

Tracking ALMA System Temperature with Water Vapor Data at High Frequency

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ABSTRACT

As the world-leading submillimeter telescope, the ALMA observatory is now putting more focus on high-frequency observations at Band 7 – 10 (frequencies from 300 – 890 GHz). However, high-frequency observations often suffer from rapid variations in atmospheric opacity that directly affects the measured system temperature T_{sys} . Current T_{sys} measurements use discrete atmosphere (ATM) calibrations done every few minutes, which usually involve 10 ~ 20 ATM calibrations within a <2 hour observation at high frequencies. In order to obtain more accurate flux measurements and reduce the number of ATM calibrations, a new method to monitor T_{sys} continuously is proposed using existing data in the measurement set. In this work, we demonstrate the viability of using water vapor radiometer (WVR) data to track the T_{sys} continuously. We find a tight linear correlation between T_{sys} measured using the traditional method and T_{sys} extrapolated based on WVR data with scatter of 0.5% – 3%. Although the exact form of the linear relation varies among different data sets and spectral windows, we can use a small number of discrete T_{sys} measurements to fit the linear relation and use this heuristic relationship to derive T_{sys} every 10 seconds. We also test this correlation with atmospheric transmission (ATM) modeling and find a good agreement on results between modeled data and the real observation. We apply the semi-continuous T_{sys} method on a few data sets from Band 7 to Band 10 and compare the flux measured using these methods. We find the discrete and continuous T_{sys} methods give us consistent flux measurements with differences up to 5%. Furthermore, the calibrated fluxes from different subsets of the observation, or for different observations of the same target, are slightly more consistent with the continuous T_{sys} method. This method can help to save up to 10% of time for ALMA high-frequency observations.

1. INTRODUCTION

1.1. Flux Calibration in ALMA

Calibration is the process by which the astronomer converts electronic signals from the telescope into meaningful astronomical data. Accurate calibration is crucial for the Atacama Large Millimeter/submillimeter Array (ALMA), as millimeter and submillimeter wavelength radiation will be adversely affected by the atmosphere and the electronic signal path in a variety of ways, and the antennas will also be affected by the observing environment (Remjian et al. 2019, ALMA technical handbook, Chapter 10). One of the important calibration processes is the amplitude and flux calibration. The aim of this calibration is to convert the raw visibilities (and auto-correlations) from the correlator into brightness temperature or flux density by carefully tracking the instrumental and atmospheric variations and determining accurate conversion factors. Because of the large and rapidly varying opacity of water vapor, standard calibration procedures are less accurate at submillimeter wavelengths. For the flux calibration, a well defined scientific goal can be elucidated and set as the requirement. In numerous meetings and discussions, the scientific community

originally made clear its desire to reach 1% flux density accuracy (e.g. [Bachiller et al. 2003](#), report of the spring 2003 ASAC meeting), which means that we must be able to determine the overall flux density scale (and apply it to the visibilities and total power measurements) to 1% accuracy. In addition, the capability of achieving a dynamic range of 10000 or higher in ALMA images means that we must track the amplitude fluctuations to better than 1% ([Yun et al. 1998](#)). A later study by [Moreno & Guilloteau \(2002\)](#) showed that it is impractical to achieve 1% at submillimeter wavelengths, and so a requirement of 3% has been adopted for frequencies >300 GHz. The current achieved calibration accuracy for ALMA is 5% at the lower bands (100 GHz), 10% in mid-bands (200–400 GHz) and 20% in the higher bands (>400 GHz) ([Remjian et al. 2019](#)). This paper is part of the work being done to improve the overall flux calibration accuracy.

Currently there are two flux calibration strategies, the astronomical flux calibration and the direct instrumental amplitude calibration. The astronomical flux calibration uses an astronomical source with known flux and scales up the recorded amplitude based on that flux standard. This method requires the astronomical source to be bright and have stable flux. Currently planets are used as the primary flux standard while quasars are also used as an alternative flux standard due to their compact size and availability over the sky. However, the estimated accuracy of the planets’ fluxes is only about 10% ([Remjian et al. 2019](#), 10.4.7). Therefore, people are still searching for ideal flux calibrators with high accuracy, especially at high frequencies. In addition to the flux calibrator standard, the relative sky transmission on the calibrator and the science target, as well as the time variability of the transmissions will also affect the overall flux calibration. This is the standard method currently used by ALMA. On the other hand, for a stable system, one can directly translate the measured counts in total power into flux units using a direct instrumental amplitude calibration method. Both methods rely on accurate measurement of the sky opacity and tracking its variations during the observation. At millimeter wavelengths, the changes in atmospheric transparency will usually be very modest, under 1% over 10 minutes about 80% of the time. Since the same amount of water vapor results in much larger opacities in the submillimeter, the transparency fluctuations in the submillimeter over characteristic calibration time scales will be much larger, typically several percent during median stability conditions and sometimes $> 10\%$.

For ALMA, both calibration methods require the precise measurement of the system temperature T_{sys} and complex gain G . T_{sys} represents the total thermal noise of the measurement. T_{sys} includes contributions from the sky, receiver, and system losses, with a large contribution coming from the sky temperature. Since ALMA is equipped with receivers of sufficiently low noise, the sky noise often dominates the total thermal noise. Therefore, it is necessary to track the changes in system temperatures caused by the fluctuations in the atmosphere. Current ALMA T_{sys} measurements use discrete atmosphere (ATM) calibrations done every few minutes with a cadence depending on the observing band. At low frequencies (< 300 GHz), we generally perform 2 or 3 T_{sys} measurements over a typical hour-long observation due to the assumed small variation in the atmosphere transmission. At high frequencies (> 300 GHz), due to the rapid opacity change in atmosphere, we generally perform 10 \sim 20 ATM calibrations per hour. So the time overheads just due to ATM calibration can become quite significant – up to 20-30% at the highest bands (9 and 10, at 600–900 GHz). Moreover the variations of T_{sys} on timescales faster than the ATM calibration interval are not tracked with this discrete ATM calibration method. Therefore, one of the major goals in high-frequency flux calibration is to track T_{sys} more closely while also reducing the time spent on discrete ATM calibrations.

1.2. T_{sys} Measurements in Flux Calibration

The system temperature (T_{sys}) is the fundamental parameter to determine the system sensitivity and the real flux of the source. T_{sys} includes various contributions, and can be written in a basic form as (adapted from [Mangum 2017](#))

$$T_{\text{sys}} = \frac{1}{\eta_{\text{eff}} e^{-\tau_{\text{sky}}}} (T_{\text{rx}} + \eta_{\text{eff}} T_{\text{sky}} + (1 - \eta_{\text{eff}}) \times T_{\text{amb}}) \quad (1)$$

where

- T_{rx} is receiver temperature
- T_{sky} is sky temperature
- T_{amb} is ambient temperature where spillover is assumed to be terminated
- η_{eff} is the forward efficiency. This is equal to the fraction of the antenna power pattern that is contained within the main beam and is currently assumed to be 0.95

- $e^{-\tau_{\text{sky}}}$ is the fractional transmission of the atmosphere, where τ_{sky} is equal to the atmospheric opacity along the target's line of sight.

Note this equation is for single sideband (SB) and sideband separating (2SB) receivers, which are used for ALMA Band 3 – 8 observation. For this configuration, the image sideband gain is assumed negligibly small. The Band 9 and 10 receivers are using the double sideband configuration and hence T_{sys} are calculated differently (Mangum 2017, Eq. 6). T_{sky} and T_{amb} can be further expressed as

$$\begin{aligned} T_{\text{sky}} &= T_{\text{atm}}(1 - e^{-\tau_{\text{sky}}}) \\ T_{\text{amb}} &\approx T_{\text{atm}} \end{aligned} \quad (2)$$

where T_{atm} is the representative atmosphere temperature. Note this is an approximation for now. Therefore, by combining equation 1 and 2, T_{sys} can be calculated as

$$\begin{aligned} T_{\text{sys}} &= \frac{1}{\eta_{\text{eff}} e^{-\tau_{\text{sky}}}} [T_{\text{rx}} + T_{\text{amb}}(1 - \eta_{\text{eff}} e^{-\tau_{\text{sky}}})] \\ &\approx \frac{1}{e^{-\tau_{\text{sky}}}} (T_{\text{rx}} + T_{\text{sky}}) \quad (\eta_{\text{eff}} \sim 1) \end{aligned} \quad (3)$$

This equation suggests that the key parameters to measure T_{sys} are T_{rx} and T_{sky} (as τ_{sky} can be derived from T_{sky} using Eq. 2).

In ALMA flux calibration, the intensity of the observed source is directly proportional to T_{sys} by the following equation (e.g. Brogan 2018)

$$S_{\text{final}} \sim S_0 \times \sqrt{T_{\text{sys}}(i)T_{\text{sys}}(j)} \times \Gamma \quad (4)$$

where S_0 and S_{final} are the fluxes measured before and after the flux calibration. Γ is the antenna efficiency factor to convert K to Jy and i and j represent the two antennas forming the baseline. Note that ALMA uses an antenna-based calibration method to simplify the calibration process. Nearly all of the changes to the visibility function (e.g. atmosphere, system noise, amplitude changes, delay changes) can be decomposed into the two complex antenna-based gain factors associated with any baseline. This approach reduces the number of gain correction terms for an N -element array from $N(N-1)/2$ baselines to N antennas. In this case, T_{sys} is associated with each antenna and S_{final} is associated with each baseline.

On the other hand, T_{sys} also determines the achieved rms noise of the observation. ALMA uses a modified form of the radiometer equation (Condon & Ransom 2016) to calculate the rms in kelvin from T_{sys} , as shown below.

$$\text{rms} \approx \frac{cT_{\text{sys}}}{\sqrt{\Delta\nu t_{\text{int}}}} \quad (5)$$

where $\Delta\nu$ is the frequency bandwidth, t_{int} is the integration time of the observation and c includes the quantization and correlator efficiencies, and is typically 0.8-0.9 for ALMA. Therefore, higher T_{sys} means the data has a larger noise within one observation. In addition, for ALMA the weighting function used to combine visibility data is inversely proportional to T_{sys} as

$$\text{Weight} \propto \frac{1}{T_{\text{sys}}(i)T_{\text{sys}}(j)} \quad (6)$$

1.3. Traditional Method to Measure T_{sys}

As noted above, T_{sys} is highly dependent on the sky opacity (eq. 2). ALMA antennas use a two-load system for T_{sys} measurement in Band 3 and higher, which is different from the one-load system used for other radio telescopes. The two-load system in theory can achieve a T_{sys} measurement accuracy of 1%, which is significantly better than that of a one-load system ("chopper wheel") of 5% (Yun et al. 1998). For ALMA, T_{sys} is obtained from an atmospheric calibration (ATM-cal) scan where a hot load, ambient load and sky are consecutively placed in front of the feed using an Amplitude Calibration Device (ACD). Typically this process takes 30-40 seconds, including antenna slew time and overheads. At frequencies below about 400 GHz, where the system temperatures are stable, an ATM-cal scan is made every 10 to 20 minutes. However, at higher frequencies, and wherever the opacity is large and more variable, every scan on the astronomical target will have an associated ATM-cal measurement (Remjian et al. 2019), implying a cadence

Table 1. Summary of different methods to track T_{sys}

	WVR ¹	AC & SQLD ²
Advantage	1. The data is continuously calibrated to measure T_{WVR} ^a 2. Does not suffer from internal electronic gain drift ^b	1. Directly proportional to T_{sys} when τ_{sky} is small 2. Has the same frequency coverage as the science target
Disadvantage	1. Has different frequency coverage as the science target 2. Directly tracks T_{sky} not T_{sys}	1. The data is not calibrated. 2. Suffers from the electronic gain drift ^b or gain variations 3. For AC, no linearity correction in FDM mode.

Columns: 1. Water vapor radiometer data. 2. Auto-correlation and square law detector data.

References: a. Hills et al. (2001). b. Payne et al. (2001).

of ATM calibration as fast as once every 2-3 minutes. From the two-load system, we can also measure T_{rx} . In this case, the measured voltage can be expressed as (Mangum 2002)

$$\begin{aligned} V_{\text{hot}} &= K (T_{\text{rx}} + T_{\text{hot}}) \\ V_{\text{amb}} &= K (T_{\text{rx}} + T_{\text{amb}}) \\ V_{\text{sky}} &= K (T_{\text{rx}} + T_{\text{sky}}) \end{aligned} \quad (7)$$

where K is the gain to convert the temperature to the measured voltage. Therefore, T_{rx} and T_{sky} can be expressed as

$$\begin{aligned} T_{\text{rx}} &= \frac{T_{\text{hot}}V_{\text{amb}} - T_{\text{amb}}V_{\text{hot}}}{V_{\text{hot}} - V_{\text{amb}}} \\ &= \frac{T_{\text{hot}} - Y_1 T_{\text{amb}}}{Y_1 - 1} \\ T_{\text{sky}} &= \frac{V_{\text{sky}}T_{\text{amb}} - (V_{\text{amb}} - V_{\text{sky}})T_{\text{rx}}}{V_{\text{amb}}} \\ &= Y_2 T_{\text{amb}} - (1 - Y_2)T_{\text{rx}} \end{aligned} \quad (8)$$

where $Y_1 \equiv V_{\text{hot}}/V_{\text{amb}}$ and $Y_2 \equiv V_{\text{sky}}/V_{\text{amb}}$. Unlike the atmosphere, T_{rx} is relatively constant throughout the observation. Measurements performed by ALMA show fluctuations of T_{rx} are generally smaller than 1% during normal sidereal tracking. With the measurement of T_{sky} , we can further derive the optical depth based on Eq. 2 and calculate the T_{sys} based on Eq. 3. In summary, the expressions for the key quantities to measure T_{sys} are

$$\begin{aligned} T_{\text{rx}} &= \frac{T_{\text{hot}} - Y_1 T_{\text{amb}}}{Y_1 - 1} \approx \text{const} \\ T_{\text{sky}} &= Y_2 T_{\text{amb}} - (1 - Y_2)T_{\text{rx}} \\ T_{\text{sys}} &\approx \frac{1}{e^{-\tau_{\text{sky}}}} (T_{\text{rx}} + T_{\text{sky}}) \end{aligned} \quad (9)$$

Therefore, during each ATM cal, we point the array to hot load, ambient load and sky to measure T_{rx} and T_{sky} and then calculate the T_{sys} at that time.

1.4. Candidate Data to Track the Continuous T_{sys}

As mentioned above, the current method takes extra time to obtain a spot measurement of T_{sys} every few minutes. If we want to continuously track T_{sys} , in theory there are 3 types of measurement data available from ALMA to achieve this goal: Water Vapor Radiometer (WVR) data, auto-correlation (AC) data or square law detector (SQLD) data. We will describe where these data arise, and the theory behind each method below. The advantages and disadvantages of each method are summarized in Table. 1.

The WVR data are used by ALMA to track the optical depth of the water vapor along the line of sight to each antenna, and hence are used to correct for the resulting effective pathlength and delay errors. The WVRs do Dicke switching and have internal calibrated loads, so the output from each WVR is the calibrated sky temperature (T_{WVR}) at 4 frequencies (184.19, 185.25, 186.485 and 188.51 GHz respectively; Hills 2004) around the 183 GHz water line

taken every 1.152 seconds (Remjian et al. 2019, Section A.6). By comparing T_{WVR} with T_{amb} , we can calculate the precipitable water vapour (PWV), which is proportional to the atmospheric opacity caused by the water absorption. Since T_{sky} at our observing frequency (Eq. 9) and T_{WVR} are tracking sky temperatures at different frequencies, we would expect

$$\begin{aligned} \tau_{\text{sky}} &\propto \tau_{183\text{GHz}} \\ T_{\text{sky}} &\propto T_{\text{WVR}} \quad (\tau_{\text{sky}}, \tau_{183\text{GHz}} \ll 1) \end{aligned} \quad (10)$$

where τ_{sky} is the sky opacity at the observed frequencies and $\tau_{183\text{GHz}}$ is the optical depth for the water vapor line. If optical depth is small enough, we would expect the observed temperature is proportional to the optical depth and hence the proportion relation between the two optical depths holds also for the two measured temperatures. Since the major change in T_{sys} is caused by the variation in T_{sky} , we would expect that T_{WVR} is tracking T_{sys} . The major advantage of using the WVR data to trace T_{sys} is that the radiometer is constantly monitoring the sky and internally calibrating itself. Therefore, we can extrapolate T_{sys} throughout the entire observation based on the WVR data. Furthermore, since T_{WVR} is internally calibrating and tracking the sky variation, it does not suffer from the internal electronic drift or small changes in system gain, which can affect the measured values of an uncalibrated signal (see Table 1)

Alternatively, we would expect T_{sys} is tightly correlated with the total power signal received by each antenna. To be more precise, the total power signal should be directly proportional to $(T_{\text{rx}} + T_{\text{sky}})$, which can be used to calculate T_{sys} given the optical depth τ_{sky} using Eq. 9 (see detailed discussion in Section 3). The total power signal received by each antenna is measured by a square-law detector built into the ALMA signal path, whose data is also recorded in the datasets. Additionally, the autocorrelation data recorded in the measurement set should also give us the total signal received by each antenna. We would expect

$$T_{\text{rx}} + T_{\text{sky}} \propto P_{\text{AC}} \propto P_{\text{SQLD}} \quad (11)$$

where P_{AC} and P_{SQLD} are the power of auto-correlation data and SQLD data read from the measurement set, respectively. If τ_{sky} is small, we would expect direct proportionality between T_{sys} and the total power received which could help us derive continuous T_{sys} . In addition, both AC and SQLD data cover the same frequency rangels as the actual observed science data so we do not need to assume atmosphere variation has the same effect on data at different wavelengths (the ratio proportionality in Eq. 10).

