### PGF transformer semantics

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## You may have doubts

The theme: PGF transform semantics based equivalence checking of pGCL programs

#### Equivalence checking?

This work is about linearity no normalization is ever involved.

#### I heard the problem is undecidable!

We will focus on a restricted fragment of pGCL called ReDiP.

- Introduction
  - Backgrounds
  - Limitations of previous works
- 2 Formulation
  - Research questions
  - Overview of the solution
- g pGCL and ReDiP
  - Syntax and Semantics of pGCL
  - Restrictions on pGCL: ReDiP
- 4 PGF transformer semantics
  - Review on PGFs

- PGF transformer semantics of ReDiP
- Handling loops with fixed point induction
- Properties of the PGF transformer semantics
- Evaluation
  - Setup
  - Results
  - Case Study
- O Discussion
  - Conclusion of this project
  - Future works

# Backgrounds

### Motivation

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## The research questions

### Overview of our solution

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# Syntax of pGCL

# Semantics of pGCL

A fragement of pGCL: ReDiP

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### Review on PGFs

### PGF transformer semantics

### Fixed Point Induction

## Linearity & Closed-form preservation

# Summary

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# Benchmark setup

### Results

# Case Study

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### Conclusion

### Limitations and future works

Q & A

Questions are welcomed.



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