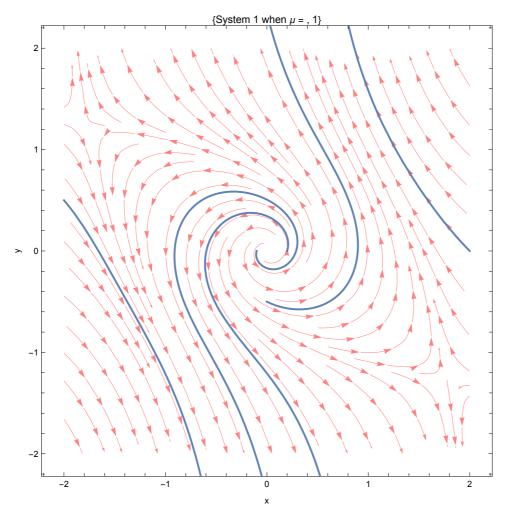
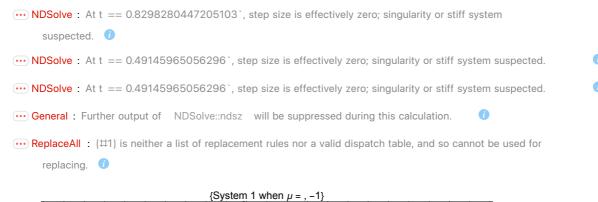
3.2

```
d)
      SYSTEM1
In[49]:= ClearAll["Global`*"]
      (*{\mu*x-3*y-1*x^3,3*x+\mu*y+2*y^3}*)
       (*Define systems*)
      mu = 1;
      eq1 = x'[t] = mu * x[t] - 3 * y[t] - 1 * x[t] ^3;
      eq2 = y'[t] == 3 * x[t] + mu * y[t] + 2 * y[t]^3;
      system = {eq1, eq2};
      startPt = \{\{x[0] = -2, y[0] = 0.5\}, \{x[0] = 0.2, y[0] = 0\},
           \{x[0] = -0.1, y[0] = 0\}, \{x[0] = 2, y[0] = 0\}, \{x[0] = 0, y[0] = -0.5\}\};
      t0 = 0;
      tMax = 5;
      sol = Table[NDSolve[{system, mu}, {x, y}, {t, t0, tMax}], {mu, startPt}];
      sp = StreamPlot[\{mu * x - 3 * y - 1 * x^3, 3 * x + mu * y + 2 * y^3\},
           \{x, -2, 2\}, \{y, -2, 2\}, StreamColorFunction \rightarrow None,
           StreamStyle → Pink, PlotRange → All, ImageSize → 500];
      tp = ParametricPlot[Evaluate[{x[t], y[t]} /. #] & /@ sol, {t, t0, tMax}];
      Show[sp, tp, FrameLabel \rightarrow {"x", "y"}, PlotLabel \rightarrow {"System 1 when \mu = ", mu}]
      ••• NDSolve: At t == 0.4459972190136199`, step size is effectively zero; singularity or stiff system
      ••• NDSolve: At t == 1.6955137738977624`, step size is effectively zero; singularity or stiff system
           suspected.
      ••• NDSolve: At t == 2.6168319771891846`, step size is effectively zero; singularity or stiff system
           suspected. 0
      General: Further output of NDSolve::ndsz will be suppressed during this calculation.
      error ReplaceAll: {#1} is neither a list of replacement rules nor a valid dispatch table, and so cannot be used for
           replacing.
```

