SmallK: A Library for Nonnegative Matrix Factorization, Topic Modeling, and Clustering of Large-Scale Data

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I. Introduction

High-dimensional data sets are ubiquitous in data science, and they often present serious problems for researchers. Our work in dimensionality reduction focuses on, but is not limited to, low-rank approximations via nonnegative matrix factorization (NMF) [1, 2]. NMF is a non-convex optimization problem with important applications in data and interactive visual analytics of high-dimensional data.

The impetus for this document is to provide a step-by-step procedure for the application of the theory to real-world large-scale data analytics. We have instantiated our research efforts in a software framework that includes high-level driver code via Python and a simple command line interface, SmallK, which hides most of the details of the input parameters. Our low-level code, also usable from the command line, is written in C++, which provides efficient NMF algorithms. The algorithms discussed herein have numerous practical applications; this document will hopefully provide the information required to quickly begin real work.

Below is a brief description of our fundamental research on NMF algorithms (please see the references section for more detail). Following the brief motivational introduction to the NMF are detailed installation instructions for the NMF software framework.

Low-rank approximations and NMF

Algorithms that enable dimension reduction and clustering are two critical areas in data analytics and interactive visual analysis of high-dimensional data. A low-rank approximation framework has the ability to facilitate faster processing times and utilize fewer resources. These approximations provide a natural way to compute only what we need for significant dimension reduction, and are analogous to singular value decomposition (SVD) and principal component analysis (PCA). The algorithm framework also works efficiently for clustering since clustering can be viewed as a specific way of achieving a low-rank approximation so that the clustered structure of the data is well represented in a few basis vectors.

Matrix low-rank approximations such as the SVD have played a key role as a fundamental tool in machine learning, data mining, and other areas of computational science and engineering. The NMF has recently emerged as an important constrained low rank approximation method as well. A distinguishing feature of the NMF is the requirement of nonnegativity: NMF is considered for high-dimensional and large scale data in which the representation of each element is inherently nonnegative, and it seeks low-rank factor matrices that are constrained to have only nonnegative elements. There are many examples of data with a nonnegative representation. In a standard term-frequency encoding, a text document is represented as a vector of nonnegative numbers since each element represents the number of appearances of each term in each document. In image processing, digital images are represented by pixel intensities, which are nonnegative. In the life sciences, chemical concentrations or gene expression levels are naturally represented as nonnegative data.

Our algorithm framework utilizes various constraints on the non-convex optimization problem that gives rise to the nonnegative factors. With these various constraints NMF is a versatile tool for a large variety of data analytics problems. NMF algorithms have been an active area of research for several years. Since much of the data for many important problems in numerous domains is nonnegative NMF is the correct computational model for mining and/or integrating information from such data. NMF also offers enhanced interpretation of results since nonnegativity of the data is preserved.

II. SmallK Overview

The SmallK library provides routines for low-rank matrix approximation via nonnegative matrix factorization (NMF). The term "nonnegative matrix" means that, for a given matrix, all of its elements are greater than or equal to zero, which we express as ≥ 0 . Given a nonnegative matrix A, the SmallK software computes nonnegative matrices W and H such that

$A \cong W H$

The matrix A has m rows and n columns and can be either sparse or dense. W has m rows and k columns, and H has k rows and n columns. The value of k is an input parameter to the approximation routines; typically k << m and k << n. The parameter k is called the 'reduced rank' of the low rank approximation. In applications it could

represent the reduced dimension in dimension reduction, the number of clusters for clustering various data sets, or the number of topics in topic discovery.

NMF algorithms seek to approximate a matrix A by the product of two much smaller matrices W and H. The idea is to choose the smallest value of k (width of W and height of H) that gives an acceptable approximation error. Due to the nonconvex nature of the optimization problem associated with finding W and H, they can only be approximated after an NMF algorithm satisfies a convergence criterion. Thus, the minimization of the objective function proceeds iteratively, attempting to reach a stationary point, which is the best possible solution. As the iterations proceed, the SmallK code computes a metric that estimates the progress and, when the metric falls below a user-specified tolerance, the iterations stop and convergence is declared.

The SmallK library provides implementations of several NMF algorithms. These algorithms are:

- 1. Multiplicative Updating (NMF-MU)
- 2. Hierarchical Alternating Least Squares (NMF-HALS)
- 3. Block Principal Pivoting (NMF-BPP)
- 4. Rank2 Specialization (NMF-RANK2)

Additional NMF algorithms will be provided in future updates.

SmallK also provides implementations of hierarchical and flat data clustering. These routines are:

- 1. Hierarchical Clustering via NMF-RANK2
- 2. Flat Clustering via NMF-RANK2
- 3. Flat Clustering via NMF-BPP or NMF-HALS

The suite of SmallK implementations of NMF algorithms are suitable in many applications such as image processing, interactive visual analytics, speckle removal from SAR images, recommender systems, information fusion, outlier detection, chemometrics, and many more.

The SmallK library requires either MacOSX or Linux. A Windows version may be provided in the future.

III. Build and Installation Instructions

III.1 Quick Start: Build a SmallK Virtual Machine using Vagrant

Installing SmallK into a virtual machine (OSX, Linux, Windows) is intended for those who are not doing development and/or do not have a reason to do the full installation on Linux or OSX outlined in sections III.2 to III.4 (Windows full installation coming soon).

The complete stack of software dependencies for SmallK as well as SmallK itself can be rapidly set up and configured through use of Vagrant and VirtualBox and the files included in the repository. To deploy the SmallK VM:

1. Install Vagrant and VirtualBox.

[Note: For Windows, ensure that you have a VirtualBox version >= 4.3.12. After installing Vagrant, you may need to log out and log back in to ensure that you can run vagrant commands in the command prompt.]

2. From within the vagrant/ directory in the repository run:

```
vagrant up
```

This can take as long as an hour to build the VM, which will be based on a minimal Ubuntu 14.04 installation. The Vagrantfile can be customized in many ways to change the specifications for the VM that is built. See more information here. The default configuration provides the VM with 4 GB of memory and 2 CPUs. Increasing these allocations will improve the performance of the application. This can be done by modifying this line in the Vagrantfile:

```
vb.customize ["modifyvm", :id, "--memory", "4056", "--cpus", "2"]
```

3. Once the VM has been built, run:

```
vagrant ssh
```

[Note: For Windows, you will need an ssh client in order to run the above command. This can be obtained via CygWin, MinGW, or Git. If you would like to use PuTTY to connect to your virtual machine, follow these instructions.

This will drop you into the command line of the VM that was just created. From there, you can navigate to /home/vagrant/smallk-1.4.0 and run

```
make check
```

to verify your installation was successful. In case you need it, the username/password for the VM created will be vagrant/vagrant.

4. When you are ready to shut down the VM, run one of the following:

```
vagrant suspend # save the current running state

vagrant halt # gracefully shut down the machine

vagrant destroy # remove the VM from your machine
```

If you want to work with the VM again, from any of the above states you can run

```
vagrant up
```

again, and the VM will be resumed or recreated.

III.2 Standard Build and Installation

Prerequisites

- A modern C++ compiler that supports the C++11 standard, such as the latest release of the GNU or clang compilers
- Elemental, a high-performance library for dense, distributed linear algebra, which requires:
 - An MPI installation, such as OpenMPI
 - A BLAS implementation, preferably optimized/tuned for the local system
 - libFLAME: (optional) a high-performance library for dense linear algebra
 - OpenMP: (optional)
 - CMake
- Optional: Python 2.7, including the following libraries (required to build the Python interface to SmallK, which is optional):
 - numpy
 - scipy
 - cython

Elemental can make use of OpenMP parallelization if available. This is generally advantageous for large problems. The SmallK code is also internally parallelized to take full advantage of multiple CPU cores for maximum performance. SmallK does not currently support distributed computation. However, future updates are planned that will provide this capability.

We **strongly** recommend that users install both the HybridRelease and PureRelease builds of Elemental. OpenMP is enabled in the HybridRelease build and disabled in the PureRelease build. So why install both? For smaller problems the overhead of *OpenMP* can actually cause code to run slower than without it. Whereas for large problems OpenMP parallelization generally helps, but there is no clear transition point between where it helps and where it hurts. Thus we encourage users to experiment with both builds to find the one that performs best for their typical problems.

We also recommend that users clearly separate the different build types as well as the versions of Elemental on their systems. Elemental is under active development, and new releases can introduce changes to the API that are not backwards compatible with previous releases. To minimize build problems and overall hassle, we recommend that Elemental be installed so that the different versions and build types are cleanly separated.

The SmallK software supports Elemental versions 0.81, 0.83, 0.84, 0.84-p1, and 0.85.

A note of caution: copying the command lines from this document and pasting them into a terminal may result in the commands not properly executing due to how Word interprets the double dash --, "double quotes", and perhaps other characters or symbols. For pasting the commands to a terminal, first copy the command lines to a text editor and copy/paste from there.

III.3 How to Install Elemental on MacOSX

On MacOSX we recommend using <u>Homebrew</u> as the package manager. Homebrew does not require sudo privileges for package installation, unlike other package managers such as MacPorts. Thus the chances of corrupting vital system files are greatly reduced with Homebrew.

It is convenient to be able to view hidden files (like .file) in the MacOSX Finder. To do so run the following at the command line:

```
defaults write com.apple.finder AppleShowAllFiles -bool YES
```

To hide hidden files, set the Boolean flag to NO:

```
defaults write com.apple.finder AppleShowAllFiles -bool NO
```

If you use Homebrew, ensure that your PATH is configured to search Homebrew's installation directory first. Homebrew's default installation location is /usr/local/bin, so that location needs to be first on your path. To check, run this command from a terminal window:

```
cat /etc/paths
```

If the first entry is not /usr/local/bin, you will need to edit this file. Since this is a system file, first create a backup. If permission is denied to modify this file, use sudo in front of the command to launch your editor. Move the line /usr/local/bin so that it is on the first line of the file. Save the file, then close the terminal session and start a new terminal session so that the path changes will take effect.

After starting your new terminal session, make sure your homebrew packages are up-to-date by running the following commands:

```
brew update
brew upgrade
brew cleanup
brew doctor
```

III.3.1 OSX:Install the latest GNU and clang compilers

Elemental and SmallK both require a modern C++ compiler compliant with the C++11 standard. We recommend that you install the latest stable version of the clang and GNU C++ compilers. To do this, first install the XCode command line tools with this command:

```
xcode-select --install
```

If this command produces an error, download and install the latest version of XCode from the AppStore, which includes the command line tools. After the installation completes, run this command from a terminal window to check the version of the clang compiler:

```
clang++ --version
```

You should see output similar to this:

```
Apple LLVM version 6.0 (clang-600.0.51) (based on LLVM 3.5svn) Target: x86-64-apple-darwin13.4.0 Thread model: posix
```

The latest version of the GNU compiler at the time of writing is g++-4.9.1, which is provided by the 'gcc' homebrew package. In addition to the gcc package, homebrew also provides a gcc49 package from the homebrew/versions tap. If this alternative gcc49 package is installed on your system it will prevent homebrew from symlinking the gcc package correctly. We recommend uninstalling the gcc49 versioned package and just using the gcc package instead. The Fortran compiler provided with the gcc package will also be configured to properly build numpy, which is required for the python interface to smallk.

If you need to uninstall the gcc49 package, run the following commands:

```
brew uninstall gcc49
brew cleanup
brew doctor
```

Then install the gcc package as follows:

```
brew install gcc
```

The Apple-provided gcc and g++ will not be overwritten by this installation. The new compilers will be installed into

/usr/local/bin as gcc-4.9, g++-4.9, and gfortran-4.9. The Fortran compiler is needed for the installation of MPI and for building the python interface to smallk.

III.3.2 OSX:Install OpenMPI

Install the latest version of OpenMPI with Homebrew as follows:

```
brew install open-mpi --c++11
```

The Homebrew install formula provides an option for "thread-multiple" support, but do not enable this option, as it is still experimental, not optimized for performance, and may have bugs.

III.3.3 OSX:Install the latest version of libFLAME

Next we detail the installation of the high performance numerical library libflame. The library can be downloaded from the libflame git repository on github.

It's important to perform the git clone into a subdirectory NOT called 'flame' since this can cause name conflicts with the installation. We normally do a git clone into a directory called 'libflame'. However, other directory names will work as well, but not 'flame'.

To obtain the latest version of the FLAME library, clone the FLAME git repository with this command:

```
git clone https://github.com/flame/libflame.git <libflame>
```

Run the configure script in the top-level FLAME folder as follows (assuming you want to install to /usr/local/flame; if not, change the prefix path):

```
./configure --prefix=/usr/local/flame --with-cc=/usr/local/bin/gcc-4.9 --with-ranlib=/usr/local/bin/gcc-ranlib-4.9 \,
```

A complete list of configuration options can be obtained by running: ./configure --help.

After the configuration process completes, build the FLAME library as follows:

```
make -j4
```

The -j4 option tells Make to use four processes to perform the build. This number can be increased if you have a more capable system.

```
make install
```

The FLAME library is now installed.

III.3.4 OSX:Install Elemental

Here is our recommended installation scheme for Elemental:

Choose a folder for the root of the Elemental installation. For our systems, this is

```
/usr/local/elemental
```

Download one of the smallk-supported releases of Elemental (see above), unzip and untar the distribution, and cd to the top-level folder of the unzipped distribution. This folder will be denoted by <code>UNZIP_DIR</code> in the following instructions.

For the first step of the installation, <u>for Elemental versions prior to 0.85</u>, we need to fix a few problems with the CMake configuration files. Open the following file in a text editor:

```
UNZIP DIR/cmake/tests/OpenMP.cmake
```

On the first line of the file, change

```
if(HYBRID)
```

to this:

```
if(ELEM_HYBRID)
```

Next, open this file in a text editor:

```
UNZIP_DIR/cmake/tests/Math.cmake
```

Near the first line of the file, change

```
if(PURE)
```

to this:

```
if (ELEM PURE)
```

Save both files.

HybridRelease Build

From UNZIP DIR, run the following command to create a local build folder for the HybridRelease build:

```
mkdir build_hybrid
cd build hybrid
```

Use the following CMake command for the HybridRelease build, substituting either 0.81, 0.83, 0.84, 0.84-p1, 0.85 for VERSION STRING:

```
cmake -D CMAKE_INSTALL_PREFIX=/usr/local/elemental/VERSION_STRING/HybridRelease
-D CMAKE_BUILD_TYPE=HybridRelease
-D CMAKE_CXX_COMPILER=/usr/local/bin/g++-4.9
-D CMAKE_C_COMPILER=/usr/local/bin/gcc-4.9
-D CMAKE_Fortran_COMPILER=/usr/local/bin/gfortran-4.9
-D MATH_LIBS="/usr/local/flame/lib/libflame.a;-framework Accelerate"
-D ELEM EXAMPLES=ON -D ELEM TESTS=ON ..
```

Note that we have installed g++-4.9 into /usr/local/bin and libFLAME into /usr/local/flame. Alter these paths, if necessary, to match the installation location on your system.

Once the CMake configuration step completes, you can build Elemental from the generated Makefiles with the following command:

```
make -j4
```

The -j4 option tells Make to use four processes to perform the build. This number can be increased if you have a more capable system.

After the build completes, install elemental as follows:

```
make install
```

As a final step, if you installed a version of Elemental prior to the 0.84 series releases, edit the file /usr/local/elemental/<version>/HybridRelease/conf/ElemVars and replace the line

```
CXX = /usr/local/bin/g++-4.9
```

With this:

```
CXX = /usr/local/bin/g++-4.9 -std=c++11
```

This will eliminate some compiler warnings about C++11 constructs.

If you installed Elemental version 0.85, you need to setup your system to find the Elemental dynamic library. Either in your startup script (~/.bash_profile) or in a terminal window, enter the following command on a single line, replacing VERSION_STRING as above:

PureRelease Build

After this, run these commands to create a build folder for the PureRelease build:

```
cd ..
```

```
mkdir build_pure
cd build pure
```

Then repeat the CMake configuration process, this time with the following command for the PureRelease build:

```
cmake -D CMAKE_INSTALL_PREFIX=/usr/local/elemental/VERSION_STRING/PureRelease
-D CMAKE_BUILD_TYPE=PureRelease -D CMAKE_CXX_COMPILER=/usr/local/bin/g++-4.9
-D CMAKE_C_COMPILER=/usr/local/bin/gcc-4.9
-D CMAKE_Fortran_COMPILER=/usr/local/bin/gfortran-4.9
-D MATH_LIBS="/usr/local/flame/lib/libflame.a;-framework Accelerate"
-D ELEM EXAMPLES=ON -D ELEM TESTS=ON ..
```

Repeat the build commands and install this build of Elemental. Then, if you installed a version of Elemental prior to the 0.84 series releases, edit the

 $/{\tt usr/local/elemental/< version} > /{\tt PureRelease/conf/ElemVars} ~ {\tt file} ~ {\tt and} ~ {\tt replace} ~ {\tt the} ~ {\tt CXX} ~ {\tt line} ~ {\tt as} ~ {\tt indicated} ~ {\tt above}.$

If you installed Elemental version 0.85, you need to setup your system to find the Elemental dynamic library for the PureRelease build. Enter the following command in a terminal window on a single line, replacing VERSION_STRING as above:

Note: you will need to set this variable to point to either the HybridRelease or the PureRelease build of the Elemental dynamic library whenever you want to use smallk.

This completes the two builds of Elemental.

To test the installation, follow Elemental's <u>test instructions</u> for the SVD test to verify that Elemental is working correctly.

III.4 How to Install Elemental on Linux

We strongly recommend using a package manager for your Linux distribution for installation and configuration of the required dependencies. We cannot provide specific installation commands for every variant of Linux, so we specify the high-level steps below.

III.4.1 Linux:Install the latest GNU compilers

We recommend installation of the latest stable release of the GNU C++ compiler, which is g++-4.9 at the time of this writing.

Also install the latest version of GNU Fortran, which is needed for the installation of MPI.

III.4.2 Linux:Install OpenMPI

Download the latest version of <u>OpenMPI</u>, unzip and untar the downloaded zip file, and cd to the untarred directory. Run configure as follows, all on a single line. This command assumes that gcc-4.9 has been installed; change the paths if needed to match your system:

```
./configure --prefix=/usr/local CC=/usr/local/bin/gcc-4.9 CXX=/usr/local/bin/g++-4.9 F77=/usr/local/bin/gfortran-4.9 FC=/usr/local/bin/gfortran-4.9
```

Wait for the configure script to finish – this could take several minutes. Then build the code as follows:

```
make -j4
```

Install with:

```
make install
```

OpenMPI provides many tests to verify the installation; it's a good idea to run at least some of these tests to ensure that MPI was installed successfully.

III.4.3 Linux:Install the latest version of libFlame

To obtain the latest version of the FLAME library, clone the FLAME git repository with this command:

```
git clone https://github.com/flame/libflame.git
```

Run the configure script in the top-level FLAME folder as follows (assuming you want to install to /usr/local/flame; if not, change the prefix path):

```
./configure --prefix=/usr/local/flame --with-cc=/usr/local/bin/gcc-4.9 --with-ranlib=/usr/local/bin/gcc-ranlib-4.9
```

A complete list of configuration options can be obtained by running

```
./configure --help
```

After the configuration process completes, build the FLAME library as follows:

```
make -j4
make install
```

This completes the installation of the FLAME library.

III.4.4 Linux:Install an accelerated BLAS library

It is essential to link Elemental with an accelerated BLAS library for maximum performance. Linking Elemental with a 'reference' BLAS implementation will cripple performance, since the reference implementations are designed for correctness not speed.

If you do not have an accelerated BLAS on your system, you can download and build <u>OpenBLAS</u>. Download, unzip, and untar the tarball (version 0.2.8 as of this writing) and cd into the top-level folder. Build OpenBLAS with this command, assuming you have a 64-bit system:

```
make BINARY=64 USE OPENMP=1
```

Install with this command, assuming the installation directory is /usr/local/openblas/0.2.8/:

```
make PREFIX=/usr/local/openblas/0.2.8/ install
```

This completes the installation of OpenBLAS.