In Fig. 1, we plot the correlation between AC and WVR and SQLD data. We can see the AC and SQLD data follow a tighter linear correlation. These two types of data are expected to be equivalent and thus should follow a proportional correlation. We see a slight offset from the linear correlation, which is likely due to the lack of linearity correction for the 3-bit quantisation in the digital samplers of the ALMA Baseline correlator, as well as small DC offsets in the SQLD. On the other hand, we can see that the WVR and AC data do not follow the same proportional relation. This can be caused by various reasons summarized in Table 1. In particular, the distribution in the AC data at similar WVR levels on the left panel is indicative of slightly different system gains in different scans during the observation. This is thought to be partly due to the imperfect reproducibility of a stepped attenuator setting, which needs to be set and reset between ATM calibration scans. In this case, we need to compare the two types of data to explore which one is better in tracking T_{sys} .

1.5. Outline of This Paper

In the following sections, we will explore how well different data track T_{sys} measurements. In Section 2, we explore the viability of using T_{WVR} to track T_{sys} . We find that T_{WVR} has a tight linear correlation with T_{sys} when both values are normalized. In Section 3, we explored the viability to use AC or SQLD data to track T_{sys} . What we find is that those two types of data do not work well in tracking T_{sys} . In Section 4, we describe our new calibration method to use alternative T_{sys} derived from T_{WVR} and how it compares to the original discrete calibration method.

For our analysis, we use measurements sets from several projects in Bands 7, 8, 9 and 10. We also include two projects with multiple measurements sets from Band 7 and 9. The summary of the data we use is given in Table 2.

2. WVR DATA TO TRACK T_{sys}

In this section, we examine how well T_{WVR} tracks T_{sys} and explore how the correlation is affected by various parameter choices. We mainly use the dataset Band8 (uid://A002/Xdb7ab7/X1880b) for illustration purposes. Examples from additional datasets are given in Appendix A.

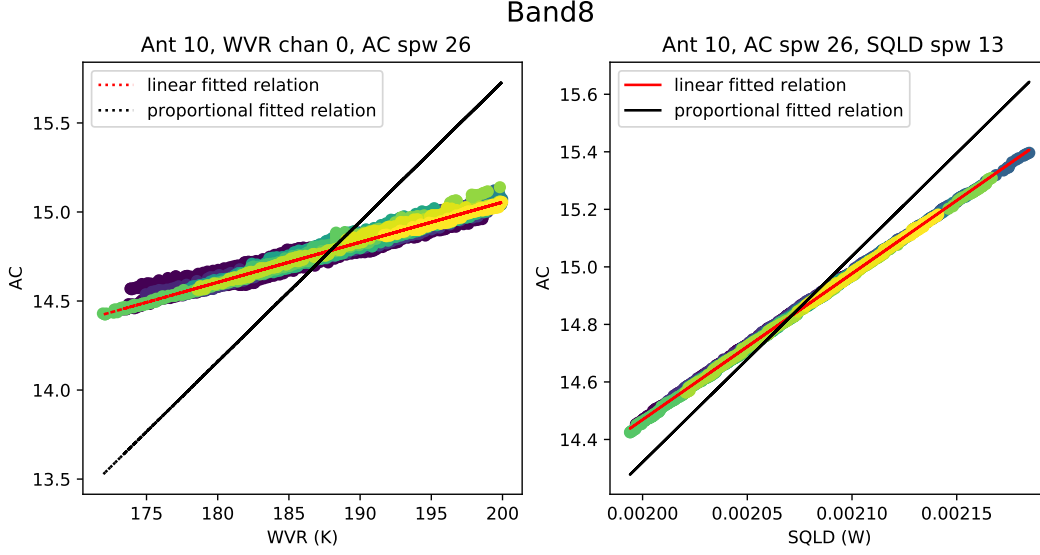


Figure 1. The correlation between water vapor radiometer (WVR) data, auto-correlation (AC) data and square law detector (SQLD) data for antenna 10 for dataset Band8 data. The scatter plots are color coded by the scan number. (Left) AC data versus WVR data. The red line is the best linear fit and black line is the proportional fit through 0. We have excluded WVR data greater than 200 as those are from samples taken on the hot load and ambient load. (Right) AC data versus SQLD data.

Table 2. Summary of Data

Dataset Label	Project	Band	Target	Data uid	PWV (mm)
(1)	(2)	(3)	(4)	(5)	(6)
Band10	2015.1.00271.S	10	Arp 220	uid://A002/Xbe0d4d/X12f5	0.28
Band9a	2016.1.00744.S	9	IRAS16293-B	uid://A002/Xbf792a/X14cc	0.37
Band8	2018.1.01778.S	8	SPT0311-58	uid://A002/Xdb7ab7/X1880b	0.85
Band7a	E2E8.1.00003.S	7	HT-Lup	uid://A002/Xec4ed2/X912	0.59
Band7b1	2018.1.01210.S	7	AS205A	uid://A002/Xda1250/X2387	0.69
Band7b2				uid://A002/Xda1250/X32df	0.53
Band7b3				uid://A002/Xda845c/X35d1	0.5
Band7b4				uid://A002/Xda1250/X3e39	0.51
Band7b5				uid://A002/Xda1250/X4db3	0.49
Band7b6				uid://A002/Xd99ff3/X15d7b	0.42
Band7b7				uid://A002/Xd99ff3/X1702c	0.51
Band7b8				uid://A002/Xd99ff3/X17da2	0.53
Band9b1	2019.1.00013.S	9	Circinus	uid://A002/Xed9025/X769c	0.43
Band9b2				uid://A002/Xed8123/X7b1	0.37
Band9b3				uid://A002/Xed4607/X1208a	0.34

Columns: (1) Label for each dataset (2) ALMA project code (3) Observed Band. (4) The target name to be observed (5) The uid for each measurement set (6) The precipitate water vapor (PWV).

2.1. T_{sys} versus T_{WVR}

To check whether T_{sys} is tracked by the WVR data, we first need to match the WVR data taken at the same time as the T_{sys} measurements. We then average the WVR values that are within 10s around the time when T_{sys} is measured and compare the averaged T_{WVR} with its corresponding T_{sys} . 10 s is a typical time for one ATM scan and hence is the

shortest timescale we expect T_{sys} to change. We also note that T_{sys} recorded in the measurement set is a spectrum with two polarizations. In our analyses to compare T_{sys} with T_{WVR} , we average T_{sys} from both polarizations and from different spectral channels within one spectral window (spw).

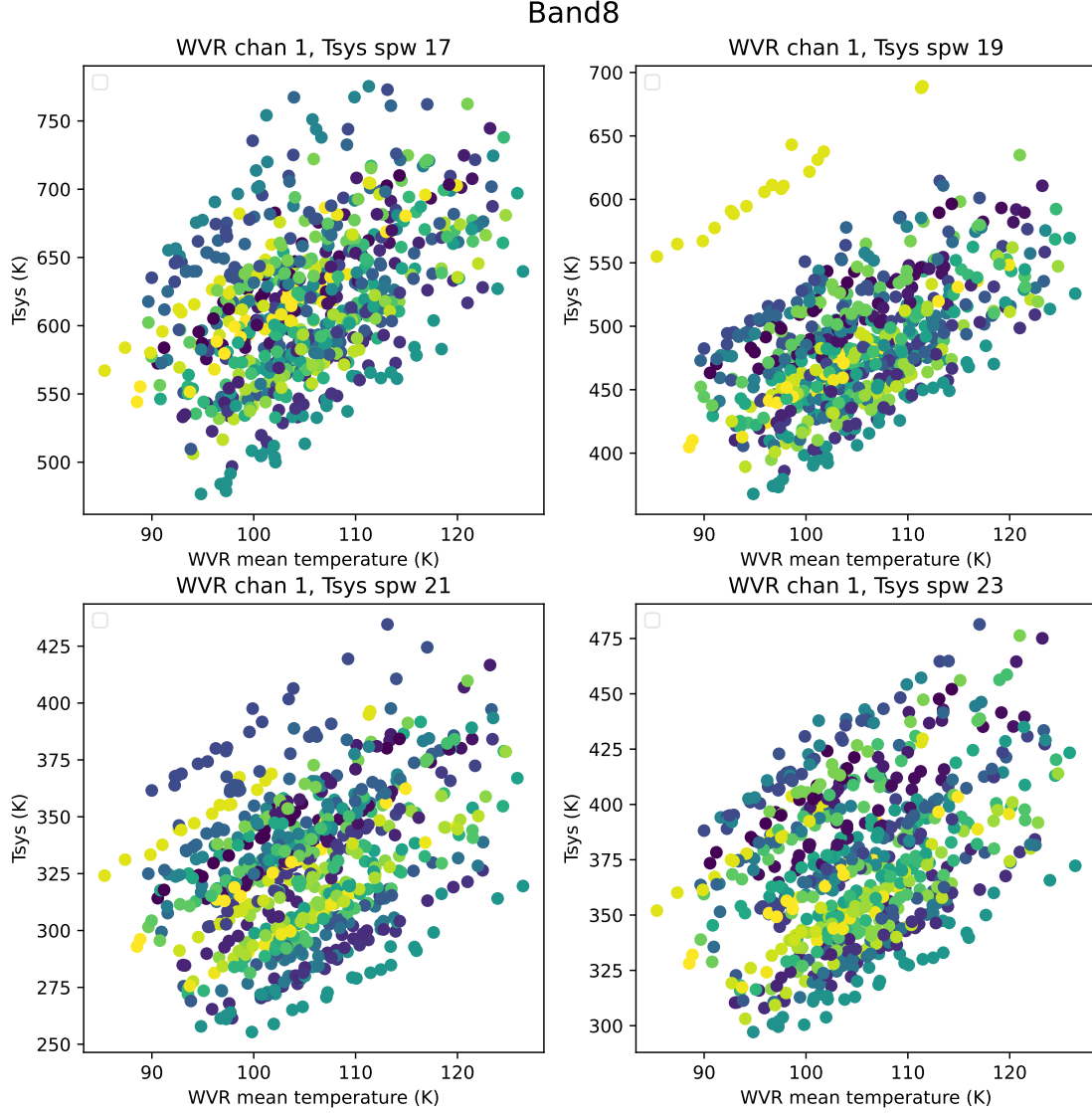


Figure 2. The correlation between T_{sys} and T_{WVR} for different spws of all the antennas from dataset Band8. Different colors specify data points from different antennas. Note all these values are averaged among all spectral channels and both polarizations. See detailed description in Section 2.1.

We first plot T_{sys} versus T_{WVR} from all antennas for each data set. One example of T_{sys} versus T_{WVR} is shown in Fig. 2. For this case, we select T_{WVR} from WVR channel 1. We will discuss in Section 2.2 how the selection of different WVR channels affects the relation between T_{WVR} and T_{sys} . As we can see, there is a significant correlation between T_{sys} and T_{WVR} for each spw. However, there is a large scatter along the direction perpendicular to the trend. Due to the differences in the receiver (T_{rx} and sideband gains) and WVR between antennas, we would expect the same WVR value might correspond to slightly different T_{sys} values from different antennas. In Fig. 2, we can clearly see data points from a single antennae generally lie along the same straight line. Furthermore, since bandpass, phase-cal and science observations are observing targets at different elevations, it is possible that the scatter is also caused by

data from different types of observations. Therefore, to see if the WVR tracks the time variation of T_{sys} , we normalize T_{sys} and T_{WVR} by the first measurement for each observing target (bandpass, phase-cal and science) of each antenna as

$$\begin{aligned}\hat{T}_{\text{sys,source}}(t) &= \frac{T_{\text{sys,obs}}(t)}{T_{\text{sys,obs}}(1^{\text{st}})} \\ \hat{T}_{\text{WVR,obs}}(t) &= \frac{T_{\text{WVR,obs}}(t)}{T_{\text{WVR,obs}}(1^{\text{st}})}\end{aligned}\quad (12)$$

where \hat{T}_{sys} and \hat{T}_{WVR} is the normalized values of T_{sys} and T_{WVR} , the subscript 'obs' is the generalized term for each type of observing target (bandpass, phase and science) and i^{th} in the bracket means the value when i^{th} T_{sys} for each observing target is measured. The correlation between the \hat{T}_{sys} and \hat{T}_{WVR} is shown in Fig. 3. We can see that these two variables have a tight linear correlation, with scatter less than 1%. This tight linear correlation is also seen in other data sets, as illustrated in Appendix A. *This correlation indicates T_{WVR} can be used to track the T_{sys} variation.* However, we note that the fitted linear relation has offsets from the 1-to-1 proportional relation. We also see different spws seem to have fits with different slopes and intercepts. This is what we expect since T_{sky} instead of T_{sys} should be proportional to T_{WVR} according to Eq. 10. Therefore, the slopes and intercepts of the fits will be different due to differences in the atmospheric opacity at different frequencies (ie. different constants of proportionality in Eq. 10. Moreover the sky temperature includes contributions from opacity due to the wet component from H_2O lines (which are relatively wide due to pressure broadening), and from the dry component (mostly due to relatively narrow lines of O_3 , but also including a continuum component as well as other molecules). T_{WVR} is dominated by the water line (wet) component, but T_{sky} around the observing frequency will depend on the relative wet and dry opacities averaged over the chosen spectral window. The slope and intercept of the correlation depends on details of the atmospheric transmission curves, and in Section 2.7 we compare with an atmospheric opacity model. However, for now, we just take the heuristic approach, to derive the constant from the data.

We can then use the fitted linear relation to extrapolate the continuous T_{sys} based on the first T_{sys} value for each observing target and the stream of T_{WVR} values. The exact equation can be expressed as

$$\begin{aligned}T_{\text{sys}}(t) &= T_{\text{sys}}(1^{\text{st}}) \cdot \hat{T}_{\text{sys,obs}}(t) \\ &= T_{\text{sys}}(1^{\text{st}}) \cdot [m \hat{T}_{\text{WVR,obs}}(t) + b]\end{aligned}\quad (13)$$

where $T_{\text{sys}}(1^{\text{st}})$ and $T_{\text{WVR}}(1^{\text{st}})$ are T_{sys} and T_{WVR} values used to normalize each antenna and each type of observing targets. m and b are slope and intercept of the fitted linear function. For making the extrapolation, we also sample and average the WVR data every 10 seconds to be consistent with our fitting parameter choice. An example of extrapolated T_{sys} for one antenna is shown in Fig. 4. As we can see, the extrapolated continuous T_{sys} is consistent with the original discrete T_{sys} values for all 4 spectral windows. The trend is also quite continuous with no obvious glitches due to the measurement noise. The trends for all 4 spectral windows are similar, which indicates T_{WVR} truly reflects the change in atmosphere.

Examples of fitting and T_{sys} extrapolation for other datasets are shown in Appendix A. We can see for all datasets, \hat{T}_{sys} and \hat{T}_{WVR} have a tight linear correlation but with different slopes and intercepts. The extrapolation also works well for most of the data sets.

2.2. Other WVR Channels

The ALMA WVRs have 4 filter channels at frequencies (184.19, 185.25, 186.485 and 188.51 GHz respectively) close to the 183GHz H_2O line (Hills et al. 2001). These channels have different sensitivities to the line-of-sight water content (PWV) and hence T_{sys} , depending on the actual pwv at the observing time. In this section, we explore how the different parameter choices will affect the correlation between T_{sys} and WVR. In Section 2.1, we selected T_{WVR} in channel 1 to track T_{sys} . Here we test using T_{WVR} from different WVR channels for T_{sys} on the same dataset (Fig. 5). As we can see, different WVR channels give us a similar tight correlation between normalized T_{sys} and T_{WVR} . As expected, T_{WVR} from the different channels also gives us different slopes and intercepts. Therefore, if we average T_{WVR} from different channels, it should not reduce the scatter around the fitted linear function.

In our later analysis to apply the continuous T_{sys} in data calibration, we select WVR channels to maximize the following weighting function

$$w = \bar{T}_{\text{WVR}}(\bar{T}_{\text{WVR}} - 275) \quad (14)$$

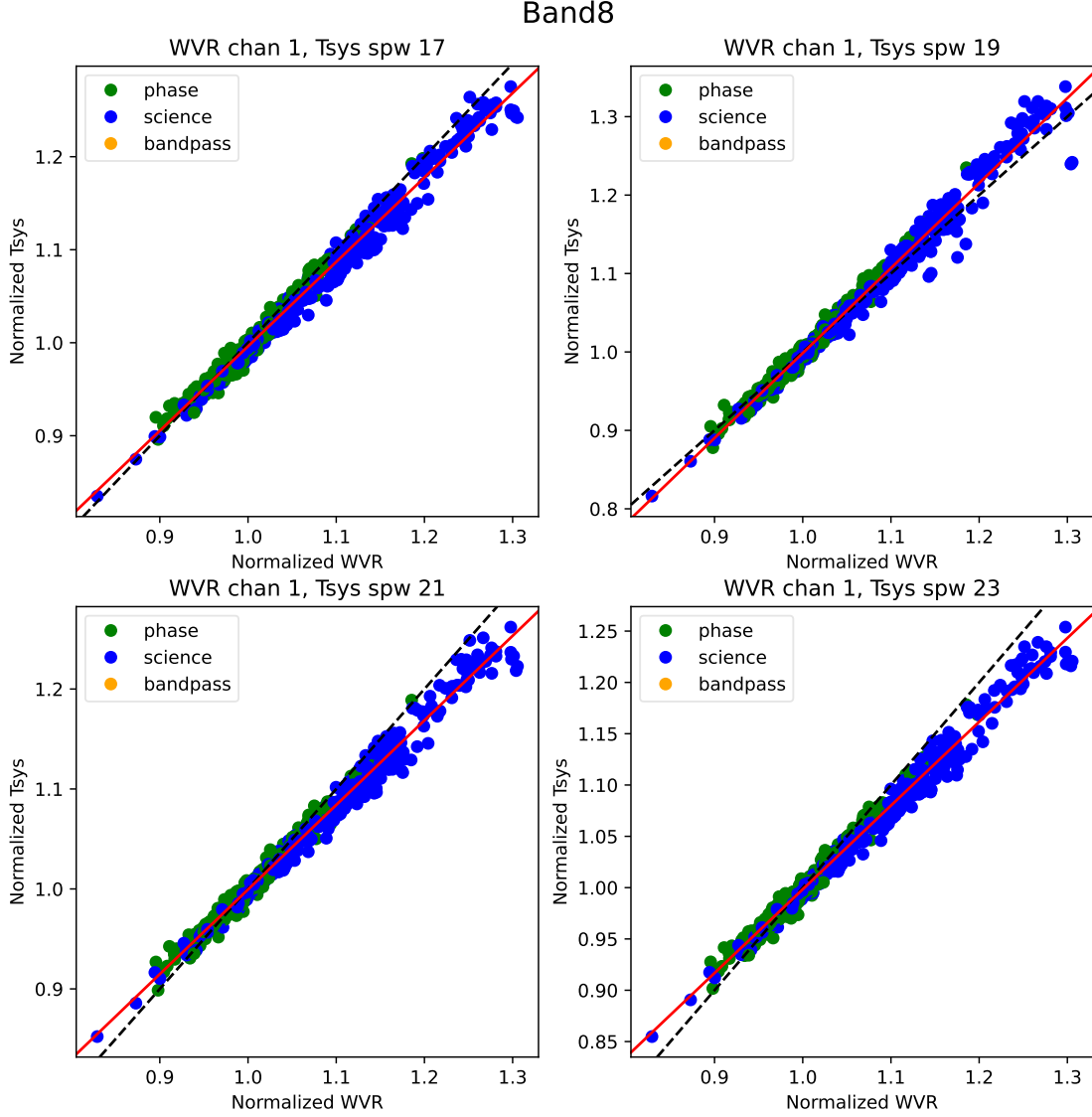


Figure 3. The same as Fig. 2, except now T_{sys} and T_{WVR} are normalized by the first measurement of each type observation (bandpass, phase and science). The orange, blue and green points are from bandpass, phase and science scans respectively. The red line is the linear fitting of the relation. The black dashed line indicates the 1-to-1 relation. See detailed description in Section 2.1.

where \bar{T}_{WVR} is the averaged T_{WVR} in one channel and 275 K is the approximate atmosphere temperature. The principle for this selection criterion is to make T_{WVR} neither too small to be robust against noise (in the case of low opacity) nor too large to be saturated (in the case of high opacity). Based on this criterion, we generally select WVR channel 0 or 1 for datasets in our analysis.