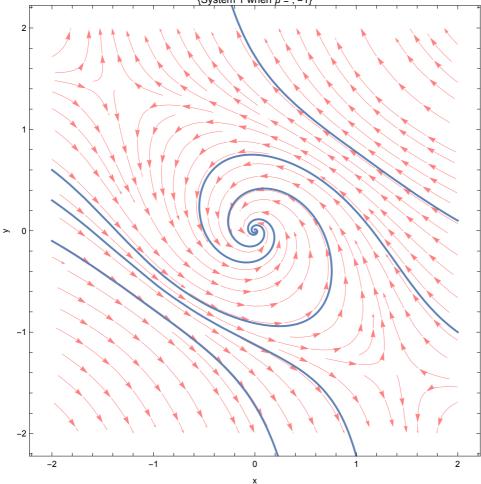




```
In[13]:= ClearAll["Global`*"]
      (*{\mu*x-3*y-1*x^3,3*x+\mu*y+2*y^3}*)
      (*Define systems*)
      mu = -1;
      eq1 = x'[t] = mu * x[t] - 3 * y[t] - 1 * x[t]^3;
      eq2 = y'[t] = 3 * x[t] + mu * y[t] + 2 * y[t]^3;
      system = {eq1, eq2};
      startPt = \{\{x[0] = -2, y[0] = 0.6\}, \{x[0] = -2, y[0] = 0.3\},
          \{x[0] = -2, y[0] = -0.1\}, \{x[0] = 2, y[0] = -1\}, \{x[0] = 2, y[0] = 0.1\}\};
      t0 = 0;
      tMax = 5;
      sol = Table[NDSolve[{system, mu}, {x, y}, {t, t0, tMax}], {mu, startPt}];
      sp = StreamPlot[\{mu * x - 3 * y - 1 * x^3, 3 * x + mu * y + 2 * y^3\},
          \{x, -2, 2\}, \{y, -2, 2\}, StreamColorFunction \rightarrow None,
          StreamStyle → Pink, PlotRange → All, ImageSize → 500];
      tp = ParametricPlot[Evaluate[{x[t], y[t]} /. #] & /@ sol, {t, t0, tMax}];
      Show[sp, tp, FrameLabel \rightarrow {"x", "y"}, PlotLabel \rightarrow {"System 1 when \mu = ", mu}]
```



Out[24]=

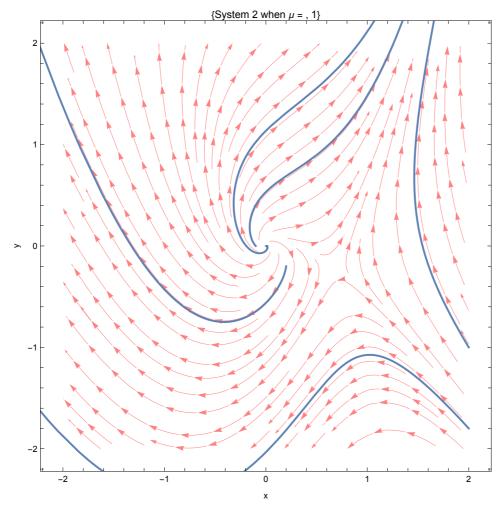


System 1 is subcritical when mu =0

SYSTEM 2

```
In[25]:= ClearAll["Global`*"]
                  (*{\mu*x+y-x^2},
                                                                                       -x+\mu*y+2*x^2*
                  (*Define systems*)
                  mu = 1;
                  eq1 = x'[t] = mu * x[t] + y[t] - x[t]^2;
                  eq2 = y'[t] = -x[t] + mu * y[t] + 2 * x[t]^2;
                  system = {eq1, eq2};
                  startPt = \{\{x[0] == 0, y[0] == 0\}, \{x[0] == 0.01, y[0] == 0\}, \{x[0] == -0.1, y[0] == 0\}, \{x[0] == 0, y[0] == 0, y[0] == 0\}, \{x[0] == 0, y[0] == 0, y[0] == 0\}, \{x[0] == 0, y[0] == 0, y[0] == 0\}, \{x[0] == 0, y[0] == 0, y[0] == 0\}, \{x[0] == 0, y[0] == 0, y[0] == 0\}, \{x[0] == 0, y[0] == 0, y[0] == 0\}, \{x[0] == 0, y[0] == 0, y[0] == 0\}, \{x[0] == 0, y[0] == 0, y[0] == 0\}, \{x[0] == 0, y[0] == 0, y[0] == 0\}, \{x[0] == 0, y[0] == 0, y[0] == 0\}, \{x[0] == 0, y[0] == 0, y[0] == 0, y[0] == 0\}, \{x[0] == 0, y[0] == 0, y[0] == 0, y[0] == 0\}, \{x[0] == 0, y[0] == 0, y[0] == 0\}, \{x[0] == 0, y[0] == 0, y[0] == 0\}, \{x[0] == 0, y[0] == 0, y[0] == 0\}, \{x[0] == 0, y[0] == 0, y[0] == 0\}, \{x[0] == 0, y[0] == 0, y[0] == 0\}, \{x[0] == 0, y[0] == 0, y[0] == 0\}, \{x[0] == 0, y[0] == 0, y[0] == 0, y[0] == 0\}, \{x[0] == 0, y[0] == 0, y[0] == 0, y[0] == 0\}, \{x[0] == 0, y[0] == 0, y[0] == 0, y
                             \{x[0] = 2, y[0] = -1\}, \{x[0] = 0.2, y[0] = -0.2\}, \{x[0] = 2, y[0] = -1.8\}\};
                  t0 = 0;
                  tMax = 5;
                  sol = Table[NDSolve[{system, mu}, {x, y}, {t, t0, tMax}], {mu, startPt}];
                  sp = StreamPlot[\{mu * x + y - x^2, -x + mu * y + 2 * x^2\},
                             \{x, -2, 2\}, \{y, -2, 2\}, StreamColorFunction \rightarrow None,
                             StreamStyle → Pink, PlotRange → All, ImageSize → 500];
                  tp = ParametricPlot[Evaluate[{x[t], y[t]} /. #] & /@ sol, {t, t0, tMax}];
                  Show[sp, tp, FrameLabel \rightarrow {"x", "y"}, PlotLabel \rightarrow {"System 2 when \mu = ", mu}]
                  ••• NDSolve: At t == 2.4530200668708932`, step size is effectively zero; singularity or stiff system
                                suspected.
                  \bigcirc NDSolve : At t == 2.246107618300271`, step size is effectively zero; singularity or stiff system
                  error ReplaceAll: {#1} is neither a list of replacement rules nor a valid dispatch table, and so cannot be used for
                               replacing.
```