III.4.5 Linux:Install Elemental

We **strongly** recommend that users install both the HybridRelease and PureRelease builds of Elemental. OpenMP is enabled in the HybridRelease build and disabled in the PureRelease build. So why install both? For smaller problems the overhead of OpenMP can actually cause code to run slower than without it. On the other hand, for large problems, OpenMP parallelization generally helps. However, there is no clear transition point between where it helps and where it hurts. Thus, we encourage users to experiment with both builds to find the one that performs best for their typical problems.

We also recommend that users clearly separate the different build types as well as the versions of Elemental on their systems. Elemental is under active development, and new releases can introduce changes to the API that are not backwards compatible with previous releases. To minimize build problems and overall hassle, we recommend that Elemental be installed so that the different versions and build types are cleanly separated.

Here is our recommended installation scheme for Elemental:

Choose a folder for the root of the Elemental installation. For our systems, this is

```
/usr/local/elemental
```

Download one of the smallk-supported releases of Elemental (see above), unzip and untar the distribution, and cd to the top-level folder of the unzipped distribution. This folder will be denoted by <code>UNZIP_DIR</code> in the following instructions.

For the first step of the installation, <u>for Elemental versions prior to 0.85</u>, we need to fix a few problems with the CMake configuration files. Open the following file in a text editor:

```
UNZIP DIR/cmake/tests/OpenMP.cmake
```

On the first line of the file, change

```
if(HYBRID)
```

to this:

```
if (ELEM HYBRID)
```

Next, open this file in a text editor:

```
UNZIP DIR/cmake/tests/Math.cmake
```

Near the first line of the file, change

```
if(PURE)
```

to this:

if(ELEM_PURE)

Save both files.

HybridRelease Build

From UNZIP DIR, run the following command to create a local build folder for the HybridRelease build:

```
mkdir build_hybrid
cd build_hybrid
```

Use the following CMake command for the HybridRelease build, substituting either 0.81, 0.83, 0.84, 0.84-p1, 0.85 for VERSION_STRING:

```
cmake -D CMAKE_INSTALL_PREFIX=/usr/local/elemental/VERSION_STRING/HybridRelease
-D CMAKE_BUILD_TYPE=HybridRelease -D CMAKE_CXX_COMPILER=/usr/local/bin/g++-4.9
-D CMAKE_C_COMPILER=/usr/local/bin/gcc-4.9
-D CMAKE_Fortran_COMPILER=/usr/local/bin/gfortran-4.9
-D MATH_LIBS="/usr/local/flame/lib/libflame.a;-L/usr/local/openblas/0.2.8/lib -lopenblas-lm"
-D ELEM EXAMPLES=ON -D ELEM TESTS=ON ..
```

Note that we have installed g++-4.9 into /usr/local/bin and libFLAME into /usr/local/flame. Alter these paths, if necessary, to match the installation location on your system.

If this command does not work on your system, you may need to define the BLAS_LIBS and/or GFORTRAN_LIB config options.

Once the CMake configuration step completes, you can build Elemental from the generated Makefiles with the following command:

```
make -j4
```

The -j4 option tells Make to use four processes to perform the build. This number can be increased if you have a more capable system.

After the build completes, install elemental as follows:

```
make install
```

As a final step, if you installed a version of Elemental prior to the 0.84 series releases, edit the file /usr/local/elemental/<version>/HybridRelease/conf/ElemVars and replace the line

```
CXX = /usr/local/bin/g++-4.9
```

With this:

```
CXX = /usr/local/bin/q++-4.9 -std=c++11
```

This will eliminate some compiler warnings about C++11 constructs.

If you installed Elemental version 0.85, you need to setup your system to find the Elemental shared library. Either in your startup script (~/.bashrc) or in a terminal window, enter the following command on a single line, replacing VERSION STRING as above:

```
export LD_LIBRARY_PATH=
    $LD_LIBRARY_PATH:/usr/local/elemental/VERSION_STRING/HybridRelease/lib/
```

PureRelease Build

After this, run these commands to create a build folder for the PureRelease build:

```
cd ..
mkdir build_pure
cd build pure
```

Then repeat the CMake configuration process, this time with the following command for the PureRelease build:

```
cmake -D CMAKE_INSTALL_PREFIX=/usr/local/elemental/VERSION_STRING/PureRelease
-D CMAKE_BUILD_TYPE=PureRelease -D CMAKE_CXX_COMPILER=/usr/local/bin/g++-4.9
-D CMAKE_C_COMPILER=/usr/local/bin/gcc-4.9
-D CMAKE_Fortran_COMPILER=/usr/local/bin/gfortran-4.9
-D MATH_LIBS="/usr/local/flame/lib/libflame.a;-L/usr/local/openblas/0.2.8/lib -lopenblas-lm"
-D ELEM EXAMPLES=ON -D ELEM TESTS=ON ..
```

If this command does not work on your system, you may need to define the BLAS_LIBS and/or GFORTRAN_LIB config options.

Repeat the build commands and install this build of Elemental. Then, if you installed a version of Elemental prior to the 0.84 series releases, edit the

 $/usr/local/elemental/< version >/ Pure Release/conf/Elem Vars \ \emph{file} \ and \ replace \ the \ CXX \ line \ as \ indicated \ above.$

If you installed Elemental version 0.85, you need to setup your system to find the Elemental shared library for the PureRelease build. Enter the following command in a terminal window on a single line, replacing VERSION_STRING as above:

```
export LD_LIBRARY_PATH=
    $LD_LIBRARY_PATH:/usr/local/elemental/VERSION_STRING/PureRelease/lib/
```

Note: you will need to set this variable to point to either the HybridRelease or the PureRelease build of the Elemental shared library whenever you want to use smallk.

This completes the two builds of Elemental.

To test the installation, follow Elemental's <u>test instructions</u> for the SVD test to verify that Elemental is working correctly.

III.6 Installing the Python libraries

III.6.1 OSX: Install Python libraries

Install Python scientific software packages

Assuming that you have used brew to install gcc, as indicated earlier, you can run the following commands to install the necessary libraries:

```
brew install python
brew install numpy
brew install scipy
```

To check your installation, run:

```
brew test numpy
```

IMPORTANT: Check to see that your numpy installation has correctly linked to the needed BLAS libraries.

Ensure that you are running the correct python:

```
which python
```

This should print out /usr/local/bin/python. Open a python terminal and run the following:

```
import numpy as np
np.__config__.show()
```

You should see something similar to the following:

```
lapack_opt_info:
    extra_link_args = ['-Wl,-framework', '-Wl,Accelerate']
    extra_compile_args = ['-msse3']
    define_macros = [('NO_ATLAS_INFO', 3)]

blas_opt_info:
    extra_link_args = ['-Wl,-framework', '-Wl,Accelerate']
    extra_compile_args = ['-msse3', '-I/System/Library/Frameworks/vecLib.framework/Headers']
    define_macros = [('NO_ATLAS_INFO', 3)]
```

If you are using OpenBLAS, you should see that indicated as well.

Install Cython: a Python interface to C/C++

First install the Python Package Index utility, pip. Many Python packages are configured to use this package manager, Cython being one.

```
brew install pip
```

To install Cython:

```
pip install cython
```

The Makefile assumes an installation path of /usr/local/lib/python2.7/site-packages for the compiled library file. If you are not using brew to install your packages, you will need to tell the Makefile where the appropriate site-packages directory is located on your system. Setting the SITE_PACKAGES_DIR command line variable when running make accomplishes this.

III.6.2 Linux: Install Python libraries

The Python libraries can easily be installed via pip and apt-get with the following commands:

```
pip install numpy
apt-get install python-scipy
pip install cython
```

IV. Build and Installation of SmallK

IV.1 Obtain the source code

The source code for the SmallK library can be downloaded from the <u>SmallK repository</u> on github. Once downloaded uncompress the tarball and follow the installation instructions below.

IV.2 Build the SmallK library

Download and unpack the SmallK code tarball and cd into the top-level SmallK directory. The makefiles assume that you followed our suggested installation plan for Elemental. If this is not the case you will need to do one of the following:

- 1. Create an environment variable called ELEMENTAL_INSTALL_DIR which contains the path to the root folder of your Elemental installation
- 2. Define the variable ELEMENTAL_INSTALL_DIR on the make command line
- 3. Edit the SmallK makefile so that it can find your Elemental installation

Assuming that the default install locations are acceptable, build the SmallK code by running this command from the root directory of the distribution:

```
make all
```

This will build the SmallK and pysmallk libraries and several command-line applications. These are:

- 1. libsmallk.a, the SmallK library
- 2. preprocess tf, a command-line application for processing and scoring term-frequency matrices
- 3. matrixgen, a command-line application for generating random matrices
- 4. nmf, a command-line application for NMF
- 5. hierclust, a command-line application for fast hierarchical clustering
- 6. flatclust, a command-line application for flat clustering via NMF
- 7. pysmallk.so, if PYSMALLK=1 (0: default) the Python-wrapped SmallK library, making SmallK available via Python

To install the code, run this command to install to the default location, which is /usr/local/smallk:

```
make install
```

This will install the binary files listed above into the /usr/local/smallk/bin directory, which needs to be on your path to run the executables from anywhere on your system and avoid prepending with the entire path. This will install pysmallk.so into the site-directories folder associated with the Python binary. To install the binary code to a different location, either create an environment variable called SMALLK_INSTALL_DIR and set it equal to the desired installation location prior to running the install command, or supply a prefix argument:

```
make prefix=/path/to/smallk install
```

To install the Python library to a different location, create an environment variable called SITE_PACKAGES_DIR and set it equal to the desired installation location prior to running the install command, or supply this as an argument for make:

```
make SITE PACKAGES DIR=/path/to/site-packages install
```

Or, as a last resort, you can edit the top-level SmallK makefile to conform to the installation scheme of your system. You may need root privileges to do the installation, depending on where you choose to install it.

To test the installation, run this command:

This will run a series of tests, none of which should report a failure. Sample output from a run of these tests can be found in section [V.6. SmallK Test Results].

Note: if you installed Elemental version 0.85, you will need to configure your system to find the Elemental shared library. See the Elemental installation instructions above for information on how to do this.

The command-line applications can be built individually by running the appropriate make command from the top-level smallk folder. These commands are:

To build the smallk library only:

To build the preprocessor only:

To build the matrix generator only:

To build the nmf only:

To build hierclust only:

To build flatclust only:

To build pysmallk only:

make libsmallk

make preprocessor

make matrixgen

make nmf

make hierclust

make flatclust

make pysmallk

Note: Pysmallk requires builds of libsmallk, preprocessor, matrixgen, hierclust, and flatclust.

IV.3 Examples of API Usage

In the examples folder you will find a file called smallk_example.cpp. This file contains several examples of how to use the SmallK library. Also included in the examples folder is a makefile that you can customize for your use. Note that the SmallK library must first be installed before the example project can be built.

As an example of how to use the sample project, assume the smallk software has been installed into /usr/local/smallk. Also assume that the user chose to create the recommended environment variable SMALLK_INSTALL_DIR that stores the location of the top-level install folder, i.e. the user's .bashrc file contains this statement:

```
export SMALLK INSTALL DIR=/usr/local/smallk
```

To build the smallk example project, open a terminal window and cd to the <code>examples</code> directory and run this command:

make

To run the example project, run this command:

```
./{\tt bin/example}\ ../../{\tt smallk\_data}
```

The output will be similar to the following (it won't be identical because some problems are randomly initialized):

```
stopping criterion: Ratio of Projected Gradients
                 height: 12411
                   width: 7984
                       k: 32
                 miniter: 5
                 maxiter: 5000
                     tol: 0.005
               matrixfile: ../data/reuters.mtx
              maxthreads: 8
     progress metric: (min_iter)
1:
    progress metric: (min iter)
3: progress metric: (min_iter)
4: progress metric: (min_iter)
5: progress metric: (min_iter)
6: progress metric: 0.07\overline{4}7031
     progress metric: 0.0597987
7:
     progress metric: 0.0462878
8:
     progress metric: 0.0362883
9:
10: progress metric: 0.030665
11:
12:
     progress metric: 0.0281802
     progress metric: 0.0267987
13: progress metric: 0.0236731
14: progress metric: 0.0220778
15: progress metric: 0.0227083
     progress metric: 0.0227083
16: progress metric: 0.0244029
17: progress metric: 0.0247552
18: progress metric: 0.0220007
19: progress metric: 0.0173831
20: progress metric: 0.0137033
Solution converged after 39 iterations.
Elapsed wall clock time: 4.354 sec.
Writing output files...
************
                Running NMF-HALS using k=16
**********
Initializing matrix W...
Initializing matrix H...
                 parameters:
               algorithm: HALS
      stopping criterion: Ratio of Projected Gradients
                  height: 12411
                   width: 7984
                       k: 16
                 miniter: 5
                 maxiter: 5000
                     tol: 0.005
              matrixfile: ../data/reuters.mtx
maxthreads: 8
   progress metric: (min_iter)
progress metric: (min_iter)
1:
2:
     progress metric: (min iter)
3:
4: progress metric: (min_iter)
     progress metric: (min_iter)
progress metric: 0.710219
5:
6:
     progress metric: 0.580951
7:
     progress metric: 0.471557
8:
9:
     progress metric: 0.491855
10: progress metric: 0.531999
11: progress metric: 0.353302
12: progress metric: 0.201634
13: progress metric: 0.1584
     progress metric: 0.1584
14: progress metric: 0.142572
15: progress metric: 0.12588
16: progress metric: 0.113239
17: progress metric: 0.0976934
18: progress metric: 0.0821207
19: progress metric: 0.0746089
```

```
20: progress metric: 0.0720616
40: progress metric: 0.0252854
60: progress metric: 0.0142085
80: progress metric: 0.0153269
Solution converged after 88 iterations.
Elapsed wall clock time: 1.560 sec.
Writing output files...
******************
        Running NMF-RANK2 with W and H initializers
************
Initializing matrix W...
Initializing matrix H...
               parameters:
              algorithm: Rank 2
      stopping criterion: Ratio of Projected Gradients
                 height: 12411
                  width: 7984
                     k: 2
                miniter: 5
                maxiter: 5000
                   tol: 0.005
             matrixfile: ../data/reuters.mtx
             maxthreads: 8
1:
   progress metric: (min_iter)
2: progress metric: (min_iter)
   progress metric: (min_iter)
progress metric: (min_iter)
3:
4:
5: progress metric: (min iter)
   progress metric: 0.0374741
progress metric: 0.0252389
6:
7:
     progress metric: 0.0169805
8:
    progress metric: 0.0113837
9:
10: progress metric: 0.00761077
11: progress metric: 0.0050782
     progress metric: 0.0050782
12: progress metric: 0.00338569
Solution converged after 12 iterations.
Elapsed wall clock time: 0.028 sec.
Writing output files...
*************
       Repeating the previous run with tol = 1.0e-5
***************
Initializing matrix W...
Initializing matrix H...
               parameters:
              algorithm: Rank 2
     stopping criterion: Ratio of Projected Gradients
                 height: 12411
                  width: 7984
                      k: 2
                miniter: 5
                maxiter: 5000
                    tol: 1e-05
             matrixfile: ../data/reuters.mtx
maxthreads: 8
1: progress metric: (min_iter)
2: progress metric: (min_iter)
3: progress metric: (min_iter)
4: progress metric: (min_iter)
5:
     progress metric: (min iter)
```

```
progress metric: 0.0374741
6:
7:
    progress metric: 0.0252389
   progress metric: 0.0169805 progress metric: 0.0113837
8:
9 •
10: progress metric: 0.00761077
11: progress metric: 0.0050782
12:
    progress metric: 0.00338569
13:
    progress metric: 0.00225761
14: progress metric: 0.00150429
15: progress metric: 0.00100167
    progress metric: 0.000666691
16:
17: progress metric: 0.000443654
18: progress metric: 0.000295213
19:
    progress metric: 0.000196411
20: progress metric: 0.000130604
Solution converged after 27 iterations.
Elapsed wall clock time: 0.061 sec.
Writing output files...
Minimum value in W matrix: 0.
Maximum value in W matrix: 0.397027.
***********
      Running HierNMF2 with 5 clusters, JSON format
**********
loading dictionary...
creating random W initializers...
creating random H initializers...
            parameters:
                height: 12411
                width: 7984
            matrixfile: ../data/reuters.mtx
              dictfile: ../data/reuters dictionary.txt
                  tol: 0.0001
              miniter: 5
              maxiter: 5000
              maxterms: 5
            maxthreads: 8
[1] [2] [3] [4]
Elapsed wall clock time: 391 ms.
9/9 factorizations converged.
Writing output files...
*************
* Running HierNMF2 with 10 clusters, 12 terms, XML format *
***********
creating random W initializers...
creating random H initializers...
            parameters:
                height: 12411
                width: 7984
            matrixfile: ../data/reuters.mtx
              dictfile: ../data/reuters dictionary.txt
                  tol: 0.0001
               miniter: 5
              maxiter: 5000
              maxterms: 12
            maxthreads: 8
[1] [2] [3] [4] [5] [6] dropping 20 items ...
Elapsed wall clock time: 837 ms.
21/21 factorizations converged.
Writing output files...
```

```
***********
  Running HierNmf2 with 18 clusters, 8 terms, with flat
creating random W initializers...
creating random H initializers...
             parameters:
                 height: 12411
                  width: 7984
             matrixfile: ../data/reuters.mtx
               dictfile: ../data/reuters dictionary.txt
                    tol: 0.0001
                miniter: 5
                maxiter: 5000
               maxterms: 8
             maxthreads: 8
[1] [2] [3] [4] [5] [6] dropping 20 items ...
[7] [8] [9] dropping 25 items ...
[10] [11] [12] [13] [14] [15] [16] [17]
Running NNLS solver...
1: progress metric: 1
   progress metric: 0.264152
2:
3: progress metric: 0.0760648
4: progress metric: 0.0226758
5: progress metric: 0.00743562
   progress metric: 0.00280826
6:
     progress metric: 0.00103682
8: progress metric: 0.000361738
9: progress metric: 0.000133087
10: progress metric: 5.84849e-05
Elapsed wall clock time: 1.362 s.
40/40 factorizations converged.
Writing output files...
```

IV.4 Matrix File Formats

The SmallK software supports comma-separated value (CSV) files for dense matrices and Matrix Market files for sparse matrices.

For example, the 5x3 dense matrix

42	47	52
43	48	53
44	49	54
45	50	55
46	51	56

would be stored in a CSV file as follows:

42,47,52 43,48,53 44,49,54 45,50,55 46,51,56

The matrix is loaded exactly as it appears in the file. **Internally, SmallK stores dense matrices in column-major order**. Sparse matrices are stored in **compressed column format**.

IV.5 SmallK API

The SmallK API is an extremely **simplistic** API for basic NMF and clustering. Users who require more control over the factorization or clustering algorithms can instead run one of the command-line applications in the SmallK distribution.

The SmallK API is exposed by the file smallk.hpp, which can be found in this location: SMALLK_INSTALL_DIR/include/smallk.hpp. All API functions are contained within the smallk namespace.

An example of how to use the API can be found in the file examples/smallk example.cpp.

The smallk library maintains a set of state variables that are used to control the Nmf and clustering routines. Once set, the state variables maintain their values until changed by an API function. For instance, one state variable represents the matrix to be factored (or used for clustering). The API provides a function to load this matrix; once loaded, it can be repeatedly factored without the need for reloading. The state variables and their default values are documented below.

All computations with the smallk library are performed in double precision.

Enumerations

The SmallK API provides two enumerated types, one for the supported NMF algorithms and one for the clustering file output format. These are:

The default NMF algorithm is BPP. The Rank2 algorithm is optimized for two-column or two-row matrices and is the underlying factorization routine for the clustering code.

```
enum OutputFormat
{
     XML, // Extensible Markup Language
     JSON // JavaScript Object Notation
};
```

API functions

Initialization and Cleanup

Call this function first, before all others in the API; initializes Elemental and the smallk library.

```
bool IsInitialized()
```

Returns true if the library has been initialized via a call to Initialize(), false otherwise.

```
void Finalize()
```

Call this function last, after all others in the API; performs cleanup for Elemental and the smallk library.

Versioning

```
unsigned int GetMajorVersion()
```

Returns the major release version number of the library as an unsigned integer.

```
unsigned int GetMinorVersion()
```

Returns the minor release version number of the library as an unsigned integer.

```
unsigned int GetPatchLevel()
```

Returns the patch version number of the library as an unsigned integer.

```
std::string GetVersionString()
```

Returns the version of the library as a string, formatted as major.minor.patch.

