



TOPIC 24 - TEMPORAL ABSTRACT CONCEPTUAL MODEL

ABSTRACT SPECIFICATION TOPIC

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Editor: Chris Little, Charles Heazel

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ABSTRACT

Traditionally, geospatial communities used 2D coordinates and the vertical and temporal aspects were considered attributes rather than fully fledged coordinate systems. In an increasingly dynamic, speedier and multidimensional world, much confusion and lack of interoperability has occurred because of inconsistent approaches to time. Much effort has been expended by various international bodies to establish the Gregorian Calendar as a consistent timeline. This suffices for low precision, such as to the nearest minute, but not so when second or sub-second accuracy is required. For example, there has been differing practices and no consensus on whether leap seconds should be part of the Gregorian timeline.

The fundamental concepts of events, clocks, timescales, coordinates and calendars have been long established, but there is no clear, straightforward defining document. This document aims to give clear consistent definitions of the fundamental concepts and terminology, so that people are well aware of the advantages and disadvantages of adopting a particular technological approach and then perhaps they can contribute to building better and more interoperable systems using other more detailed documents such as logical and implementation standards that have an agreed common conceptual basis and terminology.

This document is consistent with ISO 19111 and W3C REC-owl-time-20171019 in OWL.

The aim of this document is to establish clear concepts and terminology.



KEYWORDS

The following are keywords to be used by search engines and document catalogues.

ogcdoc, OGC document, abstract specification, conceptual model, time, temporal referencing, referencing by coordinates, calendar, clock, timescale



PREFACE

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No security considerations have been made for this document.



SUBMITTING ORGANIZATIONS

The following organizations submitted this Document to the Open Geospatial Consortium (OGC):

- U.K. Met Office, HeazelTech



SUBMITTERS

All questions regarding this submission should be directed to the editor or the submitters:

NAME	AFFILIATION
Chris Little (editor)	U.K. Met Office
Chuck Heazel	HeazelTech



INTRODUCTION

When OGC standards involve time, they generally refer to the ISO documents such as ISO 19108 (now largely superseded), ISO 19111, ISO 8601, and their freely available OGC equivalents, such as [OGC_18-005r4] (the equivalent to ISO 19111).

Much effort over decades has gone into establishing complex structures to represent calendar based time, such as the ISO 8601 notation, and many date-time schemas. Because of this effort, many people use calendar based “coordinates”, with the attendant ambiguities, imprecision and inappropriate scope.

The aim of this document is to establish clear concepts and terminology, so that people are well aware of the advantages and disadvantages of adopting a particular technological approach and then perhaps contribute to building better interoperable systems.



2

CONFORMANCE

Clause 6 of this International Standard uses the Unified Modeling Language (UML) to present conceptual schemas for describing the higher level classes of time and temporal reference systems. These schemas define conceptual classes that

- a) may be considered to comprise a cross-domain application schema, or
- b) may be used in application schemas, profiles and implementation specifications.

This flexibility is controlled by a set of UML types that can be implemented in a variety of manners. Use of alternative names that are more familiar in a particular application is acceptable, provided that there is a one- to-one mapping to classes and properties in this International Standard. The UML model in this International Standard defines conceptual classes; various software systems define implementation classes or data structures. All of these reference the same information content. The same name may be used in implementations as in the model, so that types defined in the UML model may be used directly in application schemas.

Annex A defines a set of conformance tests that will support applications whose requirements range from the minimum necessary to define data structures to full object implementation.



1

SCOPE

This document defines the major underlying concepts regarding time. It does not define any concrete temporal reference systems or give detailed guidance on implementations.



3

NORMATIVE REFERENCES

The following documents are referred to in the text in such a way that some or all of their content constitutes requirements of this document. For dated references, only the edition cited applies. For undated references, the latest edition of the referenced document (including any amendments) applies.

ISO: ISO 19103:2015, *Geographic information – Conceptual schema language*, 2015, <https://www.iso.org/standard/56734.html>

ISO: ISO 19111:2019, *Geographic information – Referencing by coordinates*, 2019, <https://www.iso.org/standard/74039.html>

W3C: Time Ontology in OWL, 2017, <https://www.w3.org/TR/2017/REC-owl-time-20171019/>



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TERMS AND DEFINITIONS

This document uses the terms defined in OGC Policy Directive 49, which is based on the ISO/IEC Directives, Part 2, Rules for the structure and drafting of International Standards. In particular, the word “shall” (not “must”) is the verb form used to indicate a requirement to be strictly followed to conform to this document and OGC documents do not use the equivalent phrases in the ISO/IEC Directives, Part 2.

