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# SmallK: A Library for Nonnegative Matrix Factorization, Topic Modeling, and Clustering of Large-Scale Data

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<b>I. INTRODUCTION</b>	<b>4</b>
LOW-RANK APPROXIMATIONS AND NMF	4
<b>II. SMALLK OVERVIEW</b>	<b>4</b>
<b>III. BUILD AND INSTALLATION INSTRUCTIONS</b>	<b>6</b>
<b>III.1 QUICK START: BUILD A SMALLK VIRTUAL MACHINE USING VAGRANT</b>	<b>6</b>
<b>III.2 STANDARD BUILD AND INSTALLATION</b>	<b>7</b>
<b>PREREQUISITES</b>	<b>7</b>
<b>III.3 HOW TO INSTALL ELEMENTAL ON MACOSX</b>	<b>8</b>
III.3.1 OSX:INSTALL THE LATEST GNU AND CLANG COMPILERS	8
III.3.2 OSX:INSTALL OPENMPI	9
III.3.3 OSX:INSTALL THE LATEST VERSION OF LIBFLAME	9
III.3.4 OSX:INSTALL ELEMENTAL	9
<b>III.4 HOW TO INSTALL ELEMENTAL ON LINUX</b>	<b>12</b>
III.4.1 LINUX:INSTALL THE LATEST GNU COMPILERS	12
III.4.2 LINUX:INSTALL OPENMPI	12
III.4.3 LINUX:INSTALL THE LATEST VERSION OF LIBFLAME	12
III.4.4 LINUX:INSTALL AN ACCELERATED BLAS LIBRARY	12
III.4.5 LINUX:INSTALL ELEMENTAL	13
<b>III.6 INSTALLING THE PYTHON LIBRARIES</b>	<b>16</b>
III.6.1 OSX: INSTALL PYTHON LIBRARIES	16
III.6.2 LINUX: INSTALL PYTHON LIBRARIES	17
<b>IV. BUILD AND INSTALLATION OF SMALLK</b>	<b>18</b>
<b>IV.1 OBTAIN THE SOURCE CODE</b>	<b>18</b>
<b>IV.2 BUILD THE SMALLK LIBRARY</b>	<b>18</b>
<b>IV.3 EXAMPLES OF API USAGE</b>	<b>19</b>
<b>IV.4 MATRIX FILE FORMATS</b>	<b>23</b>
<b>IV.5 SMALLK API</b>	<b>24</b>
ENUMERATIONS	24
API FUNCTIONS	24
<b>V. SMALLK COMMAND LINE TOOLS</b>	<b>29</b>
<b>V.1. PREPROCESSOR</b>	<b>29</b>
OVERVIEW	29
INPUT FILES	30
COMMAND LINE OPTIONS	30
SAMPLE RUNS	31
<b>V.2. MATRIXGEN</b>	<b>32</b>
OVERVIEW	32
COMMAND LINE OPTIONS	32
SAMPLE RUNS	32
<b>V.3. NONNEGATIVE MATRIX FACTORIZATION (NMF)</b>	<b>33</b>
OVERVIEW	33
COMMAND LINE OPTIONS	33
SAMPLE RUNS	34
<b>V.4. HIERCLUST</b>	<b>35</b>
OVERVIEW	35
COMMAND LINE OPTIONS	36
SAMPLE RUNS	37

<b>V.5. FLATCLUST</b>	<b>38</b>
OVERVIEW	38
COMMAND LINE OPTIONS	38
SAMPLE RUN	39
<b>V.6. SMALLK TEST RESULTS</b>	<b>40</b>
<b>VI. PYSMALLK: SMALLK PYTHON INTERFACE</b>	<b>57</b>
<b>VI.1. PREPROCESSOR</b>	<b>57</b>
<b>VI.2. MATRIXGEN</b>	<b>60</b>
<b>VI.3. SMALLKAPI</b>	<b>62</b>
<b>VI.4. FLATCLUST</b>	<b>64</b>
<b>VI.5. HIERCLUST</b>	<b>66</b>
<b>VII. REFERENCES</b>	<b>68</b>
<b>CONTACT INFORMATION</b>	<b>69</b>
<b>ACKNOWLEDGEMENTS</b>	<b>69</b>

## I. Introduction

High-dimensional data sets are ubiquitous in data science, and they often present serious problems for researchers. Our work in dimensionality reduction focuses on, but is not limited to, low-rank approximations via nonnegative matrix factorization (NMF) [1, 2]. NMF is a non-convex optimization problem with important applications in data and interactive visual analytics of high-dimensional data.

The impetus for this document is to provide a step-by-step procedure for the application of the theory to real-world large-scale data analytics. We have instantiated our research efforts in a software framework that includes high-level driver code via Python and a simple command line interface, SmallK, which hides most of the details of the input parameters. Our low-level code, also usable from the command line, is written in C++, which provides efficient NMF algorithms. The algorithms discussed herein have numerous practical applications; this document will hopefully provide the information required to quickly begin real work.

Below is a brief description of our fundamental research on NMF algorithms (please see the references section for more detail). Following the brief motivational introduction to the NMF are detailed installation instructions for the NMF software framework.

### Low-rank approximations and NMF

Algorithms that enable dimension reduction and clustering are two critical areas in data analytics and interactive visual analysis of high-dimensional data. A low-rank approximation framework has the ability to facilitate faster processing times and utilize fewer resources. These approximations provide a natural way to compute only what we need for significant dimension reduction, and are analogous to singular value decomposition (SVD) and principal component analysis (PCA). The algorithm framework also works efficiently for clustering since clustering can be viewed as a specific way of achieving a low-rank approximation so that the clustered structure of the data is well represented in a few basis vectors.

Matrix low-rank approximations such as the SVD have played a key role as a fundamental tool in machine learning, data mining, and other areas of computational science and engineering. The NMF has recently emerged as an important constrained low rank approximation method as well. A distinguishing feature of the NMF is the requirement of nonnegativity: NMF is considered for high-dimensional and large scale data in which the representation of each element is inherently nonnegative, and it seeks low-rank factor matrices that are constrained to have only nonnegative elements. There are many examples of data with a nonnegative representation. In a standard term-frequency encoding, a text document is represented as a vector of nonnegative numbers since each element represents the number of appearances of each term in each document. In image processing, digital images are represented by pixel intensities, which are nonnegative. In the life sciences, chemical concentrations or gene expression levels are naturally represented as nonnegative data.

Our algorithm framework utilizes various constraints on the non-convex optimization problem that gives rise to the nonnegative factors. With these various constraints NMF is a versatile tool for a large variety of data analytics problems. NMF algorithms have been an active area of research for several years. Since much of the data for many important problems in numerous domains is nonnegative NMF is the correct computational model for mining and/or integrating information from such data. NMF also offers enhanced interpretation of results since nonnegativity of the data is preserved.

## II. SmallK Overview

The SmallK library provides routines for low-rank matrix approximation via nonnegative matrix factorization (NMF). The term “nonnegative matrix” means that, for a given matrix, all of its elements are greater than or equal to zero, which we express as  $\geq 0$ . Given a nonnegative matrix  $A$ , the SmallK software computes nonnegative matrices  $W$  and  $H$  such that

$$A \cong W H$$

The matrix  $A$  has  $m$  rows and  $n$  columns and can be either sparse or dense.  $W$  has  $m$  rows and  $k$  columns, and  $H$  has  $k$  rows and  $n$  columns. The value of  $k$  is an input parameter to the approximation routines; typically  $k \ll m$  and  $k \ll n$ . The parameter  $k$  is called the ‘reduced rank’ of the low rank approximation. In applications it could

represent the reduced dimension in dimension reduction, the number of clusters for clustering various data sets, or the number of topics in topic discovery.

NMF algorithms seek to approximate a matrix  $A$  by the product of two much smaller matrices  $W$  and  $H$ . The idea is to choose the smallest value of  $k$  (width of  $W$  and height of  $H$ ) that gives an acceptable approximation error. Due to the nonconvex nature of the optimization problem associated with finding  $W$  and  $H$ , they can only be approximated after an NMF algorithm satisfies a convergence criterion. Thus, the minimization of the objective function proceeds iteratively, attempting to reach a stationary point, which is the best possible solution. As the iterations proceed, the SmallK code computes a metric that estimates the progress and, when the metric falls below a user-specified tolerance, the iterations stop and convergence is declared.

The SmallK library provides implementations of several NMF algorithms. These algorithms are:

1. Multiplicative Updating (NMF-MU)
2. Hierarchical Alternating Least Squares (NMF-HALS)
3. Block Principal Pivoting (NMF-BPP)
4. Rank2 Specialization (NMF-RANK2)

Additional NMF algorithms will be provided in future updates.

SmallK also provides implementations of hierarchical and flat data clustering. These routines are:

1. Hierarchical Clustering via NMF-RANK2
2. Flat Clustering via NMF-RANK2
3. Flat Clustering via NMF-BPP or NMF-HALS

The suite of SmallK implementations of NMF algorithms are suitable in many applications such as image processing, interactive visual analytics, speckle removal from SAR images, recommender systems, information fusion, outlier detection, chemometrics, and many more.

The SmallK library requires either MacOSX or Linux. A Windows version may be provided in the future.

## III. Build and Installation Instructions

### III.1 Quick Start: Build a SmallK Virtual Machine using Vagrant

Installing SmallK into a virtual machine (OSX, Linux, Windows) is intended for those who are not doing development and/or do not have a reason to do the full installation on Linux or OSX outlined in sections III.2 to III.4 (Windows full installation coming soon).

The complete stack of software dependencies for SmallK as well as SmallK itself can be rapidly set up and configured through use of Vagrant and VirtualBox and the files included in the repository. To deploy the SmallK VM:

1. Install [Vagrant](#) and [VirtualBox](#).

[Note: For Windows, ensure that you have a VirtualBox version  $\geq$  4.3.12. After installing Vagrant, you may need to log out and log back in to ensure that you can run vagrant commands in the command prompt.]

2. From within the vagrant/ directory in the repository run:

```
vagrant up
```

This can take as long as an hour to build the VM, which will be based on a minimal Ubuntu 14.04 installation. The Vagrantfile can be customized in many ways to change the specifications for the VM that is built. See more information [here](#). The default configuration provides the VM with 4 GB of memory and 2 CPUs. Increasing these allocations will improve the performance of the application. This can be done by modifying this line in the Vagrantfile:

```
vb.customize ["modifyvm", :id, "--memory", "4056", "--cpus", "2"]
```

3. Once the VM has been built, run:

```
vagrant ssh
```

[Note: For Windows, you will need an ssh client in order to run the above command. This can be obtained via [CygWin](#), [MinGW](#), or [Git](#). If you would like to use PuTTY to connect to your virtual machine, follow [these instructions](#).

This will drop you into the command line of the VM that was just created. From there, you can navigate to /home/vagrant/smallk-1.4.0 and run

```
make check
```

to verify your installation was successful. In case you need it, the username/password for the VM created will be vagrant/vagrant.

4. When you are ready to shut down the VM, run one of the following:

```
vagrant suspend    # save the current running state
```

```
vagrant halt       # gracefully shut down the machine
```

```
vagrant destroy    # remove the VM from your machine
```

If you want to work with the VM again, from any of the above states you can run

```
vagrant up
```

again, and the VM will be resumed or recreated.

## III.2 Standard Build and Installation

### Prerequisites

- A modern C++ compiler that supports the C++11 standard, such as the latest release of the GNU or clang compilers
- [Elemental](#), a high-performance library for dense, distributed linear algebra, which requires:
  - An MPI installation, such as [OpenMPI](#)
  - A BLAS implementation, preferably optimized/tuned for the local system
  - [libFLAME](#): (optional) a high-performance library for dense linear algebra
  - [OpenMP](#): (optional)
  - CMake
- Optional: Python 2.7, including the following libraries (required to build the Python interface to SmallK, which is optional):
  - numpy
  - scipy
  - cython

Elemental can make use of OpenMP parallelization if available. This is generally advantageous for large problems. The SmallK code is also internally parallelized to take full advantage of multiple CPU cores for maximum performance. SmallK does not currently support distributed computation. However, future updates are planned that will provide this capability.

We **strongly** recommend that users install both the HybridRelease and PureRelease builds of Elemental. OpenMP is enabled in the HybridRelease build and disabled in the PureRelease build. So why install both? For smaller problems the overhead of *OpenMP can actually cause code to run slower* than without it. Whereas for large problems OpenMP parallelization generally helps, but there is no clear transition point between where it helps and where it hurts. Thus we encourage users to experiment with both builds to find the one that performs best for their typical problems.

We also recommend that users clearly separate the different build types as well as the versions of Elemental on their systems. Elemental is under active development, and new releases can introduce changes to the API that are not backwards compatible with previous releases. To minimize build problems and overall hassle, we recommend that Elemental be installed so that the different versions and build types are cleanly separated.

**The SmallK software supports Elemental versions 0.81, 0.83, 0.84, 0.84-p1, and 0.85.**

**A note of caution: copying the command lines from this document and pasting them into a terminal may result in the commands not properly executing due to how Word interprets the double dash --, “double quotes”, and perhaps other characters or symbols. For pasting the commands to a terminal, first copy the command lines to a text editor and copy/paste from there.**

### III.3 How to Install Elemental on MacOSX

On MacOSX we recommend using [Homebrew](#) as the package manager. Homebrew does not require sudo privileges for package installation, unlike other package managers such as MacPorts. Thus the chances of corrupting vital system files are greatly reduced with Homebrew.

It is convenient to be able to view hidden files (like .file) in the MacOSX Finder. To do so run the following at the command line:

```
defaults write com.apple.finder AppleShowAllFiles -bool YES
```

To hide hidden files, set the Boolean flag to NO:

```
defaults write com.apple.finder AppleShowAllFiles -bool NO
```

If you use Homebrew, ensure that your PATH is configured to search Homebrew's installation directory first. Homebrew's default installation location is /usr/local/bin, so that location needs to be first on your path. To check, run this command from a terminal window:

```
cat /etc/paths
```

If the first entry is not /usr/local/bin, you will need to edit this file. Since this is a system file, first create a backup. If permission is denied to modify this file, use `sudo` in front of the command to launch your editor. Move the line /usr/local/bin so that it is on the first line of the file. Save the file, then close the terminal session and start a new terminal session so that the path changes will take effect.

After starting your new terminal session, make sure your homebrew packages are up-to-date by running the following commands:

```
brew update
brew upgrade
brew cleanup
brew doctor
```

#### III.3.1 OSX: Install the latest GNU and clang compilers

Elemental and SmallK both require a modern C++ compiler compliant with the C++11 standard. We recommend that you install the latest stable version of the clang and GNU C++ compilers. To do this, first install the XCode command line tools with this command:

```
xcode-select --install
```

If this command produces an error, download and install the latest version of XCode from the AppStore, which includes the command line tools. After the installation completes, run this command from a terminal window to check the version of the clang compiler:

```
clang++ --version
```

You should see output similar to this:

```
Apple LLVM version 6.0 (clang-600.0.51) (based on LLVM 3.5svn)
Target: x86_64-apple-darwin13.4.0
Thread model: posix
```

The latest version of the GNU compiler at the time of writing is g++-4.9.1, which is provided by the 'gcc' homebrew package. In addition to the gcc package, homebrew also provides a gcc49 package from the homebrew/versions tap. If this alternative gcc49 package is installed on your system it will prevent homebrew from symlinking the gcc package correctly. We recommend uninstalling the gcc49 versioned package and just using the gcc package instead. The Fortran compiler provided with the gcc package will also be configured to properly build numpy, which is required for the python interface to smallk.

If you need to uninstall the gcc49 package, run the following commands:

```
brew uninstall gcc49
brew cleanup
brew doctor
```

Then install the gcc package as follows:

```
brew install gcc
```

The Apple-provided gcc and g++ will not be overwritten by this installation. The new compilers will be installed into



/usr/local/bin as gcc-4.9, g++-4.9, and gfortran-4.9. The Fortran compiler is needed for the installation of MPI and for building the python interface to smallk.

### III.3.2 OSX:Install OpenMPI

Install the latest version of OpenMPI with Homebrew as follows:

```
brew install open-mpi --c++11
```

The Homebrew install formula provides an option for “thread-multiple” support, but do not enable this option, as it is still experimental, not optimized for performance, and may have bugs.

### III.3.3 OSX:Install the latest version of libFLAME

Next we detail the installation of the high performance numerical library libflame. The library can be downloaded from the libflame git repository on github.

It’s important to perform the git clone into a subdirectory NOT called ‘flame’ since this can cause name conflicts with the installation. We normally do a git clone into a directory called ‘libflame’. However, other directory names will work as well, but not ‘flame’.

To obtain the latest version of the FLAME library, clone the FLAME git repository with this command:

```
git clone https://github.com/flame/libflame.git <libflame>
```

Run the configure script in the top-level FLAME folder as follows (assuming you want to install to /usr/local/flame; if not, change the prefix path):

```
./configure --prefix=/usr/local/flame --with-cc=/usr/local/bin/gcc-4.9 --with-ranlib=/usr/local/bin/gcc-ranlib-4.9
```

A complete list of configuration options can be obtained by running: ./configure --help.

After the configuration process completes, build the FLAME library as follows:

```
make -j4
```

The `-j4` option tells Make to use four processes to perform the build. This number can be increased if you have a more capable system.

```
make install
```

The FLAME library is now installed.

### III.3.4 OSX:Install Elemental

Here is our recommended installation scheme for Elemental:

Choose a folder for the root of the Elemental installation. For our systems, this is

```
/usr/local/elemental
```

Download one of the smallk-supported releases of Elemental (see above), unzip and untar the distribution, and cd to the top-level folder of the unzipped distribution. This folder will be denoted by UNZIP\_DIR in the following instructions.

For the first step of the installation, for Elemental versions prior to 0.85, we need to fix a few problems with the CMake configuration files. Open the following file in a text editor:

```
UNZIP_DIR/cmake/tests/OpenMP.cmake
```

On the first line of the file, change

```
if (HYBRID)
```

to this:

```
if (ELEM_HYBRID)
```

Next, open this file in a text editor:

```
UNZIP_DIR/cmake/tests/Math.cmake
```

Near the first line of the file, change

```
if(PURE)
```

to this:

```
if(ELEM_PURE)
```

Save both files.