Common Functions

```
unsigned int GetOutputPrecision()
```

Returns the floating point precision with which numerical output will be written (i.e., the computed W and H matrix factors from the Nmf routine). The default precision is six digits.

```
void SetOutputPrecision(const unsigned int num digits)
```

Sets the floating point precision with which numerical output will be written. Input values should be within the range [1, precision(double)]. Any inputs outside of this range will be adjusted.

```
unsigned int GetMaxIter()
```

Returns the maximum number of iterations allowed for NMF computations. The default value is 5000.

```
void SetMaxIter(const unsigned int max_iterations = 5000)
```

Sets the maximum number of iterations allowed for NMF computations. The default of 5000 should be more than sufficient for most computations.

```
unsigned int GetMinIter()
```

Returns the minimum number of NMF iterations. The default value is 5.

```
void SetMinIter(const unsigned int min iterations = 5)
```

Sets the minimum number of NMF iterations to perform before checking for convergence. The convergence and progress estimation routines are non-trivial calculations, so increasing this value may result in faster performance.

```
unsigned int GetMaxThreads()
```

Returns the maximum number of threads used for NMF or clustering computations. The default value is hardware-dependent, but is generally the maximum number allowed by the hardware.

```
void SetMaxThreads(const unsigned int max_threads);
```

Sets an upper limit to the number of threads used for NMF and clustering computations. Inputs that exceed the capabilities of the hardware will be adjusted. This function is provided for scaling and performance studies.

```
void Reset()
```

Resets all state variables to their default values.

```
void SeedRNG(const. int. seed)
```

Seeds the random number generator (RNG) within the smallk library. Normally this RNG is seeded from the system time whenever the library is initialized. The RNG is the '19937' Mersenne Twister implementation provided by the C++ standard library.

```
void LoadMatrix(const std::string& filepath)
```

Loads a matrix contained in the given file. The file must either be a comma-separated value (.CSV) file for a dense matrix, or a MatrixMarket-format file (.MTX) for a sparse matrix. If the matrix cannot be loaded the library throws a std::runtime_error exception.

```
bool IsMatrixLoaded()
```

Returns true if a matrix is currently loaded, false if not.

```
std::string GetOuputDir()
```

Returns a string indicating the directory into which output files will be written. The default is the current directory.

```
void SetOutputDir(const std::string& outdir)
```

Sets the directory into which output files should be written. The 'outdir' argument can either be an absolute or relative path. The default is the current directory.

NMF Functions

This function factors the input matrix A of nonnegative elements into nonnegative factors such that: A ~ WH. If a matrix is not currently loaded a std::logic_error exception will be thrown. The default algorithm is NMF-BPP; provide one of the enumerated algorithm values to use a different algorithm.

Where A is mxn, W is mxk, and H is kxn. The value of k is a user defined argument, e.g., for clustering applications, k is the number of clusters.

Optional initializer matrices can be provided for the W and H factors via the 'initfile_w' and 'initfile_h' arguments. These files must contain fully dense matrices in .CSV format. The W matrix initializer must have dimension mxk, and the H matrix initializer must have dimension kxn. If the initializer matrices do not match these dimensions exactly a std::logic_error exception is thrown. If initializers are not provided, matrices W and H will be randomly initialized.

The computed factors W and H will be written to the output directory in the files 'w.csv' and 'h.csv'.

Exceptions will be thrown (either from Elemental or smallk) in case of error.

```
const double* LockedBufferW(unsigned int& ldim, unsigned int& height, unsigned int& width)
```

This function returns a READONLY pointer to the buffer containing the W factor computed by the Nmf routine, along with buffer and matrix dimensions. The 'ldim', 'height', and 'width' arguments are all out parameters. The buffer has a height of 'ldim' and a width of 'width'. The matrix W has the same width but a height of 'height', which may differ from Idim. The W matrix is stored in the buffer in column-major order. See the <code>examples/smallk_example.cpp</code> file for an illustration of how to use this function.

const double* LockedBufferH(unsigned int& ldim, unsigned int& height, unsigned int& width)

Same as LockedBufferW, but for the H matrix.

```
double GetNmfTolerance()
```

Returns the tolerance value used to determine NMF convergence. The default value is 0.005.

```
void SetNmfTolerance(const double tol=0.005)
```

Sets the tolerance value used to determine NMF convergence. The NMF algorithms are iterative, and at each iteration a progress metric is computed and compared with the tolerance value. When the metric falls below the tolerance value the iterations stop and convergence is declared. The tolerance value should satisfy 0.0 < tolerance < 1.0. Any inputs outside this range will cause a std::logic error exception to be thrown.

Clustering Functions

```
void LoadDictionary(const std::string& filepath)
```

Loads the dictionary used for clustering. The dictionary is an ASCII file of text strings as described in the preprocessor input files section below. If the dictionary file cannot be loaded a string-error exception is thrown.

```
unsigned int GetMaxTerms()
```

Returns the number of highest-probability dictionary terms to store per cluster. The default value is 5.

```
void SetMaxTerms(const unsigned int max_terms = 5)
```

Sets the number of highest-probability dictionary terms to store per cluster.

```
OutputFormat GetOutputFormat()
```

Returns a member of the OutputFormat enumerated type; this is the file format for the clustering results. The default output format is JSON.

```
void SetOutputFormat(const OutputFormat = JSON)
```

Sets the output format for the clustering result file. The argument must be one of the values in the OutputFormat enumerated type.

```
double GetHierNmf2Tolerance()
```

Returns the tolerance value used by the NMF-RANK2 algorithm for hierarchical clustering. The default value is 1.0e-4.

```
void SetHierNmf2Tolerance(const double tol=1.0e-4)
```

Sets the tolerance value used by the NMF-RANK2 algorithm for hierarchical clustering. The tolerance value should satisfy 0.0 < tolerance < 1.0. Any inputs outside this range will cause a $\texttt{std}: \texttt{logic_error}$ exception to be thrown.

```
void HierNmf2(const unsigned int num_clusters)
```

This function performs hierarchical clustering on the loaded matrix, generating the number of clusters specified by the 'num_clusters' argument. For an overview of the hierarchical clustering process, see the description below for the hierclust command line application.

This function generates two output files in the output directory: 'assignments_N.csv' and 'tree_N.{json, xml}'. Here N is the number of clusters specified as an argument, and the tree file can be in either JSON XML format.

The content of the files is described below in the section on the hierclust command line application.

void HierNmf2WithFlat(const unsigned int num_clusters)

This function performs hierarchical clustering on the loaded matrix, exactly as described for HierNmf2. In addition, it also computes a flat clustering result. Thus four output files are generated. The flat clustering result files are 'assignments_flat_N.csv' and 'clusters_N.{json, xml}'. The cluster file contents are documented below in the section on the flatclust command line application.

V. SmallK Command Line Tools

The SmallK library provides a number of algorithm implementations for low rank approximation of a matrix. These can be used for performing various data analytics tasks such as topic modeling, clustering, and dimension reduction. This section will provide more in-depth description of the tools available with examples that can be expanded/modified for other application domains.

Before diving into the various tools, it will be helpful to set up the command line environment to easily run the various executables that comprise the SmallK library. First the command line needs to know where to find the executable files to run the tools. Since while installing SmallK 'make_install' was run, the executables are located in /usr/local/smallk/bin. Thus, this should be added to the '\$PATH' system variable or added to the environment. The following command line performs the task of modifying the path avoiding the need to cd into directories were the tools are located:

```
export PATH=/usr/local/smallk/bin:$PATH
```

This allows the tools to be executed from any directory.

A subset of these tools are also available from the pysmallk library: smallkapi (mirrors the NMF command line application), matrixgen, preprocessor, flatclust, and hierclust. The command line arguments are the same as those documented below. These tools are available within the /pysmallk/tests/ directory and can be executed as follows:

```
[python binary] [tool].py [command line arguments]
```

For example:

```
python preprocessor.py --indir smallk_data
```

V.1. Preprocessor

Overview

The preprocessor prunes rows and columns from term-frequency matrices, attempting to generate a result matrix that is more suitable for clustering. It also computes tf-idf (term frequency-inverse document frequency) weights for the remaining entries. Therefore the input matrix consists of nonnegative integers, and the output matrix consists of floating point numbers between 0.0 and 1.0. The Matrix Market file format (.mtx file) is used for the input and output matrices.

Rows (terms) are pruned if a given term appears in fewer than 'DOCS_PER_TERM' documents. The value of DOCS_PER_TERM is a command-line parameter with a default value of 3. For a term-frequency input matrix, in which the matrix elements represent occurrence counts for the terms, this parameter actually specifies the minimum row sum for each term. Any rows whose row sums are less than this value will be pruned.

Columns (docs) are pruned if a given document contains fewer than 'TERMS_PER_DOC' terms. The value of TERMS_PER_DOC is a command-line parameter with a default value of 5.

Whenever columns (documents) are pruned the preprocessor checks the remaining columns for uniqueness. Any duplicate columns are identified and a representative column is chosen as the survivor. The code always selects the column with the largest column index in such groups as the survivor. The preprocessor continues to prune rows and columns until it finds no further candidates for pruning. It then computes new tf-idf scores for the resulting entries and writes out the result matrix in Matrix Market format.

If the preprocessor should prune all rows or columns, it writes an error message to the screen and terminates without generating any output.

Input Files

The preprocessor requires three input files: a matrix file, a dictionary file, and a document file. The matrix file contains a sparse matrix in Matrix Market format (.mtx). This is a term-frequency matrix, and all entries should be positive integers. The preprocessor can also read in matrices containing floating-point inputs, but only if 'boolean mode' is enabled; this will be described below. The preprocessor does not support dense matrices, since the typical matrices encountered in topic modeling problems are extremely sparse, with occupancies generally less than 1%.

The second file required by the preprocessor is a 'dictionary file'. This is a simple ASCII text file containing one entry per line. Entries represent keywords, bigrams, or other general text strings the user is interested in. Each line of the file is treated as a 'keyword'; so multi-word keywords are supported as well. The smallk/data folder contains a sample dictionary file called 'dictionary.txt'. The first few entries are:

```
triumph
dey
canada
finger
circuit
```

The third file required by the preprocessor is a 'documents file'. This is another simple ASCII text file containing one entry per line. Entries represent document names or other unique identifiers. The smallk/data folder also contains a sample documents file called 'documents.txt'. The first few entries of this file are:

```
52828-11101.txt
51820-10202.txt
104595-959.txt
60259-3040.txt
```

These are the unique document identifiers for the user who generated the file. Your identifiers will likely have a different format.

Finally, the preprocessor **requires** these files to have the following names: matrix.mtx, dictionary.txt, and documents.txt. The input folder containing these files can be specified on the command line (described below). The output of the preprocessor is a new set of files called 'reduced_matrix.mtx', 'reduced_dictionary.txt', and 'reduced_documents.txt'.

Command Line Options

The preprocessor binary is called 'preprocess_tf', to emphasize the fact that it operates on term-frequency matrices. If the binary is run with no arguments, it prints out the following information:

```
preprocess_tf
   --indir <path>
   [--outdir (defaults to current directory)]
   [--docs_per_term 3]
   [--terms_per_doc 5]
   [--maxiter 1000]
   [--precision 4]
   [--boolean mode 0]
```

Only the first parameter, --indir, is required. All remaining parameters are optional and have the default values indicated.

The meanings of the various options are as follows:

- --indir: path to the folder containing the files 'matrix.mtx', 'dictionary.txt', and 'documents.txt'
- 2. —-outdir: path to the folder to into which results should be written
- 3. --docs per term: any rows whose entries sum to less than this value will be pruned
- 4. --terms per doc: any columns whose entries sum to less than this value will be pruned
- 5. —-maxiter: perform no more than this many iterations

- 6. —-precision: the number of digits of precision with which to write the output matrix
- 7. —-boolean_mode: all nonzero matrix elements will be treated as if they had the value 1.0. In other words, the preprocessor will ignore the actual frequency counts and treat all nonzero entries as if they were 1.0.

Sample Runs

Here is a sample run of the preprocessor using the data provided in the smallk distribution. This run was performed from the top-level smallk folder after building the code:

```
preprocess_tf --indir data
      Command line options:
                   indir: data/
                  outdir: current directory
                 docs_per_term: 3
                 terms_per_doc: 5
max_iter: 1000
                 precision: 4
                 boolean mode: 0
Loading input matrix data/matrix.mtx
     Input file load time: 1.176s.
Starting iterations...
     [1] height: 39771, width: 11237, nonzeros: 877453
Iterations finished.
     New height: 39727
     New width: 11237
     New nonzero count: 877374
Processing time: 0.074s.
Writing output matrix reduced matrix.mtx
Output file write time: 2.424s.
Writing dictionary file reduced dictionary.txt
Writing documents file reduced documents.txt
Dictionary + documents write time: 0.08s.
```

V.2. Matrixgen

Overview

The matrix generator application is a simple tool for generating simple matrices. The NMF and clustering tools for various testing scenarios can load these matrices. Use of the matrix generator is entirely optional.

Command Line Options

Running the matrixgen binary with no options generates the following output:

```
matrixgen
Usage: matrixgen
         --height <number of rows>
         --width <number of cols>
          --filename <path>
        [--type UNIFORM] UNIFORM:
                                           matrix with uniformly-distributed random entries
                             DENSE DIAG: dense diagonal matrix with uniform random entries
                             SPARSE DIAG: sparse diagonal matrix with uniform random entries
                             IDENTITY: identity matrix
                             ONES:
                                           matrix of all ones
                                           matrix of all zeros
                             ZEROS:
                             SPARSE:
                                           sparse matrix with uniform random entries
                                           specify 'nz per col' to control occupancy
        [--rng_center 0.5] center of random numbers radius of random numbers digits of precision (SPARSE only) nonzeros per column
```

The --height, --width, and --filename options are required. All others are optional and have the default values indicated.

The meanings of the various options are as follows:

- 1. --height: number of rows in the generated matrix
- 2. —width: number of columns in the generated matrix
- 3. ——filename: name of the output file
- 4. —-type: the type of matrix to be generated; the default is a uniformly-distributed random matrix
- 5. —-rng center: random number distribution will be centered on this value
- 6. —-rng radius: random numbers will span this distance to either side of the center value
- 7. —-precision: the number of digits of precision with which to write the output matrix
- 8. —-nz_per_col: number of nonzero entries per sparse matrix column; valid only for SPARSE type

Sample Runs

Suppose we want to generate a matrix of uniformly distributed random numbers. The matrix should have a height of 100 and a width of 16, and should be written to a file called 'w init.csv'. Use the matrix generator as follows:

```
matrixgen --height 100 --width 16 --filename w_init.csv
```

V.3. Nonnegative Matrix Factorization (NMF)

Overview

The NMF command line application performs nonnegative matrix factorization on dense or sparse matrices. If the input matrix is denoted by A, nonnegative matrix factors W and H are computed such that $A \sim WH$. Matrix A can be either dense or sparse; matrices W and H are always dense. Matrix A has m rows and n columns; matrix W has m rows and k columns; matrix H has k rows and n columns. Parameter k is a positive integer and is typically much less than either m or n.

Command Line Options

Running the nmf application with no command line parameters will cause the application to display all params that it supports. These are:

```
Usage: nmf
        --matrixfile <filename> Filename of the matrix to be factored.
                                 Either CSV format for dense or MatrixMarket format for sparse.
                                 The common dimension for factors \mbox{W} and \mbox{H}.
        --k <integer value>
        [--algorithm BPP]
                                 NMF algorithms:
                                     MU:
                                            multiplicative updating
                                     HALS:
                                           hierarchical alternating least squares
                                     RANK2: rank2 with optimal active set selection
                                     BPP: block principal pivoting
        [--stopping PG RATIO]
                                 Stopping criterion:
                                     PG RATIO: Ratio of projected gradients
                                     DELTA: Change in relative F-norm of W
        [--tol 0.005]
                                 Tolerance for the selected stopping criterion.
        [--tolcount 1]
                                 Tolerance count; declare convergence after this many
                                 iterations with metric < tolerance; default is to
                                 declare convergence on the first such iteration.
        [--infile W (empty)]
                                 Dense mxk matrix to initialize W; CSV file.
                                 If unspecified, W will be randomly initialized.
        [--infile H (empty)]
                                 Dense kxn matrix to initialize H; CSV file.
                                 If unspecified, H will be randomly initialized.
        [--outfile_W w.csv]
[--outfile_H h.csv]
                                 Filename for the W matrix result.
                                 Filename for the H matrix result.
                                 Minimum number of iterations to perform.
        [--miniter 5]
        [--maxiter 5000]
                                 Maximum number of iterations to perform.
        [--outprecision 6]
                                 Write results with this many digits of precision.
        [--maxthreads
                        81
                                 Upper limit to thread count.
        [--normalize 1]
                                 Whether to normalize W and scale H.
                                     1 == yes, 0 == no
        [--verbose 1]
                                 Whether to print updates to the screen.
                                     1 == print updates, 0 == silent
```

The --matrixfile and --k options are required; all others are optional and have the default values indicated. The meanings of the various options are as follows:

- 1. —-matrixfile: Filename of the matrix to be factored. CSV files are supported for dense matrices and MTX files for sparse matrices.
- 2. —-k: the width of the W matrix (identical to the height of the H matrix)
- 3. ——algorithm: identifier for the factorization algorithm
- 4. ——stopping: the method used to terminate the iterations; use PG_RATIO unless you have a specific reason not to
- 5. —-tol: tolerance value used to terminate iterations; when the progress metric falls below this value iterations will stop; typical values are in the 1.0e-3 or 1.0e-4 range
- 6. —-tolcount: a positive integer representing the number of successive iterations for which the progress metric must have a value <= tolerance; default is 1, which means the iterations will terminate on the first iteration with progress_metric <= tolerance
- 7. —-infile_W: CSV file containing the mxk initial values for matrix W; if omitted, W is randomly initialized
- 8. ——infile_H: CSV file containing the kxn initial values for matrix H; if omitted, H is randomly initialized
- 9. —-outfile W: filename for the computed W factor; default is w.csv

- 10. —-outfile H: filename for the computed H factor; default is h.csv
- 11. ——miniter: the minimum number of iterations to perform before checking progress; for smaller tolerance values, you may want to increase this number to avoid needless progress checks
- 12. ——maxiter: the maximum number of iterations to perform
- 13. —-outprecision: matrices W and H will be written to disk using this many digits of precision
- 14. ——maxthreads: the maximum number of threads to use; the default is to use as many threads as the hardware can support (your number may differ from that shown)
- 15. ——normalize: whether to normalize the columns of the W matrix and correspondingly scale the rows of H after convergence
- 16. --verbose: whether to display updates to the screen as the iterations progress

Sample Runs

The smallk distribution utilizes another repository smallk_data (clone this repository from github) with a matrix file 'reuters.mtx'. This is a tf-idf weighted matrix derived from the popular Reuters data set used in machine learning experiments.

Suppose we want to factor the Reuters matrix using a k value of 8. We would do that as follows, assuming that we are in the top-level smallk folder after building the code and that the smallk_data repository was cloned into 'data':

```
nmf/bin/nmf --matrixfile data/reuters.mtx --k 8
```

Note that if 'make install' was run during installation and the \$PATH variable or environment variable was set as above, this could also be called with:

```
usr/local/smallk/bin/nmf --matrixfile data/reuters.mtx --k 8
```

If we want to instead use the HALS algorithm with k=16, a tolerance of 1.0e-4, and also perform 10 iterations prior to checking progress, we would use this command line:

```
{\tt nmf/bin/nmf\ --matrixfile\ data/reuters.mtx\ --k\ 16\ --algorithm\ HALS\ --tol\ 1.0e-4\ --miniter\ 10}
```

To repeat the previous experiment but with new names for the output files, we would do this:

```
nmf/bin/nmf --matrixfile data/reuters.mtx --k 16 --algorithm HALS --tol 1.0e-4
--miniter 10 --outfile_W w_hals.csv -outfile_H h_hals.csv
```

V.4. Hierclust

Overview

First, we briefly describe the algorithm and the references section provides pointers to papers with detailed descriptions of the algorithms. NMF-RANK2 for hierarchical clustering generates a binary tree of items. We refer to a node in the binary tree and the items associated with the node interchangeably. This method begins by placing all data items in the root node. The number of leaf nodes to generate is specified (user input). The algorithm proceeds with the following steps, repeated until the maximum number of leaf nodes, max_leaf_nodes, is reached:

- 1. Pick the leaf node with the highest score (at the very beginning where only a root node is present, just pick the root node)
- 2. Apply NMF-RANK2 to the node selected in step 1, and generate two new leaf nodes
- 3. Compute a score for each of the two leaf nodes generated in step 2
- 4. Repeat until the desired number of leaf nodes has been generated

Step 2 implements the details of the node splitting into child nodes. Outlier detection plays a crucial role in hierarchical clustering to generate a tree with well-balanced and meaningful clusters. To implement this, we have two additional parameters in step 2: *trial_allowance* and *unbalanced*.