This document also uses terms defined in the OGC Standard for Modular specifications (OGC 08-131r3), also known as the ‘ModSpec’. The definitions of terms such as standard, specification, requirement, and conformance test are provided in the ModSpec.

For the purposes of this document, the following additional terms and definitions apply.

4.1. conceptual model

description of common concepts and their relationships, particularly in order to facilitate exchange of information between parties within a specific domain. A conceptual model is explicitly chosen to be independent of design or implementation concerns.

[SOURCE:]



5

CONVENTIONS

5.1. Abbreviated terms

CRS	Coordinate Reference System
TRS	Temporal Reference System
UML	Unified Modelling Language
2D	2-dimensional
3D	3-dimensional

5.2. Identifiers

The normative provisions in this standard are denoted by the URI:

<http://www.opengis.net/doc/AS/temporal-conceptual-model/1.0>

All requirements and conformance tests that appear in this document are denoted by partial URIs which are relative to this base.



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CHARACTERISTICS OF AN ABSTRACT CONCEPTUAL MODEL

CHARACTERISTICS OF AN ABSTRACT CONCEPTUAL MODEL

The terms and definitions clause in this Abstract Specification provides a short definition for “conceptual model”. This clause provides additional information on the OGC use of “conceptual model”.

A conceptual model organizes the vocabulary needed to communicate consistently and thoroughly about the know-how of a problem domain. The aim of a conceptual model is to express the meaning of terms and concepts used by domain experts to discuss the problem, and to find the correct relationships between different concepts.

A conceptual model:

1. is a representation of a system, made of the composition of concepts which are used to help people know, understand, or simulate a subject the model represents. A documented conceptual model represents ‘concepts’ (entities), the relationships between them, and a vocabulary;
2. is explicitly defined to be independent of design or implementation concerns;
3. organizes the vocabulary needed to communicate consistently and thoroughly about the know-how of a problem domain;
4. starts with a glossary of terms and definitions. There is a very high premium on high-quality, design-independent definitions, free of data or implementation biases; the model also emphasizes rich vocabulary; and
5. is always about identifying the correct choice of terms to use in communications, including statements of rules and requirements, especially where high precision and subtle distinctions need to be made. The core concepts of a temporal geospatial problem domain are typically quite stable over time.



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TEMPORAL ABSTRACT CONCEPTUAL MODEL

This attempt at a Temporal Abstract Conceptual Model follows ISO 19111, which is the ISO adoption of [OGC_18-005r4].

The model is also informed by W3C REC-owl-time-20171019.

NOTE: This Mermaid diagram should be converted to PlantUML for Metanorma, by replacing the Mermaid container with the following.

```
[plantuml] @startuml . . @enduml

classDiagram
class ReferenceSystem {
    <<abstract>>
    dimension = 1..*
    applicableLocationTimeOrDomain
}
class SpatialReferenceSystem {
    <<abstract>>
    dimension = 1..*
    applicableLocationTimeOrDomain
}
class TemporalReferenceSystem {
    <<abstract>>
    dimension = 1
    applicableLocationTimeOrDomain
}
note for ReferenceSystem "Note: Has at least one of:\nSpatialReferenceSystem, or \nTemporalReferenceSystem"
ReferenceSystem <|-- SpatialReferenceSystem : is a
ReferenceSystem <|-- TemporalReferenceSystem : is a
class OrdinalTemporalReferenceSystem {
    dimension = 1
    applicableLocationTimeOrDomain
}
class TemporalCoordinateReferenceSystem {
    dimension = 1
    applicableLocationTimeOrDomain
}
class Calendar {
    dimension = 1
    applicableLocationTimeOrDomain
}
note for TemporalReferenceSystem "Note: Consists of one only of:\nTemporalCoordinateReferenceSystem,\nCalendar, or \nOrdinalTemporalReferenceSystem"
TemporalReferenceSystem <|-- OrdinalTemporalReferenceSystem : is a
TemporalReferenceSystem <|-- TemporalCoordinateReferenceSystem : is a
TemporalReferenceSystem <|-- Calendar : is a
OrdinalTemporalReferenceSystem "1" o-- "(ordered)" Events : consists of
OrdinalTemporalReferenceSystem "1" o-- "0..1" Epoch : has an
OrdinalTemporalReferenceSystem "1" --> "1..*" Notation : can use
TemporalCoordinateReferenceSystem "1" o-- "1" Epoch : has an
TemporalCoordinateReferenceSystem "1" --> "1..*" Notation : can use
TemporalCoordinateReferenceSystem "1" o-- "1" Timescale : has a
Calendar "1" o-- "0..1" Epoch : has an
Calendar "1" --> "1..*" Notation : can use
Calendar "1" o-- "1..*" Timescale : has a
```

```

Calendar "1" o-- "1..*" Algorithm : has a
class Timescale {
    StartCount
    EndCount
    arithmetic
}
Timescale "1" o-- "1" Clock : has a
Timescale "1" o-- "1" UnitOfMeasure : has a
class Clock {
    Tick definition
}
class UnitOfMeasure {
    Direction
}