2.3. Using PWV to track the T_{sys}

For single dish telescopes such as APEX and JCMT, WVR data has been used to continuously track optical depth at the observed frequencies (Dempsey et al. 2013). The method converts T_{WVR} values from 4 WVR channels into a single PWV value and use it to track the optical depth at any given time, which reduces the effect of measurement noise from a single channel. Given what we are doing is similar, as T_{sys} is mostly affected by the change in atmospheric optical depth, we can try to use PWV instead of T_{WVR} from a specific channel to track T_{sys} . We calculate the PWV by fitting the Lorentz profile for the water line given the T_{WVR} from the 4 channels. We then normalize the PWV values

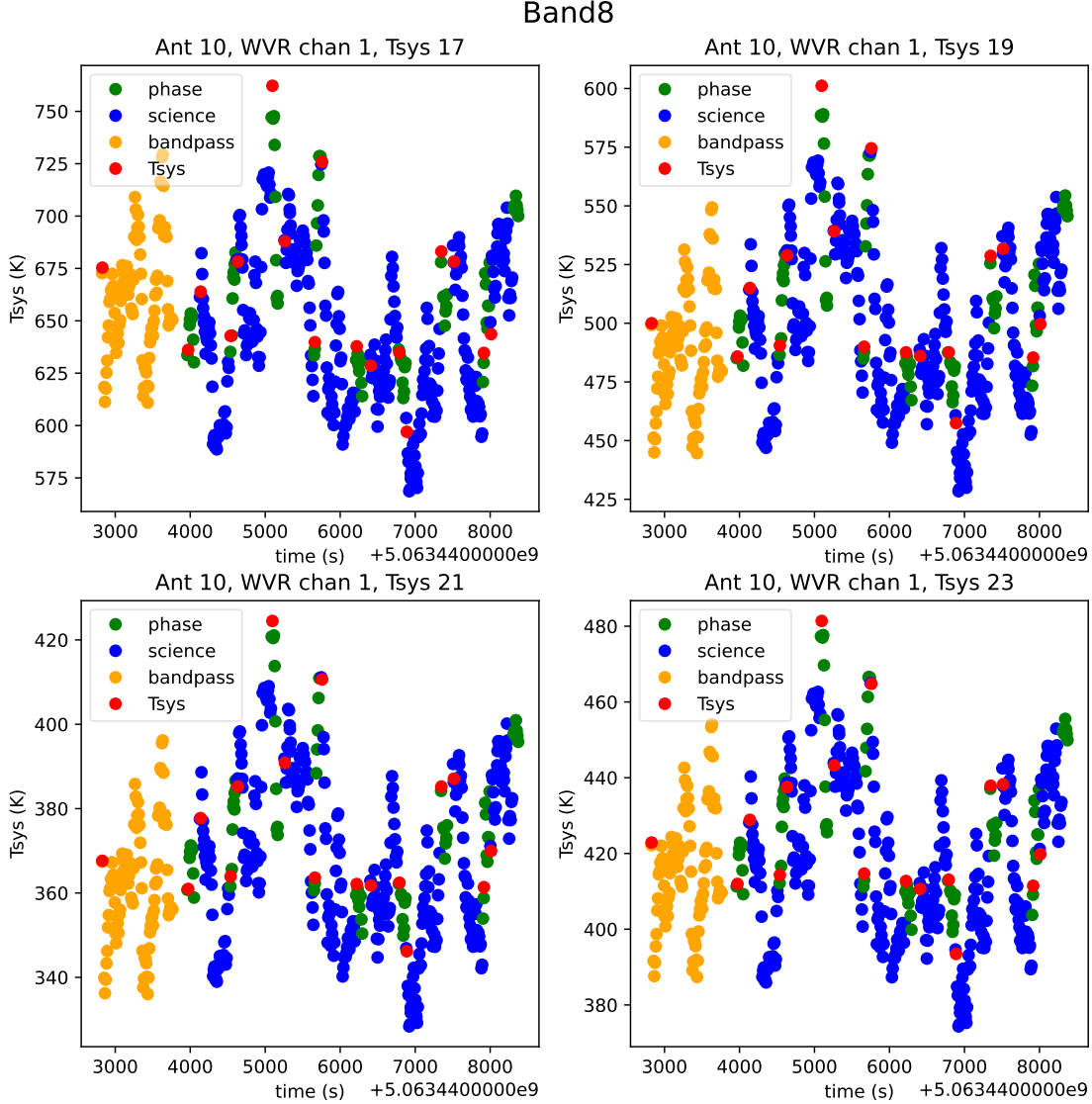


Figure 4. The extrapolated T_{sys} versus the original T_{sys} for antenna 10 of the same dataset used in Fig. 2. The orange, green and blue points are extrapolated continuous T_{sys} for each observing target based on Eq. 13 while the red points are original T_{sys} measurements.

the same way as we do for T_{WVR} (Eq. 12). The comparison between normalized T_{sys} and PWV values is shown in Fig. 6. We can see that PWVs also have a tight correlation with T_{sys} as expected. Compared with T_{WVR} in channel 2 and 3 (Fig. 5), the correlation between T_{sys} and PWV shows fewer outliers, which suggests we can also use PWVs to track T_{sys} to minimize the noise in T_{WVR} measurements. On the other hand, we still see different slope and intercepts between T_{sys} and PWV for different T_{sys} spws, which is also consistent with what we expect as different spws cover different frequency ranges and hence have slightly different portions of contribution from wet and dry components.

2.4. Fewer ATM scans to Fit the Relation

As discussed in Section 2.1, the T_{sys} in different spectral windows have different linear relations with T_{WVR} . Therefore, we are still not able to predict the exact form of the linear relation before the data is taken. To achieve the goal to reduce the number of T_{sys} measurements, we will test in this section if we can get the same linear relation between \hat{T}_{sys} and \hat{T}_{WVR} with fewer ATM scans. Since we need to calculate the normalized T_{sys} , we need at least two ATM scans to fit the linear correlation. To make the fitting more robust, we use 4 ATM scans for the fitting with 2 from

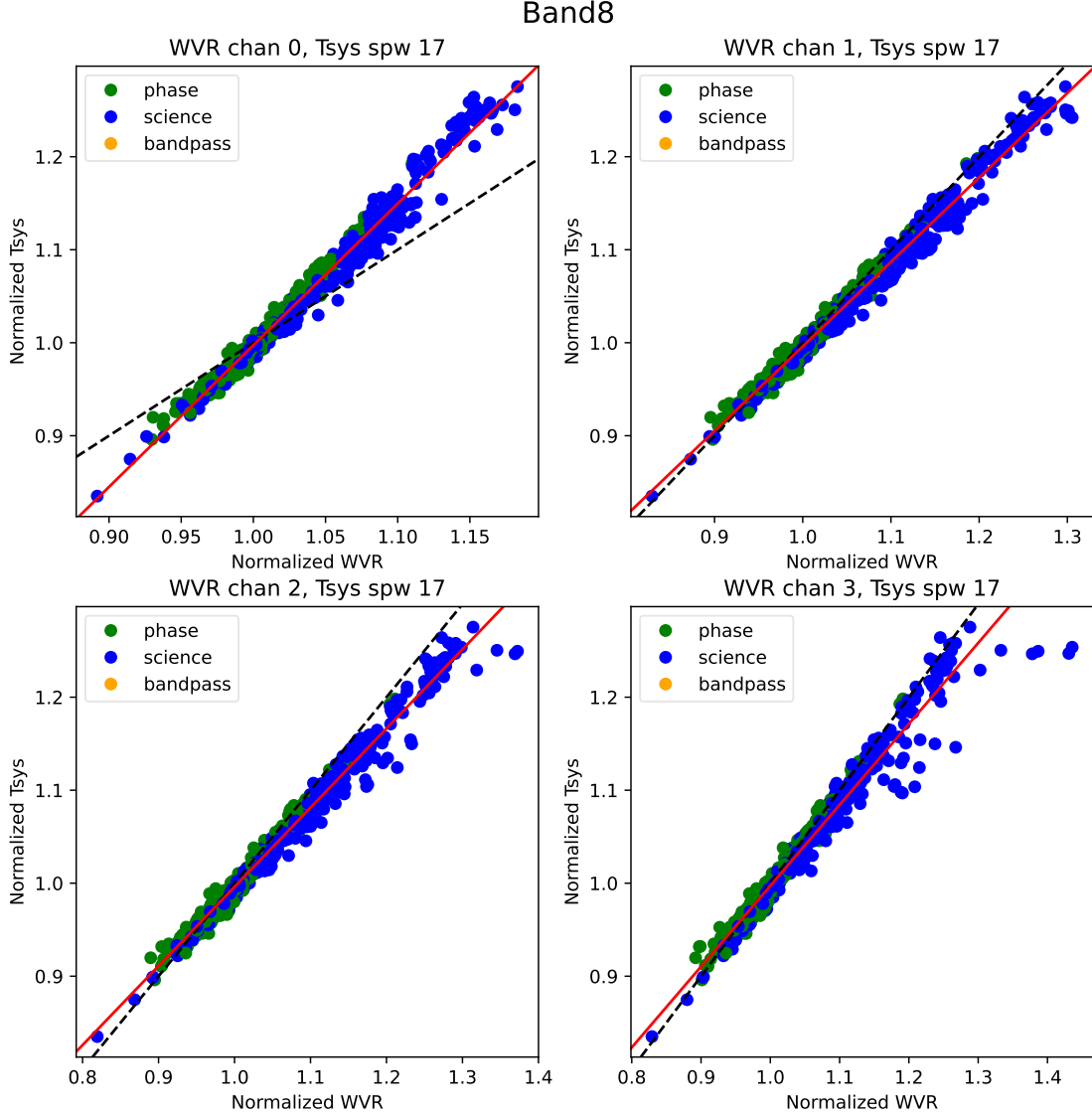


Figure 5. Correlation between the Normalized T_{sys} and T_{WVR} for different WVR channels. For T_{sys} we select the data from spectral window 17.

phase target and 2 from the science target. The 4 ATM scans give us 2 independent \hat{T}_{sys} values if we normalize the T_{sys} from phase and science target independently. For the ATM scan selection, we select 2 ATM scans at the start and 2 ATM scans in the middle. One example of the fits using 4 ATM scans is shown in Fig. 7. As we can see, the fits based on data from all ATM scans have almost no difference from the fits based on only 4 ATM scans. The scatter of all the data points around the new relation is $\sim 0.6\%$, which has almost no difference from the old scatter of $\sim 0.5\%$.

Fits using 4 ATM scans for other data sets are also shown in Appendix A. We can see that the fits do not change much for almost all data sets except for that in dataset Band9b. We will discuss the data in 2019.1.00013.S in Section 2.6. In Fig. 8, we plot the relative scatter around the fit versus the maximal difference divided by mean value of the T_{sys} for every T_{sys} spw of all the data sets. As we can see, the scatter using both fitting methods is generally below 3%. Besides, fitting with just 4 scans only slightly increases the scatter compared with fitting with all scans. From this quantitative comparison, we can see it is viable to reduce the number of discrete T_{sys} measurements when using T_{WVR} to track T_{sys} .

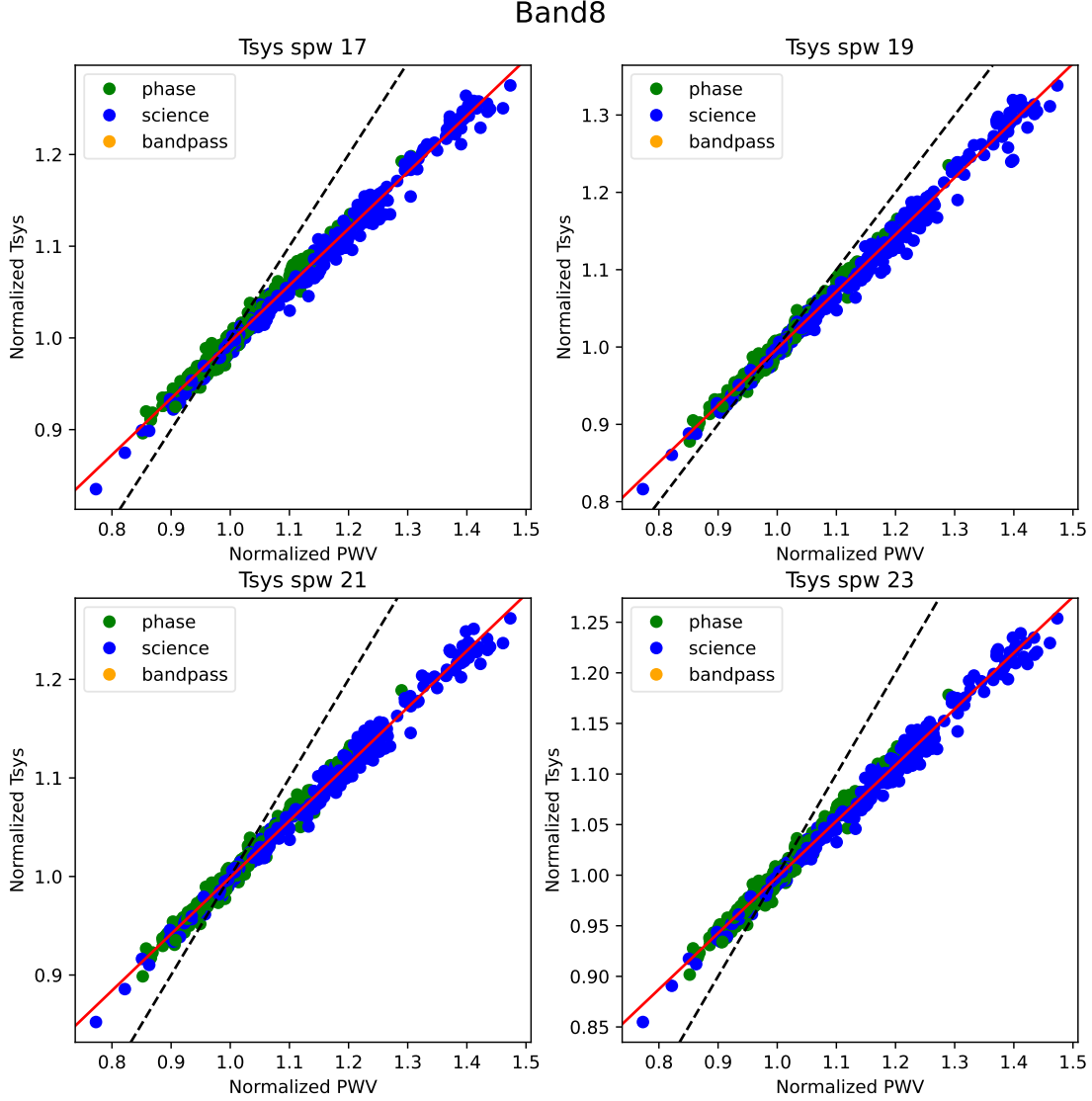


Figure 6. Correlation between the normalized T_{sys} and PWVs for different T_{sys} spws.

2.5. Normalize Only to the Science target

For some ALMA data, T_{sys} for the phase-cal target is not measured. Instead, the calibration uses the nearest science T_{sys} values as the phase-cal T_{sys} . If we can normalize all T_{sys} values to the first T_{sys} of the science target instead of the first T_{sys} of each type of observing target itself, we can further reduce the number of T_{sys} measurements and thus no longer need to measure T_{sys} for phase-cal with our new method.