The parameter *trial_allowance* is the number of times that the program will try to split a node into two meaningful clusters. In each trial, the program will check if one of the two generated leaf nodes is an outlier set. If the outlier set is detected, the program will delete the items in the outlier set from the node being split and continue to the next trial. If all the trials are finished and the program still cannot find two meaningful clusters for this node, all the deleted items are "recycled" and placed into this node again, and this node will be labeled as a "permanent leaf node" that cannot be picked in step 1 in later iterations.

The parameter *unbalanced* is a threshold parameter to determine whether two generated leaf nodes are unbalanced. Suppose two potential leaf nodes L and R are generated from the selected node and L has fewer items than R. Let us denote the number of items in a node N as |N|. L and R are called *unbalanced* if

```
|L| < unbalanced * (|L|+|R|).
```

Note that if L and R are unbalanced, the potential node L with fewer items is not necessarily regarded as an outlier set. Please see the referenced paper for more details [3].

Internally, NMF-RANK2 is applied to each leaf node to compute the score in step 3. The computed result matrices W and H in step 3 are cached so that we can avoid duplicate work in step 2 in later iterations.

The score for each leaf node is based on a modified version of the NDCG (*Normalized Discounted Cumulative Gain*) measure, a common measure in the information retrieval community. A leaf node is associated with a "topic vector", and we can define "top terms" based on the topic vector. A leaf node will receive a high score if its top terms are a good combination of the top terms of its two potential children; otherwise it receives a low score.

The hierclust application generates two output files. One file contains the assignments of documents to clusters. This file contains one integer for each document (column) of the original matrix. The integers are the cluster labels for that cluster that the document was assigned to. If the document could not be assigned to a cluster, a -1 will be entered into the file, indicating that the document is an outlier.

The other output file contains information for each node in the factorization binary tree. The items in this file are:

- 1. id: a unique id for this node
- 2. level: the level in the tree at which this node appears; the root is at level 0, the children of the root are at level 1, etc.

- 3. label: the cluster label for this node (meaningful only for leaf nodes)
- 4. parent id: the unique id of the parent of this node (the root node has parent id == 0)
- 5. parent label: the cluster label of the parent of this node
- 6. left child: a Boolean value indicating whether this node is the left or right child of its parent
- 7. left child label: the cluster label of the left child of this node (leaf nodes have -1 for this value)
- 8. right child label: the cluster label of the right child of this node (leaf nodes have -1 for this value)
- 9. doc count: the number of documents that this node represents
- 10. top terms: the highest probability dictionary terms for this node

The node id values and the left or right child indicators can be used to unambiguously reconstruct the factorization tree.

Command Line Options

Running the hierclust application with no command line parameters will cause the application to display all params that it supports. These are:

```
hierclust
Usage: hierclust
          --matrixfile <filename>
                                              Filename of the matrix to be factored.
                                              Either CSV format for dense or MatrixMarket format for sparse.
          --dictfile <filename>
                                              The name of the dictionary file.
          --clusters <integer>
                                              The number of clusters to generate.
          [--infile_W (empty)]
                                              Dense m x (4*clusters) matrix to initialize W, CSV file.
                                              If unspecified, W will be randomly initialized.
          [--infile_H (empty)]

Dense (4*clusters) x n matrix to initialize H, CSV

If unspecified, H will be randomly initialized.

[--tol 0.0001]

Tolerance value for each factorization.

Output directory. If unspecified, results will be written to the current directory.
                                              Dense (4*clusters) x n matrix to initialize H, CSV file.
                                          Minimum number of iterations to perform.

Maximum number of iterations to perform.

Number of terms per node.
          [--miniter 5]
          [--maxiter 5000]
          [--maxthreads 8] Upper limit to thread count.
[--unbalanced 0.1] Threshold for determining leaf node imbalance.
[--trial_allowance 3] Number of split attempts.
[--flat_0] Whether to generate 12
                                                   1 == yes, 0 == no
          [--verbose 1]
                                             Whether to print updates to the screen.
                                                   1 == yes, 0 == no
                                              Format of the output file containing the tree.
          [--format XML]
                                                   XMI: XMI format.
                                                   JSON: JavaScript Object Notation
          [--treefile tree_N.ext]
                                              Name of the output file containing the tree.
                                              N is the number of clusters for this run.
                                              The string 'ext' depends on the desired format.
                                              This filename is relative to the outdir.
          [--assignfile assignments N.csv] Name of the file containing final assignments.
                                                      N is the number of clusters for this run.
                                                      This filename is relative to the outdir.
```

The --matrixfile, --dictfile, and --clusters options are required; all others are optional and have the default values indicated. The meanings of the various options are as follows:

- --matrixfile: Filename of the matrix to be factored. CSV files are supported for dense matrices and MTX files for sparse matrices.
- 2. ——dictfile: absolute or relative path to the dictionary file
- 3. ——clusters: the number of leaf nodes (clusters) to generate
- 4. −-infile_W: CSV file containing the mx(4*clusters) initial values for matrix W; if omitted, W is randomly initialized
- 5. —-infile_H: CSV file containing the (4*clusters)xn initial values for matrix H; if omitted, H is randomly initialized
- 6. —-tol: tolerance value for each internal NMF-RANK2 factorization; the stopping criterion is the ratio of projected gradient method
- 7. —-outdir: path to the folder into which to write the output files; if omitted results will be written to the current directory

- 8. ——miniter: minimum number of iterations to perform before checking progress on each NMF-RANK2 factorization
- 9. --maxiter: the maximum number of iterations to perform on each NMF-RANK2 factorization
- 10. —-maxterms: the number of dictionary keywords to include in each node
- 11. —-maxthreads: the maximum number of threads to use; the default is to use as many threads as the hardware can support (your number may differ from that shown)
- 12. ——unbalanced: threshold value for declaring leaf node imbalance (see explanation above)
- 13. ——trial allowance: maximum number of split attempts for any node (see explanation above)
- 14. ——flat: whether to generate a flat clustering result in addition to the hierarchical clustering result
- 15. —-verbose: whether to display updates to the screen as the iterations progress
- 16. ——format: file format to use for the clustering results
- 17. —-treefile: name of the output file for the factorization tree; uses the format specified by the format parameter
- 18. —-assignfile: name of the output file for the cluster assignments

Sample Runs

The smallk distribution contains a 'data' directory with a matrix file 'reuters.mtx' and an associated dictionary file 'reuters_dictionary.txt'. These files are derived from the popular Reuters data set used in machine learning experiments.

As above, it is assumed that the <u>smallk_data</u> repository was cloned into 'data' and that the commands can be run as below or from /usr/local/smallk/bin.

Suppose we want to perform hierarchical clustering on this data set and generate 10 leaf nodes. We would do that as follows, assuming that we are in the top-level smallk folder after building the code:

```
hierclust/bin/hierclust --matrixfile data/reuters.mtx --dictfile data/reuters_dictionary.txt --clusters 10
```

This will generate two result files in the current directory: tree 10.xml and assignments 10.csv.

If we want to instead generate 10 clusters, each with 8 terms, using JSON output format, we would use this command line:

```
hierclust/bin/hierclust --matrixfile data/reuters.mtx --dictfile data/reuters_dictionary.txt --clusters 10 --maxterms 8 --format JSON
```

Two files will be generated: tree_10.json and assignments_10.csv. The json file will have 8 keywords per node, whereas the tree 10.xml file will have only 5.

To generate a flat clustering result (in addition to the hierarchical clustering result), use this command line:

```
hierclust/bin/hierclust --matrixfile data/reuters.mtx --dictfile data/reuters_dictionary.txt --clusters 10 --maxterms 8 --format JSON --flat 1
```

Two additional files will be generated this time (along with tree_10.json and assignments_10.csv): 'clusters_10.json', which contains the flat clustering results, and 'assignments_flat_10.csv', which contains the flat clustering assignments.

V.5. Flatclust

Overview

The flatclust command line application factors the input matrix using either NMF-HALS or NMF-BPP and generates a flat clustering result. A flatclust run generating k clusters will generally run more slowly than a hierclust run, of the same number of clusters, with the --flat option enabled. The reason for this is that the hierclust application uses the NMF-RANK2 algorithm and always generates factor matrices with two rows or columns. The runtime of NMF scales super linearly with k in this case, and thus runs fastest for the smallest k value.

The flatclust application generates two output files. The first file contains the assignments of documents to clusters and is interpreted identically to that of the hierclust application, with the exception that there are no outliers generated by flatclust.

The second file contains the node information. This file is much simpler than that of the hierclust application since there is no factorization tree. The items for each node in this file are:

- 1. id: the unique id of this node
- 2. doc count: the number of documents assigned to this node
- 3. top terms: the highest probability dictionary terms assigned to this node

Command Line Options

Running the flatclust application with no command line parameters will cause the application to display all params that it supports. These are:

```
flatclust
Usage: flatclust
         -matrixfile <filename>
                                     Filename of the matrix to be factored.
                                      Either CSV format for dense or MatrixMarket format for sparse.
        --dictfile <filename>
                                      The name of the dictionary file.
                                      The number of clusters to generate.
        --clusters <integer>
        [--algorithm BPP]
                                     The NMF algorithm to use:
                                          HALS: hierarchical alternating least squares
                                          RANK2: rank2 with optimal active set selection
                                                 (for two clusters only)
                                                 block principal pivoting
        [--infile_W (empty)]
                                      Dense matrix to initialize W, CSV file.
                                      The matrix has m rows and 'clusters' columns.
                                      If unspecified, W will be randomly initialized.
        [--infile H (empty)]
                                      Dense matrix to initialize H, CSV file.
                                     The matrix has 'clusters' rows and n columns.
                                     If unspecified, H will be randomly initialized.
        [--tol 0.0001]
                                     Tolerance value for the progress metric.
        [--tol 0.0001]
[--outdir (empty)]
                                     Output directory. If unspecified, results will be
                                     written to the current directory.
        [--miniter 5]
                                     Minimum number of iterations to perform.
        [--maxiter 5000]
                                     Maximum number of iterations to perform.
        [--maxterms 5]
                                     Number of terms per node.
        [--maxthreads
                                     Upper limit to thread count.
        [--verbose 1]
                                     Whether to print updates to the screen.
                                         1 == yes, 0 == no
        [--format XML]
                                     Format of the output file containing the tree.
                                         XML: XML format
                                          JSON: JavaScript Object Notation
        [--clustfile clusters N.ext] Name of the output XML file containing the tree.
                                     N is the number of clusters for this run. The string 'ext' depends on the desired format.
                                      This filename is relative to the outdir.
        [--assignfile assignments N.csv] Name of the file containing final assignments.
                                           N is the number of clusters for this run.
                                           This filename is relative to the outdir.
```

The --matrixfile, --dictfile, and --clusters options are required; all others are optional and have the default values indicated. The meanings of the various options are as follows:

- --matrixfile: Filename of the matrix to be factored. CSV files are supported for dense matrices and MTX files for sparse matrices.
- 2. —-dictfile: absolute or relative path to the dictionary file
- 3. —-clusters: the number of clusters to generate (equivalent to the NMF 'k' value)

- 4. ——algorithm: the factorization algorithm to use
- 5. —-infile_W: CSV file containing the m x 'clusters' initial values for matrix W; if omitted, W is randomly initialized
- 6. —-infile_H: CSV file containing the 'clusters' x n initial values for matrix H; if omitted, H is randomly initialized
- 7. —-tol: tolerance value for the factorization; the stopping criterion is the ratio of projected gradient method
- 8. —-outdir: path to the folder into which to write the output files; if omitted results will be written to the current directory
- 9. ——miniter: minimum number of iterations to perform before checking progress
- 10. —maxiter: the maximum number of iterations to perform
- 11. ——maxterms: the number of dictionary keywords to include in each node
- 12. ——maxthreads: the maximum number of threads to use; the default is to use as many threads as the hardware can support (your number may differ from that shown)
- 13. --verbose: whether to display updates to the screen as the iterations progress
- 14. ——format: file format to use for the clustering results
- 15. ——clustfile: name of the output file for the nodes; uses the format specified by the format parameter
- 16. —-assignfile: name of the output file for the cluster assignments

Sample Run

The smallk distribution contains a 'data' directory with a matrix file 'reuters.mtx' and an associated dictionary file 'reuters_dictionary.txt'. These files are derived from the popular Reuters data set used in machine learning experiments.

As above, it is assumed that the <u>smallk_data</u> repository was cloned into 'data' and that the commands can be run as below or from /usr/local/smallk/bin.

Suppose we want to perform flat clustering on this data set and generate 10 clusters. We would do that as follows, assuming that we are in the top-level smallk folder after building the code:

```
{\tt flatclust/bin/flatclust~--matrixfile~data/reuters.mtx~--dictfile~data/reuters\_dictionary.txt~--clusters~10}
```

This will generate two result files in the current directory: clusters 10.xml and assignments 10.csv.

If we want to instead generate 10 clusters, each with 8 terms, using JSON output format, we would use this command line:

```
flatclust/bin/flatclust --matrixfile data/reuters.mtx --dictfile data/reuters_dictionary.txt
--clusters 10 --maxterms 8 --format JSON
```

Two files will be generated: clusters_10.json and assignments_10.csv. The json file will have 8 keywords per node, whereas the clusters_10.xml file will have only 5.

V.6. SmallK Test Results

After building the SmallK library, the 'make check' command will run a bash script that performs a series of tests on the code. Below is a sample output of those tests:

```
make check
\verb|sh| tests/scripts/test_smallk.sh| .../xdata_data | tee smallk_test_results.txt|
           Testing the smallk interface.
WARNING: Could not achieve THREAD MULTIPLE support.
Smallk major version: 1
Smallk minor version: 6
Smallk patch level: 0
Smallk version string: 1.6.0
Loading matrix...
Running NMF-BPP...
Initializing matrix W...
Initializing matrix H...
                 parameters:
                algorithm: Nonnegative Least Squares with Block Principal Pivoting
       stopping criterion: Ratio of Projected Gradients
                  height: 12411
                    width: 7984
                        k: 8
                  miniter: 1
                  maxiter: 5000
                      tol: 0.005
               matrixfile: ../xdata_data/reuters.mtx
maxthreads: 8
    progress metric: (min_iter)
progress metric: 0.35826
    progress metric: 0.172127
3:
      progress metric: 0.106297
progress metric: 0.0696424
4:
5:
      progress metric: 0.0538889 progress metric: 0.0559478
8: progress metric: 0.0686117
9: progress metric: 0.0788641
10: progress metric: 0.0711522
20: progress metric: 0.00568349
Solution converged after 22 iterations.
Elapsed wall clock time: 0.527 sec.
Writing output files...
Running HierNmf2...
loading dictionary...
creating random W initializers...
creating random H initializers...
               parameters:
                   height: 12411
                    width: 7984
               matrixfile: ../xdata_data/reuters.mtx
                 dictfile: ../xdata data/reuters dictionary.txt
                      tol: 0.0001
                  miniter: 1
                  maxiter: 5000
                 maxterms: 5
               maxthreads: 8
[1] [2] [3] [4]
Elapsed wall clock time: 572 ms.
9/9 factorizations converged.
Writing output files...
W matrix test passed
H matrix test passed
**********
             Testing the preprocessor.
*************
```

```
indir: ../xdata data/
                  outdir: current directory
           docs per term: 3
           terms per doc: 5
               max iter: 1000
               precision: 4
            boolean mode: 0
Loading input matrix ../xdata data/matrix.mtx
      Input file load time: 1.3s.
Starting iterations...
      [1] height: 39771, width: 11237, nonzeros: 877453
Iterations finished.
      New height: 39727
      New width: 11237
      New nonzero count: 877374
Processing time: 0.048s.
Writing output matrix 'reduced_matrix.mtx'
Output file write time: 1.624s.
Writing pruned term-frequency matrix 'reduced_matrix_tf.mtx'
Output term-frequency matrix write time: 1.558s.
Writing dictionary file 'reduced_dictionary.txt'
Writing documents file 'reduced documents.txt'
Dictionary + documents write time: 0.074s.
preprocessor matrix test passed
preprocessor dictionary test passed
preprocessor documents test passed
           Testing the NMF routines.
*********************************
WARNING: Could not achieve THREAD MULTIPLE support.
Loading matrix...
Initializing matrix W...
Initializing matrix H...
     Command line options:
               algorithm: Nonnegative Least Squares with Block Principal Pivoting
      stopping criterion: Ratio of Projected Gradients
                 height: 12411
                  width: 7984
                      k: 8
                 miniter: 1
                 maxiter: 5000
                    tol: 0.005
                tolcount: 1
                 verbose: 1
               normalize: 1
            outprecision: 6
              matrixfile: ../xdata_data/reuters.mtx
infile_W: ../xdata_data/nmf_init_w.csv
infile_H: ../xdata_data/nmf_init_h.csv
              outfile_W: w.csv
outfile H: h.csv
              maxthreads: 8
     progress metric:
1:
                         (min iter)
      progress metric:
                         0.35826
2:
      progress metric:
                         0.172127
3:
      progress metric:
4:
                         0.106297
      progress metric:
                         0.0696424
5:
      progress metric:
                         0.0538889
6:
      progress metric:
                         0.0559478
7:
      progress metric:
                         0.0686117
8:
      progress metric:
                         0.0788641
9:
     progress metric:
                         0.0711522
10:
     progress metric:
20:
                         0.00568349
Solution converged after 22 iterations.
Elapsed wall clock time: 0.527 sec.
Writing output files ...
NMF W matrix test passed
Testing hierclust.
***********
WARNING: Could not achieve THREAD MULTIPLE support.
loading dictionary...
loading matrix...
loading W initializers...
```

```
loading H initializers...
     Command line options:
                  height: 12411
                   width: 7984
              matrixfile: ../xdata_data/reuters.mtx
                 infile W: ../xdata data/hierclust init w.csv
                 infile_H: ../xdata_data/hierclust_init_h.csv
                dictfile: ../xdata data/reuters dictionary.txt
              assignfile: assignments 5.csv
                  format: XML
                 treefile: tree 5.xml
                clusters: 5
                     tol: 0.0001
                  outdir:
                 miniter: 1
                 maxiter: 5000
                maxterms: 5
              maxthreads: 8
              unbalanced: 0.1
         trial allowance: 3
                  flat: 0
                 verbose: 1
[1] [2] [3] [4]
Elapsed wall clock time: 734 ms.
9/9 factorizations converged.
Writing output files...
hierclust cluster file test passed
hierclust assignment file test passed
************
              Testing flatclust.
***********
WARNING: Could not achieve THREAD MULTIPLE support.
loading dictionary...
loading matrix...
Initializing matrix W...
Initializing matrix H...
     Command line options:
                  height: 256
                   width: 256
              matrixfile: ../xdata_data/rnd_256_256.csv
                infile_W: ../xdata_data/flatclust_init_w.csv
infile_H: ../xdata_data/flatclust_init_h.csv
              dictfile: ../xdata_data/reuters_dictionary.txt assignfile: assignments_16.csv
                  format: XML
               clustfile: clusters 16.xml
               algorithm: HALS
                clusters: 16
                     tol: 0.0001
                  outdir:
                 miniter: 1
                 maxiter: 5000
                maxterms: 5
              maxthreads: 8
                 verbose: 1
                         (min_iter)
0.635556
1:
      progress metric:
      progress metric:
2:
                         0.490817
3:
      progress metric:
      progress metric:
                          0.479135
4:
      progress metric:
                          0.474986
5:
      progress metric:
                          0.44968
6:
      progress metric:
7:
                          0.422542
      progress metric:
                          0.407662
8:
      progress metric:
                          0.395145
9:
      progress metric:
                          0.379238
10:
20:
      progress metric:
                          0.272868
      progress metric:
30:
                          0.168386
40:
      progress metric:
                          0.109147
      progress metric:
50:
                          0.0767327
60:
      progress metric:
                          0.0488545
      progress metric:
70:
                          0.036226
80:
      progress metric:
                          0.0307648
      progress metric:
                          0.0266116
90:
100:
      progress metric:
                          0.0226963
     progress metric:
110:
                          0.0188616
120: progress metric:
130: progress metric:
                         0.0158307
```