```

Figure 1



8

TEMPORAL REGIMES

8.1. General

To help us think more clearly about time, this paper adopts the term “Regime” to describe the fundamentally different types of time and its measurement under consideration. This is a pragmatic approach that allows the grouping of recommendations and best practices in a practical way, but without obscuring the connection to the underlying theoretical components.

The first three regimes have deep underlying physical and mathematical foundations which cannot be legislated away. The fourth regime, of calendars, uses a seemingly random mixture of ad hoc algorithms, arithmetic, numerology and measurements. Paradoxically, this regime has historically driven advances in mathematics and physics.

The regimes are applicable to other planets and outer space, but with due consideration.

8.2. Events and Operators

The simplest way of relating entities in time is by events that can be ordered, that is, established in a sequence, and this sequence is used as an approximate measure of the passage of time.

In this regime, no clocks or time measurements are defined, only events, that are ordered in relation to each other. For example, geological layers, sediment or ice core layers, archaeological sequences, sequential entries in computer logs without coordinated time.

One set of events may be completely ordered with respect to each other, but another set of similar internally consistent events cannot be cross-referenced until extra information is available. Even then, only partial orderings may be possible.

In this regime, the Allen Operators (Maintaining Knowledge about Temporal Intervals) can be used. If A occurs before B and B occurs before C, then we can correctly deduce that A occurs before C. The full set of operators also covers pairs of intervals. So in our example, B occurs in the interval (A,C). However, we cannot perform arithmetic operations like (B-A) or (C-A) as we have not defined any timescale or measurements. For example, in geology, ‘subtracting’ Ordovician from Jurassic is meaningless; or in archeology, ‘subtracting’ a layer with a certain type of pottery remains from the layer containing burnt wood and bones is again not meaningful. Only the ordering can be deduced.

This regime constitutes an Ordinal Temporal Reference System, with discrete enumerated ordered events.

8.3. Simple Clocks and Discrete Timescales

In this regime, a clock is defined as any regularly repeating physical phenomena, such as pendulum swings, earth's rotation about sun, earth's rotation about its axis, heart beats, vibrations of electrically stimulated quartz crystals or the resonance of the unperturbed ground-state hyperfine transition frequency of the caesium 133 atom. Some phenomena make better clocks than others, in terms of the number of repetitions possible, the consistency of each repetition and the precision of each 'tick'. A mechanism for counting, or possibly measuring, the ticks is desirable.

It is an assumption that the ticks are regular and homogeneous.

There is no sub-division between two successive clock ticks. Measuring time consists of counting the complete number of repetitions of ticks since the clock started, or since some other event at a given clock count.

There is no time measurement before the clock started, or after it stops.

It may seem that time can be measured between 'ticks' by interpolation, but this needs another clock, with faster ticks. This process of devising more precise clocks continues down to the atomic scale, and then the deterministic process of physically trying to interpolate between ticks is not possible.

The internationally agreed atomic time, TAI, is an example of a timescale with an integer count as the measure of time, though in practice it is an arithmetic compromise across about two hundred separate atomic clocks, corrected for differing altitudes and temperatures.