In this case, the normalized T_{sys} is calculated as

$$\begin{aligned}\hat{T}_{\text{sys,obs}}(t) &= \frac{T_{\text{sys,obs}}(t)}{T_{\text{sys,sci}}(1^{\text{st}})} \\ \hat{T}_{\text{WVR,obs}}(t) &= \frac{T_{\text{WVR,obs}}(t)}{T_{\text{WVR,sci}}(1^{\text{st}})}\end{aligned}\tag{15}$$

where $\hat{T}_{\text{sys,obs}}(t)$ is the normalized T_{sys} averaged along the spectral axis and $\hat{T}_{\text{WVR,obs}}(t)$ is the normalized T_{WVR} . An example of \hat{T}_{sys} versus \hat{T}_{WVR} using the new normalization method is shown in Fig. 9. As we can see, all the data points follow almost the same linear correlation as the data normalized to each type of observing target. The bandpass data

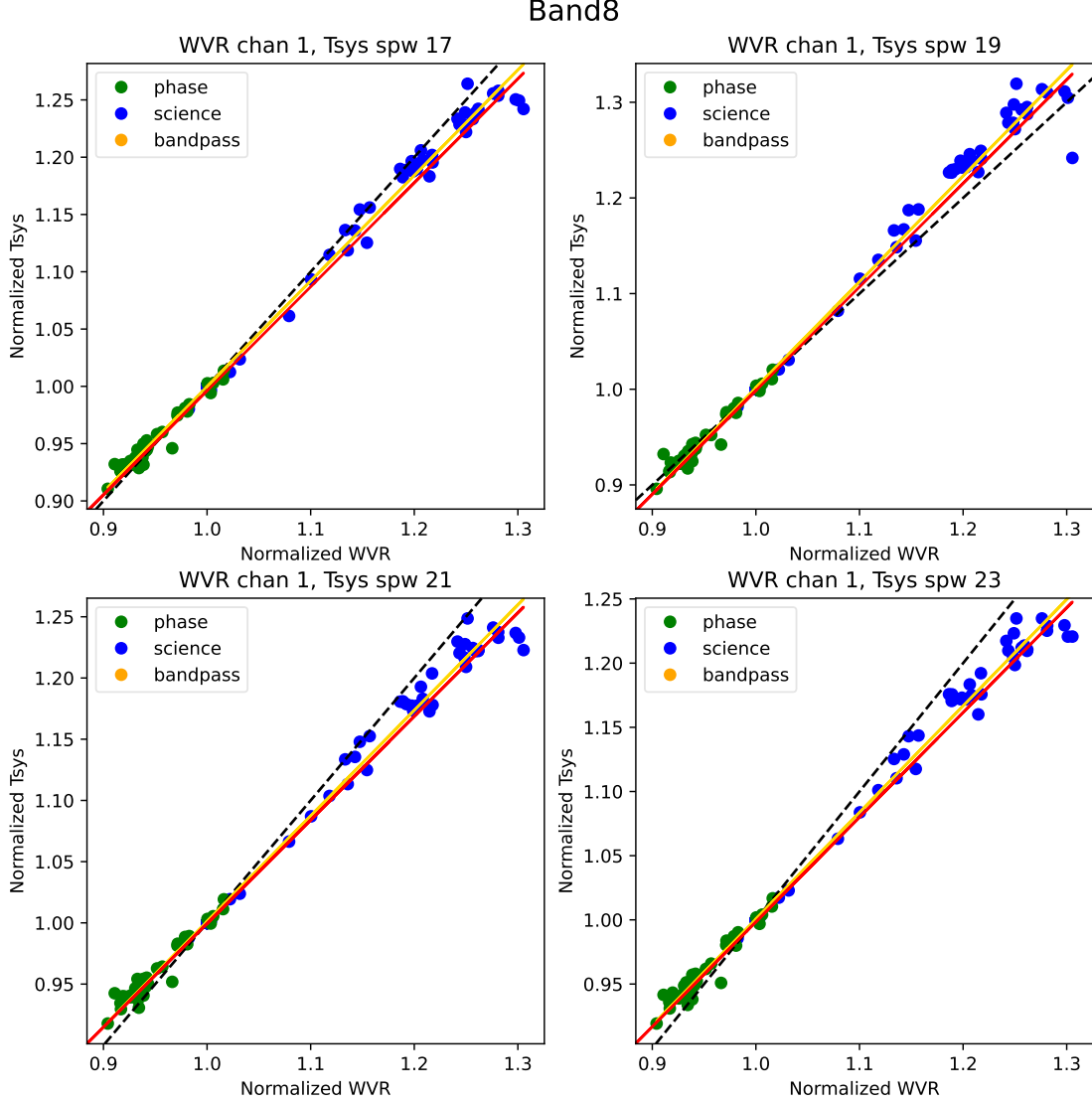


Figure 7. The correlation between the normalized T_{sys} and T_{WVR} for the 4 ATM scans we selected to fit the linear relation. The red and gold lines are the fitting relation with all ATM scans or just 4 ATM scans. The black dashed line indicates the 1-to-1 relation. We can see the fitting using all ATM scans are almost the same as just using 4 scans.

points follow the general trend but have a significant offset from other data points for spw 0. This is probably due to the different elevations of the bandpass and phase/science targets (see detailed discussion in Section 2.7). All the other measurement sets we have show that the normalized bandpass data lie along the same linear relation as the phase and science data (see another example in Fig. 25). We also test this relation in an extreme case for dataset Band10 where the science and phase-cal T_{sys} are drastically different, as shown in Fig. 10. We can see that even though the phase-cal target and science target are far apart in the sky, the two sets of data points still follow a quite similar tight linear relation. These tests show that we can further reduce the phase-cal and bandpass T_{sys} measurements as we can derive it from T_{sys} measurements for science target.

Note that for early ALMA cycles, the T_{sys} measurements are purely done for the phase-cal target. The T_{sys} for the science target is then assumed to be the same as the T_{sys} for the closest phase-cal scan. As we can see from this section, even though the phase-cal and science targets have different elevations, they generally follow the same T_{sys} vs T_{WVR} linear relation. Therefore, we can better extrapolate the science T_{sys} from the phase-cal T_{sys} using on the fitted linear relation.

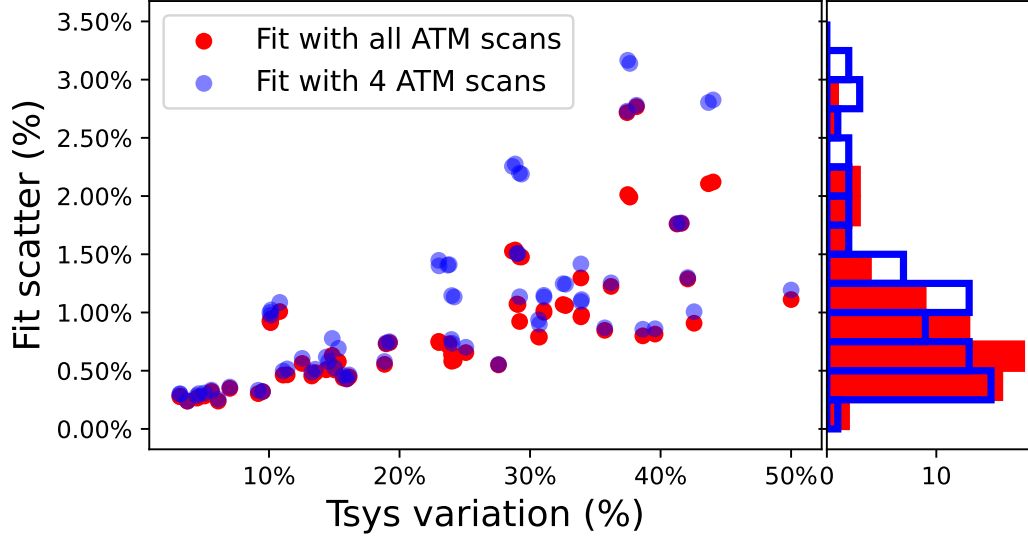


Figure 8. The scatter of data points around the T_{sys} vs T_{WVR} fits with all the antennas versus the maximal difference in \hat{T}_{sys} values for each T_{sys} spw of each dataset. The red and blue points are from fitting with all ATM scans or just 4 ATM scans respectively. The histogram at right side shows the distribution of the fit scatters using the two different methods. We can see the scatter of the fitting only increases slightly using just 4 ATM scans.

2.6. Band 9 Data with Large T_{sys} Variation

We would also like to test if this linear correlation between T_{sys} and T_{WVR} holds in Band 9 and 10 data as they have a different receiver configuration (double-sideband) and generally higher atmospheric opacities. Dataset Band9b is ideal for this purpose as the T_{sys} variation is the largest among all of our datasets (50%). In Fig. 11, we show T_{sys} fitting and extrapolation using all ATM scans or just 4 ATM scans for one measurement set in this project. We can clearly see there is a difference in the fitting functions derived from all ATM scans or just 4 ATM scans. It seems the slope becomes steeper due to data points with higher T_{sys} values, which are not included if we use just 4 scans. This is also reflected in the extrapolation plot at right side of Fig. 11, as the predicted T_{sys} is lower than the measured T_{sys} for higher T_{sys} values.

Based on the analytical expression of T_{sys} , we would expect a correlation that is actually curving up between T_{sys} and T_{WVR} . Based on Eq. 2, 3 and 10, the correlation between T_{sys} and T_{WVR} at low opacity limit can be simplified as

$$T_{\text{sys}} \approx T_{\text{rx}} + T_{\text{sky}} = T_{\text{rx}} + C_1 T_{\text{WVR}} \quad (16)$$

where C is a constant. In this case, we expect linear correlation between T_{sys} and T_{WVR} with positive intercept. However, at the high opacity limit, Eq. 3 is no longer a linear relation. Instead, the increase in T_{sys} is dominated by the increase in τ_{sky} in the exponential form. Based on Eq. 2 and 3, we would expect that

$$T_{\text{sys}} = \frac{T_{\text{sky}}}{T_{\text{amb}} - T_{\text{sky}}} (T_{\text{sky}} + T_{\text{rx}}) \quad (17)$$

When T_{sky} is large, the increase in T_{sys} is dominated by $T_{\text{sky}}^2 / (T_{\text{amb}} - T_{\text{sky}})$ term, which has increasing slopes as T_{sys} increases. If we assume T_{sky} is still relatively proportional to T_{WVR} , then we would find the correlation between T_{sys} and T_{WVR} is turning more and more upward. In this case, the linear correlation between T_{sys} and T_{WVR} we observed in other datasets should actually be a tangential line of the curving function. Because T_{sys} variations in other data sets are small, we can approximate the curving relation as a straight line. In Section 2.7, we also see a curving relation between \hat{T}_{sys} and \hat{T}_{WVR} .

2.7. Atmospheric modeling for T_{sys} versus T_{WVR}

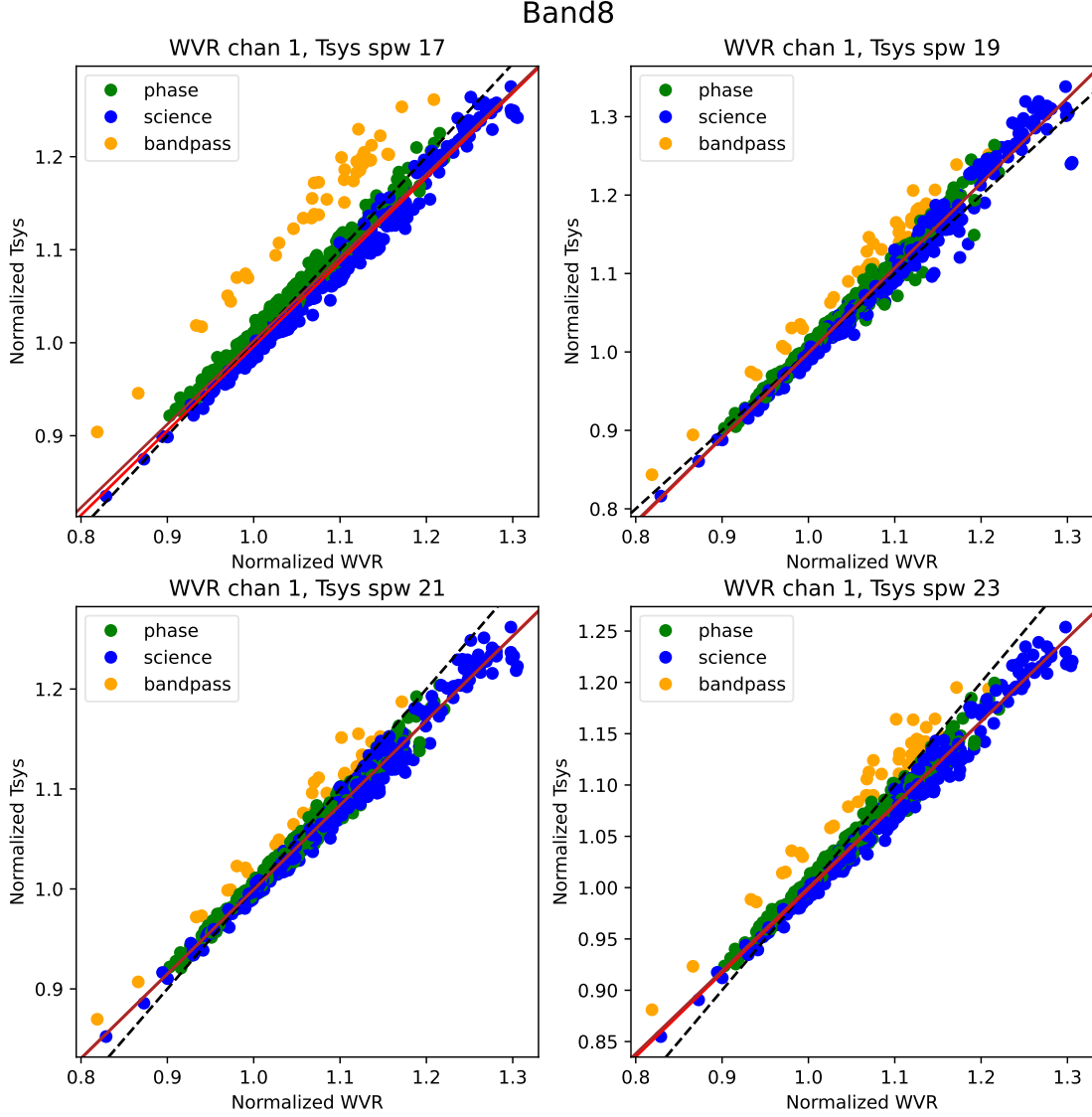


Figure 9. T_{sys} versus T_{WVR} normalized to the first science ATM scan for the dataset Band8. The black dashed line is the 1-to-1 relation. The brown solid line is the linear fitting to the data excluding the bandpass data. The red solid line is the original fitting relation to the data normalized to each type of observing target. We can see the two fitting relation are almost the same. The bandpass data for spw 0 has a significant offset from the fitted relation, which we think is probably due to the incorrect measurement of T_{sys} at that time. See Fig. 25 in Appendix A for a good example.

In the previous sections, we fit T_{sys} vs T_{WVR} heuristically and uses the fitted relation to extrapolate the T_{sys} continuously. We find in most cases the correlation between T_{sys} and T_{WVR} is linear. However, the exact slopes and intercepts of the correlations vary across different frequencies. Although we can use less than 4 ATM scans to fit the relation for each spw in each dataset, there might be cases when our selected ATM scans have similar T_{sys} values, and hence might give us inaccurate fitting relation among small T_{sys} ranges. Furthermore, the linear relation breaks up when T_{sys} variations become really large (e.g. dataset Band9b). A more robust method is to use atmospheric transmission at microwaves (ATM) modeling (Pardo et al. 2001) to predict the T_{sys} versus T_{WVR} relation in various cases. In this section, we try the ATM modeling for dataset Band8 to see if the ATM modeling can give us as good a fit as our heuristic method.

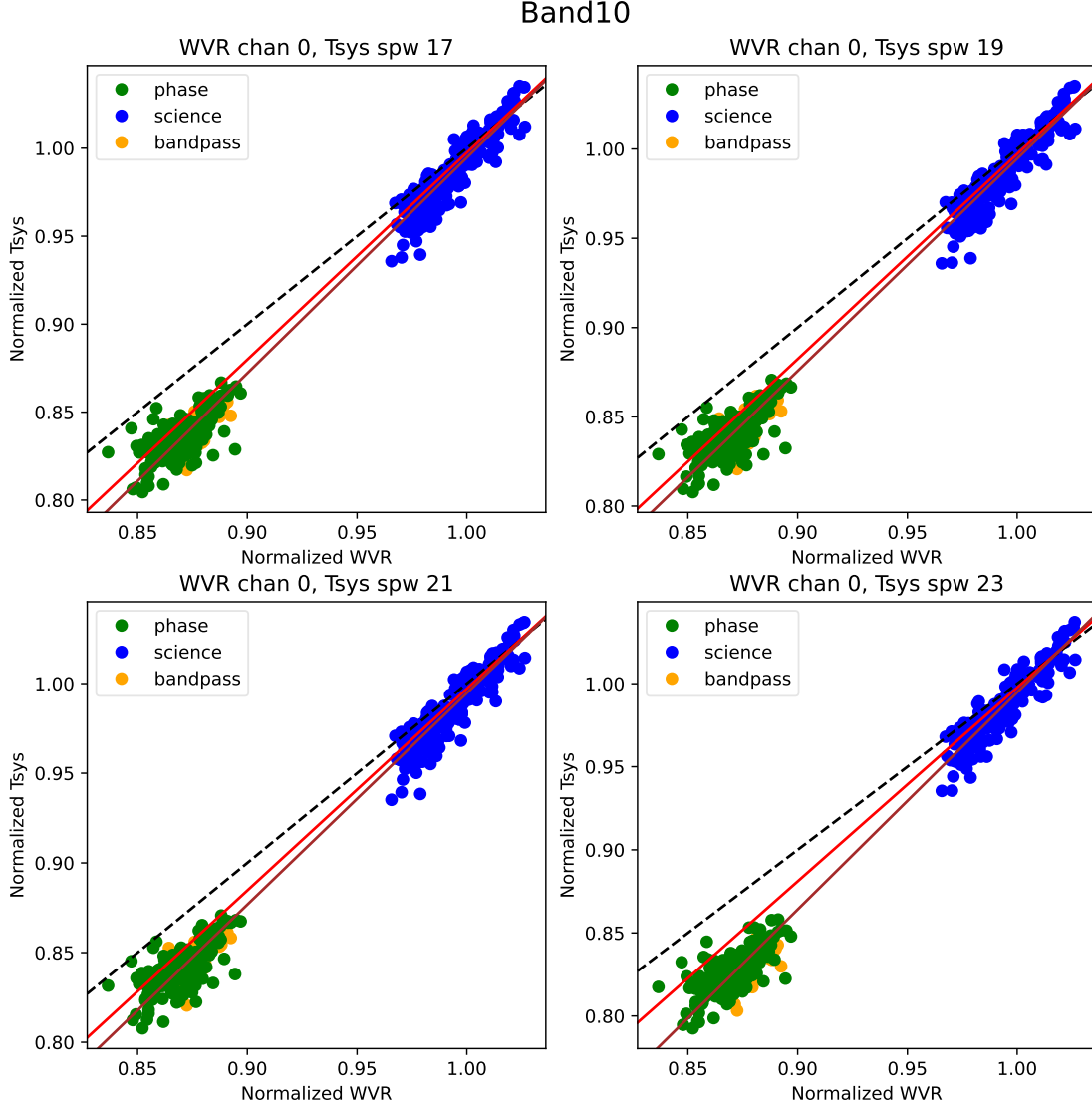


Figure 10. T_{sys} versus T_{WVR} normalized to the first science ATM scan for the Band 10 data. The black dashed line is the 1-to-1 relation. The maroon solid line is the linear fitting to the data. The red line is the original fitting relation to the data normalized to each type of observing target.