### **HybridRelease Build**

From UNZIP\_DIR, run the following command to create a local build folder for the HybridRelease build:

```
mkdir build_hybrid
cd build_hybrid
```

Use the following CMake command for the HybridRelease build, substituting either 0.81, 0.83, 0.84, 0.84-p1, 0.85 for VERSION\_STRING:

```
cmake -D CMAKE_INSTALL_PREFIX=/usr/local/elemental/VERSION_STRING/HybridRelease
-D CMAKE_BUILD_TYPE=HybridRelease
-D CMAKE_CXX_COMPILER=/usr/local/bin/g++-4.9
-D CMAKE_C_COMPILER=/usr/local/bin/gcc-4.9
-D CMAKE_Fortran_COMPILER=/usr/local/bin/gfortran-4.9
-D MATH_LIBS="/usr/local/flame/lib/libflame.a;-framework Accelerate"
-D ELEM_EXAMPLES=ON -D ELEM_TESTS=ON ..
```

Note that we have installed g++-4.9 into /usr/local/bin and libFLAME into /usr/local/flame. Alter these paths, if necessary, to match the installation location on your system.

Once the CMake configuration step completes, you can build Elemental from the generated Makefiles with the following command:

```
make -j4
```

The -j4 option tells Make to use four processes to perform the build. This number can be increased if you have a more capable system.

After the build completes, install elemental as follows:

```
make install
```

As a final step, if you installed a version of Elemental prior to the 0.84 series releases, edit the file /usr/local/elemental/<version>/HybridRelease/conf/ElemVars and replace the line

```
CXX = /usr/local/bin/g++-4.9
```

With this:

```
CXX = /usr/local/bin/g++-4.9 -std=c++11
```

This will eliminate some compiler warnings about C++11 constructs.

If you installed Elemental version 0.85, you need to setup your system to find the Elemental dynamic library. Either in your startup script (~/.bash\_profile) or in a terminal window, enter the following command on a single line, replacing VERSION\_STRING as above:

```
export DYLD_LIBRARY_PATH=
$DYLD_LIBRARY_PATH:/usr/local/elemental/VERSION_STRING/HybridRelease/lib/
```

### **PureRelease Build**

After this, run these commands to create a build folder for the PureRelease build:

```
cd ..
```

```
mkdir build_pure
cd build_pure
```

Then repeat the CMake configuration process, this time with the following command for the PureRelease build:

```
cmake -D CMAKE_INSTALL_PREFIX=/usr/local/elemental/VERSION_STRING/PureRelease
-D CMAKE_BUILD_TYPE=PureRelease -D CMAKE_CXX_COMPILER=/usr/local/bin/g++-4.9
-D CMAKE_C_COMPILER=/usr/local/bin/gcc-4.9
-D CMAKE_Fortran_COMPILER=/usr/local/bin/gfortran-4.9
-D MATH_LIBS="/usr/local/flame/lib/libflame.a;-framework Accelerate"
-D ELEM_EXAMPLES=ON -D ELEM_TESTS=ON ..
```

Repeat the build commands and install this build of Elemental. Then, if you installed a version of Elemental prior to the 0.84 series releases, edit the `/usr/local/elemental/<version>/PureRelease/conf/ElemVars` file and replace the CXX line as indicated above.

If you installed Elemental version 0.85, you need to setup your system to find the Elemental dynamic library for the PureRelease build. Enter the following command in a terminal window on a single line, replacing VERSION\_STRING as above:

```
export DYLD_LIBRARY_PATH=
$DYLD_LIBRARY_PATH:/usr/local/elemental/VERSION_STRING/PureRelease/lib/
```

Note: you will need to set this variable to point to either the HybridRelease or the PureRelease build of the Elemental dynamic library whenever you want to use smallk.

This completes the two builds of Elemental.

To test the installation, follow Elemental's [test instructions](#) for the SVD test to verify that Elemental is working correctly.

### III.4 How to Install Elemental on Linux

We strongly recommend using a package manager for your Linux distribution for installation and configuration of the required dependencies. We cannot provide specific installation commands for every variant of Linux, so we specify the high-level steps below.

#### III.4.1 Linux: Install the latest GNU compilers

We recommend installation of the latest stable release of the GNU C++ compiler, which is g++-4.9 at the time of this writing.

Also install the latest version of GNU Fortran, which is needed for the installation of MPI.

#### III.4.2 Linux: Install OpenMPI

Download the latest version of [OpenMPI](#), unzip and untar the downloaded zip file, and cd to the untarred directory. Run configure as follows, all on a single line. This command assumes that gcc-4.9 has been installed; change the paths if needed to match your system:

```
./configure --prefix=/usr/local CC=/usr/local/bin/gcc-4.9 CXX=/usr/local/bin/g++-4.9  
F77=/usr/local/bin/gfortran-4.9 FC=/usr/local/bin/gfortran-4.9
```

Wait for the configure script to finish – this could take several minutes. Then build the code as follows:

```
make -j4
```

Install with:

```
make install
```

OpenMPI provides many tests to verify the installation; it's a good idea to run at least some of these tests to ensure that MPI was installed successfully.

#### III.4.3 Linux: Install the latest version of libFlame

To obtain the latest version of the FLAME library, clone the FLAME git repository with this command:

```
git clone https://github.com/flame/libflame.git
```

Run the configure script in the top-level FLAME folder as follows (assuming you want to install to /usr/local/flame; if not, change the prefix path):

```
./configure --prefix=/usr/local/flame --with-cc=/usr/local/bin/gcc-4.9 --with-  
ranlib=/usr/local/bin/gcc-ranlib-4.9
```

A complete list of configuration options can be obtained by running

```
./configure --help
```

After the configuration process completes, build the FLAME library as follows:

```
make -j4  
make install
```

This completes the installation of the FLAME library.

#### III.4.4 Linux: Install an accelerated BLAS library

It is essential to link Elemental with an accelerated BLAS library for maximum performance. Linking Elemental with a 'reference' BLAS implementation will cripple performance, since the reference implementations are designed for correctness not speed.

If you do not have an accelerated BLAS on your system, you can download and build [OpenBLAS](#). Download, unzip, and untar the tarball (version 0.2.8 as of this writing) and cd into the top-level folder. Build OpenBLAS with this command, assuming you have a 64-bit system:

```
make BINARY=64 USE_OPENMP=1
```

Install with this command, assuming the installation directory is /usr/local/openblas/0.2.8/:

```
make PREFIX=/usr/local/openblas/0.2.8/ install
```

This completes the installation of OpenBLAS.

### III.4.5 Linux:Install Elemental

We **strongly** recommend that users install both the HybridRelease and PureRelease builds of Elemental. OpenMP is enabled in the HybridRelease build and disabled in the PureRelease build. So why install both? For smaller problems the overhead of OpenMP can actually cause code to run slower than without it. On the other hand, for large problems, OpenMP parallelization generally helps. However, there is no clear transition point between where it helps and where it hurts. Thus, we encourage users to experiment with both builds to find the one that performs best for their typical problems.

We also recommend that users clearly separate the different build types as well as the versions of Elemental on their systems. Elemental is under active development, and new releases can introduce changes to the API that are not backwards compatible with previous releases. To minimize build problems and overall hassle, we recommend that Elemental be installed so that the different versions and build types are cleanly separated.

Here is our recommended installation scheme for Elemental:

Choose a folder for the root of the Elemental installation. For our systems, this is

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/usr/local/elemental
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Download one of the smallk-supported releases of Elemental (see above), unzip and untar the distribution, and cd to the top-level folder of the unzipped distribution. This folder will be denoted by UNZIP\_DIR in the following instructions.

For the first step of the installation, for Elemental versions prior to 0.85, we need to fix a few problems with the CMake configuration files. Open the following file in a text editor:

```
UNZIP_DIR/cmake/tests/OpenMP.cmake
```

On the first line of the file, change

```
if (HYBRID)
```

to this:

```
if (ELEM_HYBRID)
```

Next, open this file in a text editor:

```
UNZIP_DIR/cmake/tests/Math.cmake
```

Near the first line of the file, change

```
if (PURE)
```

to this:

```
if (ELEM_PURE)
```

Save both files.

#### HybridRelease Build

From UNZIP\_DIR, run the following command to create a local build folder for the HybridRelease build:

```
mkdir build_hybrid
cd build_hybrid
```

Use the following CMake command for the HybridRelease build, substituting either 0.81, 0.83, 0.84, 0.84-p1, 0.85 for VERSION\_STRING:

```
cmake -D CMAKE_INSTALL_PREFIX=/usr/local/elemental/VERSION_STRING/HybridRelease
-D CMAKE_BUILD_TYPE=HybridRelease -D CMAKE_CXX_COMPILER=/usr/local/bin/g++-4.9
-D CMAKE_C_COMPILER=/usr/local/bin/gcc-4.9
-D CMAKE_Fortran_COMPILER=/usr/local/bin/gfortran-4.9
-D MATH_LIBS="/usr/local/flame/lib/libflame.a;-L/usr/local/openblas/0.2.8/lib -lopenblas
-lm"
-D ELEM_EXAMPLES=ON -D ELEM_TESTS=ON ..
```

Note that we have installed g++-4.9 into /usr/local/bin and libFLAME into /usr/local/flame. Alter these paths, if necessary, to match the installation location on your system.

If this command does not work on your system, you may need to define the BLAS\_LIBS and/or GFORTRAN\_LIB config options.

Once the CMake configuration step completes, you can build Elemental from the generated Makefiles with the following command:

```
make -j4
```

The `-j4` option tells Make to use four processes to perform the build. This number can be increased if you have a more capable system.

After the build completes, install elemental as follows:

```
make install
```

As a final step, if you installed a version of Elemental prior to the 0.84 series releases, edit the file /usr/local/elemental/<version>/HybridRelease/conf/ElemVars and replace the line

```
CXX = /usr/local/bin/g++-4.9
```

With this:

```
CXX = /usr/local/bin/g++-4.9 -std=c++11
```

This will eliminate some compiler warnings about C++11 constructs.

If you installed Elemental version 0.85, you need to setup your system to find the Elemental shared library. Either in your startup script (~/.bashrc) or in a terminal window, enter the following command on a single line, replacing VERSION\_STRING as above:

```
export LD_LIBRARY_PATH=
$LD_LIBRARY_PATH:/usr/local/elemental/VERSION_STRING/HybridRelease/lib/
```

### **PureRelease Build**

After this, run these commands to create a build folder for the PureRelease build:

```
cd ..
mkdir build_pure
cd build_pure
```

Then repeat the CMake configuration process, this time with the following command for the PureRelease build:

```
cmake -D CMAKE_INSTALL_PREFIX=/usr/local/elemental/VERSION_STRING/PureRelease
-D CMAKE_BUILD_TYPE=PureRelease -D CMAKE_CXX_COMPILER=/usr/local/bin/g++-4.9
-D CMAKE_C_COMPILER=/usr/local/bin/gcc-4.9
-D CMAKE_Fortran_COMPILER=/usr/local/bin/gfortran-4.9
-D MATH_LIBS="/usr/local/flame/lib/libflame.a;-L/usr/local/openblas/0.2.8/lib -lopenblas
-lm"
-D ELEM_EXAMPLES=ON -D ELEM_TESTS=ON ..
```

If this command does not work on your system, you may need to define the BLAS\_LIBS and/or GFORTRAN\_LIB config options.

Repeat the build commands and install this build of Elemental. Then, if you installed a version of Elemental prior to the 0.84 series releases, edit the /usr/local/elemental/<version>/PureRelease/conf/ElemVars file and replace the CXX line as indicated above.

If you installed Elemental version 0.85, you need to setup your system to find the Elemental shared library for the PureRelease build. Enter the following command in a terminal window on a single line, replacing VERSION\_STRING as above:

```
export LD_LIBRARY_PATH=
$LD_LIBRARY_PATH:/usr/local/elemental/VERSION_STRING/PureRelease/lib/
```

Note: you will need to set this variable to point to either the HybridRelease or the PureRelease build of the Elemental shared library whenever you want to use smallk.

This completes the two builds of Elemental.

To test the installation, follow Elemental's [test instructions](#) for the SVD test to verify that Elemental is working correctly.

## III.6 Installing the Python libraries

### III.6.1 OSX: Install Python libraries

#### Install Python scientific software packages

Assuming that you have used brew to install gcc, as indicated earlier, you can run the following commands to install the necessary libraries:

```
brew install python
brew install numpy
brew install scipy
```

To check your installation, run:

```
brew test numpy
```

**IMPORTANT:** Check to see that your numpy installation has correctly linked to the needed BLAS libraries.

Ensure that you are running the correct python:

```
which python
```

This should print out `/usr/local/bin/python`. Open a python terminal and run the following:

```
import numpy as np
np.__config__.show()
```

You should see something similar to the following:

```
lapack_opt_info:
  extra_link_args = ['-Wl,-framework', '-Wl,Accelerate']
  extra_compile_args = ['-msse3']
  define_macros = [('NO_ATLAS_INFO', 3)]
blas_opt_info:
  extra_link_args = ['-Wl,-framework', '-Wl,Accelerate']
  extra_compile_args = ['-msse3', '-I/System/Library/Frameworks/vecLib.framework/Headers']
  define_macros = [('NO_ATLAS_INFO', 3)]
```

If you are using OpenBLAS, you should see that indicated as well.

#### Install Cython: a Python interface to C/C++

First install the Python Package Index utility, pip. Many Python packages are configured to use this package manager, Cython being one.

```
brew install pip
```

To install Cython:

```
pip install cython
```

The Makefile assumes an installation path of `/usr/local/lib/python2.7/site-packages` for the compiled library file. If you are not using brew to install your packages, you will need to tell the Makefile where the appropriate site-packages directory is located on your system. Setting the `SITE_PACKAGES_DIR` command line variable when running make accomplishes this.



### III.6.2 Linux: Install Python libraries

The Python libraries can easily be installed via pip and apt-get with the following commands:

```
pip install numpy  
apt-get install python-scipy  
pip install cython
```

## IV. Build and Installation of SmallK

### IV.1 Obtain the source code

The source code for the SmallK library can be downloaded from the [SmallK repository](#) on github. Once downloaded uncompress the tarball and follow the installation instructions below.

### IV.2 Build the SmallK library

Download and unpack the SmallK code tarball and cd into the top-level SmallK directory. The makefiles assume that you followed our suggested installation plan for Elemental. If this is not the case you will need to do one of the following:

1. Create an environment variable called `ELEMENTAL_INSTALL_DIR` which contains the path to the root folder of your Elemental installation
2. Define the variable `ELEMENTAL_INSTALL_DIR` on the make command line
3. Edit the SmallK makefile so that it can find your Elemental installation

Assuming that the default install locations are acceptable, build the SmallK code by running this command from the root directory of the distribution:

```
make all
```

This will build the SmallK and pysmallk libraries and several command-line applications. These are:

1. libsmallk.a, the SmallK library
2. preprocess\_tf, a command-line application for processing and scoring term-frequency matrices
3. matrixgen, a command-line application for generating random matrices
4. nmf, a command-line application for NMF
5. hierclust, a command-line application for fast hierarchical clustering
6. flatclust, a command-line application for flat clustering via NMF
7. pysmallk.so, if `PYSMALLK=1` (0: default) the Python-wrapped SmallK library, making SmallK available via Python

To install the code, run this command to install to the default location, which is `/usr/local/smallk`:

```
make install
```

This will install the binary files listed above into the `/usr/local/smallk/bin` directory, which needs to be on your path to run the executables from anywhere on your system and avoid prepending with the entire path. This will install `pysmallk.so` into the `site-directories` folder associated with the Python binary. To install the binary code to a different location, either create an environment variable called `SMALLK_INSTALL_DIR` and set it equal to the desired installation location prior to running the install command, or supply a prefix argument:

```
make prefix=/path/to/smallk install
```

To install the Python library to a different location, create an environment variable called `SITE_PACKAGES_DIR` and set it equal to the desired installation location prior to running the install command, or supply this as an argument for make:

```
make SITE_PACKAGES_DIR=/path/to/site-packages install
```

Or, as a last resort, you can edit the top-level SmallK makefile to conform to the installation scheme of your system. You may need root privileges to do the installation, depending on where you choose to install it.

To test the installation, run this command:

```
make check
```

This will run a series of tests, none of which should report a failure. Sample output from a run of these tests can be found in section [V.6. SmallK Test Results].

Note: if you installed Elemental version 0.85, you will need to configure your system to find the Elemental shared library. See the Elemental installation instructions above for information on how to do this.

The command-line applications can be built individually by running the appropriate make command from the top-level smallk folder. These commands are:

To build the smallk library only:	<code>make libsmallk</code>
To build the preprocessor only:	<code>make preprocessor</code>
To build the matrix generator only:	<code>make matrixgen</code>
To build the nmf only:	<code>make nmf</code>
To build hierclust only:	<code>make hierclust</code>
To build flatclust only:	<code>make flatclust</code>
To build pysmallk only:	<code>make pysmallk</code>

*Note: Pysmallk requires builds of libsmallk, preprocessor, matrixgen, hierclust, and flatclust.*

### IV.3 Examples of API Usage

In the `examples` folder you will find a file called `smallk_example.cpp`. This file contains several examples of how to use the SmallK library. Also included in the `examples` folder is a makefile that you can customize for your use. Note that the SmallK library must first be installed before the example project can be built.

As an example of how to use the sample project, assume the smallk software has been installed into `/usr/local/smallk`. Also assume that the user chose to create the recommended environment variable `SMALLK_INSTALL_DIR` that stores the location of the top-level install folder, i.e. the user's `.bashrc` file contains this statement:

```
export SMALLK_INSTALL_DIR=/usr/local/smallk
```

To build the smallk example project, open a terminal window and `cd` to the `examples` directory and run this command:

```
make
```

To run the example project, run this command:

```
./bin/example ../../smallk_data
```

The output will be similar to the following (it won't be identical because some problems are randomly initialized):

```
Smallk major version: 1
Smallk minor version: 6
Smallk patch level: 0
Smallk version string: 1.6.0
Loading matrix...

*****
*
*           Running NMF-BPP using k=32
*
*****
Initializing matrix W...
Initializing matrix H...

parameters:

algorithm: Nonnegative Least Squares with Block Principal Pivoting
```

```

stopping criterion: Ratio of Projected Gradients
    height: 12411
    width: 7984
    k: 32
    miniter: 5
    maxiter: 5000
    tol: 0.005
    matrixfile: ../data/reuters.mtx
    maxthreads: 8

1:  progress metric: (min_iter)
2:  progress metric: (min_iter)
3:  progress metric: (min_iter)
4:  progress metric: (min_iter)
5:  progress metric: (min_iter)
6:  progress metric: 0.0747031
7:  progress metric: 0.0597987
8:  progress metric: 0.0462878
9:  progress metric: 0.0362883
10: progress metric: 0.030665
11: progress metric: 0.0281802
12: progress metric: 0.0267987
13: progress metric: 0.0236731
14: progress metric: 0.0220778
15: progress metric: 0.0227083
16: progress metric: 0.0244029
17: progress metric: 0.0247552
18: progress metric: 0.0220007
19: progress metric: 0.0173831
20: progress metric: 0.0137033

Solution converged after 39 iterations.

Elapsed wall clock time: 4.354 sec.

Writing output files...

*****
*
*           Running NMF-HALS using k=16
*
*****
Initializing matrix W...
Initializing matrix H...

    parameters:

        algorithm: HALS
    stopping criterion: Ratio of Projected Gradients
        height: 12411
        width: 7984
        k: 16
        miniter: 5
        maxiter: 5000
        tol: 0.005
        matrixfile: ../data/reuters.mtx
        maxthreads: 8

1:  progress metric: (min_iter)
2:  progress metric: (min_iter)
3:  progress metric: (min_iter)
4:  progress metric: (min_iter)
5:  progress metric: (min_iter)
6:  progress metric: 0.710219
7:  progress metric: 0.580951
8:  progress metric: 0.471557
9:  progress metric: 0.491855
10: progress metric: 0.531999
11: progress metric: 0.353302
12: progress metric: 0.201634
13: progress metric: 0.1584
14: progress metric: 0.142572
15: progress metric: 0.12588
16: progress metric: 0.113239
17: progress metric: 0.0976934
18: progress metric: 0.0821207
19: progress metric: 0.0746089

```

```
20: progress metric: 0.0720616
40: progress metric: 0.0252854
60: progress metric: 0.0142085
80: progress metric: 0.0153269
```

Solution converged after 88 iterations.

