

CS121 Parallel Computing Lab 2

Cuckoo Hashing using CUDA

A hash table is a data structure for maintaining a set of objects which allows fast insertion, deletion and lookup operations. There are a number of different methods for constructing hash tables, including chaining, linear and quadratic probing, double hashing, perfect hashing, etc. One widely used method in practice is *cuckoo hashing*, which guarantees $O(1)$ time lookup operations, in contrast to most other methods. This lab asks you to implement cuckoo hashing using CUDA. We first give an overview of how cuckoo hashing works, then describe the requirements of the lab.

Overview of Cuckoo Hashing

Cuckoo hashing is named after a type of bird which lays its eggs in other birds' nests, and whose chicks push out the other eggs from the nest after they hatch. Cuckoo hashing uses an array of size n , allowing up to n items to be stored in the hash table. For simplicity, we only consider storing keys in the hash table and ignore any associated data.

We first describe the insert operation, which is the most complex. Each key k can be stored into one of $t > 1$ locations in the table, where t is generally a small number such as 2. These locations are given by $h_1(k), h_2(k), \dots, h_t(k)$, where h_1, h_2, \dots, h_t are fixed hash functions. To insert k , we try to store it in location $h_1(k)$. If $h_1(k)$ was previously empty, then we are done. However, if there was a key k_1 previously stored in $h_1(k)$, then we need to *evict* k_1 and store it elsewhere in the table. In particular, suppose $h_1(k) = h_{i_1}(k_1)$; that is, location $h_1(k)$ is the i_1 'th location where k_1 can be stored. Then we store k_1 in the next possible location $h_{i_1+1}(k_1)$; if $i_1 + 1 > t$, we wrap around and store k_1 at location $h_1(k_1)$. Then, similar to before, we check if the new location for k_1 was previously empty. If so, we are done. Otherwise, if the location was previously occupied by a key k_2 , and if this location is the i_2 'th possible location for k_2 , i.e. $h_{i_2}(k_2)$, we evict k_2 and store it at its next possible location $h_{i_2+1}(k_2)$ (wrapping around if necessary). Storing k_2 may cause another eviction, requiring us to repeat the previous procedure.

Eventually, the insertion operation either terminates with an insertion into an empty location, or leads to a long chain of evictions. Worse still, the chain can sometimes cycle back on itself and cause an infinite loop. In order to avoid overly long eviction chains, we place an upper bound $M = O(\log n)$ on the length of a chain. If an insertion causes more than M evictions, we declare a *failure* using the current hash functions h_1, \dots, h_t . We then restart the insertion process by picking a new set of hash functions of h'_1, \dots, h'_t , and trying to insert *all* the keys using the new functions. That is, we rebuild the entire hash table using a new set of hash functions. We repeat this process until all the keys are successfully inserted using some set of hash functions. An illustration of the insertion process can be seen at the Wikipedia page https://www.wikiwand.com/en/Cuckoo_hashing.

In contrast to insertions, looking up a key k using cuckoo hashing is very simple. We simply check the locations $h_1(k), \dots, h_t(k)$ to see if k is stored in any of them. Note that this always takes a constant $O(t)$ number of steps. Similarly, to delete k we check whether it is stored at locations $h_1(k), \dots, h_t(k)$, and set a location to empty if k is found there.

Implementing Cuckoo Hashing in CUDA

For this lab, you will implement cuckoo hashing on the GPU using CUDA. First, design a parallel cuckoo hashing algorithm optimized for the GPU architecture. State clearly which hash functions you use. Your overall goal is to make the algorithm as fast as possible.

Next, use your algorithm to perform the following experiments. Perform each experiment first with two hash functions (i.e. $t = 2$), then again with three functions. When inserting n items, use a bound of $4 \log n$ on the length of an eviction chain before restarting. Measure the amount of time each experiment takes, and report the speed of your algorithm in terms of millions of operations (insertions or lookups) per second. To obtain reliable results, perform each experiment 5 times.

1. Create a hash table of size 2^{25} in GPU global memory, where each table entry stores a 32-bit integer. Insert a set of 2^s random integer keys into the hash table, for $s = 10, 11, \dots, 24$.
2. Insert a set S of 2^{24} random keys into a hash table of size 2^{25} , then perform lookups for the following sets of keys S_0, \dots, S_{10} . Each set S_i should contain 2^{24} keys, where $(100 - 10i)$ percent of the keys are randomly chosen from S , and the remainder are random 32-bit keys. For example, S_0 should contain only random keys from S , while S_5 should 50% random keys from S , and 50% completely random keys.
3. Fix a set of $n = 2^{24}$ random keys, and measure the time to insert the keys into hash tables of sizes $1.1n, 1.2n, \dots, 2n$. Also, measure the insertion times for hash tables of sizes $1.01n, 1.02n$ and $1.05n$. Terminate the experiment if it takes too long and report the time used.
4. Using $n = 2^{24}$ random keys and a hash table of size $1.4n$, experiment with different bounds on the maximum length of an eviction chain before restarting. Which bound gives the best running time for constructing the hash table? Note however you are not required to find the optimal bound.

Submission

Prepare a report clearly describing your algorithm, your benchmarks, and the configuration of the machine and GPU you benchmarked on. Also describe any optimizations you performed or problems you encountered. Create scripts to easily compile your code and for running the experiments described above. Also provide a function to create a hash table using a set of keys given in a user-specified file, and for searching for a set of keys specified in a different file. Submit your report and code to the TA. The due date for the lab is **11:59pm, January 2, 2022**.