We use the CASA function `au.plotAtmosphere` to generate T_{sys} and T_{WVR} spectra at given frequency ranges. We set most of the parameters to the default for the ALMA site (height 5000 m, pressure 557 mb and temperature 274 K). For dataset Band8, the elevation of the science target is about 53 degrees and the median PWV value is 0.85 mm (Table 2). We hence input different elevations and PWVs centered around these values to generate the T_{sys} and T_{WVR} spectra. Note that `au.plotAtmosphere` only outputs T_{sky} and zenith opacity τ_0 ($\tau_{\text{sky}} = \tau_0 \sec z$) where z is the elevation). Therefore, we use Eq. 1 to convert these values to T_{sys} for each given T_{rx} and elevation angle. An example T_{sys} spectrum is shown in Fig. 12 assuming T_{rx} of 100 K and elevation angle of 53 degrees. As we can see, the shape of T_{sys} spectrum does not vary much for different PWVs and elevations. However, it is clear that varying PWVs or elevations can have slightly different effects on the shape of the spectrum. If we increase PWV values, broader part of the spectrum (due to H_2O) increases while the narrow components due to Ozone lines do not. On the other hand, if we increase the elevation, it will increase the strengths of both continuum and Ozone lines. However, the Ozone lines are narrow and have a relatively small effect on the T_{sys} values.

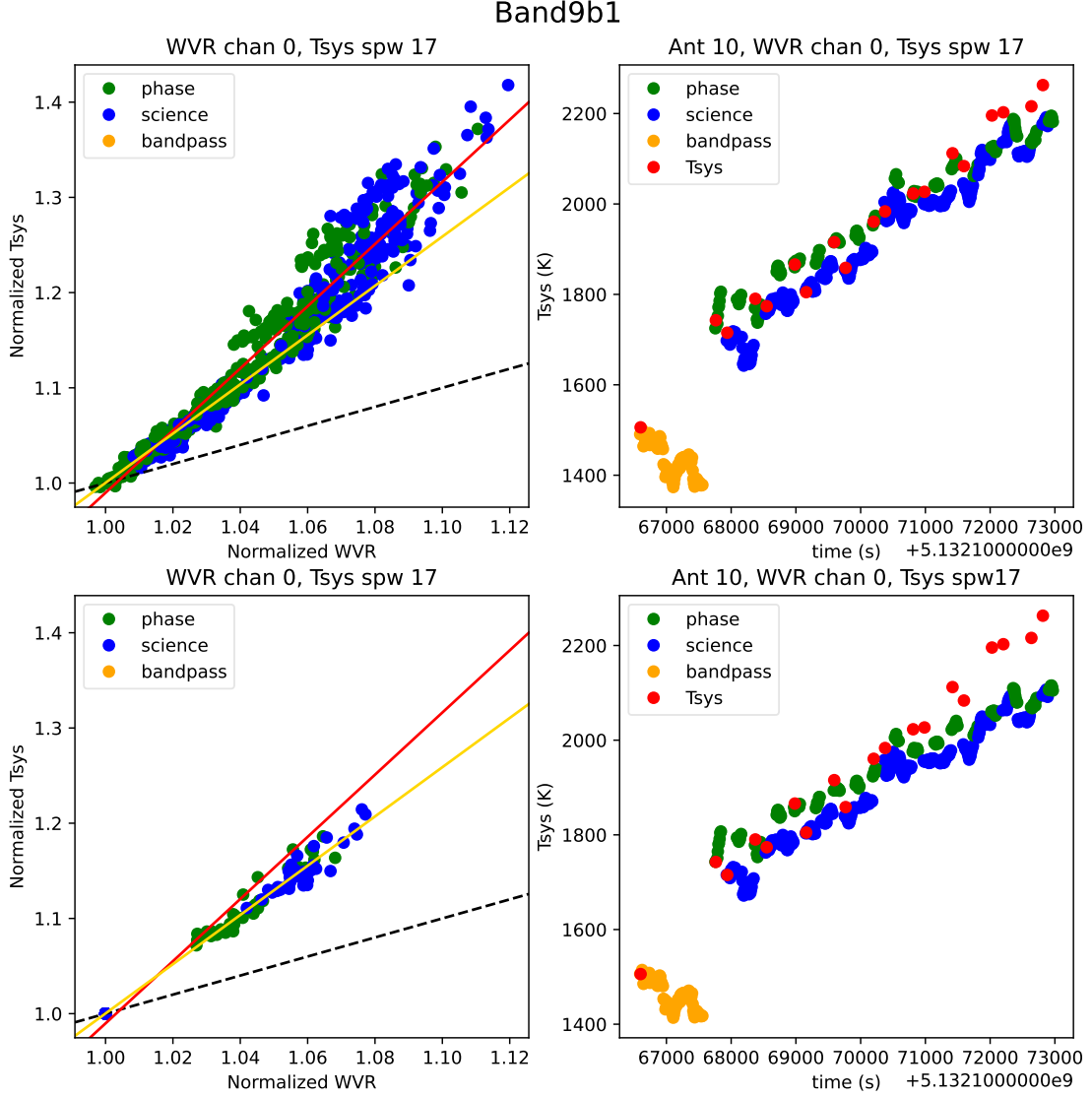


Figure 11. (Left) T_{sys} versus T_{WVR} (channel 0) for one data set in Band 9 project 2019.1.00013.S. The upper left panel shows \hat{T}_{sys} versus \hat{T}_{WVR} in spw 17 using all ATM scans while the lower left panel shows the correlation with selected 4 ATM scans. The red and yellow lines are the fits derived using all ATM scans and just 4 ATM scans. (Right) The measured and extrapolated T_{sys} for different observing targets as a function of time. Red points are measured T_{sys} values. T_{sys} in upper panel is extrapolated based on fits with all ATM scans while T_{sys} in lower panel is extrapolated based on fits using only selected 4 ATM scans.

To explore the T_{sys} versus T_{WVR} correlation, we average the T_{sys} and T_{WVR} across each spw. We first explore how T_{sys} is correlated with T_{WVR} if we just change PWV values. Fig. 13 shows our modeling overlaid by the actual normalized data for T_{sys} spw 17 and WVR channel 1. For the modeling, we vary the T_{rx} in the left panel and elevations in the right panels to see how different parameter choices affect our modeling slopes. For dataset Band8, T_{rx} varies from 50 to 130 K for different antennas while elevations of the science and phase targets are around 50 – 55 degrees. As we can see, the ATM modeling shows a slight non-linear curvature for a high range of T_{sys} , which depends slightly on the assumed T_{rx} and the elevation. However, the modeling curve is generally within the range of the data scatter. Therefore, we can still fit a linear relation and extrapolate T_{sys} with a good accuracy.

We then explore how elevations could affect the \hat{T}_{sys} vs \hat{T}_{WVR} correlation. In Fig. 14, we can see the slopes of \hat{T}_{sys} vs \hat{T}_{WVR} are much steeper than is seen in actual data. This is what we expect since reducing elevations or increasing the airmass will increase both the wet and dry components in the same way. While T_{sys} has comparable contributions from

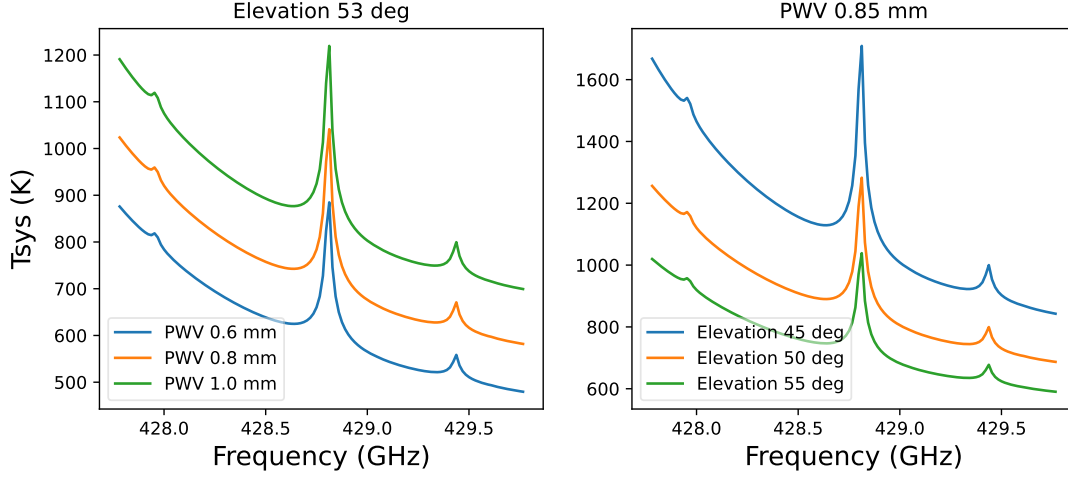


Figure 12. The ATM modeling T_{sys} spectrum for different PWV (left) and elevation (right) values for dataset Band8 spw 17.

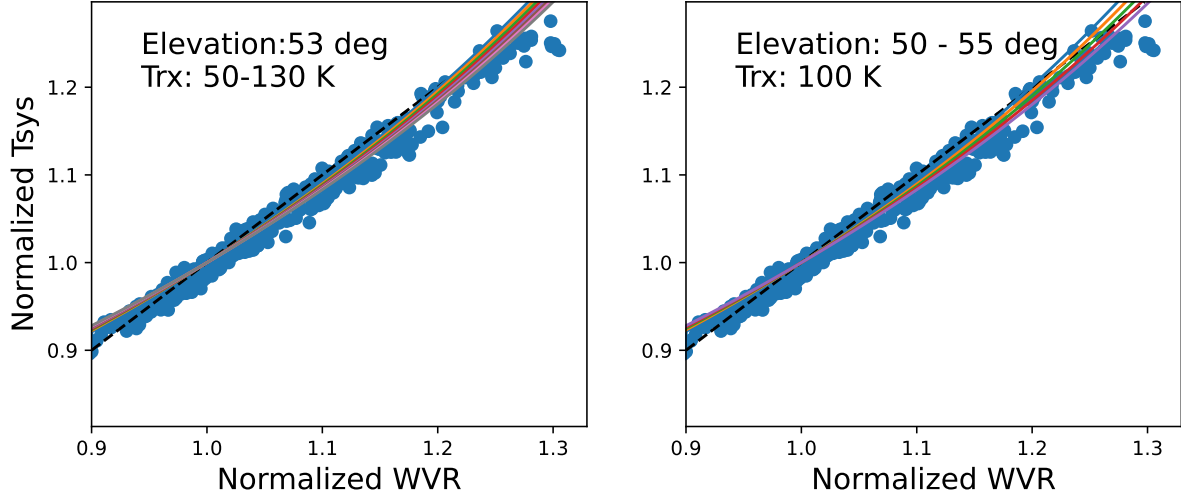


Figure 13. The correlation between \hat{T}_{sys} and \hat{T}_{WVR} (Fig. 3) overlaid by the predicted correlation curves from ATM modeling. T_{sys} is from spw 17 and T_{WVR} is from channel 1. The left panel shows curves for different T_{rx} values, while the right panel has curves for different (but fixed) elevations of the target.

wet and dry components, T_{WVR} is dominated by the wet component. Therefore, the increase in T_{sys} will be steeper than that of T_{WVR} . In our actual observations, the elevation change is quite small, generally 1 – 2 degrees, hence the change in T_{sys} and T_{WVR} should be dominated by PWV variations. For dataset Band8, we also see the difference between normalized bandpass data and science/phase data in Fig. 9. This difference could also be explained by the elevation difference between the bandpass target and phase/science target. In Fig. 14, the thick red and purple lines show the ATM modeling of two fixed elevations of 53 and 48 degrees with varying PWVs. We can see the difference in elevations could well explain the offsets between the normalized bandpass and phase/science data.

3. AC & SQLD DATA IN TRACKING T_{sys}

As mentioned in Section 1.4, we can also explore whether to use AC or SQLD data to track T_{sys} variation. Since AC and SQLD data are equivalent to one another (see Fig. 1 right panel), we only need to compare T_{sys} with one of the two quantities. We use AC data for comparison since the data size is much smaller. We use a similar method to normalize the AC data and compare it with the normalized T_{sys} . Fig. 15 shows the comparison between T_{sys} versus

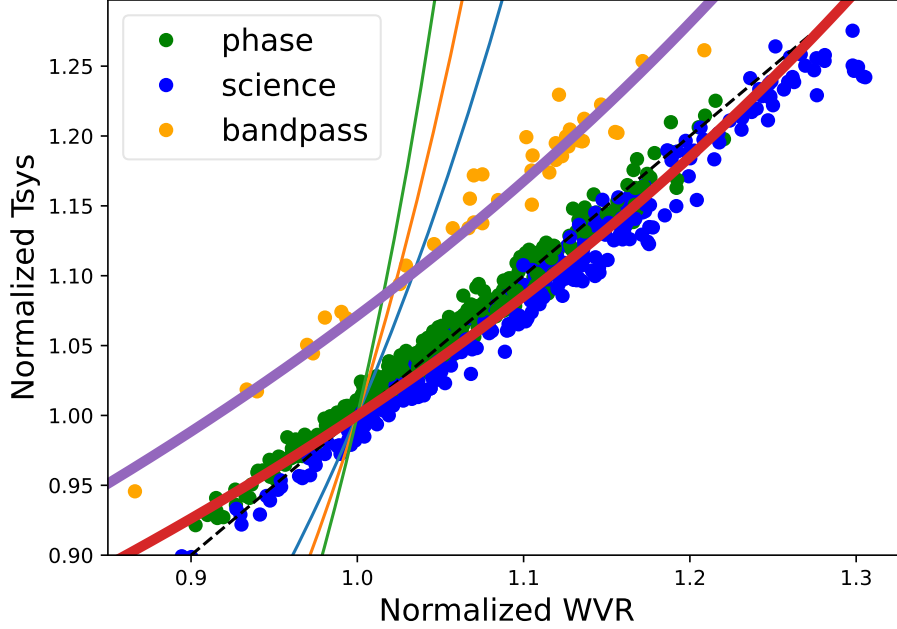


Figure 14. The correlation between \hat{T}_{sys} and \hat{T}_{WVR} (Fig. 9) overlaid by ATM modeling curves (blue, orange and green) obtained by varying the elevation (from 40-60 degrees) at a constant PWV.. Note in this case data from dataset Band8 is normalized only to the science target to show how elevation affects the data. The 3 ATM modeling curves correspond to different PWV values (blue: 0.6 mm; orange: 0.8 mm; green: 1.0 mm). The thick red line is the ATM modeling by changing PWV values from 0.5 to 1.0 mm with a fixed elevation of 53 degrees. The purple thick line is also from ATM modeling by changing PWVs with a fixed elevation of 48 degrees. Note that the purple line is normalized to the same value as the red line instead of the value from its own target for ease of comparison between absolute values in these two cases. T_{rx} in the modeling is set to be 100 K.

AC and T_{sys} versus WVR correlation for dataset Band8 and Band7a. We can see that the AC data also has a tight correlation with T_{sys} for dataset Band7. However, the correlation does not work well for dataset Band8 with a large scatter. Therefore, we cannot just fit the relation to several ATM scans to calculate the continuous T_{sys} with good precision.

The other thing we find is that AC and T_{sys} do not follow the proportional correlation as might be expected. The major reason is that AC data track the total signal received after the atmosphere attenuation while T_{sys} tracks the total signal before it comes through the atmosphere, as shown in the diagram in Fig. 17. The AC data is directly proportional to the total signal received by the antenna, which is mainly comprised of emission from the sky ($\eta_{\text{eff}}T_{\text{sky}}$), the receiver itself (T_{rx}), and other fixed losses terminating at ground ($(1 - \eta_{\text{eff}}) \times T_{\text{amb}}$). However, based on Eq. 1, T_{sys} is not directly proportional to these 3 components added together. Instead, T_{sys} can be thought of as brightness temperature of a fake source in space that generates a signal equal to the 3 components added together after atmosphere attenuation. In other words, for a single band setting,

$$P_{\text{AC}} \propto \eta_{\text{eff}} e^{-\tau_0 \sec z} T_{\text{sys}} = T_{\text{rx}} + \eta_{\text{eff}} T_{\text{sky}} + (1 - \eta_{\text{eff}}) \times T_{\text{amb}} \quad (18)$$

We call the right side of the equation attenuated T_{sys} . We also normalize the attenuated T_{sys} the same way as we do for the original T_{sys} and compare it with normalized AC data. The comparison between T_{sys} and attenuated T_{sys} versus AC correlation is shown in Fig. 16. As we can see, the normalized attenuated T_{sys} follows the 1-to-1 relation with normalized AC as suggested by Eq. 18. If we rearrange Eq. 18, it becomes

$$T_{\text{sys}} \propto \frac{P_{\text{AC}}}{e^{-\tau_{\text{sky}}}} = \frac{P_{\text{AC}}}{1 - T_{\text{sky}}/T_{\text{amb}}} \quad (19)$$

Therefore, even though we have the AC data, we still need a method to continuously monitor T_{sky} to get T_{sys} . Additionally, the AC and SQLD data suffer from gain drift and gain step changes between scans, as noted above and seen in Fig. 1. Thus we cannot measure continuous T_{sys} just with the AC data.