Elapsed wall clock time: 1.560 sec.

Writing output files...

```
*****
*
*      Running NMF-RANK2 with W and H initializers      *
*
*****
Initializing matrix W...
Initializing matrix H...
```

```
parameters:
algorithm: Rank 2
stopping criterion: Ratio of Projected Gradients
height: 12411
width: 7984
k: 2
miniter: 5
maxiter: 5000
tol: 0.005
matrixfile: ../data/reuters.mtx
maxthreads: 8
```

```
1: progress metric: (min_iter)
2: progress metric: (min_iter)
3: progress metric: (min_iter)
4: progress metric: (min_iter)
5: progress metric: (min_iter)
6: progress metric: 0.0374741
7: progress metric: 0.0252389
8: progress metric: 0.0169805
9: progress metric: 0.0113837
10: progress metric: 0.00761077
11: progress metric: 0.0050782
12: progress metric: 0.00338569
```

Solution converged after 12 iterations.

Elapsed wall clock time: 0.028 sec.

Writing output files...

```
*****
*
*      Repeating the previous run with tol = 1.0e-5      *
*
*****
Initializing matrix W...
Initializing matrix H...
```

```
parameters:
algorithm: Rank 2
stopping criterion: Ratio of Projected Gradients
height: 12411
width: 7984
k: 2
miniter: 5
maxiter: 5000
tol: 1e-05
matrixfile: ../data/reuters.mtx
maxthreads: 8
```

```
1: progress metric: (min_iter)
2: progress metric: (min_iter)
3: progress metric: (min_iter)
4: progress metric: (min_iter)
5: progress metric: (min_iter)
```

```

6:   progress metric: 0.0374741
7:   progress metric: 0.0252389
8:   progress metric: 0.0169805
9:   progress metric: 0.0113837
10:  progress metric: 0.00761077
11:  progress metric: 0.0050782
12:  progress metric: 0.00338569
13:  progress metric: 0.00225761
14:  progress metric: 0.00150429
15:  progress metric: 0.00100167
16:  progress metric: 0.000666691
17:  progress metric: 0.000443654
18:  progress metric: 0.000295213
19:  progress metric: 0.000196411
20:  progress metric: 0.000130604

```

Solution converged after 27 iterations.

Elapsed wall clock time: 0.061 sec.

Writing output files...

Minimum value in W matrix: 0.

Maximum value in W matrix: 0.397027.

```

*****
*
*   Running HierNMF2 with 5 clusters, JSON format
*
*****

```

loading dictionary...

creating random W initializers...

creating random H initializers...

parameters:

```

    height: 12411
    width: 7984
    matrixfile: ../data/reuters.mtx
    dictfile: ../data/reuters_dictionary.txt
    tol: 0.0001
    miniter: 5
    maxiter: 5000
    maxterms: 5
    maxthreads: 8

```

[1] [2] [3] [4]

Elapsed wall clock time: 391 ms.

9/9 factorizations converged.

Writing output files...

```

*****
*
*   Running HierNMF2 with 10 clusters, 12 terms, XML format
*
*****

```

creating random W initializers...

creating random H initializers...

parameters:

```

    height: 12411
    width: 7984
    matrixfile: ../data/reuters.mtx
    dictfile: ../data/reuters_dictionary.txt
    tol: 0.0001
    miniter: 5
    maxiter: 5000
    maxterms: 12
    maxthreads: 8

```

[1] [2] [3] [4] [5] [6] dropping 20 items ...

[7] [8] [9]

Elapsed wall clock time: 837 ms.

21/21 factorizations converged.

Writing output files...

```

*****
*
* Running HierNmf2 with 18 clusters, 8 terms, with flat *
*
*****
creating random W initializers...
creating random H initializers...

parameters:
    height: 12411
    width: 7984
    matrixfile: ../data/reuters.mtx
    dictfile: ../data/reuters_dictionary.txt
    tol: 0.0001
    miniter: 5
    maxiter: 5000
    maxterms: 8
    maxthreads: 8
[1] [2] [3] [4] [5] [6] dropping 20 items ...
[7] [8] [9] dropping 25 items ...
[10] [11] [12] [13] [14] [15] [16] [17]

Running NNLS solver...
1: progress metric: 1
2: progress metric: 0.264152
3: progress metric: 0.0760648
4: progress metric: 0.0226758
5: progress metric: 0.00743562
6: progress metric: 0.00280826
7: progress metric: 0.00103682
8: progress metric: 0.000361738
9: progress metric: 0.000133087
10: progress metric: 5.84849e-05

Elapsed wall clock time: 1.362 s.
40/40 factorizations converged.

Writing output files...

```

## IV.4 Matrix File Formats

The SmallK software supports comma-separated value (CSV) files for dense matrices and [Matrix Market](#) files for sparse matrices.

For example, the 5x3 dense matrix

42	47	52
43	48	53
44	49	54
45	50	55
46	51	56

would be stored in a CSV file as follows:

```

42,47,52
43,48,53
44,49,54
45,50,55
46,51,56

```

The matrix is loaded exactly as it appears in the file. Internally, SmallK stores dense matrices in **column-major order**. Sparse matrices are stored in **compressed column format**.

## IV.5 SmallK API

The SmallK API is an extremely **simplistic** API for basic NMF and clustering. Users who require more control over the factorization or clustering algorithms can instead run one of the command-line applications in the SmallK distribution.

The SmallK API is exposed by the file `smallk.hpp`, which can be found in this location:

`SMALLK_INSTALL_DIR/include/smallk.hpp`. All API functions are contained within the `smallk` namespace.

An example of how to use the API can be found in the file `examples/smallk_example.cpp`.

The `smallk` library maintains a set of state variables that are used to control the NMF and clustering routines. Once set, the state variables maintain their values until changed by an API function. For instance, one state variable represents the matrix to be factored (or used for clustering). The API provides a function to load this matrix; once loaded, it can be repeatedly factored without the need for reloading. The state variables and their default values are documented below.

All computations with the `smallk` library are performed in double precision.

### Enumerations

The SmallK API provides two enumerated types, one for the supported NMF algorithms and one for the clustering file output format. These are:

```
enum Algorithm
{
    MU,          // Multiplicative Updating, Lee & Seung
    BPP,         // Block Principal Pivoting, Kim and Park
    HALS,        // Hierarchical Alternating Least Squares, Cichocki & Pan
    RANK2        // Rank2, Kuang and Park
};
```

The default NMF algorithm is BPP. The Rank2 algorithm is optimized for two-column or two-row matrices and is the underlying factorization routine for the clustering code.

```
enum OutputFormat
{
    XML, // Extensible Markup Language
    JSON // JavaScript Object Notation
};
```

### API functions

#### *Initialization and Cleanup*

```
void Initialize(int& argc,    // in
               char**& argv) // in
```

Call this function first, before all others in the API; initializes Elemental and the `smallk` library.

```
bool IsInitialized()
```

Returns true if the library has been initialized via a call to `Initialize()`, false otherwise.

```
void Finalize()
```

Call this function last, after all others in the API; performs cleanup for Elemental and the `smallk` library.

#### *Versioning*

```
unsigned int GetMajorVersion()
```

Returns the major release version number of the library as an unsigned integer.



```
unsigned int GetMinorVersion()
```

Returns the minor release version number of the library as an unsigned integer.

```
unsigned int GetPatchLevel()
```

Returns the patch version number of the library as an unsigned integer.

```
std::string GetVersionString()
```

Returns the version of the library as a string, formatted as `major.minor.patch`.

## ***Common Functions***

```
unsigned int GetOutputPrecision()
```

Returns the floating point precision with which numerical output will be written (i.e., the computed W and H matrix factors from the Nmf routine). The default precision is six digits.

```
void SetOutputPrecision(const unsigned int num_digits)
```

Sets the floating point precision with which numerical output will be written. Input values should be within the range `[1, precision(double)]`. Any inputs outside of this range will be adjusted.

```
unsigned int GetMaxIter()
```

Returns the maximum number of iterations allowed for NMF computations. The default value is 5000.

```
void SetMaxIter(const unsigned int max_iterations = 5000)
```

Sets the maximum number of iterations allowed for NMF computations. The default of 5000 should be more than sufficient for most computations.

```
unsigned int GetMinIter()
```

Returns the minimum number of NMF iterations. The default value is 5.

```
void SetMinIter(const unsigned int min_iterations = 5)
```

Sets the minimum number of NMF iterations to perform before checking for convergence. The convergence and progress estimation routines are non-trivial calculations, so increasing this value may result in faster performance.

```
unsigned int GetMaxThreads()
```

Returns the maximum number of threads used for NMF or clustering computations. The default value is hardware-dependent, but is generally the maximum number allowed by the hardware.

```
void SetMaxThreads(const unsigned int max_threads);
```

Sets an upper limit to the number of threads used for NMF and clustering computations. Inputs that exceed the capabilities of the hardware will be adjusted. This function is provided for scaling and performance studies.

```
void Reset()
```

Resets all state variables to their default values.

```
void SeedRNG(const int seed)
```

Seeds the random number generator (RNG) within the smallk library. Normally this RNG is seeded from the system time whenever the library is initialized. The RNG is the '19937' Mersenne Twister implementation provided by the C++ standard library.

```
void LoadMatrix(const std::string& filepath)
```

Loads a matrix contained in the given file. The file must either be a comma-separated value (.CSV) file for a dense matrix, or a MatrixMarket-format file (.MTX) for a sparse matrix. If the matrix cannot be loaded the library throws a `std::runtime_error` exception.

```
bool IsMatrixLoaded()
```

Returns true if a matrix is currently loaded, false if not.

```
std::string GetOutputDir()
```

Returns a string indicating the directory into which output files will be written. The default is the current directory.

```
void SetOutputDir(const std::string& outdir)
```

Sets the directory into which output files should be written. The 'outdir' argument can either be an absolute or relative path. The default is the current directory.

## NMF Functions

```
void Nmf(const unsigned int k,
        const Algorithm algorithm = BPP,
        const std::string& initfile_w = std::string(""),
        const std::string& initfile_h = std::string(""))
```

This function factors the input matrix  $A$  of nonnegative elements into nonnegative factors such that:  $A \sim WH$ . If a matrix is not currently loaded a `std::logic_error` exception will be thrown. The default algorithm is NMF-BPP; provide one of the enumerated algorithm values to use a different algorithm.

Where  $A$  is  $m \times n$ ,  $W$  is  $m \times k$ , and  $H$  is  $k \times n$ . The value of  $k$  is a user defined argument, e.g., for clustering applications,  $k$  is the number of clusters.

Optional initializer matrices can be provided for the  $W$  and  $H$  factors via the 'initfile\_w' and 'initfile\_h' arguments. These files must contain fully dense matrices in .CSV format. The  $W$  matrix initializer must have dimension  $m \times k$ , and the  $H$  matrix initializer must have dimension  $k \times n$ . If the initializer matrices do not match these dimensions exactly a `std::logic_error` exception is thrown. If initializers are not provided, matrices  $W$  and  $H$  will be randomly initialized.

The computed factors  $W$  and  $H$  will be written to the output directory in the files 'w.csv' and 'h.csv'.

Exceptions will be thrown (either from Elemental or smallk) in case of error.

```
const double* LockedBufferW(unsigned int& ldim, unsigned int& height, unsigned int& width)
```

This function returns a READONLY pointer to the buffer containing the  $W$  factor computed by the `Nmf` routine, along with buffer and matrix dimensions. The 'ldim', 'height', and 'width' arguments are all *out* parameters. The buffer has a height of 'ldim' and a width of 'width'. The matrix  $W$  has the same width but a height of 'height', which may differ from ldim. The  $W$  matrix is stored in the buffer in column-major order. See the `examples/smallk_example.cpp` file for an illustration of how to use this function.

```
const double* LockedBufferH(unsigned int& ldim, unsigned int& height, unsigned int& width)
```

Same as `LockedBufferW`, but for the H matrix.

```
double GetNmfTolerance()
```

Returns the tolerance value used to determine NMF convergence. The default value is 0.005.

```
void SetNmfTolerance(const double tol=0.005)
```

Sets the tolerance value used to determine NMF convergence. The NMF algorithms are iterative, and at each iteration a progress metric is computed and compared with the tolerance value. When the metric falls below the tolerance value the iterations stop and convergence is declared. The tolerance value should satisfy  $0.0 < \text{tolerance} < 1.0$ . Any inputs outside this range will cause a `std::logic_error` exception to be thrown.

## Clustering Functions

```
void LoadDictionary(const std::string& filepath)
```

Loads the dictionary used for clustering. The dictionary is an ASCII file of text strings as described in the [preprocessor](#) input files section below. If the dictionary file cannot be loaded a `std::runtime_error` exception is thrown.

```
unsigned int GetMaxTerms()
```

Returns the number of highest-probability dictionary terms to store per cluster. The default value is 5.

```
void SetMaxTerms(const unsigned int max_terms = 5)
```

Sets the number of highest-probability dictionary terms to store per cluster.

```
OutputFormat GetOutputFormat()
```

Returns a member of the `OutputFormat` enumerated type; this is the file format for the clustering results. The default output format is JSON.

```
void SetOutputFormat(const OutputFormat = JSON)
```

Sets the output format for the clustering result file. The argument must be one of the values in the `OutputFormat` enumerated type.

```
double GetHierNmf2Tolerance()
```

Returns the tolerance value used by the NMF-RANK2 algorithm for hierarchical clustering. The default value is  $1.0\text{e-}4$ .

```
void SetHierNmf2Tolerance(const double tol=1.0e-4)
```

Sets the tolerance value used by the NMF-RANK2 algorithm for hierarchical clustering. The tolerance value should satisfy  $0.0 < \text{tolerance} < 1.0$ . Any inputs outside this range will cause a `std::logic_error` exception to be thrown.

```
void HierNmf2(const unsigned int num_clusters)
```

This function performs hierarchical clustering on the loaded matrix, generating the number of clusters specified by the 'num\_clusters' argument. For an overview of the hierarchical clustering process, see the description [below](#) for the hierclust command line application.

This function generates two output files in the output directory: 'assignments\_N.csv' and 'tree\_N.{json, xml}'. Here N is the number of clusters specified as an argument, and the tree file can be in either JSON XML format.

The content of the files is described below in the section on the [hierclust](#) command line application.

```
void HierNmf2WithFlat(const unsigned int num_clusters)
```

This function performs hierarchical clustering on the loaded matrix, exactly as described for `HierNmf2`. In addition, it also computes a flat clustering result. Thus four output files are generated. The flat clustering result files are 'assignments\_flat\_N.csv' and 'clusters\_N.{json, xml}'. The cluster file contents are documented below in the section on the [flatclust](#) command line application.

## V. SmallK Command Line Tools

The SmallK library provides a number of algorithm implementations for low rank approximation of a matrix. These can be used for performing various data analytics tasks such as topic modeling, clustering, and dimension reduction. This section will provide more in-depth description of the tools available with examples that can be expanded/modified for other application domains.

Before diving into the various tools, it will be helpful to set up the command line environment to easily run the various executables that comprise the SmallK library. First the command line needs to know where to find the executable files to run the tools. Since while installing SmallK `'make_install'` was run, the executables are located in `/usr/local/smallk/bin`. Thus, this should be added to the `'$PATH'` system variable or added to the environment. The following command line performs the task of modifying the path avoiding the need to `cd` into directories where the tools are located:

```
export PATH=/usr/local/smallk/bin:$PATH
```

This allows the tools to be executed from any directory.

A subset of these tools are also available from the `pysmallk` library: `smallkapi` (mirrors the NMF command line application), `matrixgen`, `preprocessor`, `flatclust`, and `hierclust`. The command line arguments are the same as those documented below. These tools are available within the `/pysmallk/tests/` directory and can be executed as follows:

```
[python binary] [tool].py [command line arguments]
```

For example:

```
python preprocessor.py --indir data
```

### V.1. Preprocessor

#### Overview

The preprocessor prunes rows and columns from term-frequency matrices, attempting to generate a result matrix that is more suitable for clustering. It also computes tf-idf (term frequency-inverse document frequency) weights for the remaining entries. Therefore the input matrix consists of nonnegative integers, and the output matrix consists of floating point numbers between 0.0 and 1.0. The Matrix Market file format (.mtx file) is used for the input and output matrices.

Rows (terms) are pruned if a given term appears in fewer than `'DOCS_PER_TERM'` documents. The value of `DOCS_PER_TERM` is a command-line parameter with a default value of 3. For a term-frequency input matrix, in which the matrix elements represent occurrence counts for the terms, this parameter actually specifies the minimum row sum for each term. Any rows whose row sums are less than this value will be pruned.

Columns (docs) are pruned if a given document contains fewer than `'TERMS_PER_DOC'` terms. The value of `TERMS_PER_DOC` is a command-line parameter with a default value of 5.

Whenever columns (documents) are pruned the preprocessor checks the remaining columns for uniqueness. Any duplicate columns are identified and a representative column is chosen as the survivor. The code always selects the column with the largest column index in such groups as the survivor. The preprocessor continues to prune rows and columns until it finds no further candidates for pruning. It then computes new tf-idf scores for the resulting entries and writes out the result matrix in Matrix Market format.

If the preprocessor should prune all rows or columns, it writes an error message to the screen and terminates without generating any output.

