

**Problem Set #7- Due 10/18/17**

You are to compute the decision problem of an agent in a nonstochastic growth model facing different prices using different interpolation methods. There is a unit measure of agents. Let lower case letters denote individual holdings and uppercase letters denote aggregates. The preferences of any agent are given by

$$\sum_{\tau=0}^{\infty} \beta^{\tau} \ln(c_{\tau})$$

where  $\beta = 0.99$ . The production technology is given by

$$Y_t = K_t^{\alpha} L_t^{1-\alpha}$$

where  $\alpha = 0.36$  and capital depreciates fully each period. Agents have 1 unit of time. Agents are endowed with initial capital  $k_0$  and can rent their capital  $k_t \in [0, \infty)$  to firms and receive rate of return  $r_t$ . Without loss of generality, we can consider one firm which hires all workers so that  $L_t = 1$  and rents  $K_t = K$  units of capital so that wages  $w_t$  and rental rates  $r_t$  are given by their marginal products:

$$\begin{aligned} w(K) &= (1 - \alpha)K^{\alpha} \\ r(K) &= \alpha K^{\alpha-1} \end{aligned} \tag{1}$$

Consumers solve

$$v(k; K) = \max_{c, k'} u(c) + \beta v(k'; K)$$

s.t.

$$c + k' = r(K)k + w(K)$$

as well as (1).

1. Solve for a closed form solution of the value function and decision rules using the method of undetermined coefficients when  $k = K$ .
2. Let  $K \in [0.15, 0.25]$  and  $k \in [0, 0.5]$ . Solve for the value function and decision rules using
  - a. Bilinear interpolation.
  - b. Cubic splines in the  $k$  dimension and linear interpolation in the  $K$  dimension.
3. Compare your results from the closed form solution to the computational solution when  $k = K$ .