s_{(tæller)}^2}{s_{(nævner)}^2} < 1 \\ 2\left[1 - F_{F(f_{(tæller)}, f_{(nævner)})}\left(\frac{s_{(tæller)}^2}{s_{(nævner)}^2}\right)\right] & \text{hvis } \frac{s_{(tæller)}^2}{s_{(nævner)}^2} > 1 \end{cases}$$