0.0137605

0.0127888 0.0123962

140: progress metric: 150: progress metric:

160:	progress	metric:	0.0124734
170:	progress	metric:	0.0123563
180:	progress	metric:	0.0122163
190:	progress	metric:	0.0120643
200:	progress	metric:	0.0117647
210:	progress	metric:	0.0114894
220:	progress	metric:	0.0110467
230:	progress	metric:	0.0107816
240:	progress	metric:	0.0105239
250:	progress	metric:	0.0103824
260:	progress	metric:	0.0100915
270:	progress	metric:	0.00965073
280:	progress	metric:	0.00938526
290:	progress	metric:	0.00914129
300:	progress	metric:	0.00896701
310:	progress	metric:	0.00886729
320:	progress	metric:	0.00841059
330:	progress	metric:	0.007793
340:	progress	metric:	0.00740095
350:	progress	metric:	0.00708869
360:	progress	metric:	0.00683069
370:	progress	metric:	0.00672093
380:	progress	metric:	0.00687906
390:	progress	metric:	0.00703777
400:	progress	metric:	0.00721928
410:	progress	metric:	0.00729384
420:	progress	metric:	0.00718332
430:	progress	metric:	0.00722893
440:	progress	metric:	0.00726766
450:	progress	metric:	0.00739665
460:	progress	metric:	0.00769819
470:	progress	metric:	0.00814673
480:	progress	metric:	0.008566
490:	progress	metric:	0.00877955
500: 510:	progress	metric:	0.00884221
520:	progress	metric:	0.0088057 0.00852345
530:	progress	metric: metric:	0.00797952
540:	progress	metric:	0.00749354
550:	progress progress	metric:	0.00689316
560:	progress	metric:	0.00623287
570:	progress	metric:	0.00576619
580:	progress	metric:	0.00541125
590:	progress	metric:	0.00501715
600:	progress	metric:	0.00466547
610:	progress	metric:	0.00432811
620:	progress	metric:	0.00412669
630:	progress	metric:	0.00383406
640:	progress	metric:	0.00352802
650:	progress	metric:	0.00331556
660:	progress	metric:	0.00315735
670:	progress	metric:	0.00304253
680:	progress	metric:	0.00296627
690:	progress	metric:	0.00289013
700:	progress	metric:	0.00279647
710:	progress	metric:	0.00271036
720:	progress	metric:	0.00261087
730:	progress	metric:	0.0025158
740:	progress	metric:	0.00245123
750:	progress	metric:	0.00237435
760:	progress	metric:	0.00231126
770:	progress	metric:	0.00228199
780:	progress	metric:	0.00227623
790:	progress	metric:	0.00228185
800:	progress	metric:	0.00227993
810: 820:	progress	metric:	0.00228216
	progress	metric:	
830: 840:	progress	metric: metric:	0.00229096
850:	progress progress	metric:	0.00232403
860:	progress	metric:	0.00234937
870:	progress	metric:	0.00210786
880:	progress	metric:	0.00210788
890:	progress	metric:	0.00193402
900:	progress	metric:	0.00173358
910:	progress	metric:	0.00173330
920:	progress	metric:	0.00156422
930:	progress	metric:	0.00150835
940:	progress	metric:	0.00146594
950:	progress	metric:	0.00143261
960:	progress	metric:	0.00137378
970:	progress	metric:	0.00131989
980:	progress	metric:	0.00126626
990:	progress	metric:	0.0012164
1000:	progress	metric:	0.00117061
1010:	progress	metric:	0.00112539
1020:	progress	metric:	0.00108626
1030:	progress	metric:	0.00105192
1040:	progress	metric:	0.00102131

1050:			
	progress	metric:	0.000992069
1060:	progress	metric:	0.000965259
1070:	progress	metric:	0.000938949
1080:	progress	metric:	0.000911962
1090:	progress	metric:	0.000884505
1100:		metric:	0.000854904
	progress		
1110:	progress	metric:	0.000820121
1120:	progress	metric:	0.000785245
1130:	progress	metric:	0.000752513
1140:	progress	metric:	0.000723279
1150:	progress	metric:	0.000697698
1160:	progress	metric:	0.000680904
1170:	progress	metric:	0.000652152
1180:	progress	metric:	0.000628268
1190:	progress	metric:	0.000612413
1200:	progress	metric:	0.000596834
1210:	progress	metric:	0.000580674
1220:	progress	metric:	0.000556549
1230:	progress	metric:	0.000535666
1240:	progress	metric:	0.00051492
1250:	progress	metric:	0.000496234
1260:	progress	metric:	0.000481147
1270:	progress	metric:	0.000461294
1280:	progress	metric:	0.000440802
1290:		metric:	0.000419049
	progress		
1300:	progress	metric:	0.000398007
1310:	progress	metric:	0.000376203
1320:	progress	metric:	0.000355811
1330:	progress	metric:	0.00033729
1340:	progress	metric:	0.000318932
1350:			0.000318932
	progress	metric:	
1360:	progress	metric:	0.000287961
1370:	progress	metric:	0.00027486
1380:	progress	metric:	0.00026403
1390:	progress	metric:	0.000255504
1400:	progress	metric:	0.000248646
1410:			
	progress	metric:	0.000242996
1420:	progress	metric:	0.000239243
1430:	progress	metric:	0.000236852
1440:	progress	metric:	0.000235313
1450:	progress	metric:	0.000234465
1460:	progress	metric:	0.000234154
1470:			0.000234154
	progress	metric:	
1480:	progress	metric:	0.00023487
1490:	progress	metric:	0.000237223
1500:	progress	metric:	0.000240043
1510:	progress	metric:	0.000243896
1520:	progress	metric:	0.00024867
1530:			0.000253981
	progress	metric:	
1540:	progress	metric:	0.000260239
1550:	progress	metric:	0.000266795
1000.			
1560:	progress	metric:	0.000273529
		metric: metric:	0.000273529
1560: 1570:	progress	metric:	0.000280678
1560: 1570: 1580:	progress progress	metric: metric:	0.000280678 0.000287273
1560: 1570: 1580: 1590:	progress progress progress	<pre>metric: metric: metric:</pre>	0.000280678 0.000287273 0.000292288
1560: 1570: 1580: 1590: 1600:	progress progress progress progress	<pre>metric: metric: metric: metric:</pre>	0.000280678 0.000287273 0.000292288 0.000296475
1560: 1570: 1580: 1590: 1600: 1610:	progress progress progress progress progress	<pre>metric: metric: metric: metric: metric:</pre>	0.000280678 0.000287273 0.000292288 0.000296475 0.000299556
1560: 1570: 1580: 1590: 1600: 1610: 1620:	progress progress progress progress progress progress	metric: metric: metric: metric: metric: metric:	0.000280678 0.000287273 0.000292288 0.000296475 0.000299556 0.00030244
1560: 1570: 1580: 1590: 1600: 1610:	progress progress progress progress progress	<pre>metric: metric: metric: metric: metric:</pre>	0.000280678 0.000287273 0.000292288 0.000296475 0.000299556
1560: 1570: 1580: 1590: 1600: 1610: 1620:	progress progress progress progress progress progress	metric: metric: metric: metric: metric: metric:	0.000280678 0.000287273 0.000292288 0.000296475 0.000299556 0.00030244
1560: 1570: 1580: 1590: 1600: 1610: 1620: 1630: 1640:	progress progress progress progress progress progress progress progress	metric: metric: metric: metric: metric: metric: metric: metric: metric:	0.000280678 0.000287273 0.000292288 0.000296475 0.000299556 0.00030244 0.000306148
1560: 1570: 1580: 1590: 1600: 1610: 1620: 1630: 1640: 1650:	progress progress progress progress progress progress progress progress progress	metric: metric: metric: metric: metric: metric: metric: metric: metric:	0.000280678 0.000287273 0.000292288 0.000296475 0.000299556 0.00030244 0.000306148 0.000310299 0.000314674
1560: 1570: 1580: 1590: 1600: 1610: 1620: 1630: 1640: 1650: 1660:	progress progress progress progress progress progress progress progress progress progress	metric:	0.000280678 0.000287273 0.000292288 0.000296475 0.000299556 0.00030244 0.000306148 0.000310299 0.000314674 0.000319052
1560: 1570: 1580: 1590: 1600: 1610: 1620: 1630: 1640: 1650: 1660: 1670:	progress progress progress progress progress progress progress progress progress progress progress	metric:	0.000280678 0.000287273 0.000292288 0.000296475 0.000299556 0.00030244 0.000306148 0.00031029 0.000314674 0.000319052
1560: 1570: 1580: 1590: 1600: 1610: 1620: 1630: 1640: 1650: 1660: 1670: 1680:	progress progress progress progress progress progress progress progress progress progress progress	metric:	0.000280678 0.000287273 0.000292288 0.000296475 0.000299556 0.00030244 0.000310299 0.000314674 0.000319052 0.000323906 0.000329536
1560: 1570: 1580: 1590: 1600: 1610: 1620: 1630: 1640: 1650: 1660: 1670: 1680: 1690:	progress progress progress progress progress progress progress progress progress progress progress progress	metric:	0.000280678 0.000287273 0.000292288 0.000296475 0.000299556 0.00030244 0.000310299 0.000314674 0.000319052 0.0003299536 0.000329536
1560: 1570: 1580: 1590: 1600: 1610: 1620: 1630: 1640: 1650: 1660: 1670: 1680: 1690: 1700:	progress progress progress progress progress progress progress progress progress progress progress	metric:	0.000280678 0.000287273 0.000292288 0.000299556 0.00030244 0.000310299 0.000314674 0.000319052 0.00032996 0.00032996 0.000329536 0.000329536
1560: 1570: 1580: 1590: 1600: 1610: 1620: 1630: 1640: 1650: 1660: 1670: 1680: 1690:	progress progress progress progress progress progress progress progress progress progress progress progress	metric:	0.000280678 0.000287273 0.000292288 0.000296475 0.000299556 0.00030244 0.000310299 0.000314674 0.000319052 0.0003299536 0.000329536
1560: 1570: 1580: 1590: 1600: 1610: 1620: 1630: 1640: 1650: 1660: 1670: 1680: 1690: 1700:	progress progress progress progress progress progress progress progress progress progress progress progress progress	metric:	0.000280678 0.000287273 0.000292288 0.000299556 0.000299556 0.00030244 0.000310249 0.000314674 0.000319052 0.000329536 0.000329536 0.000329536 0.000342834 0.000351167
1560: 1570: 1580: 1590: 1600: 1610: 1620: 1630: 1640: 1650: 1660: 1670: 1690: 1700: 1710: 1710:	progress progress progress progress progress progress progress progress progress progress progress progress progress progress progress	metric:	0.000280678 0.000287273 0.000292288 0.000299556 0.00030244 0.000310299 0.000314674 0.000310299 0.000319052 0.000329536 0.000329536 0.000342834 0.000351167 0.000352515
1560: 1570: 1580: 1590: 1600: 1610: 1620: 1630: 1640: 1650: 1660: 1670: 1680: 1700: 1710: 1720: 1730:	progress progress progress progress progress progress progress progress progress progress progress progress progress progress progress	metric:	0.000280678 0.000287273 0.000292288 0.000299556 0.00030244 0.000310299 0.000314674 0.000319052 0.000323906 0.000329536 0.000329536 0.000342834 0.000352515 0.000342834
1560: 1570: 1580: 1590: 1600: 1610: 1620: 1630: 1640: 1650: 1670: 1670: 1700: 1710: 1720: 1730: 1730:	progress progress progress progress progress progress progress progress progress progress progress progress progress progress progress progress progress	metric:	0.000280678 0.000287273 0.000292288 0.000299556 0.00030244 0.000310299 0.000314674 0.000319052 0.000329536 0.000329536 0.000329536 0.000329536 0.000352515 0.000352515 0.000348749 0.000345684
1560: 1570: 1580: 1590: 1600: 1610: 1620: 1630: 1640: 1650: 1670: 1680: 1700: 1710: 1720: 1730: 1740: 1740: 1750:	progress progress progress progress progress progress progress progress progress progress progress progress progress progress progress progress progress	metric:	0.000280678 0.000287273 0.000292288 0.000299556 0.00030244 0.000306148 0.000310299 0.000314674 0.000319052 0.00032956 0.00032956 0.000329536 0.000329536 0.000345749 0.000345749 0.000345684 0.000345749
1560: 1570: 1580: 1590: 1600: 1610: 1620: 1630: 1640: 1650: 1670: 1680: 1710: 1720: 1730: 1740: 1750: 1760:	progress progress progress progress progress progress progress progress progress progress progress progress progress progress progress progress progress progress progress	metric:	0.000280678 0.000287273 0.000292288 0.000299556 0.00030244 0.000306148 0.000310299 0.000314674 0.000319052 0.000329536 0.000329536 0.000329536 0.0003458167 0.0003458167 0.000345818 0.000345884 0.000345884 0.000345884 0.000343139 0.000340867
1560: 1570: 1580: 1590: 1600: 1610: 1620: 1630: 1640: 1650: 1670: 1680: 1700: 1710: 1720: 1730: 1740: 1740: 1750:	progress progress progress progress progress progress progress progress progress progress progress progress progress progress progress progress progress	metric:	0.000280678 0.000287273 0.000292288 0.000299556 0.00030244 0.000306148 0.000310299 0.000314674 0.000319052 0.00032956 0.00032956 0.000329536 0.000329536 0.000345749 0.000345749 0.000345684 0.000345749
1560: 1570: 1580: 1590: 1600: 1610: 1620: 1630: 1640: 1650: 1670: 1680: 1710: 1720: 1730: 1740: 1750: 1760:	progress progress progress progress progress progress progress progress progress progress progress progress progress progress progress progress progress progress progress	metric:	0.000280678 0.000287273 0.000292288 0.000299556 0.00030244 0.000306148 0.000310299 0.000314674 0.000319052 0.000329536 0.000329536 0.000329536 0.0003458167 0.0003458167 0.000345818 0.000345884 0.000345884 0.000345884 0.000343139 0.000340867
1560: 1570: 1580: 1590: 1600: 1610: 1620: 1630: 1640: 1650: 1660: 1670: 1770: 1710: 1720: 1730: 1740: 1750: 1760: 1770:	progress progress	metric:	0.000280678 0.000287273 0.000292288 0.000299556 0.00030244 0.000306148 0.000310299 0.000319052 0.000329536 0.000329536 0.000329536 0.0003451167 0.000355115 0.00034584 0.00034584 0.00034584 0.00034586 0.000340867 0.000340867 0.00034952
1560: 1570: 1580: 1590: 1600: 1610: 1620: 1630: 1640: 1650: 1670: 1660: 1770: 1710: 1720: 1730: 1740: 1750: 1760: 1770: 1770: 1770: 1770: 1780: 1780:	progress progress	metric:	0.000280678 0.000287273 0.000292288 0.000299556 0.00030244 0.000310299 0.000314674 0.000319052 0.00032956 0.00032956 0.000329536 0.000329536 0.000345749 0.000345749 0.000345684 0.000349749 0.000349749 0.000349749 0.000349749 0.000349749 0.000349749 0.000349749 0.000349749 0.000349749 0.000349749 0.000349749 0.000349749
1560: 1570: 1580: 1590: 1600: 1610: 1620: 1630: 1640: 1650: 1670: 1700: 1710: 1720: 1730: 1740: 1750: 1770: 1770: 1780: 1780: 1790: 1800:	progress progress	metric:	0.000280678 0.000287273 0.000292288 0.000299556 0.00030244 0.000306148 0.000310299 0.000314674 0.00032956 0.00032956 0.00032956 0.00032956 0.000345913 0.000345515 0.000345749 0.000345749 0.000349749 0.000349749 0.000349749 0.000349749 0.000349749 0.000349749 0.000349749 0.000349749 0.000349749 0.000349749 0.000349749 0.000349749 0.000349749
1560: 1570: 1580: 1590: 1600: 1610: 1620: 1630: 1640: 1650: 1660: 1670: 1770: 1770: 1730: 1740: 1750: 1770: 1780: 1790: 1810:	progress progress	metric:	0.000280678 0.000287273 0.000292288 0.000299556 0.00030244 0.000306148 0.000310299 0.000314674 0.000319052 0.000329536 0.000329536 0.000345834 0.000351167 0.00034581 0.00034581 0.00034581 0.00034581 0.00034581 0.00034581 0.00034581 0.00034581 0.00034581 0.00034581 0.00034581 0.00034581 0.00034581 0.00034581 0.00034581 0.00034581
1560: 1570: 1580: 1590: 1600: 1610: 1620: 1630: 1640: 1650: 1670: 1700: 1710: 1720: 1730: 1740: 1750: 1760: 1770: 1780: 1790: 1800: 1810: 1820:	progress progress	metric:	0.000280678 0.000287273 0.000292288 0.000296475 0.00030244 0.000310299 0.000314674 0.000319052 0.000323906 0.000329536 0.000325515 0.000342834 0.000352515 0.000348749 0.000348749 0.000340867 0.000340867 0.000339052 0.000337038 0.000337038 0.000335244 0.0003337038 0.000332111 0.000330198
1560: 1570: 1580: 1590: 1600: 1610: 1620: 1630: 1640: 1670: 1670: 1700: 1710: 1720: 1730: 1740: 1750: 1760: 1770: 1780: 1790: 1800: 1810: 1820: 1830:	progress progress	metric:	0.000280678 0.000287273 0.000292288 0.000299556 0.00030244 0.000310299 0.000314674 0.000319052 0.00032956 0.00032956 0.00032956 0.000329536 0.000342834 0.000352515 0.000348749 0.000348749 0.0003408684
1560: 1570: 1580: 1590: 1600: 1610: 1620: 1630: 1640: 1650: 1660: 1670: 1700: 1710: 1720: 1740: 1750: 1770: 1770: 1780: 1790: 1800: 1820: 1830: 1830:	progress progress	metric:	0.000280678 0.000287273 0.000292288 0.000299556 0.00030244 0.000306148 0.000310299 0.000314674 0.000319052 0.000329536 0.000329536 0.000329536 0.000348749 0.000348749 0.000349749 0.000349749 0.000339058 0.000339058 0.000339058 0.000339058 0.000339058 0.000339058 0.000339058 0.000339058 0.000339058 0.000339058 0.000339111 0.000332111 0.000325983 0.000325983 0.000321473
1560: 1570: 1580: 1590: 1600: 1610: 1620: 1630: 1640: 1670: 1670: 1700: 1710: 1720: 1730: 1740: 1750: 1760: 1770: 1780: 1790: 1800: 1810: 1820: 1830:	progress progress	metric:	0.000280678 0.000287273 0.000292288 0.000299556 0.00030244 0.000310299 0.000314674 0.000319052 0.00032956 0.00032956 0.00032956 0.000329536 0.000342834 0.000352515 0.000348749 0.000348749 0.0003408684
1560: 1570: 1580: 1590: 1600: 1610: 1620: 1630: 1640: 1650: 1660: 1670: 1700: 1710: 1720: 1740: 1750: 1770: 1770: 1780: 1790: 1800: 1820: 1830: 1830:	progress progress	metric:	0.000280678 0.000287273 0.000292288 0.000299556 0.00030244 0.000306148 0.000310299 0.000314674 0.000319052 0.000329536 0.000329536 0.000329536 0.000348749 0.000348749 0.000349749 0.000349749 0.000339058 0.000339058 0.000339058 0.000339058 0.000339058 0.000339058 0.000339058 0.000339058 0.000339058 0.000339058 0.000339111 0.000332111 0.000325983 0.000325983 0.000321473
1560: 1570: 1580: 1590: 1600: 1610: 1620: 1630: 1640: 1650: 1670: 1700: 1710: 1720: 1730: 1740: 1750: 1760: 1770: 1780: 1790: 1800: 1810: 1820: 1830: 1840: 1850: 1850: 1850:	progress progress	metric:	0.000280678 0.000287273 0.000292288 0.000292556 0.00030244 0.000310299 0.000314674 0.000319052 0.000329536 0.000329536 0.000329536 0.000329536 0.000342834 0.000352515 0.000348749 0.000340867 0.000340867 0.000339052 0.000339052 0.000337038 0.000335244 0.000333913 0.000335244 0.0003329111 0.0003329111 0.000325983 0.000325983 0.00031473 0.000316999 0.000315054
1560: 1570: 1580: 1590: 1600: 1610: 1620: 1630: 1640: 1670: 1670: 1700: 1710: 1720: 1730: 1740: 1750: 1760: 1790: 1800: 1800: 1810: 1820: 1830: 1840: 1850: 1860:	progress progress	metric:	0.000280678 0.000287273 0.000292288 0.000292556 0.00030244 0.000310299 0.000314674 0.000319052 0.00032956 0.00032956 0.000329536 0.000342834 0.000351167 0.000345684 0.000348749 0.000340867 0.000340867 0.000339052 0.000339052 0.000337038 0.000339052 0.000339052 0.000339052 0.000339052 0.000339052 0.000339052 0.000325983 0.000321973 0.000316998 0.000316995 0.000316954 0.000316954 0.000316954 0.000316954 0.000312054
1560: 1570: 1580: 1590: 1600: 1610: 1630: 1640: 1650: 1670: 1680: 1700: 1710: 1720: 1730: 1740: 1750: 1760: 1770: 1800: 1810: 1820: 1820: 1830: 1840: 1850: 1860: 1870: 18	progress progress	metric:	0.000280678 0.000287273 0.000292288 0.000299556 0.00030244 0.000310249 0.000310299 0.000314674 0.000319052 0.000329536 0.000329536 0.000329536 0.000345713 0.000345749 0.00034084749 0.00034084749 0.00034084749 0.00034084749 0.000339052 0.000339058 0.000339058 0.000339058 0.000339058 0.000332117 0.000329983 0.000321473 0.0003120576 0.0003905176 0.000294684
1560: 1570: 1580: 1590: 1600: 1610: 1620: 1630: 1640: 1650: 1690: 1700: 1770: 1730: 1740: 1750: 1760: 1770: 1780: 1780: 1810: 1830: 1830: 1840: 1850: 1870: 1850: 1870: 18	progress	metric:	0.000280678 0.000287273 0.000292288 0.000299556 0.00030244 0.000306148 0.000310299 0.000314674 0.000319052 0.000329536 0.000329536 0.0003551167 0.000355515 0.000348749 0.000348749 0.000340867 0.000339058 0.000339058 0.000339058 0.000339058 0.000339058 0.000339058 0.000339058 0.000339058 0.000339058 0.000325983 0.000321473 0.000312054 0.000312054 0.000312054 0.0003176 0.000394684 0.000294684 0.000294684
1560: 1570: 1580: 1590: 1600: 1610: 1620: 1630: 1640: 1650: 1670: 1770: 1770: 1730: 1740: 1770: 1780: 1790: 1880: 1810: 1820: 1840: 1850: 1840: 1850: 1850: 1860: 1870: 1890: 1890: 1890:	progress	metric:	0.000280678 0.000287273 0.000292288 0.000292556 0.00030244 0.000310299 0.000314674 0.000319052 0.000323906 0.000329536 0.000329536 0.000329536 0.000342834 0.000351167 0.000348749 0.000348749 0.000340867 0.000339052 0.000339052 0.000337038 0.000339052 0.000339052 0.000339052 0.000339052 0.000339052 0.000339052 0.000339052 0.000339052 0.000339052 0.000339052 0.000339052 0.00032111 0.000325983 0.000321473 0.000316999 0.000312054 0.0003294684 0.000284688 0.000284688
1560: 1570: 1580: 1590: 1600: 1610: 1620: 1630: 1640: 1670: 1690: 1700: 1710: 1720: 1730: 1740: 1750: 1760: 1770: 1780: 180: 1810: 1820: 1830: 1840: 1850: 1850: 1850: 1870: 1890: 1890: 1890: 1990: 1910:	progress	metric:	0.000280678 0.000287273 0.000292288 0.000292556 0.00030244 0.000310299 0.000314674 0.000319052 0.000329536 0.000335913 0.000342834 0.000351167 0.000352515 0.000348749 0.000340867 0.0003340867 0.00033345684 0.00033345684 0.00033345684 0.00033345684 0.000333458 0.000332111 0.000333458 0.000332173 0.00031699 0.000312056 0.000312054 0.000312054 0.000312054 0.000312054 0.000312056
1560: 1570: 1580: 1590: 1600: 1610: 1620: 1630: 1640: 1670: 1670: 1700: 1710: 1720: 1730: 1740: 1750: 1760: 1770: 1780: 1810: 1820: 1830: 1840: 1850: 1860: 1870: 1810: 1820: 1820: 1830: 1840: 1850: 1860: 1870: 18	progress	metric:	0.000280678 0.000287273 0.000292288 0.000292586 0.000299556 0.00030244 0.000310299 0.000314674 0.000319052 0.000329536 0.000329536 0.000335913 0.000348749 0.000340867 0.000340867 0.000339052 0.000339052 0.000339052 0.000339052 0.000339052 0.000339052 0.000339052 0.000339052 0.000339052 0.000339052 0.000339052 0.000310598 0.000325983 0.000321473 0.000316994 0.000319954 0.000319954 0.000294684 0.000284482 0.000274905 0.000265684
1560: 1570: 1580: 1590: 1600: 1610: 1620: 1630: 1640: 1670: 1690: 1700: 1710: 1720: 1730: 1740: 1750: 1760: 1770: 1780: 180: 1810: 1820: 1830: 1840: 1850: 1850: 1850: 1870: 1890: 1890: 1890: 1990: 1910:	progress	metric:	0.000280678 0.000287273 0.000292288 0.000292556 0.00030244 0.000310299 0.000314674 0.000319052 0.000329536 0.000335913 0.000342834 0.000351167 0.000352515 0.000348749 0.000340867 0.0003340867 0.00033345684 0.00033345684 0.00033345684 0.00033345684 0.000333458 0.000332111 0.000333458 0.000332173 0.00031699 0.000312056 0.000312054 0.000312054 0.000312054 0.000312054 0.000312056

```
0.000239613
1940: progress metric:
1950: progress metric:
                         0.000230677
                        0.00022218
1960: progress metric:
1970: progress metric:
                         0.000214089
1980: progress metric:
                         0.00020621
1990: progress metric:
                         0.000196915
2000: progress metric:
                         0.000187712
2010: progress metric:
                         0.000179199
2020: progress metric:
                         0.00017137
                         0.000164158
2030: progress metric:
2040: progress metric:
                         0.000157751
2050: progress metric:
                         0.000152485
2060: progress metric:
                         0.000147217
2070: progress metric:
                         0.000142083
2080: progress metric:
                         0.000137148
2090: progress metric:
                         0.000132379
2100: progress metric:
                         0.000127922
2110: progress metric:
                         0.000123617
2120: progress metric:
                         0.000119548
2130: progress metric:
                         0.000115684
2140: progress metric:
                         0.000111997
2150: progress metric: 2160: progress metric:
                         0.000108389
                         0.000104838
2170: progress metric:
Solution converged after 2175 iterations.
Elapsed wall clock time: 1.088 sec.
XML file test passed
assignment file test passed
PYTHONPATH=/Users/AshleyScripka/development/xdata/xdata3/pysmallk \
     sh tests/scripts/test pysmallk.sh ../xdata data | tee pysmallk test results.txt
**********
            pysmallk - command line
           Testing the smallk interface.
*****
WARNING: Could not achieve THREAD MULTIPLE support.
Smallk major version: 1
Smallk minor version: 6
Smallk patch level: 0
Smallk version string: 1.6.0
Loading matrix...
Initializing matrix W...
Initializing matrix H...
               algorithm: Nonnegative Least Squares with Block Principal Pivoting
      stopping criterion: Ratio of Projected Gradients
                 height: 12411
                  width: 7984
                     k: 8
                 miniter: 10
                 maxiter: 10000
                    tol: 1e-06
              matrixfile: ../xdata_data/reuters.mtx
maxthreads: 3
1:
      progress metric:
                         (min iter)
2:
      progress metric:
                         (min iter)
      progress metric:
                         (min_iter)
3:
      progress metric:
4:
                         (min iter)
      progress metric:
                         (min_iter)
5:
      progress metric:
                         (min iter)
6:
      progress metric:
                         (min_iter)
7:
      progress metric:
8:
                         (min iter)
      progress metric:
                         (min_iter)
9:
      progress metric:
10:
                         (min iter)
20:
      progress metric:
                         0.0136316
      progress metric:
30:
                         0.0137726
      progress metric:
                         0.0245057
40:
50:
      progress metric:
                         0.0116725
60:
      progress metric:
                         0.00360188
70:
      progress metric:
                         0.00217558
                         0.0014568
80:
      progress metric:
90:
      progress metric:
                         0.00105926
100:
                         0.000786066
     progress metric:
110:
     progress metric:
                         0.000591568
                         0.000455298
120:
      progress metric:
                         0.000367745
      progress metric:
130:
140:
     progress metric:
                         0.000301608
150:
     progress metric:
                         0.00025159
160:
     progress metric:
progress metric:
                         0.000214166
                         0.000179538
170:
180: progress metric: 190: progress metric:
                         0.000150486
                        0.000126573
```

```
0.000106425
200: progress metric:
210: progress metric: 220: progress metric:
                         8.94514e-05
7.49182e-05
230:
     progress metric:
                          6.2246e-05
240:
     progress metric:
                          5.20659e-05
250:
     progress metric:
                          4.38092e-05
     progress metric:
260:
                          3.68644e-05
270:
     progress metric:
                          3.10176e-05
280: progress metric:
                          1.12734e-05
290: progress metric: 4.10858e-06
300: progress metric: 1.49856e-06
Solution converged after 305 iterations.
Elapsed wall clock time: 9.725 sec.
Writing output files...
Initializing matrix W...
Initializing matrix H...
                parameters:
               algorithm: Nonnegative Least Squares with Block Principal Pivoting
      stopping criterion: Ratio of Projected Gradients
                  height: 12411
                   width: 7984
                      k: 8
                 miniter: 1
                 maxiter: 5000
                     tol: 0.005
               matrixfile: ../xdata data/reuters.mtx
               maxthreads: 8
                          (min iter)
1:
      progress metric:
      progress metric:
                         0.35826
2:
      progress metric:
3:
                          0.172127
4:
      progress metric:
                          0.106297
      progress metric:
                          0.0696424
5:
      progress metric:
                          0.0538889
6:
      progress metric:
                          0.0559478
7:
      progress metric:
                          0.0686117
8:
      progress metric:
                          0.0788641
9:
10:
      progress metric:
                          0.0711522
      progress metric:
                          0.00568349
20:
Solution converged after 22 iterations.
Elapsed wall clock time: 0.965 sec.
Writing output files...
loading dictionary...
creating random W initializers...
creating random H initializers...
              parameters:
                  height: 12411
                   width: 7984
               matrixfile: ../xdata data/reuters.mtx
                 dictfile: ../xdata_data/reuters_dictionary.txt
                     tol: 0.0001
                 miniter: 1
                 maxiter: 5000
                maxterms: 5
               maxthreads: 8
[1] [2] [3] [4]
Elapsed wall clock time: 533 ms. 9/9 factorizations converged.
Writing output files ...
W matrix test passed
H matrix test passed
              pysmallk - in memory
           Testing the smallk interface.
***********
WARNING: Could not achieve THREAD MULTIPLE support.
pysmallk/tests/smallkapi_inmem.py:59: FutureWarning: comparison to `None` will result in an elementwise object
comparison in the future.
 height=matrix.shape[0], width=matrix.shape[1], nz=len(data))
Loading sparse matrix...
Initializing matrix W...
Initializing matrix H...
```