## Input Files

The preprocessor requires three input files: a matrix file, a dictionary file, and a document file. The matrix file contains a sparse matrix in Matrix Market format (.mtx). This is a term-frequency matrix, and all entries should be positive integers. The preprocessor can also read in matrices containing floating-point inputs, but only if 'boolean mode' is enabled; this will be described below. The preprocessor does not support dense matrices, since the typical matrices encountered in topic modeling problems are extremely sparse, with occupancies generally less than 1%.

The second file required by the preprocessor is a 'dictionary file'. This is a simple ASCII text file containing one entry per line. Entries represent keywords, bigrams, or other general text strings the user is interested in. Each line of the file is treated as a 'keyword'; so multi-word keywords are supported as well. The smallk/data folder contains a sample dictionary file called 'dictionary.txt'. The first few entries are:

```
triumph
dey
canada
finger
circuit
...
```

The third file required by the preprocessor is a 'documents file'. This is another simple ASCII text file containing one entry per line. Entries represent document names or other unique identifiers. The smallk/data folder also contains a sample documents file called 'documents.txt'. The first few entries of this file are:

```
52828-11101.txt
51820-10202.txt
104595-959.txt
60259-3040.txt
...
```

These are the unique document identifiers for the user who generated the file. Your identifiers will likely have a different format.

Finally, the preprocessor **requires** these files to have the following names: matrix.mtx, dictionary.txt, and documents.txt. The input folder containing these files can be specified on the command line (described below). The output of the preprocessor is a new set of files called 'reduced\_matrix.mtx', 'reduced\_dictionary.txt', and 'reduced\_documents.txt'.

## Command Line Options

The preprocessor binary is called 'preprocess\_tf', to emphasize the fact that it operates on term-frequency matrices. If the binary is run with no arguments, it prints out the following information:

```
preprocess_tf
--indir <path>
[--outdir (defaults to current directory)]
[--docs_per_term 3]
[--terms_per_doc 5]
[--maxiter 1000]
[--precision 4]
[--boolean_mode 0]
```

Only the first parameter, --indir, is required. All remaining parameters are optional and have the default values indicated.

The meanings of the various options are as follows:

1. --indir: path to the folder containing the files 'matrix.mtx', 'dictionary.txt', and 'documents.txt'
2. --outdir: path to the folder to into which results should be written
3. --docs\_per\_term: any rows whose entries sum to less than this value will be pruned
4. --terms\_per\_doc: any columns whose entries sum to less than this value will be pruned
5. --maxiter: perform no more than this many iterations

6. `--precision`: the number of digits of precision with which to write the output matrix
7. `--boolean_mode`: all nonzero matrix elements will be treated as if they had the value 1.0. In other words, the preprocessor will ignore the actual frequency counts and treat all nonzero entries as if they were 1.0.

## Sample Runs

Here is a sample run of the preprocessor using the data provided in the smallk distribution. This run was performed from the top-level smallk folder after building the code:

```
preprocess_tf --indir data

    Command line options:

        indir: data/
        outdir: current directory
        docs_per_term: 3
        terms_per_doc: 5
        max_iter: 1000
        precision: 4
        boolean_mode: 0

Loading input matrix data/matrix.mtx
    Input file load time: 1.176s.

Starting iterations...
    [1] height: 39771, width: 11237, nonzeros: 877453
Iterations finished.
    New height: 39727
    New width: 11237
    New nonzero count: 877374
Processing time: 0.074s.

Writing output matrix reduced_matrix.mtx
Output file write time: 2.424s.
Writing dictionary file reduced_dictionary.txt
Writing documents file reduced_documents.txt
Dictionary + documents write time: 0.08s.
```

## V.2. Matrixgen

### Overview

The matrix generator application is a simple tool for generating simple matrices. The NMF and clustering tools for various testing scenarios can load these matrices. Use of the matrix generator is entirely optional.

### Command Line Options

Running the matrixgen binary with no options generates the following output:

```
matrixgen

Usage: matrixgen
    --height <number of rows>
    --width <number of cols>
    --filename <path>
    [--type UNIFORM]  UNIFORM:    matrix with uniformly-distributed random entries
                       DENSE_DIAG: dense diagonal matrix with uniform random entries
                       SPARSE_DIAG: sparse diagonal matrix with uniform random entries
                       IDENTITY:   identity matrix
                       ONES:        matrix of all ones
                       ZEROS:       matrix of all zeros
                       SPARSE:      sparse matrix with uniform random entries
                                specify 'nz_per_col' to control occupancy

    [--rng_center 0.5]  center of random numbers
    [--rng_radius 0.5]  radius of random numbers
    [--precision 6]     digits of precision
    [--nz_per_col 1]    (SPARSE only) nonzeros per column
```

The `--height`, `--width`, and `--filename` options are required. All others are optional and have the default values indicated.

The meanings of the various options are as follows:

1. `--height`: number of rows in the generated matrix
2. `--width`: number of columns in the generated matrix
3. `--filename`: name of the output file
4. `--type`: the type of matrix to be generated; the default is a uniformly-distributed random matrix
5. `--rng_center`: random number distribution will be centered on this value
6. `--rng_radius`: random numbers will span this distance to either side of the center value
7. `--precision`: the number of digits of precision with which to write the output matrix
8. `--nz_per_col`: number of nonzero entries per sparse matrix column; valid only for SPARSE type

### Sample Runs

Suppose we want to generate a matrix of uniformly distributed random numbers. The matrix should have a height of 100 and a width of 16, and should be written to a file called 'w\_init.csv'. Use the matrix generator as follows:

```
matrixgen --height 100 --width 16 --filename w_init.csv
```



## V.3. Nonnegative Matrix Factorization (NMF)

### Overview

The NMF command line application performs nonnegative matrix factorization on dense or sparse matrices. If the input matrix is denoted by  $A$ , nonnegative matrix factors  $W$  and  $H$  are computed such that  $A \sim WH$ . Matrix  $A$  can be either dense or sparse; matrices  $W$  and  $H$  are always dense. Matrix  $A$  has  $m$  rows and  $n$  columns; matrix  $W$  has  $m$  rows and  $k$  columns; matrix  $H$  has  $k$  rows and  $n$  columns. Parameter  $k$  is a positive integer and is typically much less than either  $m$  or  $n$ .

### Command Line Options

Running the nmf application with no command line parameters will cause the application to display all params that it supports. These are:

```
Usage: nmf
  --matrixfile <filename>  Filename of the matrix to be factored.
                           Either CSV format for dense or MatrixMarket format for sparse.
  --k <integer value>      The common dimension for factors W and H.
  [--algorithm BPP]        NMF algorithms:
                           MU:    multiplicative updating
                           HALS:  hierarchical alternating least squares
                           RANK2: rank2 with optimal active set selection
                           BPP:   block principal pivoting
  [--stopping PG_RATIO]    Stopping criterion:
                           PG_RATIO: Ratio of projected gradients
                           DELTA:   Change in relative F-norm of W
  [--tol 0.005]            Tolerance for the selected stopping criterion.
  [--tolcount 1]           Tolerance count; declare convergence after this many
                           iterations with metric < tolerance; default is to
                           declare convergence on the first such iteration.
  [--infile_W (empty)]     Dense mxk matrix to initialize W; CSV file.
                           If unspecified, W will be randomly initialized.
  [--infile_H (empty)]     Dense kxn matrix to initialize H; CSV file.
                           If unspecified, H will be randomly initialized.
  [--outfile_W w.csv]       Filename for the W matrix result.
  [--outfile_H h.csv]       Filename for the H matrix result.
  [--miniter 5]             Minimum number of iterations to perform.
  [--maxiter 5000]          Maximum number of iterations to perform.
  [--outprecision 6]        Write results with this many digits of precision.
  [--maxthreads 8]          Upper limit to thread count.
  [--normalize 1]           Whether to normalize W and scale H.
                           1 == yes, 0 == no
  [--verbose 1]            Whether to print updates to the screen.
                           1 == print updates, 0 == silent
```

The `--matrixfile` and `--k` options are required; all others are optional and have the default values indicated. The meanings of the various options are as follows:

1. `--matrixfile`: Filename of the matrix to be factored. CSV files are supported for dense matrices and MTX files for sparse matrices.
2. `--k`: the width of the  $W$  matrix (identical to the height of the  $H$  matrix)
3. `--algorithm`: identifier for the factorization algorithm
4. `--stopping`: the method used to terminate the iterations; use `PG_RATIO` unless you have a specific reason not to
5. `--tol`: tolerance value used to terminate iterations; when the progress metric falls below this value iterations will stop; typical values are in the  $1.0e-3$  or  $1.0e-4$  range
6. `--tolcount`: a positive integer representing the number of successive iterations for which the progress metric must have a value  $\leq$  tolerance; default is 1, which means the iterations will terminate on the first iteration with `progress_metric`  $\leq$  tolerance
7. `--infile_W`: CSV file containing the  $mxk$  initial values for matrix  $W$ ; if omitted,  $W$  is randomly initialized
8. `--infile_H`: CSV file containing the  $kxn$  initial values for matrix  $H$ ; if omitted,  $H$  is randomly initialized
9. `--outfile_W`: filename for the computed  $W$  factor; default is `w.csv`

10. `--outfile_H`: filename for the computed H factor; default is h.csv
11. `--miniter`: the minimum number of iterations to perform before checking progress; for smaller tolerance values, you may want to increase this number to avoid needless progress checks
12. `--maxiter`: the maximum number of iterations to perform
13. `--outprecision`: matrices W and H will be written to disk using this many digits of precision
14. `--maxthreads`: the maximum number of threads to use; the default is to use as many threads as the hardware can support (your number may differ from that shown)
15. `--normalize`: whether to normalize the columns of the W matrix and correspondingly scale the rows of H after convergence
16. `--verbose`: whether to display updates to the screen as the iterations progress

## Sample Runs

The smallk distribution contains a 'data' directory with a matrix file 'reuters.mtx'. This is a tf-idf weighted matrix derived from the popular Reuters data set used in machine learning experiments.

Suppose we want to factor the Reuters matrix using a k value of 8. We would do that as follows, assuming that we are in the top-level smallk folder after building the code:

```
nmf/bin/nmf --matrixfile data/reuters.mtx --k 8
```

If we want to instead use the HALS algorithm with k=16, a tolerance of 1.0e-4, and also perform 10 iterations prior to checking progress, we would use this command line:

```
nmf/bin/nmf --matrixfile data/reuters.mtx --k 16 --algorithm HALS --tol 1.0e-4 --miniter 10
```

To repeat the previous experiment but with new names for the output files, we would do this:

```
nmf/bin/nmf --matrixfile data/reuters.mtx --k 16 --algorithm HALS --tol 1.0e-4  
--miniter 10 --outfile_W w_hals.csv --outfile_H h_hals.csv
```

## V.4. Hierclust

### Overview

First, we briefly describe the algorithm and the references section provides pointers to papers with detailed descriptions of the algorithms. NMF-RANK2 for hierarchical clustering generates a binary tree of items. We refer to a node in the binary tree and the items associated with the node interchangeably. This method begins by placing all data items in the root node. The number of leaf nodes to generate is specified (user input). The algorithm proceeds with the following steps, repeated until the maximum number of leaf nodes, `max_leaf_nodes`, is reached:

1. Pick the leaf node with the highest score (at the very beginning where only a root node is present, just pick the root node)
2. Apply NMF-RANK2 to the node selected in step 1, and generate two new leaf nodes
3. Compute a score for each of the two leaf nodes generated in step 2
4. Repeat until the desired number of leaf nodes has been generated

Step 2 implements the details of the node splitting into child nodes. Outlier detection plays a crucial role in hierarchical clustering to generate a tree with well-balanced and meaningful clusters. To implement this, we have two additional parameters in step 2: *trial\_allowance* and *unbalanced*.

The parameter *trial\_allowance* is the number of times that the program will try to split a node into two meaningful clusters. In each trial, the program will check if one of the two generated leaf nodes is an outlier set. If the outlier set is detected, the program will delete the items in the outlier set from the node being split and continue to the next trial. If all the trials are finished and the program still cannot find two meaningful clusters for this node, all the deleted items are “recycled” and placed into this node again, and this node will be labeled as a “permanent leaf node” that cannot be picked in step 1 in later iterations.

The parameter *unbalanced* is a threshold parameter to determine whether two generated leaf nodes are unbalanced. Suppose two potential leaf nodes L and R are generated from the selected node and L has fewer items than R. Let us denote the number of items in a node N as  $|N|$ . L and R are called *unbalanced* if  $|L| < \text{unbalanced} * (|L| + |R|)$ . Note that if L and R are unbalanced, the potential node L with fewer items is not necessarily regarded as an outlier set. Please see the referenced paper for more details [3].

Internally, NMF-RANK2 is applied to each leaf node to compute the score in step 3. The computed result matrices W and H in step 3 are cached so that we can avoid duplicate work in step 2 in later iterations.

The score for each leaf node is based on a modified version of the NDCG (*Normalized Discounted Cumulative Gain*) measure, a common measure in the information retrieval community. A leaf node is associated with a “topic vector”, and we can define “top terms” based on the topic vector. A leaf node will receive a high score if its top terms are a good combination of the top terms of its two potential children; otherwise it receives a low score.

The hierclust application generates two output files. One file contains the assignments of documents to clusters. This file contains one integer for each document (column) of the original matrix. The integers are the cluster labels for that cluster that the document was assigned to. If the document could not be assigned to a cluster, a -1 will be entered into the file, indicating that the document is an outlier.

The other output file contains information for each node in the factorization binary tree. The items in this file are:

1. `id`: a unique id for this node
2. `level`: the level in the tree at which this node appears; the root is at level 0, the children of the root are at level 1, etc.
3. `label`: the cluster label for this node (meaningful only for leaf nodes)
4. `parent_id`: the unique id of the parent of this node (the root node has `parent_id == 0`)
5. `parent_label`: the cluster label of the parent of this node

6. `left_child`: a Boolean value indicating whether this node is the left or right child of its parent
7. `left_child_label`: the cluster label of the left child of this node (leaf nodes have -1 for this value)
8. `right_child_label`: the cluster label of the right child of this node (leaf nodes have -1 for this value)
9. `doc_count`: the number of documents that this node represents
10. `top_terms`: the highest probability dictionary terms for this node

The node id values and the left or right child indicators can be used to unambiguously reconstruct the factorization tree.

## Command Line Options

Running the `hierclust` application with no command line parameters will cause the application to display all params that it supports. These are:

`hierclust`

```
Usage: hierclust
--matrixfile <filename>      Filename of the matrix to be factored.
                              Either CSV format for dense or MatrixMarket format for sparse.
--dictfile <filename>        The name of the dictionary file.
--clusters <integer>          The number of clusters to generate.
[--infile_W (empty)]          Dense m x (4*clusters) matrix to initialize W, CSV file.
                              If unspecified, W will be randomly initialized.
[--infile_H (empty)]          Dense (4*clusters) x n matrix to initialize H, CSV file.
                              If unspecified, H will be randomly initialized.
[--tol 0.0001]                Tolerance value for each factorization.
[--outdir (empty)]            Output directory. If unspecified, results will be
                              written to the current directory.
[--miniter 5]                 Minimum number of iterations to perform.
[--maxiter 5000]              Maximum number of iterations to perform.
[--maxterms 5]                Number of terms per node.
[--maxthreads 8]              Upper limit to thread count.
[--unbalanced 0.1]            Threshold for determining leaf node imbalance.
[--trial_allowance 3]          Number of split attempts.
[--flat 0]                    Whether to generate a flat clustering result.
                              1 == yes, 0 == no
[--verbose 1]                 Whether to print updates to the screen.
                              1 == yes, 0 == no
[--format XML]                Format of the output file containing the tree.
                              XML: XML format
                              JSON: JavaScript Object Notation
[--treefile tree_N.ext]        Name of the output file containing the tree.
                              N is the number of clusters for this run.
                              The string 'ext' depends on the desired format.
                              This filename is relative to the outdir.
[--assignfile assignments_N.csv] Name of the file containing final assignments.
                              N is the number of clusters for this run.
                              This filename is relative to the outdir.
```

The `--matrixfile`, `--dictfile`, and `--clusters` options are required; all others are optional and have the default values indicated. The meanings of the various options are as follows:

1. `--matrixfile`: Filename of the matrix to be factored. CSV files are supported for dense matrices and MTX files for sparse matrices.
2. `--dictfile`: absolute or relative path to the dictionary file
3. `--clusters`: the number of leaf nodes (clusters) to generate
4. `--infile_W`: CSV file containing the  $m \times (4 \times \text{clusters})$  initial values for matrix W; if omitted, W is randomly initialized
5. `--infile_H`: CSV file containing the  $(4 \times \text{clusters}) \times n$  initial values for matrix H; if omitted, H is randomly initialized
6. `--tol`: tolerance value for each internal NMF-RANK2 factorization; the stopping criterion is the ratio of projected gradient method
7. `--outdir`: path to the folder into which to write the output files; if omitted results will be written to the current directory
8. `--miniter`: minimum number of iterations to perform before checking progress on each NMF-RANK2 factorization
9. `--maxiter`: the maximum number of iterations to perform on each NMF-RANK2 factorization

10. `--maxterms`: the number of dictionary keywords to include in each node
11. `--maxthreads`: the maximum number of threads to use; the default is to use as many threads as the hardware can support (your number may differ from that shown)
12. `--unbalanced`: threshold value for declaring leaf node imbalance (see explanation above)
13. `--trial_allowance`: maximum number of split attempts for any node (see explanation above)
14. `--flat`: whether to generate a flat clustering result in addition to the hierarchical clustering result
15. `--verbose`: whether to display updates to the screen as the iterations progress
16. `--format`: file format to use for the clustering results
17. `--treefile`: name of the output file for the factorization tree; uses the format specified by the `format` parameter
18. `--assignfile`: name of the output file for the cluster assignments

## Sample Runs

The `smallk` distribution contains a 'data' directory with a matrix file 'reuters.mtx' and an associated dictionary file 'reuters\_dictionary.txt'. These files are derived from the popular Reuters data set used in machine learning experiments.

Suppose we want to perform hierarchical clustering on this data set and generate 10 leaf nodes. We would do that as follows, assuming that we are in the top-level `smallk` folder after building the code:

```
hierclust/bin/hierclust --matrixfile data/reuters.mtx --dictfile data/reuters_dictionary.txt
--clusters 10
```

This will generate two result files in the current directory: `tree_10.xml` and `assignments_10.csv`.

If we want to instead generate 10 clusters, each with 8 terms, using JSON output format, we would use this command line:

```
hierclust/bin/hierclust --matrixfile data/reuters.mtx --dictfile data/reuters_dictionary.txt
--clusters 10 --maxterms 8 --format JSON
```

Two files will be generated: `tree_10.json` and `assignments_10.csv`. The json file will have 8 keywords per node, whereas the `tree_10.xml` file will have only 5.