In this regime, the Allen Operators (Maintaining Knowledge about Temporal Intervals) also can be used. If L occurs before M and M occurs before N, then we can correctly deduce that L occurs before N. The full set of operators also covers pairs of intervals. So if M occurs in the interval (L,N), we can now perform integer arithmetic operations like (M-L) or (N-L) as we have defined an integer timescale or measurement.

This regime constitutes a Temporal Coordinate Reference System, with discrete integer units of measure which can be subject to integer arithmetic.

8.4. CRS and Continuous Timescales

This regime takes a clock from the previous regime and assumes that between any two adjacent ticks, it is possible to interpolate indefinitely to finer and finer precision, using ordinary arithmetic, rather than any physical device. Units of Measure may be defined that are different from the 'ticks'. For example, a second may be defined as 9,192,631,770 vibrations of the ground-state hyperfine transition of the caesium 133 atom. Alternatively and differently, a second may be defined as 1/86400th of the rotation of the earth on its axis with respect to

the sun. The count of rotations are the 'ticks' of an earth-day clock. This latter definition is not precise enough for many uses, as the rotation of the earth on its axis varies from day to day.

Alternatively, it may be that the ticks are not counted but measured, and the precision of the clock is determined by the precision of the measurements, such as depth in an ice core, or angular position of an astronomical body, such as the sun, moon or a star.

It is also assumed that time can be extrapolated to before the time when the clock started and into the future, possibly past when the clock stops.

This gives us a continuous number line to perform theoretical measurements. It is a coordinate system. With a datum/origin/epoch, a unit of measure (a name for the 'tick marks' on the axis), positive and negative directions and the full range of normal arithmetic. It is a Coordinate Reference System.

In this regime, the Allen Operators (Maintaining Knowledge about Temporal Intervals) also can be used. If A occurs before B and B occurs before C, then we can correctly deduce that A occurs before C. The full set of operators also covers pairs of intervals. So if B occurs in the interval (A,C), we can now perform real number arithmetic operations like (B-A) or (C-A) as we have defined a timescale or measurement, and between any two instants, we can always find an infinite number of other instants.

Some examples are:

- Unix milliseconds since 1970-01-01T00:00:00.0Z
- Julian Days, and fractions of a day, since noon on 1st January, 4713 BCE.

This regime constitutes a Temporal Coordinate Reference System, with a continuous number line and units of measure, which can be subject to the full range of real or floating point arithmetic.

8.5. Calendars

In this regime, counts and measures of time are related to the various combinations of the rotations of the earth, moon and sun or other astronomical bodies. There is no simple arithmetic, so for example, the current civil year count of years in the Current Era (CE) and Before Current Era (BCE) is a calendar, albeit a very simple one, as there is no year zero. That is, Year 14CE – Year 12CE is a duration of 2 years, and Year 12BCE – Year 14BCE is also two years. However Year 1CE – Year 1BCE is one year, not two as there is no year 0CE or 0BCE.

Calendars are social constructs made by combining several clocks and their associated timescales.

This paper only addresses the internationally agreed Gregorian calendar. Astronomical Algorithms provides overwhelming detail for conversion to numerous other calendars that have developed around the world and over the millennia and to meet the various social needs of

communities, whether agricultural, religious or other. The reference is comprehensive but not exhaustive, as there are calendars that have been omitted.

A Calendar is a Temporal Reference System, but it is not a Temporal Coordinate Reference System nor an Ordinal Temporal Reference System.

8.6. Other Regimes

There are other regimes, which are out of scope of this document. This could include local solar time, useful, for example, for the calculation of illumination levels and the length of shadows on aerial photography, or relativistic time.

8.6.1. Local Solar Time

Local solar time may or may not correspond to the local statutory or legal time in a country. Local solar time can be construed as a clock and timescale, with an angular measure of the apparent position of the sun along the ecliptic (path through the sky) as the basic physical principle.

8.6.2. Space-time

When dealing with moving objects, we find that the location of the object in space depends on its location in time. That is to say, that the location is an event in space and time.

Originally developed by Hermann Minkowski to support work in Special Relativity, the concept of Space-time is useful whenever the location of an object in space is dependent on its location in time.

Since the speed of light in a vacuum is a measurable constant, Space-time uses that constant to create a coordinate axis with spatial units of measure (meters per second * seconds = meters). The result is coordinate reference system with four orthogonal axis all with the same units of measure, distance.