parameters:

```
algorithm: Nonnegative Least Squares with Block Principal Pivoting
      stopping criterion: Ratio of Projected Gradients
                 height: 12411
                  width: 7984
                     k: 8
                 miniter: 1
                maxiter: 5000
                    tol: 0.005
              matrixfile:
              maxthreads: 8
1:
      progress metric:
     progress metric: 0.35826
2:
     progress metric: 0.172127
progress metric: 0.106297
3:
4:
     progress metric:
progress metric:
                         0.0696424
5:
                         0.0538889
6:
      progress metric:
                         0.0559478
7:
8:
     progress metric:
                         0.0686117
9: progress metric:
10: progress metric:
                         0.0788641
                        0.0711522
20:
     progress metric:
Solution converged after 22 iterations.
Elapsed wall clock time: 0.939 sec.
Writing output files...
W matrix test passed
H matrix test passed
          pysmallk - command line *
            Testing the preprocessor.
************
WARNING: Could not achieve THREAD MULTIPLE support.
Default output directory: current directory
Starting iterations...
      [1] height: 39771, width: 11237, nonzeros: 877453
Iterations finished.
     New height: 39727
      New width: 11237
      New nonzero count: 877374
preprocessor matrix test passed
preprocessor dictionary test passed
preprocessor documents test passed
            pysmallk - in memory
           Testing the preprocessor.
***********
WARNING: Could not achieve THREAD MULTIPLE support.
pysmallk/tests/preprocessor_inmem.py:83: FutureWarning: comparison to `None` will result in an elementwise
object comparison in the future.
 p.load inputmatrix(height=height, width=width, nz=nz, buffer=data, row indices=row indices,
col offsets=col offsets)
about to call python load_sparse
Loading sparse matrix...
Starting iterations...
      [1] height: 39771, width: 11237, nonzeros: 877453
Iterations finished.
     New height: 39727
New width: 11237
      New nonzero count: 877374
preprocessor matrix test passed
preprocessor dictionary test passed
preprocessor documents test passed
             pysmallk - command line *
                Testing hierclust.
***********
WARNING: Could not achieve THREAD MULTIPLE support.
   progress metric: (min_iter)
1:
      progress metric:
progress metric:
2:
                        (min_iter)
(min_iter)
3:
     progress metric: (min_iter)
progress metric: (min_iter)
4:
5:
                        0.0374741
     progress metric:
progress metric:
6:
7:
     progress metric: 0.0169805
progress metric: 0.0113837
8:
9:
10: progress metric: 20: progress metric:
                         0.00761077
```

0.000130604

progress metric:

```
Solution converged after 21 iterations.
1:
      progress metric:
                           (min iter)
2:
      progress metric:
                          (min iter)
3:
      progress metric:
                          (min iter)
4:
      progress metric:
                           (min iter)
5:
      progress metric:
                           (min iter)
      progress metric:
                           0.0371935
6:
      progress metric:
7:
                           0.0431956
      progress metric:
                           0.056867
      progress metric:
                           0.0745391
      progress metric:
                           0.0890112
      progress metric:
20:
                          0.092225
                          0.00649718
30:
      progress metric:
                          0.00224739
40:
      progress metric:
50:
      progress metric:
                          0.000846835
60:
      progress metric:
                          0.000303034
70:
      progress metric:
                         0.000107818
Solution converged after 71 iterations.
      progress metric:
                          (min_iter)
                          (min iter)
2:
      progress metric:
3:
      progress metric:
                           (min iter)
      progress metric:
                           (min_iter)
4:
5:
      progress metric:
                           (min iter)
6:
      progress metric:
                           0.0278454
7:
      progress metric:
                           0.0153121
8:
      progress metric:
                          0.0084199
      progress metric:
                          0.00463192
10:
      progress metric:
                          0.0025471
Solution converged after 16 iterations.
[1] 1: progress metric:
                           (min iter)
     progress metric:
                          (min_iter)
2:
3:
      progress metric:
                           (min iter)
      progress metric:
                           (min iter)
4:
                           (min_iter)
0.011482
      progress metric:
5:
      progress metric:
6:
      progress metric:
                           0.0088452
7:
8:
      progress metric:
                           0.00709218
      progress metric:
                           0.00576048
9:
10:
      progress metric:
                           0.00474146
20:
      progress metric:
                           0.00145962
30:
      progress metric:
                           0.00060763
40:
      progress metric:
                          0.000297382
      progress metric:
                          0.000148919
50:
Solution converged after 57 iterations.
1:
      progress metric:
                           (min iter)
                          (min_iter)
(min_iter)
2:
      progress metric:
3:
      progress metric:
      progress metric:
                           (min_iter)
4:
      progress metric:
                           (min iter)
5:
      progress metric:
                           0.0476236
6:
7:
      progress metric:
                           0.034979
      progress metric:
                           0.0255046
8:
9:
      progress metric:
                           0.0179983
      progress metric:
                          0.0131529
10:
20:
      progress metric:
                           0.00233685
30:
      progress metric:
                          0.00061225
      progress metric:
                          0.000172714
40:
Solution converged after 45 iterations.
[2] 1: progress metric:
                           (min iter)
      progress metric:
                           (min_iter)
2:
3:
      progress metric:
                           (min iter)
4:
      progress metric:
                           (min_iter)
      progress metric:
5:
                           (min iter)
      progress metric:
                           0.0348016
6:
      progress metric:
                           0.0168893
7:
                          0.0087407
      progress metric:
8:
      progress metric:
                          0.00469118
9:
                          0.00255868
10:
      progress metric:
Solution converged after 16 iterations.
      progress metric:
                           (min_iter)
1:
      progress metric:
2:
                           (min iter)
                           (min_iter)
3:
      progress metric:
      progress metric:
                           (min iter)
4:
      progress metric:
                           (min_iter)
0.0732844
5:
      progress metric:
6:
```

progress metric:

progress metric:

7: 8: 0.077964

```
progress metric: 0.0999774
     progress metric: 0.0994555
progress metric: 0.00114661
10:
Solution converged after 25 iterations.
[3] 1: progress metric:
                           (min_iter)
                          (min_iter)
(min_iter)
2:
      progress metric:
      progress metric:
3:
4:
      progress metric:
                            (min iter)
                            (min iter)
5:
      progress metric:
6:
      progress metric:
                           0.0710298
      progress metric:
                           0.038312
      progress metric:
progress metric:
8:
                           0.021048
                           0.0117472
10: progress metric: 0.00662412
Solution converged after 18 iterations.
1:
      progress metric:
                           (min iter)
2:
      progress metric:
                           (min_iter)
3:
      progress metric:
                           (min iter)
                           (min_iter)
4:
      progress metric:
5:
      progress metric:
                            (min iter)
      progress metric:
                           0.0801544
6:
      progress metric:
                           0.072948
7:
8:
      progress metric:
                           0.0736511
9:
      progress metric:
                           0.0752686
10:
      progress metric:
                           0.0718868
20:
      progress metric:
                           0.0192989
      progress metric:
                           0.0121039
40:
50:
      progress metric:
                           0.00743925
      progress metric:
                           0.00544292
60:
      progress metric:
progress metric:
                           0.00557543
70:
                           0.00725721
      progress metric:
progress metric:
80:
                           0.0123311
90:
                           0.0359475
100: progress metric:
110: progress metric:
                           0.104473
                           0.0239986
      progress metric:
progress metric:
120:
                           0.01361
130:
                           0.00776367
140: progress metric: 0.00349198
150: progress metric: 0.000247399
Solution converged after 153 iterations.
Writing output files...
hierclust cluster file test passed
hierclust assignment file test passed
              pysmallk - in memory
               Testing hierclust.
*************
WARNING: Could not achieve THREAD MULTIPLE support.
pysmallk/tests/hierclust inmem.py:50: FutureWarning: comparison to `None` will result in an elementwise object
comparison in the future.
 height=matrix.shape[0], width=matrix.shape[1], nz=len(data))
about to call python load sparse
Loading sparse matrix...
    progress metric:
                            (min_iter)
1:
      progress metric: (min_iter)
progress metric: (min_iter)
2:
3:
      progress metric:
progress metric:
                           (min_iter)
4:
                            (min iter)
5:
      progress metric:
progress metric:
                           0.0374741
6:
                           0.0252389
7:
      progress metric:
progress metric:
                           0.0169805
8:
9:
                           0.0113837
10:
      progress metric:
                           0.00761077
20:
      progress metric:
                           0.000130604
Solution converged after 21 iterations.
                           (min iter)
1:
       progress metric:
       progress metric:
2:
                           (min_iter)
3:
      progress metric:
                            (min iter)
4:
      progress metric:
                            (min_iter)
      progress metric:
                            (min iter)
5:
      progress metric:
progress metric:
                           0.0371935
6:
                           0.0431956
7:
      progress metric:
progress metric:
                           0.056867
8:
                           0.0745391
9:
      progress metric:
progress metric:
                           0.0890112
10:
                           0.092225
20:
      progress metric:
30:
40:
                           0 00649718
                          0.00224739
      progress metric:
```

```
50:
                          0.000846835
      progress metric:
                          0.000303034
60:
      progress metric:
                         0.000107818
70:
      progress metric:
Solution converged after 71 iterations.
      progress metric:
                           (min_iter)
                           (min iter)
2:
      progress metric:
3:
      progress metric:
                           (min iter)
4:
      progress metric:
                           (min iter)
                           (min iter)
5:
      progress metric:
                           0.0278454
6:
      progress metric:
      progress metric:
                           0.0153121
      progress metric:
8:
                          0.0084199
      progress metric:
                          0.00463192
10:
      progress metric:
                          0.0025471
Solution converged after 16 iterations.
[1] 1: progress metric:
                           (min iter)
      progress metric:
                          (min_iter)
2:
3:
      progress metric:
                           (min iter)
4:
      progress metric:
                           (min iter)
5:
      progress metric:
                           (min iter)
                           0.011482
      progress metric:
6:
      progress metric:
                           0.0088452
7:
8:
      progress metric:
                           0.00709218
9:
      progress metric:
                           0.00576048
10:
      progress metric:
                           0.00474146
20:
      progress metric:
                           0.00145962
30:
      progress metric:
                           0.00060763
                          0.000297382
40:
      progress metric:
      progress metric:
                          0.000148919
50:
Solution converged after 57 iterations.
      progress metric:
                           (min_iter)
2:
      progress metric:
                           (min iter)
3:
      progress metric:
                           (min iter)
                           (min_iter)
      progress metric:
4:
      progress metric:
                           (min iter)
5:
      progress metric:
                           0.0476236
6:
7:
      progress metric:
                           0.034979
      progress metric:
                           0.0255046
8:
9:
      progress metric:
                           0.0179983
10:
      progress metric:
                           0.0131529
20:
      progress metric:
                           0.00233685
30:
      progress metric:
                          0.00061225
      progress metric:
                          0.000172714
40:
Solution converged after 45 iterations.
[2] 1: progress metric:
                           (min iter)
                           (min_iter)
(min_iter)
      progress metric:
2:
3:
      progress metric:
      progress metric:
                           (min_iter)
4:
      progress metric:
                           (min iter)
5:
      progress metric:
                           0.0348016
6:
7:
      progress metric:
                           0.0168893
      progress metric:
                          0.0087407
8:
      progress metric:
                          0.00469118
     progress metric:
                          0.00255868
10:
Solution converged after 16 iterations.
1:
      progress metric:
                           (min_iter)
      progress metric:
                           (min iter)
2:
      progress metric:
                           (min_iter)
3:
      progress metric:
4:
                           (min iter)
      progress metric:
                           (min_iter)
0.0732844
5:
6:
      progress metric:
7:
      progress metric:
                           0.077964
      progress metric:
                           0.0906559
8:
                           0.0999774
      progress metric:
9:
      progress metric:
                           0.0994555
10:
                          0.00114661
      progress metric:
20:
Solution converged after 25 iterations.
[3] 1: progress metric:
                           (min iter)
      progress metric:
                           (min_iter)
2:
                           (min_iter)
3:
      progress metric:
      progress metric:
                           (min iter)
4:
      progress metric:
                           (min_iter)
0.0710298
5:
      progress metric:
6:
      progress metric:
                           0.038312
7:
      progress metric:
8:
                          0.021048
      progress metric:
9.
                          0 0117472
```

10:

progress metric:

```
Solution converged after 18 iterations.
                         (min_iter)
(min_iter)
      progress metric:
      progress metric:
2:
     progress metric:
progress metric:
                         (min_iter)
(min_iter)
3:
4:
      progress metric:
                          (min iter)
6:
      progress metric:
                          0.0801544
7:
      progress metric:
      progress metric:
                          0.0736511
      progress metric:
     progress metric:
                          0.0718868
20:
      progress metric:
                          0.0192989
      progress metric:
                          0.0121039
40:
50:
      progress metric:
                          0.00743925
      progress metric:
                          0.00544292
60:
      progress metric:
                          0.00557543
70:
      progress metric:
                          0.00725721
80:
      progress metric:
                          0.0123311
90:
      progress metric:
                          0.0359475
100:
     progress metric:
                          0.104473
110: progress metric:
                         0.0239986
120:
     progress metric:
                          0.01361
130: progress metric:
                         0.00776367
140: progress metric: 0.00349198
150: progress metric: 0.000247399
Solution converged after 153 iterations.
assignment file test passed
*************
            pysmallk - command line
              Testing flatclust.
***********
WARNING: Could not achieve THREAD MULTIPLE support.
   progress metric: (min_iter)
progress metric: 0.635556
1:
     progress metric: 0.490817
progress metric: 0.479135
3:
4:
   progress metric:
progress metric:
                          0.474986
5:
6:
                          0.44968
     progress metric:
progress metric:
                          0.422542
7:
                          0.407662
8:
      progress metric:
                          0.395145
9:
10:
     progress metric:
                          0.379238
20:
      progress metric:
                          0.272868
      progress metric:
                          0.168386
40:
      progress metric:
                          0.109147
50:
      progress metric:
                          0.0767327
      progress metric:
60:
                          0.0488545
70:
      progress metric:
                          0.036226
80:
      progress metric:
                          0.0307648
90:
      progress metric:
                          0.0266116
100:
      progress metric:
                          0.0226963
110:
     progress metric:
                          0.0188616
120:
      progress metric:
                          0.0158307
130:
     progress metric:
                          0.0137605
     progress metric:
progress metric:
140:
                          0.0127888
150:
                          0.0123962
160:
      progress metric:
                          0.0124734
170:
     progress metric:
                          0.0123563
     progress metric:
progress metric:
180:
                          0.0122163
                          0.0120643
190:
200:
      progress metric:
                          0.0117647
210:
     progress metric:
                          0.0114894
220:
      progress metric:
                          0.0110467
230:
                          0.0107816
     progress metric:
240:
      progress metric:
                          0.0105239
250:
      progress metric:
                          0.0103824
260:
      progress metric:
                          0.0100915
270:
      progress metric:
                          0.00965073
                          0.00938526
280:
      progress metric:
290:
      progress metric:
                          0.00914129
300:
                          0.00896701
      progress metric:
310:
      progress metric:
                          0.00886729
                          0.00841059
320:
      progress metric:
330:
      progress metric:
                          0.007793
340:
      progress metric:
progress metric:
                          0.00740095
                          0.00708869
350:
360:
      progress metric:
                          0.00683069
370:
                          0.00672093
      progress metric:
380: progress metric: 390: progress metric:
                          0.00687906
                          0.00703777
400: progress metric:
410: progress metric:
                          0.00721928
```

400			0 00710000
420:	progress	metric:	0.00718332
430:	progress	metric:	0.00722893
440:	progress	metric:	0.00726766
450:	progress	metric:	0.00739665
460:		metric:	0.00769819
	progress		
470:	progress	metric:	0.00814673
480:	progress	metric:	0.008566
490:	progress	metric:	0.00877955
500:	progress	metric:	0.00884221
510:	progress	metric:	0.0088057
520:	progress	metric:	0.00852345
530:	progress	metric:	0.00797952
540:	progress	metric:	0.00749354
550:	progress	metric:	0.00689316
560:	progress	metric:	0.00623287
570:	progress	metric:	0.00576619
580:	progress	metric:	0.00541125
590:			
	progress	metric:	0.00501715
600:	progress	metric:	0.00466547
610:	progress	metric:	0.00432811
620:	progress	metric:	0.00412669
630:			0.00383406
	progress	metric:	
640:	progress	metric:	0.00352802
650:	progress	metric:	0.00331556
660:	progress	metric:	0.00315735
		metric:	0.00313733
670:	progress		
680:	progress	metric:	0.00296627
690:	progress	metric:	0.00289013
700:	progress	metric:	0.00279647
710:		metric:	0.00271036
	progress		
720:	progress	metric:	0.00261087
730:	progress	metric:	0.0025158
740:	progress	metric:	0.00245123
750:			0.00237435
	progress	metric:	
760:	progress	metric:	0.00231126
770:	progress	metric:	0.00228199
780:	progress	metric:	0.00227623
790:			0.00228185
	progress	metric:	
800:	progress	metric:	0.00227993
810:	progress	metric:	0.00228216
820:	progress	metric:	0.00228018
830:		metric:	0.00229096
	progress		
840:	progress	metric:	0.00232403
850:	progress	metric:	0.00234957
860:	progress	metric:	0.00227868
870:		metric:	0.00210786
	progress		
880:	progress	metric:	0.00195462
890:	progress	metric:	0.00183587
900:	progress	metric:	0.00173358
910:	progress	metric:	0.0016405
920:	progress	metric:	0.00156422
930:	progress	metric:	0.00150835
940:	progress	metric:	0.00146594
950:	progress	metric:	0.00143261
960:	progress	metric:	0.00137378
970:	progress	metric:	0.00131989
980:	progress	metric:	0.00126626
990:	progress	metric:	0.0012164
1000:		metric:	0.00117061
	progress		
1010:	progress	metric:	0.00112539
1020:	progress	metric:	0.00108626
1030:	progress	metric:	0.00105192
1040:	progress	metric:	0.00102131
			0.000992069
1050:	progress	metric:	
1060:	progress	metric:	0.000965259
1070:	progress	metric:	0.000938949
1080:	progress	metric:	0.000911962
		metric:	0.000311302
1090:	progress		
1100:	progress	metric:	0.000854904
1110:	progress	metric:	0.000820121
1120:	progress	metric:	0.000785245
1130:		metric:	0.000752513
	progress		
1140:	progress	metric:	0.000723279
1150:	progress	metric:	0.000697698
1160:	progress	metric:	0.000680904
1170:		metric:	0.000652152
	progress		
1180:	progress	metric:	0.000628268
1190:	progress	metric:	0.000612413
1200:	progress	metric:	0.000596834
1210:	progress	metric:	0.000580674
1220:	progress	metric:	0.000556549
1230:	progress	metric:	0.000535666
1240:	progress	metric:	0.00051492
1250:	progress	metric:	0.000496234
1260:		metric:	0.000490234
	progress		
1270:	progress	metric:	0.000461294
1280:	progress	metric:	0.000440802
1290:	progress	metric:	0.000419049
1300:	progress	metric:	0.000398007
± J U U ;	PIOGIESS		0.000000000/

1310:	progress	metric:	0.000376203
1320:	progress	metric:	0.000355811
1330:	progress	metric:	0.00033729
1340:	progress	metric:	0.000318932
1350:	progress	metric:	0.000302528
1360:	progress	metric:	0.000287961
1370:	progress	metric:	0.00027486
1380:	progress	metric:	0.00026403
1390:	progress	metric:	0.000255504
1400:	progress	metric:	0.000248646
1410:		metric:	0.000242996
	progress		
1420:	progress	metric:	0.000239243
1430:	progress	metric:	0.000236852
1440:	progress	metric:	0.000235313
1450:	progress	metric:	0.000234465
1460:	progress	metric:	0.000234154
1470:	progress	metric:	0.000234253
1480:	progress	metric:	0.00023487
1490:	progress	metric:	0.000237223
1500:			0.000240043
	progress	metric:	
1510:	progress	metric:	0.000243896
1520:	progress	metric:	0.00024867
1530:	progress	metric:	0.000253981
1540:	progress	metric:	0.000260239
1550:	progress	metric:	0.000266795
1560:	progress	metric:	0.000273529
1570:			
	progress	metric:	0.000280678
1580:	progress	metric:	0.000287273
1590:	progress	metric:	0.000292288
1600:	progress	metric:	0.000296475
1610:	progress	metric:	0.000299556
1620:	progress	metric:	0.00030244
1630:	progress	metric:	0.000306148
1640:	progress	metric:	0.000310299
1650:	progress	metric:	0.000314674
			0.000319052
1660:	progress	metric:	
1670:	progress	metric:	0.000323906
1680:	progress	metric:	0.000329536
1690:	progress	metric:	0.000335913
1700:	progress	metric:	0.000342834
1710:	progress	metric:	0.000351167
1720:	progress	metric:	0.000352515
1730:	progress	metric:	0.000348749
1740:	progress	metric:	0.000345684
1750:	progress	metric:	0.000343139
1760:	progress	metric:	0.000340867
1770:	progress	metric:	0.000339052
1780:	progress	metric:	0.000337038
1790:	progress	metric:	0.000335244
1800:		metric:	0.000333452
	progress		
1810:	progress	metric:	0.000332111
1820:	progress	metric:	0.000330198
1830:	progress	metric:	0.000325983
1840:	progress	metric:	0.000321473
1850:	progress	metric:	0.000316999
1860:	progress	metric:	0.000312054
1870:		metric:	0.000305176
	progress		
1880:	progress	metric:	0.000294684
1890:	progress	metric:	0.000284482
1900:	progress	metric:	0.000274905
1910:	progress	metric:	0.000265684
1920:		metric:	0.000256761
	progress		
1930:	progress	metric:	0.000248203
1940:	nrograce	metric:	0.000239613
	progress		
1950:	progress	metric:	0.000230677
1960:	progress	metric:	0.00022218
1970:	progress	metric:	0.000214089
1980:	progress	metric:	0.00020621
1990:	progress	metric:	0.000196915
2000:	progress	metric:	0.000187712
2010:		metric:	0.000179199
	progress		
2020:	progress	metric:	0.00017137
2030:	progress	metric:	0.000164158
2040:	progress	metric:	0.000157751
2050:	progress	metric:	0.000152485
2060:	progress	metric:	0.000147217
2070:	progress	metric:	0.000142083
			0.000137148
2080:	progress	metric:	
2090:	progress	metric:	0.000132379
2100:	progress	metric:	0.000127922
2110:	progress	metric:	0.000123617
2120:	progress	metric:	0.000119548
2130:	progress	metric:	0.000115684
2140:	progress	metric:	0.000111997
2150:	progress	metric:	0.000108389
2160:	progress	metric:	0.000104838
	progress	metric:	0.000101387
2. 1 / 11 *			/
2170:	progress		

Solution converged after 2175 iterations.

Writing output files... XML file test passed assignment file test passed pysmallk - in memory Testing flatclust. WARNING: Could not achieve THREAD MULTIPLE support. progress metric: (min_iter) progress metric: 0.635556 progress metric: 0.490817 progress metric: 0.479135 3: 4: 5: progress metric: 0.474986 progress metric: 0.44968 6: progress metric: 0.422542 7: 8: progress metric: 0.407662 9: progress metric: 0.395145 progress metric: 0.379238 10: 20: 30: progress metric: 0.272868 progress metric: 0.168386 40: progress metric: 50: progress metric: 0.0767327 60: progress metric: 0.0488545 70: progress metric: 0.036226 80: progress metric: 0.0307648 90: progress metric: 0.0266116 100: progress metric: 0.0226963 0.0188616 110: progress metric: 120: progress metric: 0.0158307 progress metric: 0.0137605 140: progress metric: 0.0127888 150: progress metric: 0.0123962 160: progress metric: 0.0124734 170: progress metric: 0.0123563 180: progress metric: 0.0122163 190: progress metric: 0.0120643 200: progress metric: 0.0117647 210: progress metric: 0.0114894 220: progress metric: 0.0110467 230: progress metric: 0.0107816 240: progress metric: 0.0105239 250: progress metric: 0.0103824 260: progress metric: 0.0100915 270: progress metric: 0.00965073 280: progress metric: 0.00938526 290: progress metric: 0.00914129 300: progress metric: 0.00896701 310: progress metric: 0.00886729 320: progress metric: 0.00841059 330: progress metric: 0.007793 340: progress metric: 0.00740095 350: progress metric: 0.00708869 360: progress metric: 0.00683069 370: progress metric: 0.00672093 380: progress metric: 0.00687906 390: progress metric: 0.00703777 400: progress metric: 0.00721928 progress metric: 410. 0.00729384 420: progress metric: 0.00718332 430: progress metric: 0.00722893 440: progress metric: 0.00726766 progress metric: 450: 0.00739665 460: progress metric: 0.00769819 0.00814673 470: progress metric: 480: 0.008566 progress metric: 0.00877955 490: progress metric: 500: progress metric: 0.00884221 510: progress metric: 0.0088057 520: progress metric: 0.00852345 530: progress metric: 0.00797952 0.00749354 540: progress metric: progress metric: 0.00689316 550: 560: 0.00623287 progress metric: 570: progress metric: 0.00576619 580: 0.00541125 progress metric: 590: progress metric: 0.00501715 600: 0.00466547 progress metric: 610: progress metric: 0.00432811 620: progress metric: 0.00412669 0.00383406 630: progress metric: 640: 0.00352802 progress metric: 0.00331556 650: progress metric: progress metric: progress metric: 660: 0.00315735 670: 0.00304253 680: progress metric: 690: progress metric: 0.00296627