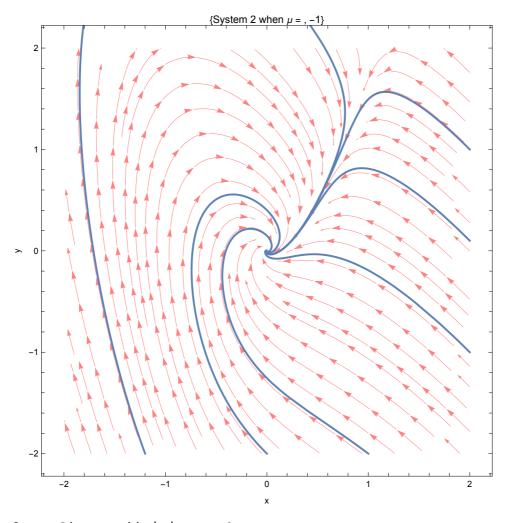


```
In[37]:= ClearAll["Global`*"]
      (*{\mu*x+y-x^2},
                             -x+\mu*y+2*x^2*
      (*Define systems*)
     mu = -1;
      eq1 = x'[t] = mu * x[t] + y[t] - x[t]^2;
      eq2 = y'[t] = -x[t] + mu * y[t] + 2 * x[t]^2;
      system = {eq1, eq2};
      startPt = \{\{x[0] = 1, y[0] = -2\}, \{x[0] = 0, y[0] = -2\}, \{x[0] = -1.2, y[0] = -2\},
          \{x[0] = 2, y[0] = -1\}, \{x[0] = 2, y[0] = 0.1\}, \{x[0] = 2, y[0] = 1\}\};
      t0 = 0;
      tMax = 5;
      sol = Table[NDSolve[{system, mu}, {x, y}, {t, t0, tMax}], {mu, startPt}];
      sp = StreamPlot[\{mu * x + y - x^2, -x + mu * y + 2 * x^2\},
          \{x, -2, 2\}, \{y, -2, 2\}, StreamColorFunction \rightarrow None,
          StreamStyle → Pink, PlotRange → All, ImageSize → 500];
      tp = ParametricPlot[Evaluate[{x[t], y[t]} /. #] & /@ sol, {t, t0, tMax}];
      Show[sp, tp, FrameLabel \rightarrow {"x", "y"}, PlotLabel \rightarrow {"System 2 when \mu = ", mu}]
```

6 | HW31f.nb

••• ReplaceAll: {#1} is neither a list of replacement rules nor a valid dispatch table, and so cannot be used for replacing. 0

Out[48]=



System 2 is supercritical when mu =0