8.6.3. Relativistic

A regime may be needed for 'space-time', off the planet Earth, such as for recording and predicting space weather approaching from the sun, where the speed of light and relativistic effects such as gravity may be relevant.

Once off the planet Earth, distances and velocities can become very large. The speed of light becomes a limiting factor in measuring both where and when an event takes place. Special Relativity deals with the accurate measurement of Space-time events as measured between two moving objects. The core concepts are the Lorentz Transforms. These transforms allow one

to calculate the degree of “contraction” a measurement undergoes due to the relative velocity between the observing and observed object.

The key to this approach is to ensure each moving feature of interest has its own local clock and time, known as its ‘proper time’. This example can be construed as a fitting into the clock and timescale regime. The relativistic effects are addressed through the relationships between the separate clocks, positions and velocities of the features.

Relativistic effects may need to be taken into account for satellites and other space craft because of their relative speed and position in Earth’s gravity well.

The presence of gravitational effects requires special relativity to be replaced by general relativity, and it can no longer be assumed that space (or space-time) is Euclidean. That is, Pythagoras’ Theorem does not hold except locally over small areas. This is somewhat unfamiliar territory for geospatial experts.

8.6.4. Accountancy

The financial and administrative domains often use weeks, quarters, and other calendrical measures. These may be convenient (though often not!) for the requisite tasks, but are usually inappropriate for scientific or technical purposes.



9

NOTATION

There are often widely agreed, commonly accepted, notations used for temporal reference systems, but few have been standardised. Any particular notation may be capable of expressing a wider range of times than are valid for the reference system.

Example : The [IETF_RFC_3999] timestamp notation, a restrictive profile of [ISO_8601], can express times before 1588CE, when the Gregorian calendar was first introduced in some parts of the world.



10

ATTRIBUTES OF THE REGIMES/CLASSES

The top level Reference System is an abstract super-class and does not have many attributes or properties. So far, only the total dimension of the reference system and the Location, Time or Domain of Applicability have been identified as essential.

The 'ReferenceSystem' has two abstract sub-classes: 'SpatialReferenceSystem', which is defined in ISO 19111, and 'TemporalReferenceSystem', each with the attributes of Dimension and Domains of Applicability.

The Dimension is one for time, or a vertical reference system, but may be as much as 6 for spatial location with orientation.

Besides the conventional space and time, there may be other reference systems, such as wavelength/frequency, that can be addressed by the Abstract Conceptual Model.

10.1. Attributes of Events and Ordinal Temporal Reference Systems

1. An OrdinalTemporal Reference System has a well-ordered finite sequence of events against which other events can be compared.
2. Name/Id
3. Optional location, time or domain of applicability
4. Optional Epoch, defined in some temporal reference system
5. Listed or enumerated sequence of events with the first and last events
6. Optional notations

Example : Ancient annals of a country may give a sequence of emperors which could be used to 'date' another event such as "Emperor Xi built a canal", or may be used to date a particular reign. For example: "In the reign of Emperor Yi, a comet was sighted" and later research identifies this as an appearance of Hailey's Comet.

The events from the list may be instants, such as the change of reign, or intervals, such as the complete reign of each king.

Other documents may enable two such 'king lists' to be related, though not completely.

10.2. Attributes of simple Clock and Discrete Timescale

A clock is a regular, repeating, physical event, or 'tick', that can be counted. The sequence of tick counts is a timescale. The ticks may be grouped into a Unit of Measure for convenience. Other events can be compared to the ticks on the timescale.

1. Name/Id
2. Optional location, time or domain of applicability
3. Optional Epoch, defined in some temporal reference system
4. Arithmetic: Integer
5. Optional name for each tick
6. Optional Start time or count
7. Optional End time or count
8. Optional Unit of Measure and number of ticks per Unit
9. Optional notations

Example 1: A well preserved fossilised log is recovered and the tree rings establish an annual 'tick'. The start and end times may be known accurately by comparison and matching with other known tree ring sequences, or perhaps only dated imprecisely via Carbon Dating, or its archaeological or geological context.

Example 2: A clock is started, but undergoes a calibration process against some standards clock, so the initial, reliable Start Time does not start at Count Zero. The clock is accidentally knocked so that it is no longer correctly calibrated, but is still working. the End Time is not the last time that the clock ticks.