			0 00070647
700:	progress	metric:	0.00279647
710:	progress	metric:	0.00271036
720:	progress	metric:	0.00261087
730:	progress	metric:	0.0025158
740:	progress	metric:	0.00245123
750:	progress	metric:	0.00237435
760:	progress	metric:	0.00231126
770:	progress	metric:	0.00228199
780:	progress	metric:	0.00227623
790:	progress	metric:	0.00228185
800:	progress	metric:	0.00227993
810:	progress	metric:	0.00228216
820:	progress	metric:	0.00228018
830:	progress	metric:	0.00229096
840:		metric:	0.00232403
850:	progress		0.00232403
		metric:	
860:	progress	metric:	0.00227868
870:	progress	metric:	0.00210786
880:	progress	metric:	0.00195462
890:	progress	metric:	0.00183587
900:	progress	metric:	0.00173358
910:	progress	metric:	0.0016405
920:	progress	metric:	0.00156422
930:	progress	metric:	0.00150835
940:	progress	metric:	0.00146594
950:	progress	metric:	0.00143261
960:	progress	metric:	0.00137378
970:	progress	metric:	0.00131989
980:	progress	metric:	0.00126626
990:	progress	metric:	0.0012164
1000:	progress	metric:	0.0012104
1010:		metric:	0.00117001
	progress		0.00112339
1020:	progress	metric:	
1030:	progress	metric:	0.00105192
1040:	progress	metric:	0.00102131
1050:	progress	metric:	0.000992069
1060:	progress	metric:	0.000965259
1070:	progress	metric:	0.000938949
1080:	progress	metric:	0.000911962
1090:	progress	metric:	0.000884505
1100:	progress	metric:	0.000854904
1110:	progress	metric:	0.000820121
1120:	progress	metric:	0.000785245
1130:	progress	metric:	0.000752513
1140:	progress	metric:	0.000723279
1150:	progress	metric:	0.000697698
1160:	progress	metric:	0.000680904
1170:	progress	metric:	0.000652152
1180:		metric:	0.000628268
1190:	progress	metric:	0.000612413
	progress		
1200:	progress	metric:	0.000596834
1210:	progress	metric:	0.000580674
1220:	progress	metric:	0.000556549
1230:	progress	metric:	0.000535666
1240:	progress	metric:	0.00051492
1250:	progress	metric:	0.000496234
1260:	progress	metric:	0.000481147
1270:	progress	metric:	0.000461294
1280:	progress	metric:	0.000440802
1290:	progress	metric:	
1300:	progress		0.000419049
1210.	1 2	metric:	0.000398007
1310:	progress	metric:	0.000398007 0.000376203
1320:			0.000398007 0.000376203 0.000355811
	progress	metric:	0.000398007 0.000376203
1320:	progress progress	metric: metric:	0.000398007 0.000376203 0.000355811
1320: 1330:	progress progress progress	<pre>metric: metric: metric:</pre>	0.000398007 0.000376203 0.000355811 0.00033729
1320: 1330: 1340:	progress progress progress progress progress	<pre>metric: metric: metric: metric:</pre>	0.000398007 0.000376203 0.000355811 0.00033729 0.000318932
1320: 1330: 1340: 1350: 1360:	progress progress progress progress progress progress	metric: metric: metric: metric: metric: metric:	0.000398007 0.000376203 0.000355811 0.00033729 0.000318932 0.000302528 0.000287961
1320: 1330: 1340: 1350: 1360: 1370:	progress progress progress progress progress progress progress	metric: metric: metric: metric: metric: metric: metric: metric:	0.000398007 0.000376203 0.000355811 0.00033729 0.000318932 0.000302528 0.000287961 0.00027486
1320: 1330: 1340: 1350: 1360: 1370: 1380:	progress progress progress progress progress progress progress	metric: metric: metric: metric: metric: metric: metric: metric: metric:	0.000398007 0.000376203 0.000355811 0.00033729 0.000318932 0.000302528 0.000287961 0.00027486 0.00026403
1320: 1330: 1340: 1350: 1360: 1370: 1380: 1390:	progress progress progress progress progress progress progress progress	metric: metric: metric: metric: metric: metric: metric: metric: metric:	0.000398007 0.000376203 0.000355811 0.00033729 0.000318932 0.000302528 0.000287961 0.00027486 0.00026403 0.000255504
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1320: 1330: 1340: 1350: 1360: 1370: 1380: 1400: 1410: 1420: 1430:	progress progress progress progress progress progress progress progress progress progress progress	metric:	0.000398007 0.000376203 0.000355811 0.00033729 0.000318932 0.000302528 0.00027486 0.00026403 0.000248646 0.000242996 0.000242996 0.000239243 0.000239243
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1320: 1330: 1340: 1350: 1360: 1370: 1380: 1400: 1410: 1420: 1430: 1440: 1450:	progress progress progress progress progress progress progress progress progress progress progress progress progress	metric:	0.000398007 0.000376203 0.000357811 0.00033729 0.000318932 0.000302528 0.00027486 0.00026403 0.000255504 0.000248646 0.000242996 0.000239243 0.000235313 0.000235313
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1320: 1330: 1340: 1350: 1360: 1370: 1380: 1440: 1440: 1440: 1440: 1450: 1460: 1470:	progress progress progress progress progress progress progress progress progress progress progress progress progress progress	metric:	0.000398007 0.000376203 0.000355811 0.00033729 0.000318932 0.000287961 0.00027486 0.00026403 0.000255504 0.000242996 0.000234253 0.000234253 0.000234154 0.000234253
1320: 1330: 1340: 1350: 1360: 1370: 1380: 1440: 1440: 1440: 1450: 1450: 1460: 1470: 1480:	progress progress progress progress progress progress progress progress progress progress progress progress progress progress progress progress	metric:	0.000398007 0.000376203 0.000357810 0.00033729 0.000318932 0.000287961 0.00027486 0.000255504 0.000242996 0.000239243 0.000233243 0.000234253 0.000234253 0.000234253
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1320: 1330: 1340: 1350: 1360: 1370: 1380: 1490: 1410: 1420: 1430: 1440: 1450: 1460: 1470: 1480: 1490: 1500:	progress progress progress progress progress progress progress progress progress progress progress progress progress progress progress progress progress progress	metric:	0.000398007 0.000376203 0.000357811 0.00033729 0.000318932 0.000302528 0.00027486 0.00026403 0.000255504 0.000248646 0.00024996 0.000239243 0.000235313 0.000234465 0.00023425 0.00023425 0.00023425 0.00023425 0.00023425 0.00023425 0.00023425
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1320: 1330: 1340: 1350: 1360: 1370: 1380: 1400: 1410: 1420: 1440: 1450: 1460: 1470: 1480: 1490: 1500: 1510: 1520: 1530:	progress progress	metric:	0.000398007 0.000376203 0.000357819 0.000318932 0.000318932 0.000287961 0.00027486 0.000255504 0.000248646 0.000242996 0.000239243 0.000234253 0.000234253 0.000234253 0.000234253 0.000234253 0.000234253 0.000234253 0.000234253 0.000234253 0.000234253 0.00024867 0.00024867 0.000253981
1320: 1330: 1340: 1350: 1360: 1370: 1380: 1400: 1440: 1440: 1450: 1470: 1460: 1470: 1480: 1500: 1510: 1520: 1530: 1540:	progress progress	metric:	0.000398007 0.000376203 0.000357810 0.000318932 0.000318932 0.000287961 0.00027486 0.000255504 0.000248646 0.000239243 0.000239243 0.000234465 0.000234465 0.00023425 0.00023425 0.00023425 0.00023425 0.00023425 0.00023425 0.00023425 0.00023425 0.00023425 0.00023425 0.00023425 0.00023425 0.00023425 0.00023425 0.00023425 0.00023425
1320: 1330: 1340: 1350: 1360: 1370: 1380: 1390: 1440: 1440: 1440: 1450: 1450: 1450: 1550: 1550:	progress progress	metric:	0.000398007 0.000376203 0.000355811 0.00033729 0.000302528 0.000287961 0.00027486 0.000246403 0.0002455504 0.00024894 0.00024894 0.000239243 0.000234154 0.000234154 0.000234154 0.000234253 0.000234253 0.000234253 0.000234253 0.000234253 0.000234253 0.000240043 0.000240043 0.000243896 0.000243896 0.00024399 0.000260239 0.000260239 0.000260239
1320: 1330: 1340: 1350: 1360: 1370: 1380: 1390: 1440: 1440: 1440: 1450: 1450: 1550: 1530: 1540: 1550: 1550: 1550:	progress progress	metric:	0.000398007 0.000376203 0.000357810 0.00033729 0.000318932 0.000287961 0.00027486 0.00026403 0.000255504 0.000248646 0.000239243 0.000239243 0.000234253 0.000240043 0.000240043 0.000260795 0.000266795 0.000273529
1320: 1330: 1340: 1350: 1360: 1370: 1380: 1390: 1410: 1420: 1440: 1450: 1460: 1470: 1500: 1510: 1520: 1530: 1550: 1550: 1550: 1570:	progress progress	metric:	0.000398007 0.000376203 0.000357810 0.00033729 0.000318932 0.000287961 0.00027486 0.000255504 0.000248646 0.000242996 0.000239243 0.000234253 0.000234253 0.000234253 0.000234253 0.000234253 0.000234253 0.000234253 0.000234253 0.000234253 0.000234253 0.0002408467 0.000253981 0.000266795 0.000267529 0.000273529 0.000273529
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```
0.000292288
1590: progress metric:
1600: progress metric:
                           0.000296475
1610: progress metric:
                           0.000299556
                           0.00030244
1620: progress metric:
1630: progress metric:
                           0.000306148
                           0.000310299
1640: progress metric:
1650: progress metric:
                           0.000314674
                           0.000319052
1660: progress metric:
1670: progress metric:
                           0.000323906
1680: progress metric:
                           0.000329536
1690: progress metric:
                           0.000335913
1700: progress metric:
                           0.000342834
1710: progress metric:
                           0.000351167
1720: progress metric:
                           0.000352515
1730: progress metric:
                           0.000348749
                           0.000345684
1740: progress metric:
1750: progress metric:
                           0.000343139
1760: progress metric:
                           0.000340867
1770: progress metric:
                           0.000339052
1780: progress metric:
                           0.000337038
1790: progress metric:
                           0.000335244
                           0.000333452
1800: progress metric:
1810: progress metric:
                           0.000332111
1820: progress metric:
                           0.000330198
1830: progress metric:
                           0.000325983
1840: progress metric: 1850: progress metric:
                           0.000321473
                           0.000316999
1860: progress metric:
                           0.000312054
1870: progress metric:
                           0.000305176
1880: progress metric: 1890: progress metric:
                           0.000294684
                           0.000284482
                           0.000274905
1900: progress metric:
1910: progress metric:
                           0.000265684
1920: progress metric:
                           0.000256761
1930: progress metric:
                           0.000248203
1940: progress metric:
                           0.000239613
1950: progress metric:
                           0.000230677
1960: progress metric:
                           0.00022218
1970: progress metric:
                           0.000214089
1980: progress metric:
                           0.00020621
1990: progress metric:
                           0.000196915
2000: progress metric:
                           0.000187712
2010: progress metric:
                           0.000179199
2020: progress metric:
                           0.00017137
2030: progress metric:
                           0.000164158
2040: progress metric:
                           0.000157751
2050: progress metric:
                           0.000152485
2060: progress metric:
                           0.000147217
2070: progress metric:
                           0.000142083
2080: progress metric:
                           0.000137148
2090: progress metric:
                           0.000132379
2100: progress metric:
                           0.000127922
2110: progress metric:
                           0.000123617
2120: progress metric:
                           0.000119548
2130: progress metric:
                           0.000115684
2140: progress metric:
                           0.000111997
2150: progress metric:
                           0.000108389
2160: progress metric:
2170: progress metric:
                           0.000104838
                           0.000101387
```

Solution converged after 2175 iterations.

assignment file test passed
fuzzy assignment file test passed
***** SmallK: All tests passed. *****

VI. Pysmallk: SmallK Python Interface

Why Python? Although it's perfectly fine to run SmallK from the command line, Python provides a great deal more flexibility that augments the C++ code with other tasks that are much more easily accomplished with a very high level language. Python distributions can be easily extended with open source libraries from third party sources as well, two examples being numpy and scipy, well-known standards for scientific computing in the Python community. There are numerous packages available that extend these scientific libraries into the data analytics domain as well, such as scikit-learn.

For using scientific Python, we strongly recommend the Anaconda Python distribution provided by Continuum Analytics. Download and installation instructions for all platforms can be found here. Anaconda includes many if not most of the commonly used scientific and data analytics packages available and a very easy to use package manager and updating system. After installing Anaconda there will be available at the command line both a standard Python interpreter (type 'python') and an iPython interpreter (type 'ipython'). We recommend using the iPython interpreter. In addition to the command line interfaces to Python, Anaconda includes the Spyder visual development environment featuring a very well thought out interface that makes developing Python code almost "too easy". Spyder has many features found in the Matlab™ editor and a similar look and feel.

Anaconda also includes the <u>Cython</u> package, which is used by SmallK to integrate the Python and C++ code. Cython includes support for most of the C++ standard and supports the latest GNU C++ compilers. Most if not all the standard libraries are supported and the latest version (20.2) has support for the standard template library (STL) as well.

Pysmallk has five classes, each of which represents one of the Smallk tools: SmallkAPI (the simplistic Smallk API), Flatclust, Hierclust, Matrixgen, and Preprocessor. A particular instance of these classes can be imported as follows:

```
from pysmallk import smallkapi as sk from pysmallk import flatclust as f from pysmallk import hierclust as h from pysmallk import matrixgen as m from pysmallk import preprocessor as p
```

Each class's primary functions are documented below.

These tools can be chained together to combine functionalities. An example of this can be found in pysmallk/examples/pysmallk example.py.

VI.1. Preprocessor

```
def parser(self):
```

Creates a parser that takes the same inputs and has the same defaults as the binary preprocessor tool. Returns a dictionary containing the command line inputs or their default values. The fields in that dictionary are: indir, outdir, docs_per_term, terms_per_doc, maxiter, precision, boolean_mode.

Load the input matrix. Two combinations are available, which provide for loading via a file path or direct loading of a sparse matrix. For example:

```
File path: load inputmatrix(filepath='/path/to/file/')
```

```
Sparse matrix: load_inputmatrix(height=matrix_height, width=matrix_width, nz=non_zero_count,
        buffer=non zero elements, row indices=rows, col offsets=cols)
def load dictionary(self, filepath=None, dictionary=None):
        Load the dictionary, either by providing the path to the file, filepath, or by providing a list of the terms,
        dictionary.
def load documents(self, filepath=None, documents=None):
        Load the documents, either by providing the path to the file, filepath, or by providing a list of the
        documents, documents.
def get reduced documents(self):
        Returns the pruned list of document ids.
def get reduced dictionary(self):
        Returns the pruned dictionary.
def get reduced scores(self):
        Returns the list of non-zero values in the pruned sparse matrix.
def get reduced row indices (self):
        Returns the list of row indices for the pruned sparse matrix.
def get reduced col offsets (self):
        Returns the list of col_offsets for the pruned sparse matrix.
def preprocess(self, maxiter=1000, docsperterm=3,termsperdoc=5, boolean mode=0):
        Preprocesses the matrix, dictionary, and documents provided.
def write output(self, matrix filepath, dict filepath, docs filepath, precision=4):
```

Writes the results of the preprocessing to the filesystem. The matrix is written to matrix_filepath, the dictionary to dict_filepath, and the documents to docs_filepath. The outputs are written with the specified precision.

VI.2. Matrixgen

```
def parser(self):
```

Creates a parser that takes the same inputs and has the same defaults as the binary matrixgen tool. Returns a dictionary containing the command line inputs or their default values. The fields in that dictionary are: height, width, filename, type, rng_center, rng_radius, precision, and nz_per_col.

```
def uniform(self, m, n, center=0.5, radius=0.5):
```

Generates a uniform matrix of height m and width n with the RNG attributes of center and radius.

```
def densediag(self, m, n, center=0.5, radius=0.5):
```

Generates a dense diagonal matrix of height m and width n with the RNG attributes of center and radius.

```
def identify(self, m, n):
```

Generates an identify matrix of height ${\tt m}$ and width ${\tt n}$.

```
def sparsediag(self, n, center=0.5, radius=0.5):
```

Generates a sparse diagonal matrix of width n with the RNG attributes of center and radius.

```
def ones(self, m, n):
```

Generates an ones matrix of height ${\tt m}$ and width ${\tt n}$.

```
def zeros(self, m, n):
```

Generates a zeros matrix of height m and width n.

```
def sparse(self, m, n, nz):
```

Generates an identify matrix of height m and width n and nz non-zero elements.

```
def write output(self, filename, precision=6):
```

Writes the generated matrix to the ${\tt filename}$ with the specified ${\tt precision}.$

VI.3. SmallkAPI

```
def parser(self):
```

Creates a parser that takes the same inputs and has the same defaults as the binary smallk tool. Returns a dictionary containing the command line inputs or their default values. The fields in that dictionary are: matrixfile, k, algorithm, dictfile, hiernmf2, maxterms, stopping, tol, tolcount, infile_W, infile H, outfile H, outfile H, outprecision, maxiter, miniter, maxthreads, normalize, and verbose.

```
def get major version(self):
```

Returns SmallK's major version

```
def get minor version(self):
```

Returns SmallK's minor version

```
def get patch level(self):
```

Returns SmallK's patch level

```
def get_version_string(self):
```

Returns SmallK's version in a string

Load the input matrix. Four combinations are available, which provide for loading via a file path, numpy matrix, direct loading of a dense matrix, or direct loading of a sparse matrix. For example:

```
File path: load_matrix(filepath='/path/to/file/')
Sparse matrix: load_matrix(height=matrix_height, width=matrix_width, nz=non_zero_count, buffer=non_zero_elements, row_indices=rows, col_offsets=cols)
Dense matrix: load_matrix(buffer=matrix_buffer, height=matrix_height, width=matrix_width)
Numpv matrix: load_matrix(matrix=matrix)
```

Note: Internal to SmallK, the matrix is stored in column-major order. When you are loading a numpy matrix, the assumption is that your matrix is in row-major order. If this is not the case, you can pass column_major=True in as a keyword argument. When directly loading a dense matrix, the assumption is that your buffer holds the data in column-major order as well.

```
def is matrix loaded(self):
```

Returns a boolean that indicates whether or not a matrix has been loaded yet.

```
def nmf(self, k, algorithm, infile W="", infile_H="", precision=4, min_iter=5, max_iter=5000,
    tol=0.005, max threads=8, outdir="."):
```

Runs NMF on the loaded matrix using the supplied algorithm and implementation details.

```
def get_inputs(self):
```

Returns a dictionary of the supplied inputs to the nmf function.

```
def get H(self):
```

Returns the output H matrix as a numpy array.

```
def get_W(self):
```

Returns the output W matrix as a numpy array.

Runs HierNMF2 on the loaded matrix, using the provided running parameters. There are two options for loading the dictionary: passing a filepath or a list containing the dictionary.

File path: hiernmf2(5, dict_filepath='/path/to/dictionary/')
List: hiernmf2(5, dictionary=[list, containing, terms, from, dictionary])

VI.4. Flatclust

```
def parser(self):
```

Creates a parser that takes the same inputs and has the same defaults as the binary smallk tool. Returns a dictionary containing the command line inputs or their default values. The fields in that dictionary are: matrixfile, dictfile, clusters, algorithm, tol, infile_W, infile_H, outdir, maxterms, verbose, format, assignfile, treefile, maxiter, miniter, maxthreads.

Load the input matrix. Four combinations are available, which provide for loading via a file path, numpy matrix, direct loading of a dense matrix, or direct loading of a sparse matrix. For example:

```
File path: load_matrix(filepath='/path/to/file/')
Sparse matrix: load_matrix(height=matrix_height, width=matrix_width, nz=non_zero_count, buffer=non_zero_elements, row_indices=rows, col_offsets=cols)
Dense matrix: load_matrix(buffer=matrix_buffer, height=matrix_height, width=matrix_width)
Numpy matrix: load_matrix(matrix=matrix)
```

Note: Internal to SmallK, the matrix is stored in column-major order. When you are loading a numpy matrix, the assumption is that your matrix is in row-major order. If this is not the case, you can pass column_major=True in as a keyword argument. When directly loading a dense matrix, the assumption is that your buffer holds the data in column-major order as well.

```
def load dictionary(self, filepath):
```

Load the dictionary by providing the path to the file, filepath.

Run flat clustering on the loaded matrix, using the provided input options

```
def get_flat_top_terms(self):
```

Return the top term indices for each cluster. The length of the returned array is maxterms*k, with the first maxterms elements belonging to the first cluster, the second maxterms elements belonging to the second cluster, etc.

```
def get assignments(self):
```

Return the list of cluster assignments for each document.

```
def write output(self, assignfile, treefile, outdir='./', format='XML'):
```

Writes the assignment file and treefile in the provided format and to the provided output directory.

VI.5. Hierclust

```
def parser(self):
```

Creates a parser that takes the same inputs and has the same defaults as the binary smallk tool. Returns a dictionary containing the command line inputs or their default values. The fields in that dictionary are: matrixfile, dictfile, clusters, tol, infile_W, infile_H, outdir, maxterms, verbose, format, assignfile, treefile, maxiter, miniter, maxthreads, unbalanced, trial allowance, flat.

Load the input matrix. Four combinations are available, which provide for loading via a file path, numpy matrix, direct loading of a dense matrix, or direct loading of a sparse matrix. For example:

```
File path: load_matrix(filepath='/path/to/file/')
Sparse matrix: load_matrix(height=matrix_height, width=matrix_width, nz=non_zero_count, buffer=non_zero_elements, row_indices=rows, col_offsets=cols)
Dense matrix: load_matrix(buffer=matrix_buffer, height=matrix_height, width=matrix_width)
Numpy matrix: load_matrix(matrix=matrix)
```

Note: Internal to SmallK, the matrix is stored in column-major order. When you are loading a numpy matrix, the assumption is that your matrix is in row-major order. If this is not the case, you can pass column_major=True in as a keyword argument. When directly loading a dense matrix, the assumption is that your buffer holds the data in column-major order as well.

```
def load dictionary(self, filepath):
```

Load the dictionary by providing the path to the file, filepath.

```
def cluster(self, k, infile_W='', infile_H='', maxterms=5, unbalanced=0.1, trial_allowance=3, verbose=True, flat=0, min iter=5, max iter=5000, max threads=8, tol=0.0001):
```

Run hierarchical clustering on the loaded matrix, using the provided input options.

```
def get flat top terms(self):
```

Return the top term indices for each cluster. The length of the returned array is maxterms*k, with the first maxterms elements belonging to the first cluster, the second maxterms elements belonging to the second cluster, etc.

```
def get assignments(self):
```

Return the list of cluster assignments for each document.

```
def write output(self, assignfile, treefile, outdir='./', format='XML'):
```

Writes the assignment file and treefile in the provided format and to the provided output directory.

VII. References

References

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If the SmallK library is used to obtain results for publication, please use the following BibTeX citation:

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