

# Sudoku Solver Using Backtracking

Heet Shah(2021A7PS0125U) & Arjun Nadar(2021A7PS0062U)

The algorithm used to solve the sudoku puzzle is **Backtracking**. It is basically an add on to the CSP algorithm and uses constraints to solve the problem.

## Initialization:

The backtracking algorithm begins with an initial partially filled Sudoku grid. It aims to find a solution by systematically trying different combinations of numbers in the empty cells.

## Recursive Approach:

The algorithm adopts a recursive approach to explore possible solutions. At each step, it selects an empty cell and tries digits from 1 to 9 to fill that cell.

## Constraint Satisfaction:

Before placing a digit in a cell, the algorithm checks if the placement satisfies the Sudoku Rules:

- No duplicate digits in the same row.
- No duplicate digits in the same column.
- No duplicate digits in the same 3x3 subgrid.

If the placement violates any of these constraints, the algorithm backtracks and explores a different digit for that cell.

## Backtracking Mechanism:

If the algorithm encounters a dead-end where no valid digit can be placed in an empty cell, it backtracks to the previous step.

Backtracking involves undoing the previous assignment and trying a different digit in the previous cell.

By backtracking, the algorithm explores alternative paths and continues the search for a valid solution.

## Exploration of Solution Space:

The algorithm continues this process of recursion and backtracking until it finds a valid solution or exhausts all possibilities.

It systematically explores the solution space, trying different combinations of digits in the empty cells until a valid solution is found.

## Optimization Techniques:

While the basic backtracking algorithm guarantees finding a solution (if one exists), optimization techniques can be applied to improve efficiency:

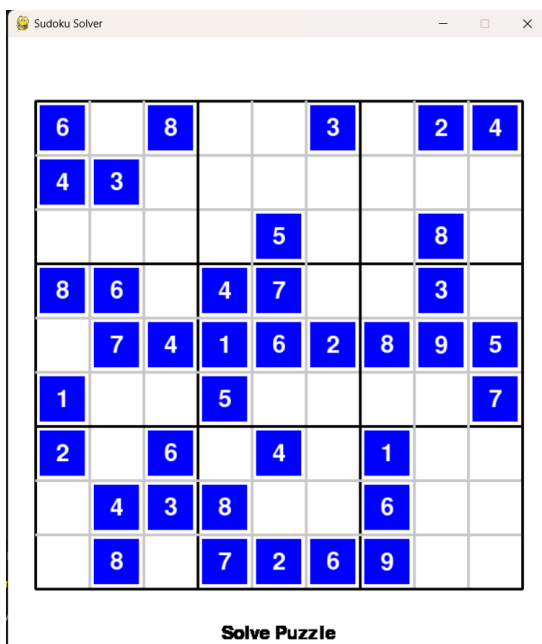
Heuristic selection of the next empty cell to reduce the search space.  
Forward checking to eliminate invalid choices early in the process.  
Constraint propagation techniques to prune the search tree.

### Complexity Analysis:

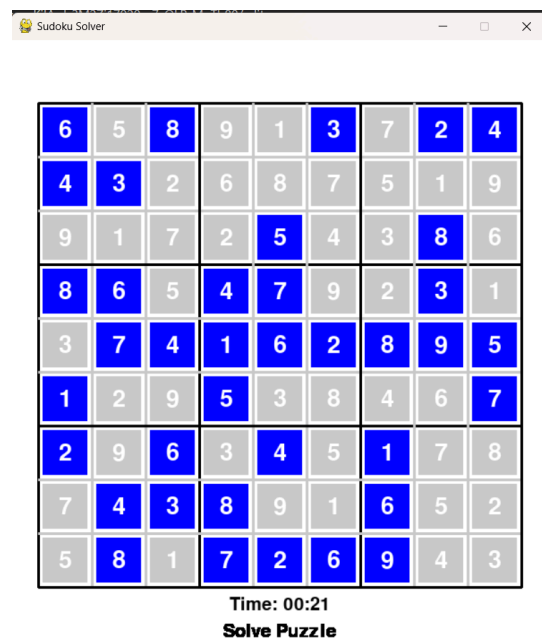
The time complexity of the backtracking algorithm for Sudoku depends on the number of empty cells in the initial puzzle.

In the worst-case scenario, where the puzzle is mostly empty, the algorithm explores a large solution space, resulting in exponential time complexity.

However, for typical Sudoku puzzles, the algorithm performs efficiently and finds solutions quickly.



Unsolved Puzzle



Solved Puzzle