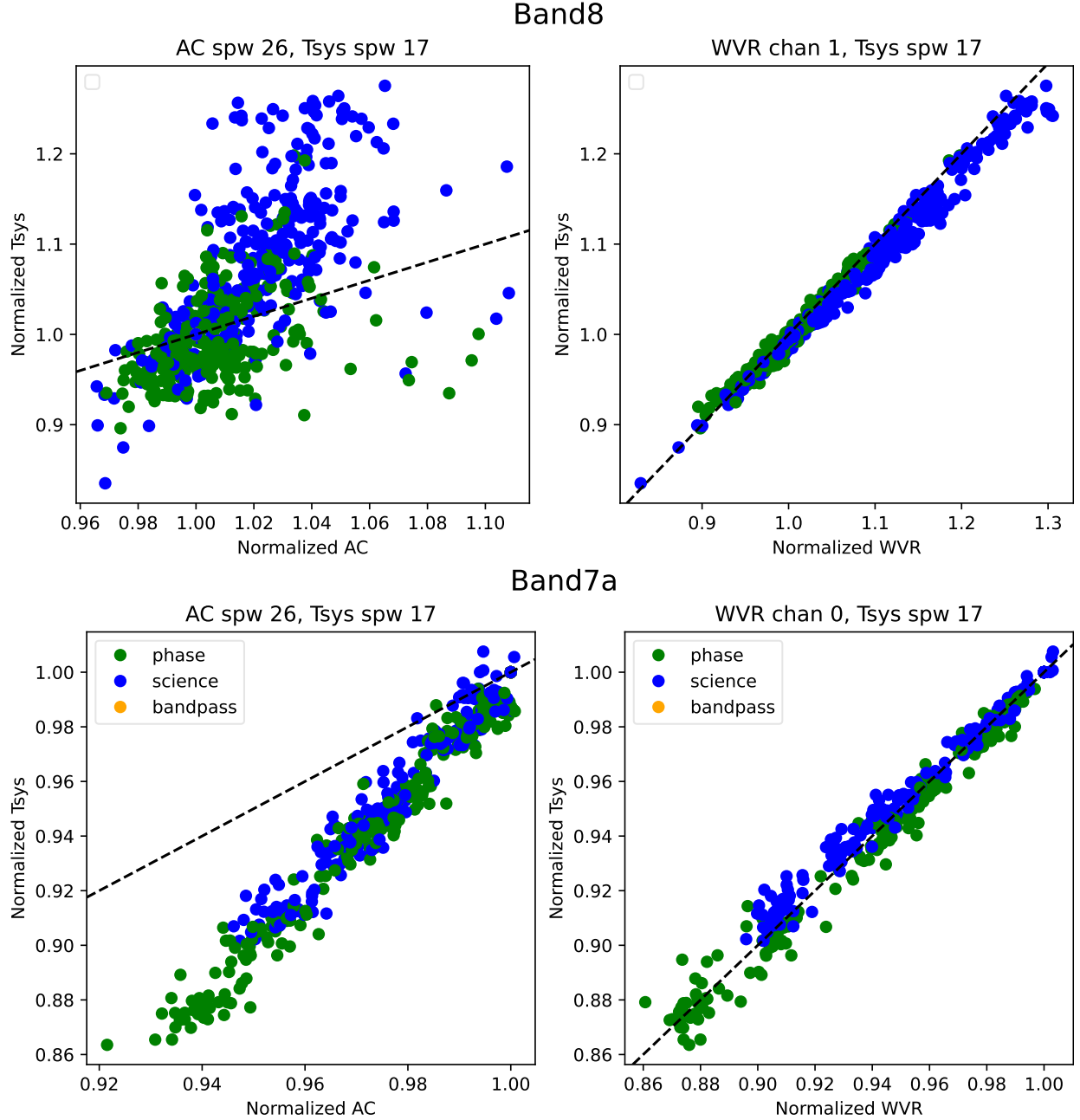


Figure 15. The correlation between the \hat{T}_{sys} and matched \hat{T}_{WVR} and normalized A_{AC} for all the antennas. Both WVR and auto-correlation data is averaged over 10 seconds.

4. APPLYING CONTINUOUS T_{sys} TO THE CALIBRATION

In Section 2, we demonstrated the viability to use WVR data to track T_{sys} continuously. In this section, we apply the extrapolated continuous T_{sys} in calibration to test whether our new method for measuring T_{sys} works. We calibrate each dataset with the original T_{sys} table, the new continuous T_{sys} table extrapolated using all ATM scans and that using just 4 ATM scans with CASA (McMullin et al. 2007) package. We then make images from data calibrated using these 3 different methods and see if the measured fluxes for the same target are more consistent with each other using our new methods. The detailed description of the scripts we use for the data processing can be found at https://github.com/heh15/ALMA_intern_Tsys.git.

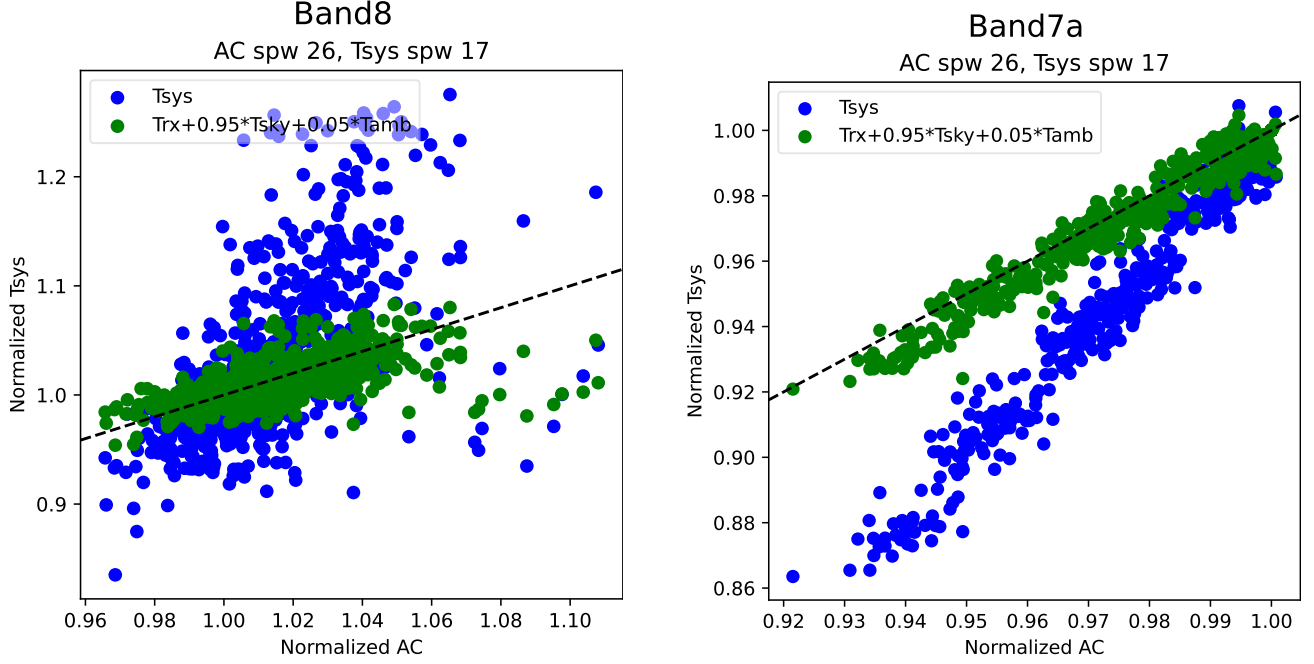


Figure 16. The correlation between the normalized T_{sys} (blue) and attenuated T_{sys} (green) and normalized AC data for the Band 8 and 7 data we have for all antennas of one spectral window. As we can see, the attenuated T_{sys} follows the 1-to-1 correlation with AC data, which proves equation 18 to be right.

4.1. Creation of T_{sys} Table

In this subsection we discuss how we construct the new T_{sys} table used for the calibration. We note that the original T_{sys} table used for calibration is a spectrum with two polarizations. Recording all the extrapolated T_{sys} spectra in one big table would take a lot of disk space. Based on our check of the T_{sys} spectrum plots generated using the original calibration script, the shape of the T_{sys} spectrum of each spectral window does not vary much as a function of time. Therefore, we can just record the initial T_{sys} for each observing target in the T_{sys} table and record the ratio of the extrapolated T_{sys} relative to the initial T_{sys} into an amplitude gain table. In this case, the two tables we provide for T_{sys} calibration are

$$T_{\text{sys}}(t, \nu) = T_{\text{sys,obs}}(1^{\text{st}}, \nu)$$

$$G(t) = \sqrt{1 / \left[\frac{T_{\text{sys}}(t)}{T_{\text{sys}}(1^{\text{st}})} \right]_{\text{fit}}} \quad (20)$$

where $T_{\text{sys}}(t, \nu)$ is the recorded T_{sys} spectrum as a function of time t and frequency ν , and G is the derived gain as a function of t , $T_{\text{sys,obs}}(1^{\text{st}}, \nu)$ is the first T_{sys} spectrum measured for each type of observation of given antenna and spectral window and $\left[\frac{T_{\text{sys}}}{T_{\text{sys}}(1^{\text{st}})} \right]_{\text{fit}}$ is the extrapolated normalized T_{sys} from the fitting. We note that G is not directly equal to the \hat{T}_{sys} values. This is due to the different methods that CASA uses to handle T_{sys} and gain table. For each baseline, the correlated amplitude is

$$S(i, j) \propto \sqrt{T_{\text{sys}}(i)T_{\text{sys}}(j)} \propto \frac{1}{G(i)G(j)} \quad (21)$$

Therefore, the G is written so that it can be properly translated to the variation in T_{sys} .

In Section 2.4, we tested using only 4 T_{sys} measurements to fit the linear relation between \hat{T}_{sys} and \hat{T}_{WVR} . We saw that the difference between this method and using all T_{sys} measurements is small. However, we still need to quantify if the small difference in the linear fits makes much difference in the measured flux of the image product. In this case, we

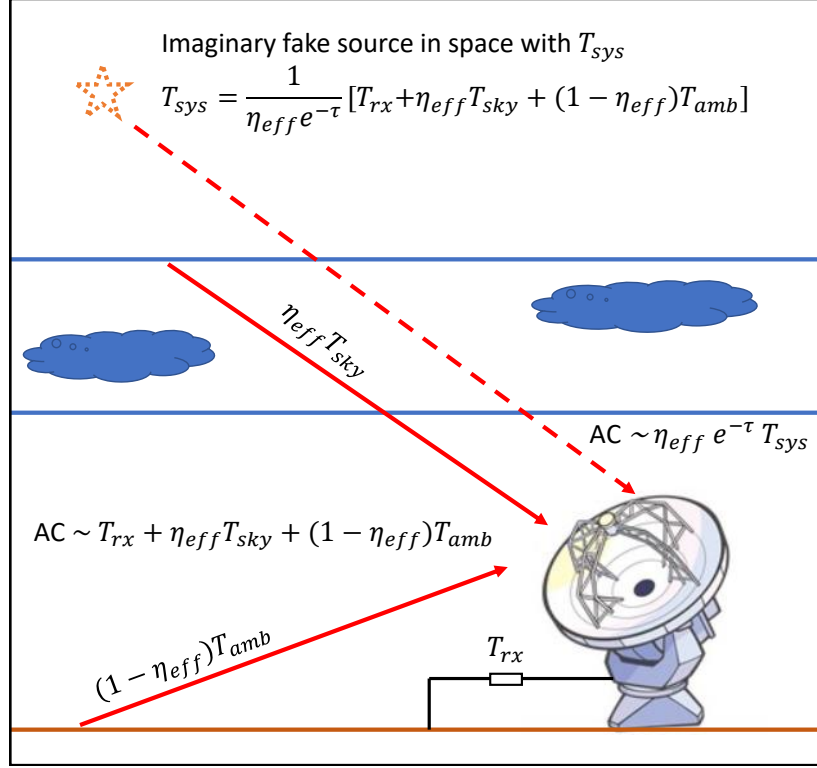


Figure 17. Illustration of the theoretical relationship between the autocorrelation signal AC and T_{sys} . AC is proportional to the total power signal received by an antenna, which includes receiver noise (T_{rx}), sky noise (T_{sky}), and thermal noise due to losses and spillover terminating around the ambient temperature $((1 - \eta_{\text{eff}}) \times T_{\text{amb}})$. However, T_{sys} is corrected for a source outside the atmosphere, and includes an extra term due to the atmospheric attenuation.

also apply Eq. 20 to create the alternative T_{sys} table with the fitting relation derived from 4 ATM scans. Therefore, we also extrapolate T_{sys} based on the fitting relation from 4 ATM scans.

4.2. Calibrating and Imaging the Data

After we create the T_{sys} table, we then apply the continuous T_{sys} in calibration. The calibration script we use is generated from the command `es.generateReducScript()`. We then modify the script to use the alternative T_{sys} and amplitude gain tables created (see details in https://github.com/heh15/ALMA_intern.Tsys.git). We also run the original calibration script to calibrate the data with the original discrete T_{sys} method for comparison.

After calibration, we then proceed with making continuum images. We generally adopt the default settings using the command `tclean`. We set the `robust` parameter to be 2.0 instead of the default 0.5 to maximize the sensitivity and hence flux accuracy. We also set the number of iterations to be 0 to only make the dirty image. This process will reduce any effects from `tclean` itself when making comparisons between fluxes from different calibration datasets. For projects with multiple datasets, we directly compare the measured fluxes from different datasets to see if they are consistent with each other. For projects with just one measurement set, we further make images using just the first half or the second half of the science scans and then compare fluxes among these 3 images. The top panel in Fig. 18 shows an example of images made with the 3 different methods for dataset Band8. We can see that the structure of these images looks almost the same. This is what we expect since T_{sys} should only affect the intensity scale of the final image. The bottom panel of Fig. 18 shows the images of the same target made with all scans or just half of the scans using the new method to extrapolate T_{sys} from all ATM scans. We can see the structures of these images are also almost the same, which is also what we expect as images from the same dataset should have the similar uv coverage. On the other hand, if we compare images made from different datasets, we can see there is a larger difference in image structure. This is most obvious in the Band 9 project 2019.1.00013.S shown in Fig. 19. The beam sizes for the 3

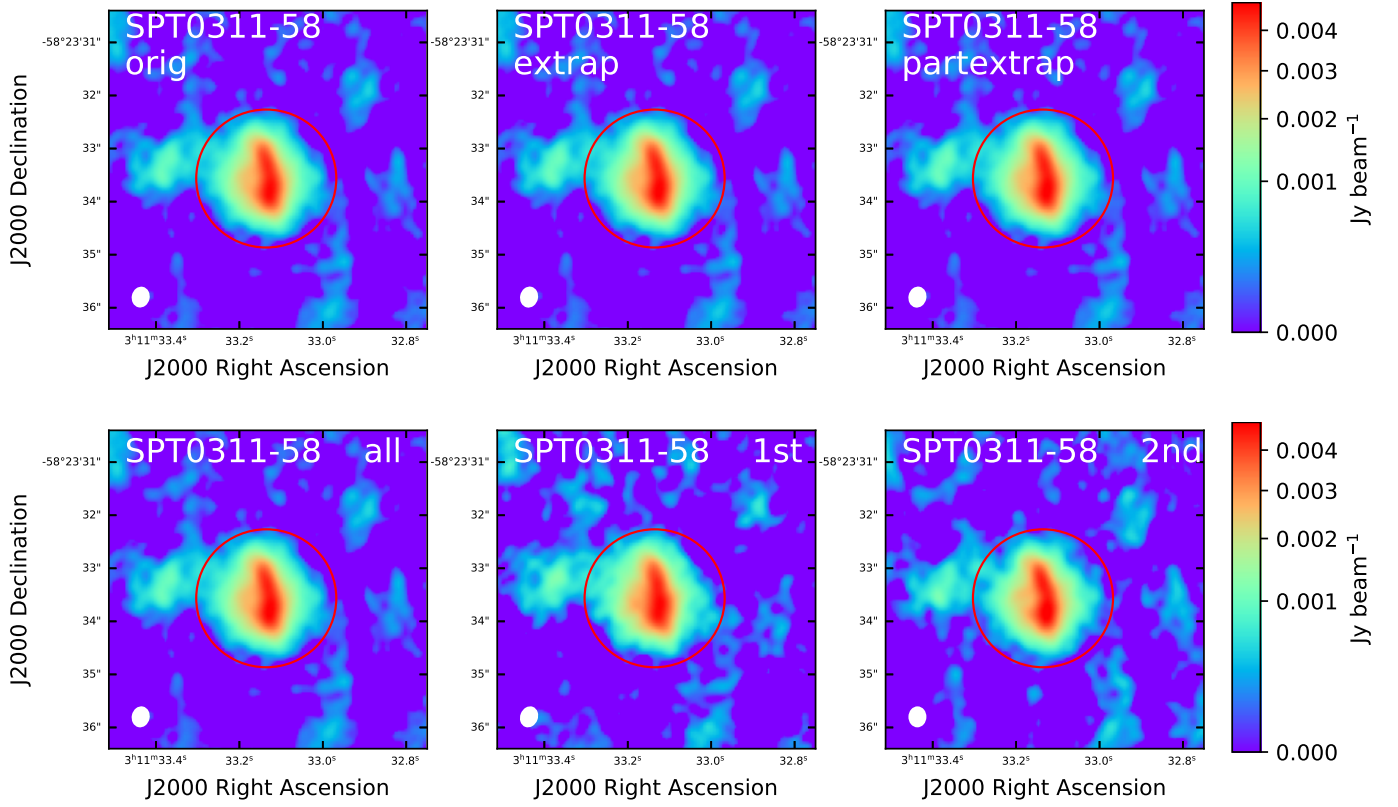


Figure 18. (Top) dirty images made using originally measured T_{sys} (orig), extrapolated continuous T_{sys} with all ATM scans (extrap) and that with just 4 ATM scans (partextrap) for dataset Band8 of SPT0311-58. The red circle is the aperture used for flux measurements. The fluxes for these 3 images are 0.0425, 0.0429 and 0.0407 Jy. (Bottom) dirty images made using alternative continuous T_{sys} table derived from fitting all ATM scans. The 3 columns are images made using all, 1st half and 2nd half of the science scans. The fluxes for these 3 images are 0.0429, 0.0432 and 0.0428 Jy.