To generate a flat clustering result (in addition to the hierarchical clustering result), use this command line:

```
hierclust/bin/hierclust --matrixfile data/reuters.mtx --dictfile data/reuters_dictionary.txt
--clusters 10 --maxterms 8 --format JSON --flat 1
```

Two additional files will be generated this time (along with `tree_10.json` and `assignments_10.csv`): 'clusters\_10.json', which contains the flat clustering results, and 'assignments\_flat\_10.csv', which contains the flat clustering assignments.

## V.5. Flatclust

### Overview

The flatclust command line application factors the input matrix using either NMF-HALS or NMF-BPP and generates a flat clustering result. A flatclust run generating  $k$  clusters will generally run more slowly than a hierclust run, of the same number of clusters, with the `--flat` option enabled. The reason for this is that the hierclust application uses the NMF-RANK2 algorithm and always generates factor matrices with two rows or columns. The runtime of NMF scales super linearly with  $k$ , and thus runs fastest for the smallest  $k$  value.

The flatclust application generates two output files. The first file contains the assignments of documents to clusters and is interpreted identically to that of the hierclust application, with the exception that there are no outliers generated by flatclust.

The second file contains the node information. This file is much simpler than that of the hierclust application since there is no factorization tree. The items for each node in this file are:

1. `id`: the unique id of this node
2. `doc_count`: the number of documents assigned to this node
3. `top_terms`: the highest probability dictionary terms assigned to this node

### Command Line Options

Running the flatclust application with no command line parameters will cause the application to display all params that it supports. These are:

flatclust

```
Usage: flatclust
--matrixfile <filename>      Filename of the matrix to be factored.
                              Either CSV format for dense or MatrixMarket format for sparse.
--dictfile <filename>        The name of the dictionary file.
--clusters <integer>         The number of clusters to generate.
--algorithm BPP              The NMF algorithm to use:
                              HALS: hierarchical alternating least squares
                              RANK2: rank2 with optimal active set selection
                              (for two clusters only)
                              BPP: block principal pivoting
--infile_W (empty)           Dense matrix to initialize W, CSV file.
                              The matrix has m rows and 'clusters' columns.
                              If unspecified, W will be randomly initialized.
--infile_H (empty)           Dense matrix to initialize H, CSV file.
                              The matrix has 'clusters' rows and n columns.
                              If unspecified, H will be randomly initialized.
--tol 0.0001                 Tolerance value for the progress metric.
--outdir (empty)             Output directory. If unspecified, results will be
                              written to the current directory.
--miniter 5                  Minimum number of iterations to perform.
--maxiter 5000               Maximum number of iterations to perform.
--maxterms 5                 Number of terms per node.
--maxthreads 8               Upper limit to thread count.
--verbose 1                  Whether to print updates to the screen.
                              1 == yes, 0 == no
--format XML                  Format of the output file containing the tree.
                              XML: XML format
                              JSON: JavaScript Object Notation
--clustfile clusters_N.ext    Name of the output XML file containing the tree.
                              N is the number of clusters for this run.
                              The string 'ext' depends on the desired format.
                              This filename is relative to the outdir.
--assignfile assignments_N.csv Name of the file containing final assignments.
                              N is the number of clusters for this run.
                              This filename is relative to the outdir.
```

The `--matrixfile`, `--dictfile`, and `--clusters` options are required; all others are optional and have the default values indicated. The meanings of the various options are as follows:

1. `--matrixfile`: Filename of the matrix to be factored. CSV files are supported for dense matrices and MTX files for sparse matrices.
2. `--dictfile`: absolute or relative path to the dictionary file
3. `--clusters`: the number of clusters to generate (equivalent to the NMF ' $k$ ' value)

4. `--algorithm`: the factorization algorithm to use
5. `--infile_W`: CSV file containing the  $m \times \text{'clusters'}$  initial values for matrix  $W$ ; if omitted,  $W$  is randomly initialized
6. `--infile_H`: CSV file containing the  $\text{'clusters'} \times n$  initial values for matrix  $H$ ; if omitted,  $H$  is randomly initialized
7. `--tol`: tolerance value for the factorization; the stopping criterion is the ratio of projected gradient method
8. `--outdir`: path to the folder into which to write the output files; if omitted results will be written to the current directory
9. `--miniter`: minimum number of iterations to perform before checking progress
10. `--maxiter`: the maximum number of iterations to perform
11. `--maxterms`: the number of dictionary keywords to include in each node
12. `--maxthreads`: the maximum number of threads to use; the default is to use as many threads as the hardware can support (your number may differ from that shown)
13. `--verbose`: whether to display updates to the screen as the iterations progress
14. `--format`: file format to use for the clustering results
15. `--clustfile`: name of the output file for the nodes; uses the format specified by the format parameter
16. `--assignfile`: name of the output file for the cluster assignments

## Sample Run

The `smallk` distribution contains a `'data'` directory with a matrix file `'reuters.mtx'` and an associated dictionary file `'reuters_dictionary.txt'`. These files are derived from the popular Reuters data set used in machine learning experiments.

Suppose we want to perform flat clustering on this data set and generate 10 clusters. We would do that as follows, assuming that we are in the top-level `smallk` folder after building the code:

```
flatclust/bin/flatclust --matrixfile data/reuters.mtx --dictfile data/reuters_dictionary.txt
--clusters 10
```

This will generate two result files in the current directory: `clusters_10.xml` and `assignments_10.csv`.

If we want to instead generate 10 clusters, each with 8 terms, using JSON output format, we would use this command line:

```
flatclust/bin/flatclust --matrixfile data/reuters.mtx --dictfile data/reuters_dictionary.txt
--clusters 10 --maxterms 8 --format JSON
```

Two files will be generated: `clusters_10.json` and `assignments_10.csv`. The json file will have 8 keywords per node, whereas the `clusters_10.xml` file will have only 5.

## V.6. SmallK Test Results

After building the SmallK library, the 'make check' command will run a bash script that performs a series of tests on the code. Below is a sample output of those tests:

```
make check
sh tests/scripts/test_smallk.sh ../xdata_data | tee smallk_test_results.txt
*****
*                                     *
*           Testing the smallk interface.           *
*                                     *
*****
WARNING: Could not achieve THREAD_MULTIPLE support.
Smallk major version: 1
Smallk minor version: 6
Smallk patch level: 0
Smallk version string: 1.6.0
Loading matrix...

Running NMF-BPP...

Initializing matrix W...
Initializing matrix H...

        parameters:

        algorithm: Nonnegative Least Squares with Block Principal Pivoting
        stopping criterion: Ratio of Projected Gradients
            height: 12411
            width: 7984
            k: 8
        miniter: 1
        maxiter: 5000
            tol: 0.005
        matrixfile: ../xdata_data/reuters.mtx
        maxthreads: 8

1:   progress metric:   (min_iter)
2:   progress metric:   0.35826
3:   progress metric:   0.172127
4:   progress metric:   0.106297
5:   progress metric:   0.0696424
6:   progress metric:   0.0538889
7:   progress metric:   0.0559478
8:   progress metric:   0.0686117
9:   progress metric:   0.0788641
10:  progress metric:   0.0711522
20:  progress metric:   0.00568349

Solution converged after 22 iterations.

Elapsed wall clock time: 0.527 sec.

Writing output files...

Running HierNmf2...

loading dictionary...
creating random W initializers...
creating random H initializers...

        parameters:

            height: 12411
            width: 7984
        matrixfile: ../xdata_data/reuters.mtx
        dictfile: ../xdata_data/reuters_dictionary.txt
            tol: 0.0001
        miniter: 1
        maxiter: 5000
        maxterms: 5
        maxthreads: 8

[1] [2] [3] [4]

Elapsed wall clock time: 572 ms.
9/9 factorizations converged.

Writing output files...
W matrix test passed
H matrix test passed
*****
*                                     *
*           Testing the preprocessor.           *
*                                     *
*****

        Command line options:
```



```

        indir: ../xdata_data/
        outdir: current directory
docs_per_term: 3
terms_per_doc: 5
        max_iter: 1000
        precision: 4
        boolean_mode: 0

Loading input matrix ../xdata_data/matrix.mtx
Input file load time: 1.3s.

Starting iterations...
[1] height: 39771, width: 11237, nonzeros: 877453
Iterations finished.
    New height: 39727
    New width: 11237
    New nonzero count: 877374
Processing time: 0.048s.

Writing output matrix 'reduced_matrix.mtx'
Output file write time: 1.624s.
Writing pruned term-frequency matrix 'reduced_matrix_tf.mtx'
Output term-frequency matrix write time: 1.558s.
Writing dictionary file 'reduced_dictionary.txt'
Writing documents file 'reduced_documents.txt'
Dictionary + documents write time: 0.074s.
preprocessor matrix test passed
preprocessor dictionary test passed
preprocessor documents test passed
*****
*                                     *
*           Testing the NMF routines.           *
*                                     *
*****
WARNING: Could not achieve THREAD_MULTIPLE support.
Loading matrix...
Initializing matrix W...
Initializing matrix H...

Command line options:

        algorithm: Nonnegative Least Squares with Block Principal Pivoting
stopping criterion: Ratio of Projected Gradients
        height: 12411
        width: 7984
        k: 8
        miniter: 1
        maxiter: 5000
        tol: 0.005
        tolcount: 1
        verbose: 1
        normalize: 1
        outprecision: 6
        matrixfile: ../xdata_data/reuters.mtx
        infile_W: ../xdata_data/nmf_init_w.csv
        infile_H: ../xdata_data/nmf_init_h.csv
        outfile_W: w.csv
        outfile_H: h.csv
        maxthreads: 8

1:   progress metric:   (min_iter)
2:   progress metric:   0.35826
3:   progress metric:   0.172127
4:   progress metric:   0.106297
5:   progress metric:   0.0696424
6:   progress metric:   0.0538889
7:   progress metric:   0.0559478
8:   progress metric:   0.0686117
9:   progress metric:   0.0788641
10:  progress metric:   0.0711522
20:  progress metric:   0.00568349

Solution converged after 22 iterations.

Elapsed wall clock time: 0.527 sec.

Writing output files...
NMF W matrix test passed
NMF H matrix test passed
*****
*                                     *
*           Testing hierclust.           *
*                                     *
*****
WARNING: Could not achieve THREAD_MULTIPLE support.
loading dictionary...
loading matrix...
loading W initializers...

```

loading H initializers...

Command line options:

```
height: 12411
width: 7984
matrixfile: ../xdata_data/reuters.mtx
infile_W: ../xdata_data/hierclust_init_w.csv
infile_H: ../xdata_data/hierclust_init_h.csv
dictfile: ../xdata_data/reuters_dictionary.txt
assignfile: assignments_5.csv
format: XML
treefile: tree_5.xml
clusters: 5
tol: 0.0001
outdir:
miniter: 1
maxiter: 5000
maxterms: 5
maxthreads: 8
unbalanced: 0.1
trial_allowance: 3
flat: 0
verbose: 1
```

[1] [2] [3] [4]

Elapsed wall clock time: 734 ms.

9/9 factorizations converged.

Writing output files...

hierclust cluster file test passed

hierclust assignment file test passed

```
*****
*                                     *
*           Testing flatclust.         *
*                                     *
*****
```

WARNING: Could not achieve THREAD\_MULTIPLE support.

loading dictionary...

loading matrix...

Initializing matrix W...

Initializing matrix H...

Command line options:

```
height: 256
width: 256
matrixfile: ../xdata_data/rnd_256_256.csv
infile_W: ../xdata_data/flatclust_init_w.csv
infile_H: ../xdata_data/flatclust_init_h.csv
dictfile: ../xdata_data/reuters_dictionary.txt
assignfile: assignments_16.csv
format: XML
clustfile: clusters_16.xml
algorithm: HALS
clusters: 16
tol: 0.0001
outdir:
miniter: 1
maxiter: 5000
maxterms: 5
maxthreads: 8
verbose: 1
```

```
1:   progress metric:   (min_iter)
2:   progress metric:   0.635556
3:   progress metric:   0.490817
4:   progress metric:   0.479135
5:   progress metric:   0.474986
6:   progress metric:   0.44968
7:   progress metric:   0.422542
8:   progress metric:   0.407662
9:   progress metric:   0.395145
10:  progress metric:   0.379238
20:  progress metric:   0.272868
30:  progress metric:   0.168386
40:  progress metric:   0.109147
50:  progress metric:   0.0767327
60:  progress metric:   0.0488545
70:  progress metric:   0.036226
80:  progress metric:   0.0307648
90:  progress metric:   0.0266116
100: progress metric:   0.0226963
110: progress metric:   0.0188616
120: progress metric:   0.0158307
130: progress metric:   0.0137605
140: progress metric:   0.0127888
150: progress metric:   0.0123962
```

160: progress metric: 0.0124734  
170: progress metric: 0.0123563  
180: progress metric: 0.0122163  
190: progress metric: 0.0120643  
200: progress metric: 0.0117647  
210: progress metric: 0.0114894  
220: progress metric: 0.0110467  
230: progress metric: 0.0107816  
240: progress metric: 0.0105239  
250: progress metric: 0.0103824  
260: progress metric: 0.0100915  
270: progress metric: 0.00965073  
280: progress metric: 0.00938526  
290: progress metric: 0.00914129  
300: progress metric: 0.00896701  
310: progress metric: 0.00886729  
320: progress metric: 0.00841059  
330: progress metric: 0.007793  
340: progress metric: 0.00740095  
350: progress metric: 0.00708869  
360: progress metric: 0.00683069  
370: progress metric: 0.00672093  
380: progress metric: 0.00687906  
390: progress metric: 0.00703777  
400: progress metric: 0.00721928  
410: progress metric: 0.00729384  
420: progress metric: 0.00718332  
430: progress metric: 0.00722893  
440: progress metric: 0.00726766  
450: progress metric: 0.00739665  
460: progress metric: 0.00769819  
470: progress metric: 0.00814673  
480: progress metric: 0.008566  
490: progress metric: 0.00877955  
500: progress metric: 0.00884221  
510: progress metric: 0.0088057  
520: progress metric: 0.00852345  
530: progress metric: 0.00797952  
540: progress metric: 0.00749354  
550: progress metric: 0.00689316  
560: progress metric: 0.00623287  
570: progress metric: 0.00576619  
580: progress metric: 0.00541125  
590: progress metric: 0.00501715  
600: progress metric: 0.00466547  
610: progress metric: 0.00432811  
620: progress metric: 0.00412669  
630: progress metric: 0.00383406  
640: progress metric: 0.00352802  
650: progress metric: 0.00331556  
660: progress metric: 0.00315735  
670: progress metric: 0.00304253  
680: progress metric: 0.00296627  
690: progress metric: 0.00289013  
700: progress metric: 0.00279647  
710: progress metric: 0.00271036  
720: progress metric: 0.00261087  
730: progress metric: 0.0025158  
740: progress metric: 0.00245123  
750: progress metric: 0.00237435  
760: progress metric: 0.00231126  
770: progress metric: 0.00228199  
780: progress metric: 0.00227623  
790: progress metric: 0.00228185  
800: progress metric: 0.00227993  
810: progress metric: 0.00228216  
820: progress metric: 0.00228018  
830: progress metric: 0.00229096  
840: progress metric: 0.00232403  
850: progress metric: 0.00234957  
860: progress metric: 0.00227868  
870: progress metric: 0.00210786  
880: progress metric: 0.00195462  
890: progress metric: 0.00183587  
900: progress metric: 0.00173358  
910: progress metric: 0.0016405  
920: progress metric: 0.00156422  
930: progress metric: 0.00150835  
940: progress metric: 0.00146594  
950: progress metric: 0.00143261  
960: progress metric: 0.00137378  
970: progress metric: 0.00131989  
980: progress metric: 0.00126626  
990: progress metric: 0.0012164  
1000: progress metric: 0.00117061  
1010: progress metric: 0.00112539  
1020: progress metric: 0.00108626  
1030: progress metric: 0.00105192  
1040: progress metric: 0.00102131

1050: progress metric: 0.000992069  
1060: progress metric: 0.000965259  
1070: progress metric: 0.000938949  
1080: progress metric: 0.000911962  
1090: progress metric: 0.000884505  
1100: progress metric: 0.000854904  
1110: progress metric: 0.000820121  
1120: progress metric: 0.000785245  
1130: progress metric: 0.000752513  
1140: progress metric: 0.000723279  
1150: progress metric: 0.000697698  
1160: progress metric: 0.000680904  
1170: progress metric: 0.000652152  
1180: progress metric: 0.000628268  
1190: progress metric: 0.000612413  
1200: progress metric: 0.000596834  
1210: progress metric: 0.000580674  
1220: progress metric: 0.000556549  
1230: progress metric: 0.000535666  
1240: progress metric: 0.00051492  
1250: progress metric: 0.000496234  
1260: progress metric: 0.000481147  
1270: progress metric: 0.000461294  
1280: progress metric: 0.000440802  
1290: progress metric: 0.000419049  
1300: progress metric: 0.000398007  
1310: progress metric: 0.000376203  
1320: progress metric: 0.000355811  
1330: progress metric: 0.00033729  
1340: progress metric: 0.000318932  
1350: progress metric: 0.000302528  
1360: progress metric: 0.000287961  
1370: progress metric: 0.00027486  
1380: progress metric: 0.00026403  
1390: progress metric: 0.000255504  
1400: progress metric: 0.000248646  
1410: progress metric: 0.000242996  
1420: progress metric: 0.000239243  
1430: progress metric: 0.000236852  
1440: progress metric: 0.000235313  
1450: progress metric: 0.000234465  
1460: progress metric: 0.000234154  
1470: progress metric: 0.000234253  
1480: progress metric: 0.00023487  
1490: progress metric: 0.000237223  
1500: progress metric: 0.000240043  
1510: progress metric: 0.000243896  
1520: progress metric: 0.00024867  
1530: progress metric: 0.000253981  
1540: progress metric: 0.000260239  
1550: progress metric: 0.000266795  
1560: progress metric: 0.000273529  
1570: progress metric: 0.000280678  
1580: progress metric: 0.000287273  
1590: progress metric: 0.000292288  
1600: progress metric: 0.000296475  
1610: progress metric: 0.000299556  
1620: progress metric: 0.00030244  
1630: progress metric: 0.000306148  
1640: progress metric: 0.000310299  
1650: progress metric: 0.000314674  
1660: progress metric: 0.000319052  
1670: progress metric: 0.000323906  
1680: progress metric: 0.000329536  
1690: progress metric: 0.000335913  
1700: progress metric: 0.000342834  
1710: progress metric: 0.000351167  
1720: progress metric: 0.000352515  
1730: progress metric: 0.000348749  
1740: progress metric: 0.000345684  
1750: progress metric: 0.000343139  
1760: progress metric: 0.000340867  
1770: progress metric: 0.000339052  
1780: progress metric: 0.000337038  
1790: progress metric: 0.000335244  
1800: progress metric: 0.000333452  
1810: progress metric: 0.000332111  
1820: progress metric: 0.000330198  
1830: progress metric: 0.000325983  
1840: progress metric: 0.000321473  
1850: progress metric: 0.000316999  
1860: progress metric: 0.000312054  
1870: progress metric: 0.000305176  
1880: progress metric: 0.000294684  
1890: progress metric: 0.000284482  
1900: progress metric: 0.000274905  
1910: progress metric: 0.000265684  
1920: progress metric: 0.000256761  
1930: progress metric: 0.000248203

```

1940: progress metric: 0.000239613
1950: progress metric: 0.000230677
1960: progress metric: 0.00022218
1970: progress metric: 0.000214089
1980: progress metric: 0.00020621
1990: progress metric: 0.000196915
2000: progress metric: 0.000187712
2010: progress metric: 0.000179199
2020: progress metric: 0.00017137
2030: progress metric: 0.000164158
2040: progress metric: 0.000157751
2050: progress metric: 0.000152485
2060: progress metric: 0.000147217
2070: progress metric: 0.000142083
2080: progress metric: 0.000137148
2090: progress metric: 0.000132379
2100: progress metric: 0.000127922
2110: progress metric: 0.000123617
2120: progress metric: 0.000119548
2130: progress metric: 0.000115684
2140: progress metric: 0.000111997
2150: progress metric: 0.000108389
2160: progress metric: 0.000104838
2170: progress metric: 0.000101387

```

Solution converged after 2175 iterations.

