## Home Assignment 2

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## Solutions

1. "A rotor on a helicopter has four blades and rotates with 4 500 revolutions/minute, counter clockwise, (note, revolutions/minute). The rotor is filmed with a digital camera that takes 50 pictures/second. What will the perceived rotation speed be when watching the recorded film sequence? What will be the resulting direction of rotation? How does it look if the rotor goes slightly slower, with 4 499 revolutions/minute?"

Let the frequency of the helicopters' rotor be  $4500rpm = \frac{4500}{60}Hz = 75Hz$ . The video camera does the sampling with  $F_s = 50Hz$ . This means we get the relative frequency  $f = \frac{75Hz}{50Hz} = 1.5 = 0.5 + 1$ . Since we are under-sampling, the video of the rotor is only going to show f = 0.5(half a turn). When really the rotors are spinning 1.5 turns per picture.

If we then can't distinguish between the four rotor blades, it will look like the rotorblades are static in place.

Lets now assume the helicopters' rotor is spinning at 4499rpm = 74.98Hz. With this we get f = 1.499 = 0.499 + 1. Now the video camera shows 0.499 revolutions per minute. This will give the effect of a slow movement clockwise (The rotor is actually spinning  $counter\ clockwise$ ).

We could also take an extra look at the rotor: Because the four rotor blades are seated in a +-sign, only rotations less than  $\frac{\pi}{2}rad$  can be distinguished. This means the f in the first case can be written as f=1.5=0+0.25\*6 which means that the rotor blades appears to stand still. The second case can be written as f=1.499=(-0.001)+0.25\*6 where the blade appears to have a relative frequency of -0.001.

2. "The following discrete-time signals are given:"

$$x_1(n) = \begin{bmatrix} 1 & \underline{-3} & -1 & 3 \end{bmatrix}, x_2(n) = \begin{bmatrix} \underline{-1} & -1 & 2 & -2 & 1 & -2 \end{bmatrix}$$

"Determine the following: (3 out of 4 correct answers gives full points.)"

(a) "The linear convolution of the sequences, that is,  $y(n) = x_1(n) * x_2(n)$ ."

$$y(n) = x_1(n) * x_2(n) = \begin{bmatrix} 1 & \underline{-3} & -1 & 3 \end{bmatrix} * \begin{bmatrix} \underline{-1} & -1 & 2 & -2 & 1 & -2 \end{bmatrix}$$

- (b) ""
- (c) "The linear correlation of the sequences, that is,  $r_{x_1x_2}(n) = x_1(n) * x_2(-n)$ ."

$$x_1(n) = \begin{bmatrix} 1 & \underline{-3} & -1 & 3 \end{bmatrix}, x_2(-n) = \begin{bmatrix} -2 & 1 & -2 & 2 & -1 & \underline{-1} \end{bmatrix}$$

Do not know how to perform circular convolution.

$$x_1 * x_2 = \begin{bmatrix} x_{11} & 1 & x_{11} & x$$

(d) ""

- Also circular convolution
- 3. "Signals are sampled, down sampled or up sampled and reconstructed ideally according to the items below. Determine what the resulting signal will be."
  - (a) "The signal cos(2450t) is sampled using Fs = 1000 Hz, and then down sampled by a factor 3 (that is, only every third sample value is kept). The resulting signal is then ideally reconstructed (using Fs = 1000 Hz)."
  - (b)