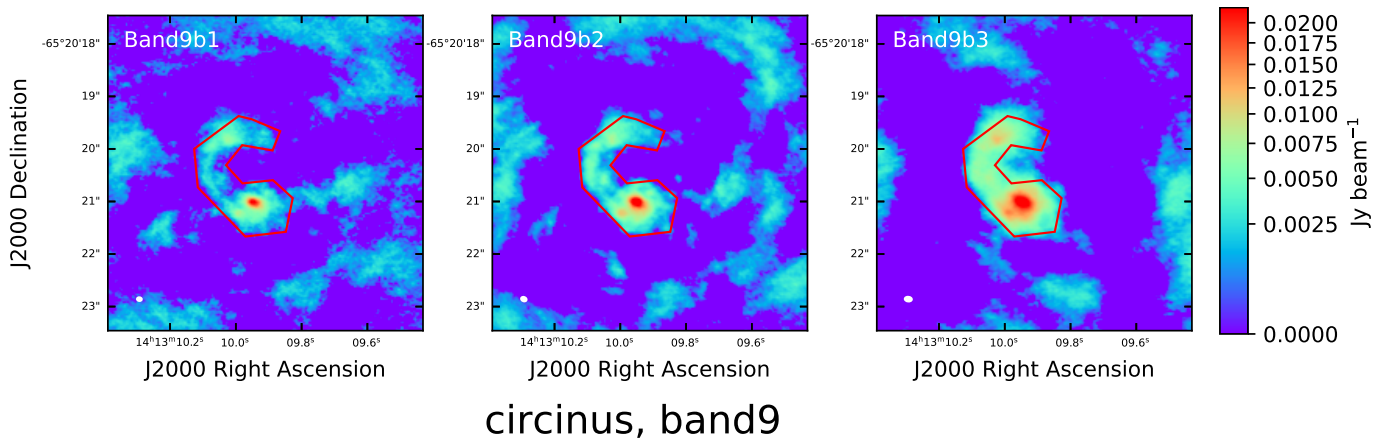


Figure 19. Dirty images made using alternative continuous T_{sys} table using all ATM scans for the 3 data sets in the Band 9 project 2019.1.00013.S. The red polygons are apertures used to measure the flux. The fluxes for these 3 images are 0.875, 1.0 and 1.35 Jy.

different images are also significantly different from each other. For dataset Band7b, all images have similar beam shapes so differences among the image structures are not that significant.

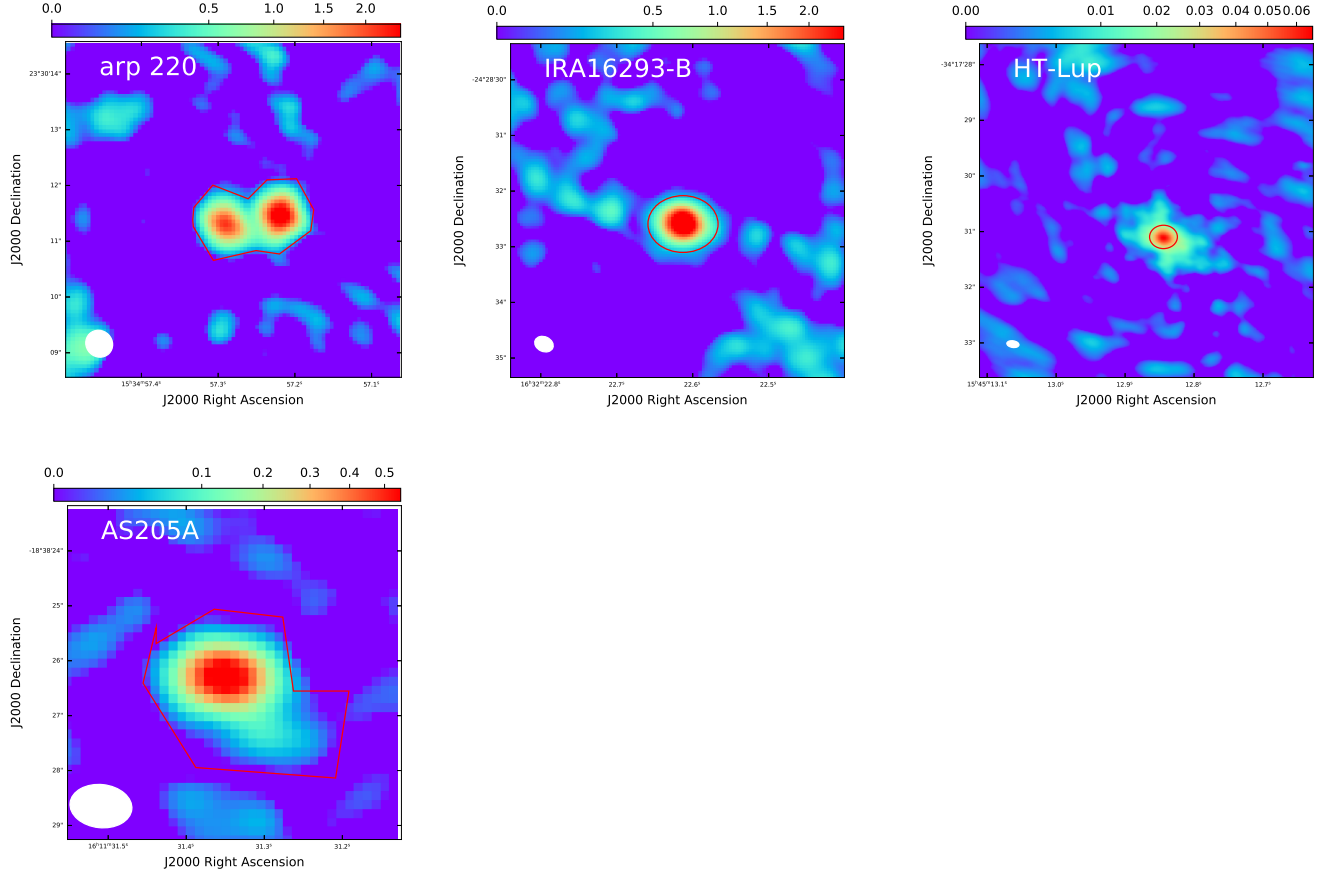


Figure 20. Dirty images for other sources made using alternative continuous T_{sys} table using all ATM scans. For Band 7 project 2018.1.01210.S (AS205A), we show the image made from data uid://A002/Xda1250/X2387 (Band7b1). The red polygons are apertures used to measure the flux.

Once the images are made, we draw an aperture around the central point source to measure the flux. Since the change in T_{sys} does not change the structure of the continuum image, we can compare the fluxes measured from the same aperture for the same target (as long as the aperture is not missing any flux, or there is no decorrelation – as decorrelation will reduce the total flux potentially). The apertures we used to measure the fluxes are shown in Fig. 18, 20 and 19. Note that as well as changes in T_{sys} , changes in phase decorrelation during a single observation and between observations may also affect the measured fluxes, and account for some of the scatter in fluxes in Table 3, 4 and 5. However, we assume this effect is the same in all reductions, independent of the T_{sys} calibration method.

4.3. Flux Comparison

The measured fluxes are recorded in Table 3, 4 and 5. The flux uncertainty can be separated into two parts, the measurement error and the calibration error. The measurement error is calculated as

$$\text{Meas.Err} = \text{rms} \sqrt{N_{\text{beam}}} \quad (22)$$

where the rms is the measured noise of the image and N_{beam} is the number of beams across the aperture used to measure the flux. On the other hand, our alternative method to measure T_{sys} should mainly work on reducing the calibration error. To test if our new method improves the flux calibration accuracy, we need to quantify the calibration error for each method we use. For projects with single dataset, we compare fluxes of images made with 1st half, 2nd

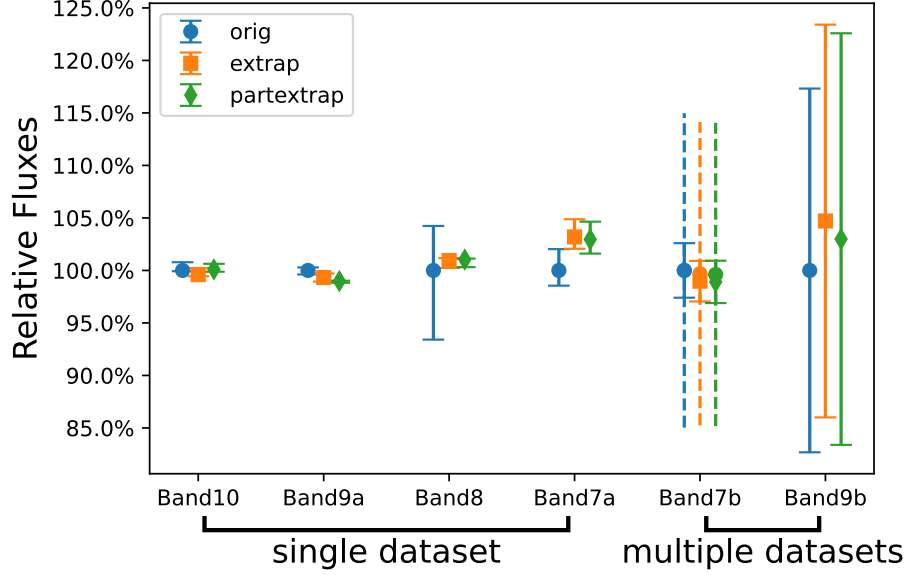


Figure 21. Comparison of fluxes of images made using the original T_{sys} (orig), continuous T_{sys} extrapolated from all ATM scans (extrap) and that extrapolated from 4 ATM scans (partextrap). The vertical axis are the ratio of fluxes to the fluxes using original method. The first 4 projects contain single dataset while the last two projects contain multiple datasets. The dashed line for Band7b project shows the error including the two datasets that has abnormal flux values (see Table .4). We can see the flux consistency is generally better for most of the projects with smaller uncertainties. See description in Section 4.3.

half and all scans and calculate the maximal difference between the 3 flux values as the calibration error. For projects with multiple datasets, the calibration error is calculated as the standard deviation of fluxes of the different datasets. Both measurement and calibration errors are recorded in Table 3, 4 and 5.

To further compare how our methods work for datasets from different frequency bands, we normalize the flux values to the flux value using the original discrete T_{sys} calibration method with all ATM scans. The relative uncertainties are calculated as the calibration error divided by the flux value for each method using all ATM scans. The comparison is shown in Fig. 21. We can see that fluxes using the original T_{sys} table do not differ significantly from the fluxes using alternative T_{sys} and gain tables, with maximal differences smaller than 5 %. We also demonstrate that the extrapolated T_{sys} using 4 ATM scans gives us fluxes that are almost the same as when using all ATM scans, which proves it is viable to significantly reduce the number of T_{sys} measurements by using WVR-tracked T_{sys} . Furthermore, it seems for most of the datasets, our new methods give better flux consistency, especially for dataset Band8 which has the highest PWV value of 0.85 mm among all the datasets. As shown in Fig. 4, T_{sys} variation throughout the observation is dramatic without a straightforward pattern (monotonously increasing or decreasing). In this case, the discrete T_{sys} measurements probably did not catch the fluctuations of the real T_{sys} . Our new method instead catches the variation in T_{sys} between the discrete ATM calibrations, and thus keeps the flux consistent. This method also works for dataset Band7b with multiple data sets with relative flux uncertainties reduce from 2.5% to 1.9%. The only project that gives us larger flux uncertainties using our new methods is the dataset Band9b. For this project, the uncertainties using all 3 methods are quite large ($\sim 15\%$). The large uncertainties are probably due to different uv-coverages, the complex target structure and relatively high phase noise in these datasets. This is also a tricky dataset for which the linear fitting does not work as well as for other data sets. In our future work, we will explore if the larger uncertainty is caused by imperfect fitting of T_{sys} versus T_{WVR} relation.

4.4. Additional considerations for the continuous T_{sys} method

For some targets, the source brightness temperature in single-dish measurements can be significant compared with T_{sys} . For example, this may occur for bright galactic targets in 12CO, bright masers, or for some Solar System objects in continuum. As the widths of galactic spectral lines are generally negligible ($\lesssim 1\%$) compared with the normal bandwidth (2GHz) used to measure T_{sys} , and the continuous T_{sys} method uses a spectrally-averaged broad-band T_{sys} ,

Table 3. Flux measured for project with only one dataset

Data Label	Target	Scans used	Flux (Jy)			Meas. Err. (Jy)	Beam (")
			Tsys_orig	Tsys_extrap	Tsys_partextrap		
(1)	(2)	(3)	(4)	(5)	(6)	(7)	(8)
Band10	Arp 220	all	7.169	7.146	7.187	0.39	0.5 x 0.47
		1st half	7.1638	7.135	7.171	0.42	0.52 x 0.45
		2nd half	7.1077	7.09	7.133	0.4	0.48 x 0.48
		MAX. DIFF ^a	0.06	0.056	0.054		
Band9a	IRAS16293-B	all	10.43	10.36	10.324	0.34	0.34 x 0.27
		1st half	10.4	10.32	10.32	0.36	0.35 x 0.27
		2nd half	10.47	10.4	10.34	0.38	0.34 x 0.26
		MAX. DIFF.	0.07	0.04	0.02		
Band8	SPT0311-58	all	0.0425	0.0429	0.0429	0.0015	0.35 x 0.3
		1st half	0.0453	0.0432	0.0433	0.0019	0.36 x 0.29
		2nd half	0.0407	0.0428	0.0429	0.0017	0.35 x 0.3
		MAX. DIFF	0.0046	0.0003	0.0003		
Band7a	HT-Lup	all	0.173	0.178	0.178	0.0038	0.22 x 0.12
		1st half	0.169	0.175	0.175	0.0044	0.22 x 0.12
		2nd half	0.175	0.18	0.18	0.0045	0.22 x 0.12
		MAX. DIFF.	0.006	0.005	0.005		

Columns: (1) The label of each dataset (see Table 2) (2) The target name. (3) The science scans used to make images. (4) Fluxes of the source with images made using original calibration script. (5) Fluxes of the source with images made using modified script with alternative T_{sys} table. The T_{sys} is extrapolated based on all ATM scans. (6) The images made with modified script but T_{sys} is extrapolated from 4 ATM scans. (7) The measured flux errors for the images made with original T_{sys} table (8) The beam size of images using original T_{sys} table.

Rows: a. The maximal differences for fluxes at each column.

Table 4. Flux measured for data for Band7b project (AS205A)

Dataset Label	Flux (Jy)			Meas. Err. (Jy)	Beam (")
	Tsys_orig	Tsys_extrap	Tsys_partextrap		
(1)	(2)	(3)	(4)	(5)	(6)
Band7b1	0.7699	0.759	0.7594	0.031	1.13 x 0.79
Band7b2	0.713	0.7146	0.7129	0.029	0.96 x 0.77
Band7b3*	1.001	1.005	1.003	0.043	0.68 x 0.53
Band7b4	0.747	0.7378	0.7359	0.028	1.03 x 0.78
Band7b5*	0.556	0.58	0.58	0.029	1.31 x 0.72
Band7b6	0.749	0.7534	0.7533	0.03	0.91 x 0.08
Band7b7	0.7355	0.7347	0.7348	0.029	1.01 x 0.81
Band7b8	0.768	0.737	0.7372	0.029	1.24 x 0.79
AVG. ^a	0.7471	0.7394	0.7389		
STD. ^b	0.0194	0.0143	0.0149		

Columns: (1) The label for each dataset (see Table 2). (2) Flux of the data set using the original T_{sys} table. (3) Flux of the data set using alternative continuous T_{sys} table with the linear relation fitted using all ATM scans. (4) Flux of the data set using continuous T_{sys} table with the linear relation fitted using part of ATM scans. (5) Measured flux errors using original T_{sys} table. (6) Beams of the image using original T_{sys} table.

Rows: a. The average value for each column. b. The standard deviation for each column.

Notes: * denotes data with unusual fluxes. Fluxes from these data are not included in the calculation of the average and standard deviation value.

Table 5. Flux measured for data for dataset Band9b (Circinus)

Dataset Label	Flux (Jy)			Meas. Err. (Jy)	Beam (")
	Tsys_orig	Tsys_extrap	Tsys_partextrap		
(1)	(2)	(3)	(4)	(5)	(6)
Band9b1	0.85	0.875	0.849	0.018	0.086 x 0.065
Band9b2	0.96	1	0.983	0.021	0.104 x 0.077
Band9b3	1.27	1.35	1.34	0.016	0.131 x 0.085
AVG.	1.027	1.075	1.057		
STD.	0.178	0.201	0.207		

Columns: (1) The label for each dataset (see Table 2). (2) Flux of the data set using the original T_{sys} table. (3) Flux of the data set using alternative continuous T_{sys} table with the linear relation fitted using all ATM scans. (4) Flux of the data set using continuous T_{sys} table with the linear relation fitted using part of ATM scans.

Rows: a. The average value for each column. b. The standard deviation for each column.

then the effect of bright lines in such cases will be negligible. But for very bright continuum sources such as planets, the spectrally-averaged T_{sys} will potentially be affected by the target brightness. However, the beam of the WVR unit on each antenna is offset from the optical axes of the receiver beams by several arc minutes (depending on the receiver band in use - see ALMA Technical handbook); this means that the WVRs are not pointing to the science target, and in general will not be affected by its strong continuum. Additionally, it has recently become apparent that the method used by ALMA to measure T_{sys} , using off-source data along with the normalisation of the visibilities using the autocorrelation, introduces a calibration error for bright sources. The planned change is to measure Tsys on-source. Again, this should not significantly affect the continuous Tsys method, for reasons given above.