Elapsed wall clock time: 1.088 sec.

XML file test passed

assignment file test passed

```

PYTHONPATH=/Users/AshleyScripka/development/xdata/xdata3/pysmallk \
sh tests/scripts/test_pysmallk.sh ../xdata_data | tee pysmallk_test_results.txt

```

```

*****
*          pysmallk - command line          *
*                                           *
*          Testing the smallk interface.    *
*                                           *
*****

```

WARNING: Could not achieve THREAD\_MULTIPLE support.

Smallk major version: 1

Smallk minor version: 6

Smallk patch level: 0

Smallk version string: 1.6.0

Loading matrix...

Initializing matrix W...

Initializing matrix H...

parameters:

```

          algorithm: Nonnegative Least Squares with Block Principal Pivoting
stopping criterion: Ratio of Projected Gradients
          height: 12411
          width: 7984
            k: 8
        miniter: 10
        maxiter: 10000
          tol: 1e-06
matrixfile: ../xdata_data/reuters.mtx
maxthreads: 3

```

```

1:   progress metric: (min_iter)
2:   progress metric: (min_iter)
3:   progress metric: (min_iter)
4:   progress metric: (min_iter)
5:   progress metric: (min_iter)
6:   progress metric: (min_iter)
7:   progress metric: (min_iter)
8:   progress metric: (min_iter)
9:   progress metric: (min_iter)
10:  progress metric: (min_iter)
20:  progress metric: 0.0136316
30:  progress metric: 0.0137726
40:  progress metric: 0.0245057
50:  progress metric: 0.0116725
60:  progress metric: 0.00360188
70:  progress metric: 0.00217558
80:  progress metric: 0.0014568
90:  progress metric: 0.00105926
100: progress metric: 0.000786066
110: progress metric: 0.000591568
120: progress metric: 0.000455298
130: progress metric: 0.000367745
140: progress metric: 0.000301608
150: progress metric: 0.00025159
160: progress metric: 0.000214166
170: progress metric: 0.000179538
180: progress metric: 0.000150486
190: progress metric: 0.000126573

```

```

200: progress metric: 0.000106425
210: progress metric: 8.94514e-05
220: progress metric: 7.49182e-05
230: progress metric: 6.2246e-05
240: progress metric: 5.20659e-05
250: progress metric: 4.38092e-05
260: progress metric: 3.68644e-05
270: progress metric: 3.10176e-05
280: progress metric: 1.12734e-05
290: progress metric: 4.10858e-06
300: progress metric: 1.49856e-06

```

Solution converged after 305 iterations.

Elapsed wall clock time: 9.725 sec.

Writing output files...  
 Initializing matrix W...  
 Initializing matrix H...

parameters:

```

algorithm: Nonnegative Least Squares with Block Principal Pivoting
stopping criterion: Ratio of Projected Gradients
height: 12411
width: 7984
k: 8
miniter: 1
maxiter: 5000
tol: 0.005
matrixfile: ../xdata_data/reuters.mtx
maxthreads: 8

```

```

1: progress metric: (min iter)
2: progress metric: 0.35826
3: progress metric: 0.172127
4: progress metric: 0.106297
5: progress metric: 0.0696424
6: progress metric: 0.0538889
7: progress metric: 0.0559478
8: progress metric: 0.0686117
9: progress metric: 0.0788641
10: progress metric: 0.0711522
20: progress metric: 0.00568349

```

Solution converged after 22 iterations.

Elapsed wall clock time: 0.965 sec.

Writing output files...  
 loading dictionary...  
 creating random W initializers...  
 creating random H initializers...

parameters:

```

height: 12411
width: 7984
matrixfile: ../xdata_data/reuters.mtx
dictfile: ../xdata_data/reuters_dictionary.txt
tol: 0.0001
miniter: 1
maxiter: 5000
maxterms: 5
maxthreads: 8

```

[1] [2] [3] [4]

Elapsed wall clock time: 533 ms.

9/9 factorizations converged.

Writing output files...  
 W matrix test passed  
 H matrix test passed

```

*****
* pysmallk - in memory *
* *
* Testing the smallk interface. *
* *
*****

```

WARNING: Could not achieve THREAD\_MULTIPLE support.

pysmallk/tests/smallkapi\_inmem.py:59: FutureWarning: comparison to `None` will result in an elementwise object comparison in the future.

```

height=matrix.shape[0], width=matrix.shape[1], nz=len(data))
Loading sparse matrix...
Initializing matrix W...
Initializing matrix H...

```

parameters:

```

        algorithm: Nonnegative Least Squares with Block Principal Pivoting
    stopping criterion: Ratio of Projected Gradients
        height: 12411
        width: 7984
        k: 8
        miniter: 1
        maxiter: 5000
        tol: 0.005
        matrixfile:
        maxthreads: 8

1:    progress metric:    (min_iter)
2:    progress metric:    0.35826
3:    progress metric:    0.172127
4:    progress metric:    0.106297
5:    progress metric:    0.0696424
6:    progress metric:    0.0538889
7:    progress metric:    0.0559478
8:    progress metric:    0.0686117
9:    progress metric:    0.0788641
10:   progress metric:    0.0711522
20:   progress metric:    0.00568349

Solution converged after 22 iterations.

Elapsed wall clock time: 0.939 sec.

Writing output files...
W matrix test passed
H matrix test passed
*****
*          pysmallk - command line          *
*                                           *
*          Testing the preprocessor.         *
*                                           *
*****
WARNING: Could not achieve THREAD_MULTIPLE support.
Default output directory: current directory

Starting iterations...
[1] height: 39771, width: 11237, nonzeros: 877453
Iterations finished.
    New height: 39727
    New width: 11237
    New nonzero count: 877374
preprocessor matrix test passed
preprocessor dictionary test passed
preprocessor documents test passed
*****
*          pysmallk - in memory             *
*                                           *
*          Testing the preprocessor.         *
*                                           *
*****
WARNING: Could not achieve THREAD_MULTIPLE support.
pysmallk/tests/preprocessor_inmem.py:83: FutureWarning: comparison to `None` will result in an elementwise
object comparison in the future.
    p.load_inputmatrix(height=height, width=width, nz=nz, buffer=data, row_indices=row_indices,
col_offsets=col_offsets)
about to call python load_sparse
Loading sparse matrix...

Starting iterations...
[1] height: 39771, width: 11237, nonzeros: 877453
Iterations finished.
    New height: 39727
    New width: 11237
    New nonzero count: 877374
preprocessor matrix test passed
preprocessor dictionary test passed
preprocessor documents test passed
*****
*          pysmallk - command line          *
*                                           *
*          Testing hierclust.               *
*                                           *
*****
WARNING: Could not achieve THREAD_MULTIPLE support.
1:    progress metric:    (min_iter)
2:    progress metric:    (min_iter)
3:    progress metric:    (min_iter)
4:    progress metric:    (min_iter)
5:    progress metric:    (min_iter)
6:    progress metric:    0.0374741
7:    progress metric:    0.0252389
8:    progress metric:    0.0169805
9:    progress metric:    0.0113837
10:   progress metric:    0.00761077
20:   progress metric:    0.000130604

```

Solution converged after 21 iterations.

```
1:   progress metric:   (min_iter)
2:   progress metric:   (min_iter)
3:   progress metric:   (min_iter)
4:   progress metric:   (min_iter)
5:   progress metric:   (min_iter)
6:   progress metric:   0.0371935
7:   progress metric:   0.0431956
8:   progress metric:   0.056867
9:   progress metric:   0.0745391
10:  progress metric:   0.0890112
20:  progress metric:   0.092225
30:  progress metric:   0.00649718
40:  progress metric:   0.00224739
50:  progress metric:   0.000846835
60:  progress metric:   0.000303034
70:  progress metric:   0.000107818
```

Solution converged after 71 iterations.

```
1:   progress metric:   (min_iter)
2:   progress metric:   (min_iter)
3:   progress metric:   (min_iter)
4:   progress metric:   (min_iter)
5:   progress metric:   (min_iter)
6:   progress metric:   0.0278454
7:   progress metric:   0.0153121
8:   progress metric:   0.0084199
9:   progress metric:   0.00463192
10:  progress metric:   0.0025471
```

Solution converged after 16 iterations.

```
[1] 1: progress metric:   (min_iter)
2:   progress metric:   (min_iter)
3:   progress metric:   (min_iter)
4:   progress metric:   (min_iter)
5:   progress metric:   (min_iter)
6:   progress metric:   0.011482
7:   progress metric:   0.0088452
8:   progress metric:   0.00709218
9:   progress metric:   0.00576048
10:  progress metric:   0.00474146
20:  progress metric:   0.00145962
30:  progress metric:   0.00060763
40:  progress metric:   0.000297382
50:  progress metric:   0.000148919
```

Solution converged after 57 iterations.

```
1:   progress metric:   (min_iter)
2:   progress metric:   (min_iter)
3:   progress metric:   (min_iter)
4:   progress metric:   (min_iter)
5:   progress metric:   (min_iter)
6:   progress metric:   0.0476236
7:   progress metric:   0.034979
8:   progress metric:   0.0255046
9:   progress metric:   0.0179983
10:  progress metric:   0.0131529
20:  progress metric:   0.00233685
30:  progress metric:   0.00061225
40:  progress metric:   0.000172714
```

Solution converged after 45 iterations.

```
[2] 1: progress metric:   (min_iter)
2:   progress metric:   (min_iter)
3:   progress metric:   (min_iter)
4:   progress metric:   (min_iter)
5:   progress metric:   (min_iter)
6:   progress metric:   0.0348016
7:   progress metric:   0.0168893
8:   progress metric:   0.0087407
9:   progress metric:   0.00469118
10:  progress metric:   0.00255868
```

Solution converged after 16 iterations.

```
1:   progress metric:   (min_iter)
2:   progress metric:   (min_iter)
3:   progress metric:   (min_iter)
4:   progress metric:   (min_iter)
5:   progress metric:   (min_iter)
6:   progress metric:   0.0732844
7:   progress metric:   0.077964
8:   progress metric:   0.0906559
```



```

9:    progress metric:    0.0999774
10:   progress metric:    0.0994555
20:   progress metric:    0.00114661

```

Solution converged after 25 iterations.

```

[3] 1: progress metric:    (min_iter)
2:    progress metric:    (min_iter)
3:    progress metric:    (min_iter)
4:    progress metric:    (min_iter)
5:    progress metric:    (min_iter)
6:    progress metric:    0.0710298
7:    progress metric:    0.038312
8:    progress metric:    0.021048
9:    progress metric:    0.0117472
10:   progress metric:    0.00662412

```

Solution converged after 18 iterations.

```

1:    progress metric:    (min_iter)
2:    progress metric:    (min_iter)
3:    progress metric:    (min_iter)
4:    progress metric:    (min_iter)
5:    progress metric:    (min_iter)
6:    progress metric:    0.0801544
7:    progress metric:    0.072948
8:    progress metric:    0.0736511
9:    progress metric:    0.0752686
10:   progress metric:    0.0718868
20:   progress metric:    0.0192989
30:   progress metric:    0.0121039
40:   progress metric:    0.00743925
50:   progress metric:    0.00544292
60:   progress metric:    0.00557543
70:   progress metric:    0.00725721
80:   progress metric:    0.0123311
90:   progress metric:    0.0359475
100:  progress metric:    0.104473
110:  progress metric:    0.0239986
120:  progress metric:    0.01361
130:  progress metric:    0.00776367
140:  progress metric:    0.00349198
150:  progress metric:    0.000247399

```

Solution converged after 153 iterations.

```

[4]
Writing output files...
hierclust cluster file test passed
hierclust assignment file test passed
*****
*          pysmallk - in memory          *
*                                         *
*          Testing hierclust.            *
*                                         *
*****
WARNING: Could not achieve THREAD_MULTIPLE support.
pysmallk/tests/hierclust_inmem.py:50: FutureWarning: comparison to `None` will result in an elementwise object
comparison in the future.
    height=matrix.shape[0], width=matrix.shape[1], nz=len(data))
about to call python load_sparse
Loading sparse matrix...
1:    progress metric:    (min_iter)
2:    progress metric:    (min_iter)
3:    progress metric:    (min_iter)
4:    progress metric:    (min_iter)
5:    progress metric:    (min_iter)
6:    progress metric:    0.0374741
7:    progress metric:    0.0252389
8:    progress metric:    0.0169805
9:    progress metric:    0.0113837
10:   progress metric:    0.00761077
20:   progress metric:    0.000130604

```

Solution converged after 21 iterations.

```

1:    progress metric:    (min_iter)
2:    progress metric:    (min_iter)
3:    progress metric:    (min_iter)
4:    progress metric:    (min_iter)
5:    progress metric:    (min_iter)
6:    progress metric:    0.0371935
7:    progress metric:    0.0431956
8:    progress metric:    0.056867
9:    progress metric:    0.0745391
10:   progress metric:    0.0890112
20:   progress metric:    0.092225
30:   progress metric:    0.00649718
40:   progress metric:    0.00224739

```

```
50:   progress metric:    0.000846835
60:   progress metric:    0.000303034
70:   progress metric:    0.000107818
```

Solution converged after 71 iterations.

```
1:   progress metric:    (min_iter)
2:   progress metric:    (min_iter)
3:   progress metric:    (min_iter)
4:   progress metric:    (min_iter)
5:   progress metric:    (min_iter)
6:   progress metric:    0.0278454
7:   progress metric:    0.0153121
8:   progress metric:    0.0084199
9:   progress metric:    0.00463192
10:  progress metric:    0.0025471
```

Solution converged after 16 iterations.

```
[1] 1: progress metric:    (min_iter)
2:   progress metric:    (min_iter)
3:   progress metric:    (min_iter)
4:   progress metric:    (min_iter)
5:   progress metric:    (min_iter)
6:   progress metric:    0.011482
7:   progress metric:    0.0088452
8:   progress metric:    0.00709218
9:   progress metric:    0.00576048
10:  progress metric:    0.00474146
20:  progress metric:    0.00145962
30:  progress metric:    0.00060763
40:  progress metric:    0.000297382
50:  progress metric:    0.000148919
```

Solution converged after 57 iterations.

```
1:   progress metric:    (min_iter)
2:   progress metric:    (min_iter)
3:   progress metric:    (min_iter)
4:   progress metric:    (min_iter)
5:   progress metric:    (min_iter)
6:   progress metric:    0.0476236
7:   progress metric:    0.034979
8:   progress metric:    0.0255046
9:   progress metric:    0.0179983
10:  progress metric:    0.0131529
20:  progress metric:    0.00233685
30:  progress metric:    0.00061225
40:  progress metric:    0.000172714
```

Solution converged after 45 iterations.

```
[2] 1: progress metric:    (min_iter)
2:   progress metric:    (min_iter)
3:   progress metric:    (min_iter)
4:   progress metric:    (min_iter)
5:   progress metric:    (min_iter)
6:   progress metric:    0.0348016
7:   progress metric:    0.0168893
8:   progress metric:    0.0087407
9:   progress metric:    0.00469118
10:  progress metric:    0.00255868
```

Solution converged after 16 iterations.

```
1:   progress metric:    (min_iter)
2:   progress metric:    (min_iter)
3:   progress metric:    (min_iter)
4:   progress metric:    (min_iter)
5:   progress metric:    (min_iter)
6:   progress metric:    0.0732844
7:   progress metric:    0.077964
8:   progress metric:    0.0906559
9:   progress metric:    0.0999774
10:  progress metric:    0.0994555
20:  progress metric:    0.00114661
```

Solution converged after 25 iterations.

```
[3] 1: progress metric:    (min_iter)
2:   progress metric:    (min_iter)
3:   progress metric:    (min_iter)
4:   progress metric:    (min_iter)
5:   progress metric:    (min_iter)
6:   progress metric:    0.0710298
7:   progress metric:    0.038312
8:   progress metric:    0.021048
9:   progress metric:    0.0117472
10:  progress metric:    0.00662412
```

Solution converged after 18 iterations.

```
1:   progress metric:   (min_iter)
2:   progress metric:   (min_iter)
3:   progress metric:   (min_iter)
4:   progress metric:   (min_iter)
5:   progress metric:   (min_iter)
6:   progress metric:   0.0801544
7:   progress metric:   0.072948
8:   progress metric:   0.0736511
9:   progress metric:   0.0752686
10:  progress metric:   0.0718868
20:  progress metric:   0.0192989
30:  progress metric:   0.0121039
40:  progress metric:   0.00743925
50:  progress metric:   0.00544292
60:  progress metric:   0.00557543
70:  progress metric:   0.00725721
80:  progress metric:   0.0123311
90:  progress metric:   0.0359475
100: progress metric:   0.104473
110: progress metric:   0.0239986
120: progress metric:   0.01361
130: progress metric:   0.00776367
140: progress metric:   0.00349198
150: progress metric:   0.000247399
```

Solution converged after 153 iterations.

```
[4]
assignment file test passed
*****
*           pysmallk - command line           *
*                                           *
*           Testing flatclust.               *
*                                           *
*****
WARNING: Could not achieve THREAD_MULTIPLE support.
1:   progress metric:   (min_iter)
2:   progress metric:   0.635556
3:   progress metric:   0.490817
4:   progress metric:   0.479135
5:   progress metric:   0.474986
6:   progress metric:   0.44968
7:   progress metric:   0.422542
8:   progress metric:   0.407662
9:   progress metric:   0.395145
10:  progress metric:   0.379238
20:  progress metric:   0.272868
30:  progress metric:   0.168386
40:  progress metric:   0.109147
50:  progress metric:   0.0767327
60:  progress metric:   0.0488545
70:  progress metric:   0.036226
80:  progress metric:   0.0307648
90:  progress metric:   0.0266116
100: progress metric:   0.0226963
110: progress metric:   0.0188616
120: progress metric:   0.0158307
130: progress metric:   0.0137605
140: progress metric:   0.0127888
150: progress metric:   0.0123962
160: progress metric:   0.0124734
170: progress metric:   0.0123563
180: progress metric:   0.0122163
190: progress metric:   0.0120643
200: progress metric:   0.0117647
210: progress metric:   0.0114894
220: progress metric:   0.0110467
230: progress metric:   0.0107816
240: progress metric:   0.0105239
250: progress metric:   0.0103824
260: progress metric:   0.0100915
270: progress metric:   0.00965073
280: progress metric:   0.00938526
290: progress metric:   0.00914129
300: progress metric:   0.00896701
310: progress metric:   0.00886729
320: progress metric:   0.00841059
330: progress metric:   0.007793
340: progress metric:   0.00740095
350: progress metric:   0.00708869
360: progress metric:   0.00683069
370: progress metric:   0.00672093
380: progress metric:   0.00687906
390: progress metric:   0.00703777
400: progress metric:   0.00721928
410: progress metric:   0.00729384
```

420: progress metric: 0.00718332  
430: progress metric: 0.00722893  
440: progress metric: 0.00726766  
450: progress metric: 0.00739665  
460: progress metric: 0.00769819  
470: progress metric: 0.00814673  
480: progress metric: 0.008566  
490: progress metric: 0.00877955  
500: progress metric: 0.00884221  
510: progress metric: 0.0088057  
520: progress metric: 0.00852345  
530: progress metric: 0.00797952  
540: progress metric: 0.00749354  
550: progress metric: 0.00689316  
560: progress metric: 0.00623287  
570: progress metric: 0.00576619  
580: progress metric: 0.00541125  
590: progress metric: 0.00501715  
600: progress metric: 0.00466547  
610: progress metric: 0.00432811  
620: progress metric: 0.00412669  
630: progress metric: 0.00383406  
640: progress metric: 0.00352802  
650: progress metric: 0.00331556  
660: progress metric: 0.00315735  
670: progress metric: 0.00304253  
680: progress metric: 0.00296627  
690: progress metric: 0.00289013  
700: progress metric: 0.00279647  
710: progress metric: 0.00271036  
720: progress metric: 0.00261087  
730: progress metric: 0.0025158  
740: progress metric: 0.00245123  
750: progress metric: 0.00237435  
760: progress metric: 0.00231126  
770: progress metric: 0.00228199  
780: progress metric: 0.00227623  
790: progress metric: 0.00228185  
800: progress metric: 0.00227993  
810: progress metric: 0.00228216  
820: progress metric: 0.00228018  
830: progress metric: 0.00229096  
840: progress metric: 0.00232403  
850: progress metric: 0.00234957  
860: progress metric: 0.00227868  
870: progress metric: 0.00210786  
880: progress metric: 0.00195462  
890: progress metric: 0.00183587  
900: progress metric: 0.00173358  
910: progress metric: 0.0016405  
920: progress metric: 0.00156422  
930: progress metric: 0.00150835  
940: progress metric: 0.00146594  
950: progress metric: 0.00143261  
960: progress metric: 0.00137378  
970: progress metric: 0.00131989  
980: progress metric: 0.00126626  
990: progress metric: 0.0012164  
1000: progress metric: 0.00117061  
1010: progress metric: 0.00112539  
1020: progress metric: 0.00108626  
1030: progress metric: 0.00105192  
1040: progress metric: 0.00102131  
1050: progress metric: 0.000992069  
1060: progress metric: 0.000965259  
1070: progress metric: 0.000938949  
1080: progress metric: 0.000911962  
1090: progress metric: 0.000884505  
1100: progress metric: 0.000854904  
1110: progress metric: 0.000820121  
1120: progress metric: 0.000785245  
1130: progress metric: 0.000752513  
1140: progress metric: 0.000723279  
1150: progress metric: 0.000697698  
1160: progress metric: 0.000680904  
1170: progress metric: 0.000652152  
1180: progress metric: 0.000628268  
1190: progress metric: 0.000612413  
1200: progress metric: 0.000596834  
1210: progress metric: 0.000580674  
1220: progress metric: 0.000556549  
1230: progress metric: 0.000535666  
1240: progress metric: 0.00051492  
1250: progress metric: 0.000496234  
1260: progress metric: 0.000481147  
1270: progress metric: 0.000461294  
1280: progress metric: 0.000440802  
1290: progress metric: 0.000419049  
1300: progress metric: 0.000398007

1310: progress metric: 0.000376203  
1320: progress metric: 0.000355811  
1330: progress metric: 0.00033729  
1340: progress metric: 0.000318932  
1350: progress metric: 0.000302528  
1360: progress metric: 0.000287961  
1370: progress metric: 0.00027486  
1380: progress metric: 0.00026403  
1390: progress metric: 0.000255504  
1400: progress metric: 0.000248646  
1410: progress metric: 0.000242996  
1420: progress metric: 0.000239243  
1430: progress metric: 0.000236852  
1440: progress metric: 0.000235313  
1450: progress metric: 0.000234465  
1460: progress metric: 0.000234154  
1470: progress metric: 0.000234253  
1480: progress metric: 0.00023487  
1490: progress metric: 0.000237223  
1500: progress metric: 0.000240043  
1510: progress metric: 0.000243896  
1520: progress metric: 0.00024867  
1530: progress metric: 0.000253981  
1540: progress metric: 0.000260239  
1550: progress metric: 0.000266795  
1560: progress metric: 0.000273529  
1570: progress metric: 0.000280678  
1580: progress metric: 0.000287273  
1590: progress metric: 0.000292288  
1600: progress metric: 0.000296475  
1610: progress metric: 0.000299556  
1620: progress metric: 0.00030244  
1630: progress metric: 0.000306148  
1640: progress metric: 0.000310299  
1650: progress metric: 0.000314674  
1660: progress metric: 0.000319052  
1670: progress metric: 0.000323906  
1680: progress metric: 0.000329536  
1690: progress metric: 0.000335913  
1700: progress metric: 0.000342834  
1710: progress metric: 0.000351167  
1720: progress metric: 0.000352515  
1730: progress metric: 0.000348749  
1740: progress metric: 0.000345684  
1750: progress metric: 0.000343139  
1760: progress metric: 0.000340867  
1770: progress metric: 0.000339052  
1780: progress metric: 0.000337038  
1790: progress metric: 0.000335244  
1800: progress metric: 0.000333452  
1810: progress metric: 0.000332111  
1820: progress metric: 0.000330198  
1830: progress metric: 0.000325983  
1840: progress metric: 0.000321473  
1850: progress metric: 0.000316999  
1860: progress metric: 0.000312054  
1870: progress metric: 0.000305176  
1880: progress metric: 0.000294684  
1890: progress metric: 0.000284482  
1900: progress metric: 0.000274905  
1910: progress metric: 0.000265684  
1920: progress metric: 0.000256761  
1930: progress metric: 0.000248203  
1940: progress metric: 0.000239613  
1950: progress metric: 0.000230677  
1960: progress metric: 0.00022218  
1970: progress metric: 0.000214089  
1980: progress metric: 0.00020621  
1990: progress metric: 0.000196915  
2000: progress metric: 0.000187712  
2010: progress metric: 0.000179199  
2020: progress metric: 0.00017137  
2030: progress metric: 0.000164158  
2040: progress metric: 0.000157751  
2050: progress metric: 0.000152485  
2060: progress metric: 0.000147217  
2070: progress metric: 0.000142083  
2080: progress metric: 0.000137148  
2090: progress metric: 0.000132379  
2100: progress metric: 0.000127922  
2110: progress metric: 0.000123617  
2120: progress metric: 0.000119548  
2130: progress metric: 0.000115684  
2140: progress metric: 0.000111997  
2150: progress metric: 0.000108389  
2160: progress metric: 0.000104838  
2170: progress metric: 0.000101387

Solution converged after 2175 iterations.

```

Writing output files...
XML file test passed
assignment file test passed
*****
*                pysmallk - in memory                *
*                                                        *
*                Testing flatclust.                    *
*                                                        *
*****
WARNING: Could not achieve THREAD_MULTIPLE support.
1:   progress metric:   (min_iter)
2:   progress metric:   0.635556
3:   progress metric:   0.490817
4:   progress metric:   0.479135
5:   progress metric:   0.474986
6:   progress metric:   0.44968
7:   progress metric:   0.422542
8:   progress metric:   0.407662
9:   progress metric:   0.395145
10:  progress metric:   0.379238
20:  progress metric:   0.272868
30:  progress metric:   0.168386
40:  progress metric:   0.109147
50:  progress metric:   0.0767327
60:  progress metric:   0.0488545
70:  progress metric:   0.036226
80:  progress metric:   0.0307648
90:  progress metric:   0.0266116
100: progress metric:   0.0226963
110: progress metric:   0.0188616
120: progress metric:   0.0158307
130: progress metric:   0.0137605
140: progress metric:   0.0127888
150: progress metric:   0.0123962
160: progress metric:   0.0124734
170: progress metric:   0.0123563
180: progress metric:   0.0122163
190: progress metric:   0.0120643
200: progress metric:   0.0117647
210: progress metric:   0.0114894
220: progress metric:   0.0110467
230: progress metric:   0.0107816
240: progress metric:   0.0105239
250: progress metric:   0.0103824
260: progress metric:   0.0100915
270: progress metric:   0.00965073
280: progress metric:   0.00938526
290: progress metric:   0.00914129
300: progress metric:   0.00896701
310: progress metric:   0.00886729
320: progress metric:   0.00841059
330: progress metric:   0.007793
340: progress metric:   0.00740095
350: progress metric:   0.00708869
360: progress metric:   0.00683069
370: progress metric:   0.00672093
380: progress metric:   0.00687906
390: progress metric:   0.00703777
400: progress metric:   0.00721928
410: progress metric:   0.00729384
420: progress metric:   0.00718332
430: progress metric:   0.00722893
440: progress metric:   0.00726766
450: progress metric:   0.00739665
460: progress metric:   0.00769819
470: progress metric:   0.00814673
480: progress metric:   0.008566
490: progress metric:   0.00877955
500: progress metric:   0.00884221
510: progress metric:   0.0088057
520: progress metric:   0.00852345
530: progress metric:   0.00797952
540: progress metric:   0.00749354
550: progress metric:   0.00689316
560: progress metric:   0.00623287
570: progress metric:   0.00576619
580: progress metric:   0.00541125
590: progress metric:   0.00501715
600: progress metric:   0.00466547
610: progress metric:   0.00432811
620: progress metric:   0.00412669
630: progress metric:   0.00383406
640: progress metric:   0.00352802
650: progress metric:   0.00331556
660: progress metric:   0.00315735
670: progress metric:   0.00304253
680: progress metric:   0.00296627
690: progress metric:   0.00289013

```

700: progress metric: 0.00279647  
710: progress metric: 0.00271036  
720: progress metric: 0.00261087  
730: progress metric: 0.0025158  
740: progress metric: 0.00245123  
750: progress metric: 0.00237435  
760: progress metric: 0.00231126  
770: progress metric: 0.00228199  
780: progress metric: 0.00227623  
790: progress metric: 0.00228185  
800: progress metric: 0.00227993  
810: progress metric: 0.00228216  
820: progress metric: 0.00228018  
830: progress metric: 0.00229096  
840: progress metric: 0.00232403  
850: progress metric: 0.00234957  
860: progress metric: 0.00227868  
870: progress metric: 0.00210786  
880: progress metric: 0.00195462  
890: progress metric: 0.00183587  
900: progress metric: 0.00173358  
910: progress metric: 0.0016405  
920: progress metric: 0.00156422  
930: progress metric: 0.00150835  
940: progress metric: 0.00146594  
950: progress metric: 0.00143261  
960: progress metric: 0.00137378  
970: progress metric: 0.00131989  
980: progress metric: 0.00126626  
990: progress metric: 0.0012164  
1000: progress metric: 0.00117061  
1010: progress metric: 0.00112539  
1020: progress metric: 0.00108626  
1030: progress metric: 0.00105192  
1040: progress metric: 0.00102131  
1050: progress metric: 0.000992069  
1060: progress metric: 0.000965259  
1070: progress metric: 0.000938949  
1080: progress metric: 0.000911962  
1090: progress metric: 0.000884505  
1100: progress metric: 0.000854904  
1110: progress metric: 0.000820121  
1120: progress metric: 0.000785245  
1130: progress metric: 0.000752513  
1140: progress metric: 0.000723279  
1150: progress metric: 0.000697698  
1160: progress metric: 0.000680904  
1170: progress metric: 0.000652152  
1180: progress metric: 0.000628268  
1190: progress metric: 0.000612413  
1200: progress metric: 0.000596834  
1210: progress metric: 0.000580674  
1220: progress metric: 0.000556549  
1230: progress metric: 0.000535666  
1240: progress metric: 0.00051492  
1250: progress metric: 0.000496234  
1260: progress metric: 0.000481147  
1270: progress metric: 0.000461294  
1280: progress metric: 0.000440802  
1290: progress metric: 0.000419049  
1300: progress metric: 0.000398007  
1310: progress metric: 0.000376203  
1320: progress metric: 0.000355811  
1330: progress metric: 0.00033729  
1340: progress metric: 0.000318932  
1350: progress metric: 0.000302528  
1360: progress metric: 0.000287961  
1370: progress metric: 0.00027486  
1380: progress metric: 0.00026403  
1390: progress metric: 0.000255504  
1400: progress metric: 0.000248646  
1410: progress metric: 0.000242996  
1420: progress metric: 0.000239243  
1430: progress metric: 0.000236852  
1440: progress metric: 0.000235313  
1450: progress metric: 0.000234465  
1460: progress metric: 0.000234154  
1470: progress metric: 0.000234253  
1480: progress metric: 0.00023487  
1490: progress metric: 0.000237223  
1500: progress metric: 0.000240043  
1510: progress metric: 0.000243896  
1520: progress metric: 0.00024867  
1530: progress metric: 0.000253981  
1540: progress metric: 0.000260239  
1550: progress metric: 0.000266795  
1560: progress metric: 0.000273529  
1570: progress metric: 0.000280678  
1580: progress metric: 0.000287273

```

1590: progress metric: 0.000292288
1600: progress metric: 0.000296475
1610: progress metric: 0.000299556
1620: progress metric: 0.00030244
1630: progress metric: 0.000306148
1640: progress metric: 0.000310299
1650: progress metric: 0.000314674
1660: progress metric: 0.000319052
1670: progress metric: 0.000323906
1680: progress metric: 0.000329536
1690: progress metric: 0.000335913
1700: progress metric: 0.000342834
1710: progress metric: 0.000351167
1720: progress metric: 0.000352515
1730: progress metric: 0.000348749
1740: progress metric: 0.000345684
1750: progress metric: 0.000343139
1760: progress metric: 0.000340867
1770: progress metric: 0.000339052
1780: progress metric: 0.000337038
1790: progress metric: 0.000335244
1800: progress metric: 0.000333452
1810: progress metric: 0.000332111
1820: progress metric: 0.000330198
1830: progress metric: 0.000325983
1840: progress metric: 0.000321473
1850: progress metric: 0.000316999
1860: progress metric: 0.000312054
1870: progress metric: 0.000305176
1880: progress metric: 0.000294684
1890: progress metric: 0.000284482
1900: progress metric: 0.000274905
1910: progress metric: 0.000265684
1920: progress metric: 0.000256761
1930: progress metric: 0.000248203
1940: progress metric: 0.000239613
1950: progress metric: 0.000230677
1960: progress metric: 0.00022218
1970: progress metric: 0.000214089
1980: progress metric: 0.00020621
1990: progress metric: 0.000196915
2000: progress metric: 0.000187712
2010: progress metric: 0.000179199
2020: progress metric: 0.00017137
2030: progress metric: 0.000164158
2040: progress metric: 0.000157751
2050: progress metric: 0.000152485
2060: progress metric: 0.000147217
2070: progress metric: 0.000142083
2080: progress metric: 0.000137148
2090: progress metric: 0.000132379
2100: progress metric: 0.000127922
2110: progress metric: 0.000123617
2120: progress metric: 0.000119548
2130: progress metric: 0.000115684
2140: progress metric: 0.000111997
2150: progress metric: 0.000108389
2160: progress metric: 0.000104838
2170: progress metric: 0.000101387

```

Solution converged after 2175 iterations.

```

assignment file test passed
***** SmallK: All tests passed. *****
***** PysmallK: All tests passed. *****

```



## VI. Pysmallk: SmallK Python Interface

Why Python? Although it's perfectly fine to run SmallK from the command line, Python provides a great deal more flexibility that augments the C++ code with other tasks that are much more easily accomplished with a very high level language. Python distributions can be easily extended with open source libraries from third party sources as well, two examples being numpy and scipy, well-known standards for scientific computing in the Python community. There are numerous packages available that extend these scientific libraries into the data analytics domain as well, such as [scikit-learn](#).

For using scientific Python, we strongly recommend the Anaconda Python distribution provided by [Continuum Analytics](#). Download and installation instructions for all platforms can be found [here](#). Anaconda includes many if not most of the commonly used scientific and data analytics packages available and a very easy to use package manager and updating system. After installing Anaconda there will be available at the command line both a standard Python interpreter (type 'python') and an iPython interpreter (type 'ipython'). We recommend using the iPython interpreter. In addition to the command line interfaces to Python, Anaconda includes the Spyder visual development environment featuring a very well thought out interface that makes developing Python code almost "too easy". Spyder has many features found in the Matlab™ editor and a similar look and feel.

Anaconda also includes the [Cython](#) package, which is used by SmallK to integrate the Python and C++ code. Cython includes support for most of the C++ standard and supports the latest GNU C++ compilers. Most if not all the standard libraries are supported and the latest version (20.2) has support for the standard template library (STL) as well.