For spectral lines, an assumption is made that T_{sys} is mainly affected by PWV, and the correlation of Tsys with PWV uses T_{sys} averaged over the spectral window. This is considered reasonable for continuum and most spectral lines, but for calibration of spectral lines coincident with deep Ozone absorption (eg see Figure 12), the correlation will have a slightly different slope and intercept. In general this is considered a second-order effect; for example, a line exactly coincident with the strong O₃ peak at 428.8GHz in Fig. 12, the error in the correction of T_{sys} based on the PWV would be $\sim \pm 3\%$. A future improvement might be correct the data spectrally rather than using a single channel-averaged value per timestamp. However, this would make the correction table significantly larger (see Section 4.1).

An additional use of the continuous T_{sys} method could be to correct for the increase in T_{sys} due to shadowing of the antennas. On ALMA, the default is that data taken with any slight blocking of the beam from an antenna, for example by a nearby antenna or building, is flagged and removed during data reduction. In general this cannot be corrected for using the gain calibrator amplitude solution, as this is not observed at the same sky location as the target. However, if the corresponding increase in Tsys due to shadowing is measured continuously, it may be possible to calibrate out some degree of shadowing. Further investigation of this technique should be done.

5. CONCLUSIONS AND FUTURE WORK

In this paper, we explore a new method to use continuous datastreams available from WVR monitoring to track the atmospheric opacity and hence T_{sys} in mm and submm data. The aim is to improve flux calibration in conditions where the sky opacity is rapidly varying, and to reduce overheads needed for frequent discrete calibration using internal loads. Here we summarize our main conclusions regarding initial tests of this method.

- There is a tight linear correlation between normalized T_{sys} and T_{WVR} , with typical scatter of $\sim 1\%$. Although the exact form of the linear relation varies among different spectral windows and different data sets, we can use as few as 4 ATM scans to determine the slope and intercept of the linear relation, which suggests it is possible to significantly reduce the number of discrete T_{sys} measurements during observations, particularly at high frequencies. Furthermore it is not necessary to perform separate calibrations on the phase calibrator and science target, as the continuous T_{sys} method is able to track differences in T_{sys} between the two. We also try the ATM modeling and find a good agreement between the data and ATM generated correlation between T_{sys} and T_{WVR} .

- We apply the continuous T_{sys} in calibration and find that it generally gives us more consistent fluxes for the same target. The only exception is the dataset Band9b as our new methods give higher flux uncertainties. We suspect part of reasons are due to the imperfect linear fitting of the T_{sys} vs T_{WVR} relation. Since the uv-coverages for the data sets in this project are significantly different, it is hard to confirm this scenario for this data set.
- If this method is used for sub-mm observatories such as ALMA, it can reduce the number of T_{sys} measurements required at high frequencies from 10 \sim 20 down to 5 (4 T_{sys} measurements for the fitting and 1 bandpass T_{sys}) or fewer. Assuming each observation block takes \sim 60 mins and each T_{sys} measurement takes about 30 – 40 seconds, it has the potential to save \sim 10% of observing time for high frequency observing, which is made more valuable as the amount of time in such good conditions is limited.

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ADS/JAO.ALMA #2015.1.00271.S

ADS/JAO.ALMA #2016.1.00744.S

ADS/JAO.ALMA #2018.1.01778.S

ADS/JAO.ALMA #E2E8.1.00003.S

ADS/JAO.ALMA #2018.1.01210.S

ADS/JAO.ALMA #2019.1.00013.S. ALMA is a partnership of ESO (representing its member states), NSF (USA) and NINS (Japan), together with NRC (Canada), MOST and ASIAA (Taiwan), and KASI (Republic of Korea), in cooperation with the Republic of Chile. The Joint ALMA Observatory is operated by ESO, AUI/NRAO and NAOJ. The National Radio Astronomy Observatory is a facility of the National Science Foundation operated under cooperative agreement by Associated Universities, Inc. This research made use of Astropy,¹ a community-developed core Python package for Astronomy (Astropy Collaboration et al. 2013, 2018). HH acknowledges the support of NSERC-CREATE NTCO training program. The research of C.D.W. is supported by grants from the Natural Sciences and Engineering Research Council of Canada and the Canada Research Chairs program.

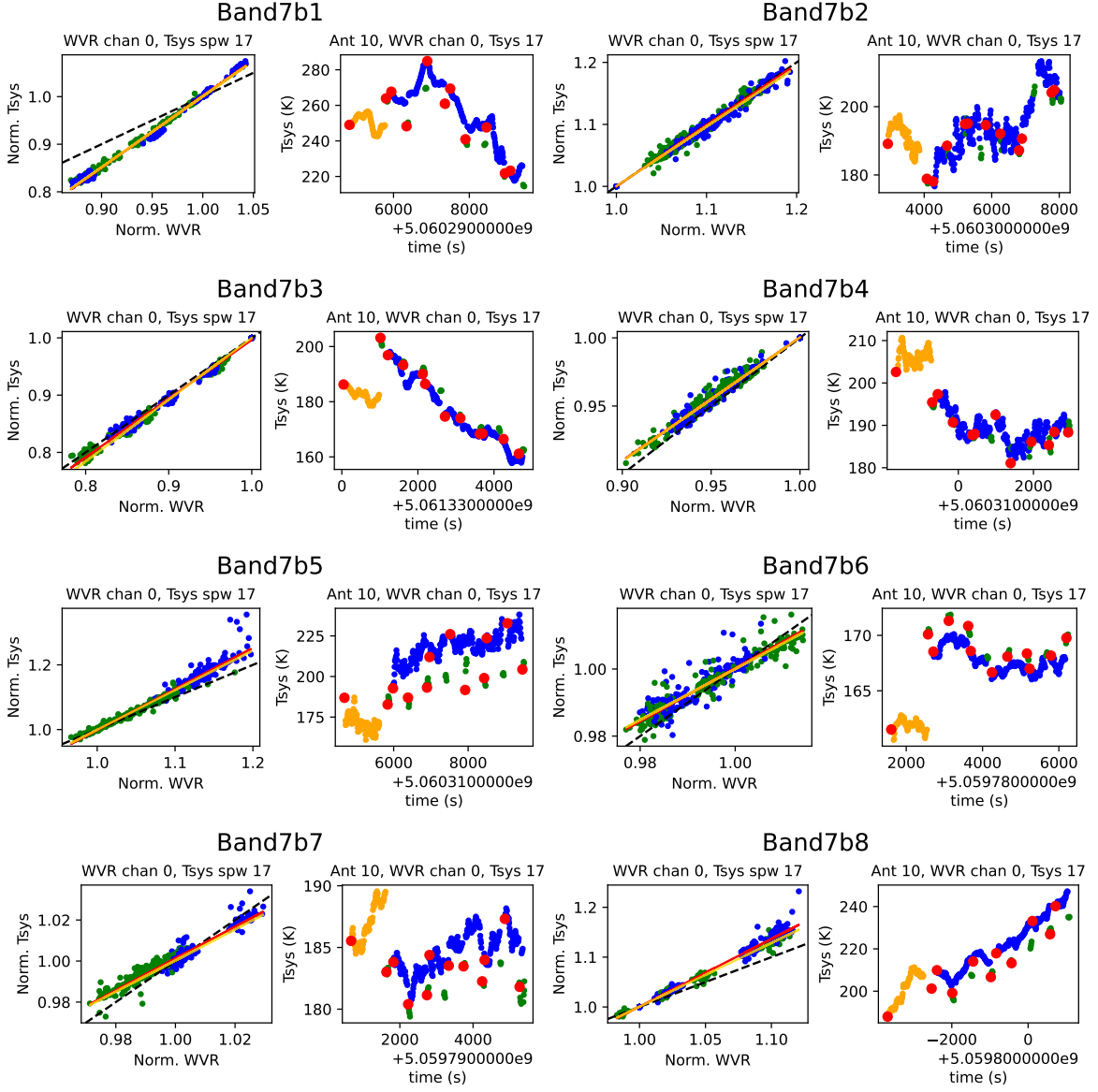
Software: astropy (Astropy Collaboration et al. 2013, 2018), CASA (McMullin et al. 2007)

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APPENDIX

A. EXTRA FIGURES



Project: 2018.1.01210.S; Band 7

Figure 22. The summary of linear relation between T_{sys} and T_{WVR} and comparison between measured and extrapolated T_{sys} for measurement sets in project 2018.1.01210.S. For each measurement set, the left subplot shows the linear correlation between normalized T_{sys} and T_{WVR} . The blue and green points are from science and phase scan. The dashed line shows the 1-to-1 relation. The red and golden solid line is the fitted linear relation using data from all ATM scans or just 4 ATM scans. The right plot shows the extrapolated T_{sys} based on the fitting relation using all ATM scans. The orange, green and blue points are extrapolated T_{sys} for bandpass, phase and science targets. The red points are the original measured T_{sys} .

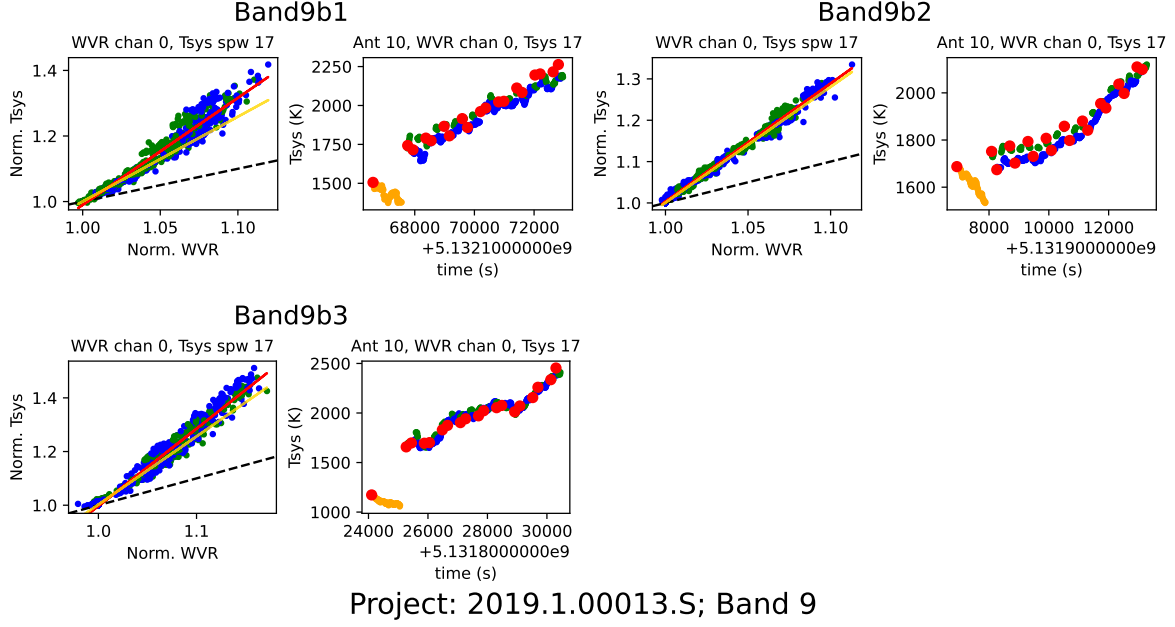


Figure 23. The summary of linear relation between T_{sys} and T_{WVR} and comparison between measured and extrapolated T_{sys} for measurement sets in project 2019.1.01210.S. See details in Fig. 22.

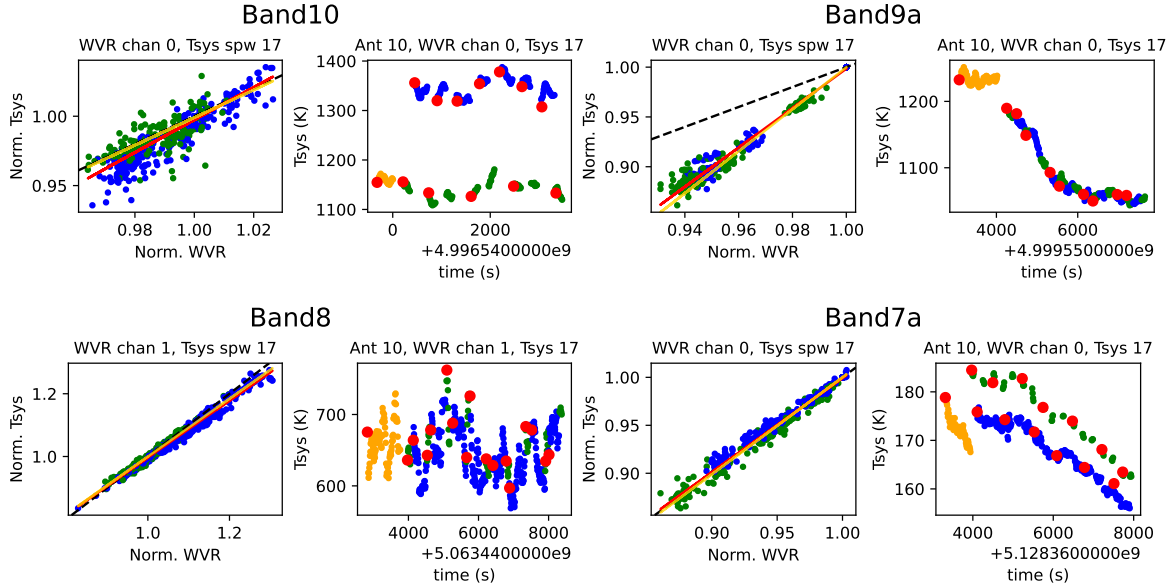


Figure 24. The summary of linear relation between T_{sys} and T_{WVR} and comparison between measured and extrapolated T_{sys} for the other 4 projects used in this paper with just one measurement set. See details in Fig. 22.

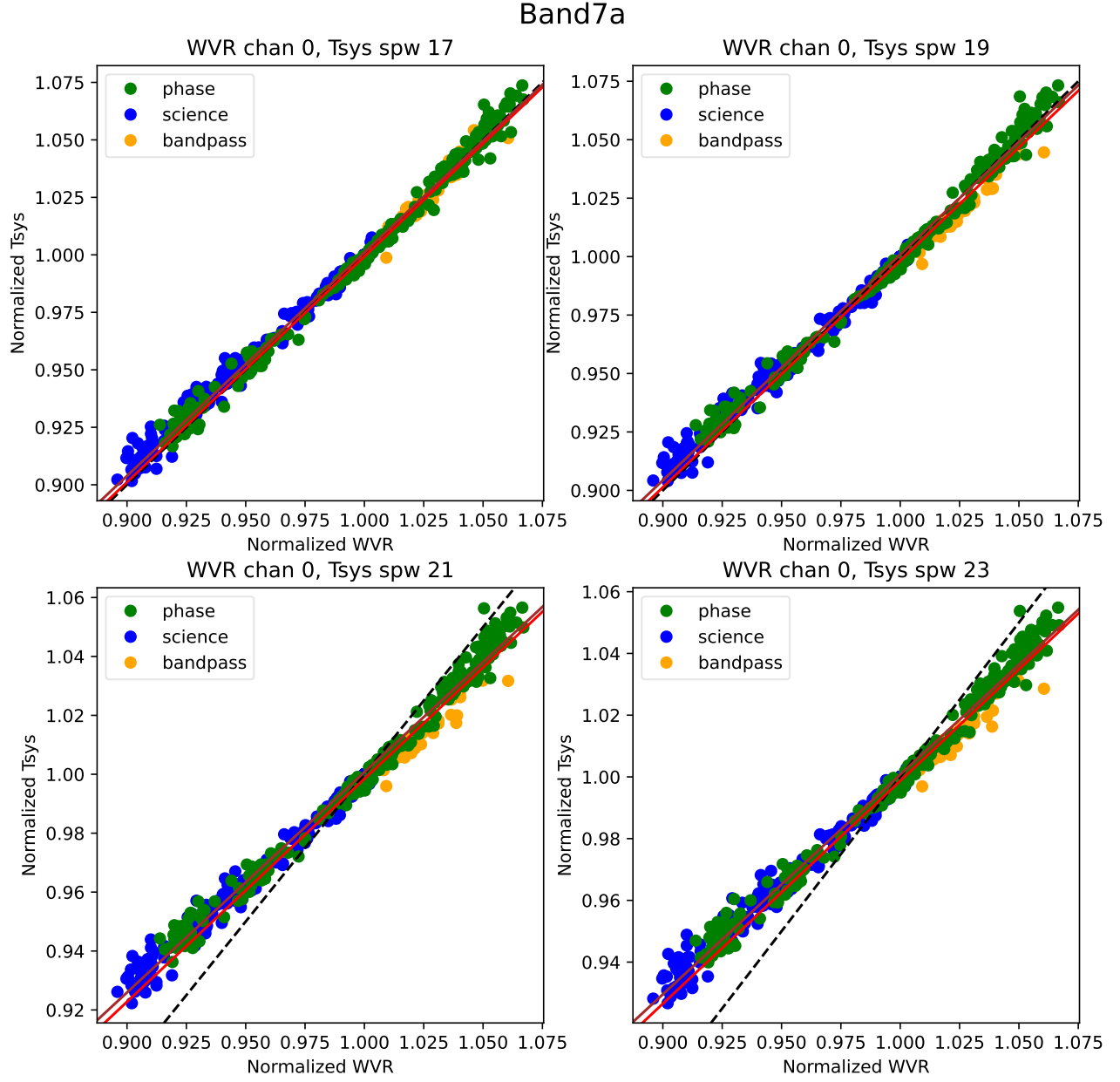


Figure 25. T_{sys} versus T_{WVR} normalized to the first science ATM scan for the dataset Band7a. The black dashed line is the 1-to-1 relation. The brown solid line is the linear fitting to the data. The red solid line is the original fitting relation to the data normalized to each type of observing target.