Pysmallk has five classes, each of which represents one of the SmallK tools: SmallkAPI (the simplistic Smallk API), Flatclust, Hierclust, Matrixgen, and Preprocessor. Each of these classes can be imported as follows:

```
from pysmallk import SmallkAPI
from pysmallk import Flatclust
from pysmallk import Hierclust
from pysmallk import Matrixgen
from pysmallk import Preprocessor
```

Each class's primary functions are documented below. The parameters are either marked [in] or [kwarg] which represent, respectively, positional and keyword arguments.

These tools can be chained together to combine functionalities. An example of this can be found in `examples/pysmallk_example.py`.

## VI.1. Preprocessor

```
def parser(self):
```

\brief Returns the parsed arguments for the default command line application

The command line arguments are the same as those for the C++ binary application preprocessor

\return The dictionary containing the parsed arguments

```
def load_matrix(self, filepath="", height=0, width=0, nz=0, buffer=[],
               row_indices=[], col_offsets=[]):
```

\brief Load an input matrix

To load a matrix from a file:

\param[kwarg] filepath The path to the input matrix

To load a sparse matrix from Matrixgen:

\param[kwarg] height The height of the sparse matrix

\param[kwarg] width The width of the sparse matrix

\param[kwarg] sparse\_matrix The sparse matrix returned from Matrixgen

To load a sparse matrix from python:

\param[kwarg] height The height of the sparse matrix

\param[kwarg] width The width of the sparse matrix

\param[kwarg] nz The number of non-zeros in the sparse matrix

\param[kwarg] buffer List of doubles containing the non-zero elements of the sparse matrix

\param[kwarg] row\_indices List of integers representing the row indices of the sparse matrix

\param[kwarg] col\_offsets List of integers representing the column offsets of the sparse matrix

```
def load_dictionary(self, filepath=None, dictionary=None):
```

\brief Loads a dictionary

\param[kwarg] filepath The filepath for the dictionary

OR

\param[kwarg] dictionary List containing the dictionary strings

```
def load_documents(self, filepath=None, documents=None):
```

\brief Loads the documents file

\param[kwarg] filepath The filepath for the documents

OR

\param[kwarg] documents List containing the documents strings

```
def get_reduced_documents(self):
```

\brief Returns the reduced documents

\return The documents in a list

```
def get_reduced_dictionary(self):
```

\brief Returns the reduced dictionary

\return The dictionary in a list

```
def get_reduced_scores(self):
```

\brief Returns the non-zero scores from the reduced matrix

\return The scores in a list

```

def get_reduced_row_indices (self):

    \brief Returns the row indices for the reduced matrix
    \return The row indices in a list

def get_reduced_col_offsets (self):

    \brief Returns the column offsets for the reduced matrix
    \return The column offsets in a list

def get_reduced_field (self, filepath="", values=[]):

    \brief Loads the additional field file
    \param[kwarg] filepath  The filepath for the field
    OR
    \param[kwarg] values    List containing the field strings

def preprocess(self, maxiter=1000, docsperterm=3, termsperdoc=5, boolean_mode=0):

    \brief Preprocesses the matrix
    \param[kwarg] maxiter    The maximum number of iterations (optional)
    \param[kwarg] docsperterm The number of documents required per term (optional)
    \param[kwarg] termsperdoc The number of terms required per document (optional)
    \param[kwarg] boolean_mode All nonzero matrix elements will be treated as if they had
                             the value 1.0 (optional)

def write_output(self, matrix_filepath, dict_filepath, docs_filepath, precision=4):

    \brief Writes the preprocessor results to files
    \param[in]    matrix_filepath  The filepath for writing the matrix
    \param[in]    dict_filepath    The filepath for writing the dictionary
    \param[in]    docs_filepath    The filepath for the documents
    \param[kwargs] precision      The precision with which to write the outputs (optional)

```

## VI.2. Matrixgen

```
def parser(self):
```

```
\brief Returns the parsed arguments for the default command line application
```

```
The command line arguments are the same as those for the C++ binary application matrixgen
```

```
\return The dictionary containing the parsed arguments
```

```
def uniform(self, m, n, center=0.5, radius=0.5):
```

```
\brief Generates a uniform matrix
```

```
\param[in] m The desired height
```

```
\param[in] n The desired width
```

```
\param[kwarg] center Center with which to initialize the RNG
```

```
\param[kwarg] radius Radius with which to initialize the RNG
```

```
\return A tuple of the list of values, the height, and the width
```

```
def denseddiag(self, m, n, center=0.5, radius=0.5):
```

```
\brief Generates a dense diagonal matrix
```

```
\param[in] m The desired height
```

```
\param[in] n The desired width
```

```
\param[kwarg] center Center with which to initialize the RNG
```

```
\param[kwarg] radius Radius with which to initialize the RNG
```

```
\return A tuple of the list of values, the height, and the width
```

```
def identify(self, m, n):
```

```
\brief Generates an identify matrix of height m and width n.
```

```
\param[in] m The desired height
```

```
\param[in] n The desired width
```

```
\return A tuple of the list of values, the height, and the width
```

```
def sparseddiag(self, n, center=0.5, radius=0.5):
```

```
\brief Generates a sparse diagonal matrix of width n with the RNG attributes of center and radius
```

```
\param[in] n The desired width
```

```
\param[kwarg] center Center with which to initialize the RNG
```

```
\param[kwarg] radius Radius with which to initialize the RNG
```

```
\return A tuple of the list of values, the height, and the width
```

```
def ones(self, m, n):
```

```
\brief Generates a matrix of ones of height m and width n
```

```
\param[in] m The desired height
```

```
\param[in] n The desired width
```

```
\return A tuple of the list of values, the height, and the width
```

```
def zeros(self, m, n):
```

```
\brief Generates a matrix of zeros of height m and width n
```

```
\param[in] m The desired height
```

```
\param[in] n The desired width
```

```
\return A tuple of the list of values, the height, and the width
```

```

def sparse(self, m, n, nz):

    \brief Generates a random sparse matrix
    \param[in]    m    The desired height
    \param[in]    n    The desired width
    \param[in]    nz    The desired non-zeros
    \return A tuple of the list of values, the height, and the width

def write_output(self, filename, precision=6):

    \brief Writes the generated matrix to file
    \param[in]    filename    The filepath for writing the matrix
    \param[kwarg] precision    The precision with which to write the matrix

```

## VI.3. SmallKAPI

```
def parser(self):

    \brief Returns the parsed arguments for the default command line application
    \return The dictionary containing the parsed arguments

def get_major_version(self):

    \brief Returns the major version of SmallK
    \return unsigned int representing major version

def get_minor_version(self):

    \brief Returns the minor version of SmallK
    \return unsigned int representing minor version

def get_patch_level(self):

    \brief Returns the patch level of SmallK
    \return unsigned int representing patch level

def get_version_string(self):

    \brief Returns a string representation of the version of SmallK
    \return string representing the major and minor version and patch level

def load_matrix(self, filepath="", height=0, width=0, delim="", buffer=[], matrix=[],
    nz=0, row_indices=[], col_offsets=[], column_major=False, sparse_matrix=None):

    \brief Load an input matrix

    To load a matrix from a file:
    \param[kwarg] filepath    The path to the input matrix

    To load a sparse matrix from python:
    \param[kwarg] height      The height of the sparse matrix
    \param[kwarg] width       The width of the sparse matrix
    \param[kwarg] nz          The number of non-zeros in the sparse matrix
    \param[kwarg] buffer      List of doubles containing the non-zero elements of the sparse matrix
    \param[kwarg] row_indices List of integers representing the row indices of the sparse matrix
    \param[kwarg] col_offsets List of integers representing the column offsets of the sparse matrix

    To load a dense matrix from python:
    \param[kwarg] height      The height of the dense matrix
    \param[kwarg] width       The width of the dense matrix
    \param[kwarg] buffer      List of doubles containing the elements of the dense matrix

    To load a numpy matrix from python:
    \param[kwarg] matrix      The numpy matrix
    \param[kwarg] column_major Boolean for whether or not the matrix is column major (optional)
```

**Note:** Internal to SmallK, the matrix is stored in column-major order. When you are loading a numpy matrix, the assumption is that your matrix is in row-major order. If this is not the case, you can pass `column_major=True` in as a keyword argument. When directly loading a dense matrix, the assumption is that your buffer holds the data in column-major order as well.

```

def is_matrix_loaded(self):

    \brief Indicates whether or not a matrix has been loaded
    \return boolean representing if a matrix is loaded

def nmf(self, k, algorithm, infile_W="", infile_H="", precision=4, min_iter=5, max_iter=5000,
    tol=0.005, max_threads=8, outdir="."):

    \brief Runs NMF on the loaded matrix using the supplied algorithm and implementation details
    \param[in] k      The desired number of clusters
    \param[in] algorithm The desired NMF algorithm
    \param[kwarg] infile_W  Initialization for W (optional)
    \param[kwarg] infile_H  Initialization for H (optional)
    \param[kwarg] precision Precision for calculations (optional)
    \param[kwarg] min_iter  Minimum number of iterations (optional)
    \param[kwarg] max_iter  Maximum number of iterations (optional)
    \param[kwarg] tol      Tolerance for determining convergence (optional)
    \param[kwarg] max_threads Maximum number of threads to use (optional)
    \param[kwarg] outdir   Output directory for files (optional)

def get_inputs(self):

    \brief Returns a dictionary of the supplied inputs to the nmf function
    \return The dictionary containing the supplied inputs

def get_H(self):

    \brief Returns the output H matrix
    \return Numpy array of the output H matrix

def get_W(self):

    \brief Returns the output W matrix
    \return Numpy array of the output W matrix

def load_dictionary (self, filepath="", dictionary=[]):

    \brief Loads a dictionary to use for computing top terms
    \param[kwarg] filepath  The filepath for the dictionary
    OR
    \param[kwarg] dictionary List containing the dictionary strings

def hiernmf2(self, k, format="XML", maxterms=5, tol=0.0001):

    \brief Runs HierNMF2 on the loaded matrix
    \param[in] k      The desired number of clusters
    \param[kwarg] format  Output format, XML or JSON (optional)
    \param[kwarg] maxterms Maximum number of terms (optional)
    \param[kwarg] tol    Tolerance to use for determining convergence (optional)

def finalize(self):

    \brief Cleans up the elemental and smallk environment

```

## VI.4. Flatclust

```
def parser(self):
```

\brief Returns the parsed arguments for the default command line application

The command line arguments are the same as those for the C++ binary application flatclust

\return The dictionary containing the parsed arguments

```
def load_matrix(self, **kwargs):
```

\brief Load an input matrix

To load a matrix from a file:

\param[kwarg] filepath The path to the input matrix

To load a sparse matrix from python:

\param[kwarg] height The height of the sparse matrix

\param[kwarg] width The width of the sparse matrix

\param[kwarg] nz The number of non-zeros in the sparse matrix

\param[kwarg] buffer List of doubles containing the non-zero elements of the sparse matrix

\param[kwarg] row\_indices List of integers representing the row indices of the sparse matrix

\param[kwarg] col\_offsets List of integers representing the column offsets of the sparse matrix

To load a sparse matrix from Matrixgen:

\param[kwarg] height The height of the sparse matrix

\param[kwarg] width The width of the sparse matrix

\param[kwarg] sparse\_matrix The sparse matrix returned from Matrixgen

To load a dense matrix from python:

\param[kwarg] height The height of the dense matrix

\param[kwarg] width The width of the dense matrix

\param[kwarg] buffer List of doubles containing the elements of the dense matrix

To load a numpy matrix from python:

\param[kwarg] matrix The numpy matrix

\param[kwarg] column\_major Boolean for whether or not the matrix is column major (optional)

**Note:** Internal to SmallK, the matrix is stored in column-major order. When you are loading a numpy matrix, the assumption is that your matrix is in row-major order. If this is not the case, you can pass column\_major=True in as a keyword argument. When directly loading a dense matrix, the assumption is that your buffer holds the data in column-major order as well.

```
def load_dictionary (self, filepath="", dictionary=[]):
```

\brief Loads a dictionary to use for computing top terms

\param[kwarg] filepath The filepath for the dictionary

OR

\param[kwarg] dictionary List containing the dictionary strings



```
def cluster(self, k, infile_W='', infile_H='', algorithm="BPP", maxterms=5, verbose=True,
            min_iter=5, max_iter=5000, max_threads=8, tol=0.0001):
```

```
\brief Runs NMF on the loaded matrix using the supplied algorithm and implementation details
\param[in] k      The desired number of clusters
\param[kwarg] infile_W  Initialization for W (optional)
\param[kwarg] infile_H  Initialization for H (optional)
\param[kwarg] algorithm The desired NMF algorithm (optional)
\param[kwarg] maxterms  Maximum number of terms per cluster (optional)
\param[kwarg] verbose   Boolean for whether or not to be verbose (optional)
\param[kwarg] min_iter  Minimum number of iterations (optional)
\param[kwarg] max_iter  Maximum number of iterations (optional)
\param[kwarg] max_threads Maximum number of threads to use (optional)
\param[kwarg] tol       Tolerance for determining convergence (optional)
```

```
def get_top_indices(self):
```

```
\brief Return the top term indices for each cluster
```

The length of the returned array is maxterms\*k, with the first maxterms elements belonging to the first cluster, the second maxterms elements belonging to the second cluster, etc.

```
\return List of the term_indices
```

```
def get_top_terms(self):
```

```
\brief Return the top terms for each cluster
```

The length of the returned array is maxterms\*k, with the first maxterms elements belonging to the first cluster, the second maxterms elements belonging to the second cluster, etc.

```
\return List of the top terms
```

```
def get_assignments(self):
```

```
\brief Return the list of cluster assignments for each document
```

```
\return List of the assignments
```

```
def write_output(self, assignfile, fuzzyfile, □/□/□/□/□□□/□/////treefile, outdir='./',
format='XML'):
```

```
\brief Writes the flatclust results to files
```

```
\param[in] assignfile  The filepath for writing assignments
\param[in] fuzzyfile    The filepath for writing fuzzy assignments
\param[in] treefile     The filepath for the tree results
\param[kwargs] outdir   The output directory for the output files (optional)
\param[kwargs] format   The output format JSON or XML (optional)
```

```
def finalize(self):
```

```
\brief Cleans up the elemental and smallk environment
```

## VI.5. Hierclust

```
def parser(self):
```

\brief Returns the parsed arguments for the default command line application

The command line arguments are the same as those for the C++ binary application hierclust

\return The dictionary containing the parsed arguments

```
def load_matrix(self, **kwargs):
```

\brief Load an input matrix

To load a matrix from a file:

\param[kwarg] filepath The path to the input matrix

To load a sparse matrix from python:

\param[kwarg] height The height of the sparse matrix

\param[kwarg] width The width of the sparse matrix

\param[kwarg] nz The number of non-zeros in the sparse matrix

\param[kwarg] buffer List of doubles containing the non-zero elements of the sparse matrix

\param[kwarg] row\_indices List of integers representing the row indices of the sparse matrix

\param[kwarg] col\_offsets List of integers representing the column offsets of the sparse matrix

To load a sparse matrix from Matrixgen:

\param[kwarg] height The height of the sparse matrix

\param[kwarg] width The width of the sparse matrix

\param[kwarg] sparse\_matrix The sparse matrix returned from Matrixgen

To load a dense matrix from python:

\param[kwarg] height The height of the dense matrix

\param[kwarg] width The width of the dense matrix

\param[kwarg] buffer List of doubles containing the elements of the dense matrix

To load a numpy matrix from python:

\param[kwarg] matrix The numpy matrix

\param[kwarg] column\_major Boolean for whether or not the matrix is column major (optional)

**Note:** Internal to SmallK, the matrix is stored in column-major order. When you are loading a numpy matrix, the assumption is that your matrix is in row-major order. If this is not the case, you can pass column\_major=True in as a keyword argument. When directly loading a dense matrix, the assumption is that your buffer holds the data in column-major order as well.

```
def load_dictionary (self, filepath="", dictionary=[]):
```

\brief Loads a dictionary to use for computing top terms

\param[kwarg] filepath The filepath for the dictionary

OR

\param[kwarg] dictionary List containing the dictionary strings

```
def finalize(self):
```

\brief Cleans up the elemental and smallk environment

```
def cluster(self, k, infile_W='', infile_H='', maxterms=5, unbalanced=0.1, trial_allowance=3,
verbose=True, flat=0, min_iter=5, max_iter=5000, max_threads=8, tol=0.0001):
```

```

    \brief Runs HierNMF2 on the loaded matrix using the supplied algorithm and implementation details
    \param[in] k The desired number of clusters
    \param[kwarg] initdir Initialization matrices (optional)
    \param[kwarg] maxterms Maximum number of terms per cluster (optional)
    \param[kwarg] unbalanced Unbalanced parameter (optional)
    \param[kwarg] trial_allowance Number of trials to use (optional)
    \param[kwarg] verbose Boolean for whether or not to be verbose (optional)
    \param[kwarg] flat Whether or not to flatten the results (optional)
    \param[kwarg] min_iter Minimum number of iterations (optional)
    \param[kwarg] max_iter Maximum number of iterations (optional)
    \param[kwarg] max_threads Maximum number of threads to use (optional)
    \param[kwarg] tol Tolerance for determining convergence (optional)

```

```
def get_assignments(self):
```

```

    \brief Return the list of cluster assignments for each document
    \return List of the assignments

```

```
def get_top_indices(self):
```

```
    \brief Return the top term indices for each cluster
```

The length of the returned array is maxterms\*k, with the first maxterms elements belonging to the first cluster, the second maxterms elements belonging to the second cluster, etc.

```
    \return List of the term_indices
```

```
def write_output(self, assignfile, fuzzyfile, treefile, outdir='./', format='XML'):
```

```
    \brief Writes the flatclust results to files
```

```

    \param[in] assignfile The filepath for writing assignments
    \param[in] fuzzyfile The filepath for writing fuzzy assignments
    \param[in] treefile The filepath for the tree results
    \param[kwargs] outdir The output directory for the output files (optional)
    \param[kwargs] format The output format JSON or XML (optional)

```

## VII. References

### References

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If the SmallK library is used to obtain results for publication, please use the following BibTeX citation:

```
@misc{SmallK,  
  author    = {Richard Boyd and Barry Drake and Da Kuang and  
               Haesun Park},  
  title     = {SmallK is a {C++}/{P}ython high-performance software  
               library for nonnegative matrix factorization  
               (NMF) and hierarchical and flat clustering using  
               the NMF; current version 1.2.0},  
  howpublished = {\url{http://smallk.github.io/}},  
  month     = June,  
  year      = 2014
```

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