10.3. Attributes of Clocks

1. Name/Id
2. Optional location, time or domain of applicability
3. Optional Epoch, defined in some temporal reference system
4. Tick definition

Example 1: An atomic clock may be calibrated to be valid only for a given temperature range and altitude.

Example 2: A pendulum clock may have each tick or swing of the pendulum adjusted to be an exact fraction or multiple of a second. The famous London “Big Ben” clock’s pendulum is 4.4m long and ticks every two seconds.

10.4. Attributes of Timescales

1. Name/Id
2. Optional location, time or domain of applicability
3. Optional Epoch, defined in some temporal reference system
4. Arithmetic, whether counted integers or measured real/floating point numbers
5. Optional Unit of Measure

Example 1: TAI (International Atomic Time, Temps Atomique International) is coordinated by the BIPM (International Bureau of Weights and Measures, Bureau International de Poids et Mesures) in Paris, France. It is based on the average of hundreds of separate atomic clocks around the world, all corrected to be at mean sea level and standard pressure and temperature. The epoch is defined by Julian Date 2443144.5003725 (1 January 1977 00:00:32.184).

Example 2: The Julian Day is the continuous count of days (rotations of the Earth with respect to the Sun) since the beginning of the year 4173 BCE and will terminate at the end of the year 3267 CE. The count then starts again as “Period 2”. Many computer based timescales, such as Unix Time, are based on the Julian Day timescale, but with different epochs, to fit the numbers into the limited computer words.

10.5. Attributes of Units of Measure

The Direction attribute indicates whether counts or measures increase in the positive (future) or negative (past) direction. The attribute could be part of ‘Timescale’ or ‘TemporalCoordinateReferenceSystem’ rather than a separate class ‘UnitOfMeasure’, but on balance, it seems better here, as the names often imply directionality, such as fathoms increasing downwards, MYA (Millions of Years Ago) increasing earlier, Atmospheric Pressure in NPs (HectoPascals) decreasing upwards, and FL (FlightLevel) increasing upwards.

1. Name/Id/Abbreviation
2. Direction

Example : The number of years before the Current Era (BCE, previously known as BC) increase further back in time, whereas the number of years in the Current Era (CE, previously known as AD) increase further into the future. This is an example of two timescales, adjacent but with no overlap. If there was a year zero defined, they could be replaced with one continuous timescale.

10.6. Attributes of a CRS and Continuous Timescales

Some clocks allow the measurement of intervals between ticks, such as the movement of the sun across the sky. Alternatively, the ticks may not be completely distinguishable, but are still stable enough over the time of applicability to allow measurements rather than counting to determine the passage of time.

1. Name/Id
2. Optional location, time or domain of applicability
3. Optional Epoch, defined in some temporal reference system
4. Arithmetic: Real/Floating point
5. Optional name for the Unit of Measure
6. Optional Start time or measure
7. Optional End time of measure
8. Optional notations

Example 1: A long, deep ice core is retrieved from a stable ice-sheet. From long term meteorological observations, the rate of accumulation of ice is known, so linear length can be equated to time (assuming a stable climate too). This enables the dates of some previously unknown large scale volcanic eruptions to be identified and timed. Identifiable nuclear fallout from specific atmospheric atomic bomb tests increase the confidence in the timing accuracy.

Example 2: A long, deep, sediment core is extracted from the bottom of a lake with a long geological history. Two layers in the core are dated using radiocarbon dating. Assuming steady rates of sediment deposition, a continuous timescale can be interpolated between the dated layers, and extrapolated before and after the dated layers.



11

ATTRIBUTES OF CALENDARS

Calendars combine different timescales and their clocks and units of measure, and other events, to make a complex timeline against which events can be compared. Calculated algorithms are used to determine which instants of intervals on the compound timescale are identified and labeled.

1. Name/id
2. Optional location, time or domain of applicability
3. Optional Epoch, defined in some temporal reference system
4. Astronomical Type (e.g. solar, sidereal, lunar, luni-solar)
5. Predictive type (e.g. observed or calculated)
6. Optional Start time
7. Optional End time
8. Constituent units or clocks and counts or timescales
9. Algorithms to link constituent timescales
10. Optional notations

Example 1: The modern Gregorian calendar is a calculated solar calendar, with various epochs from 1588 CE through to 1922 CE depending on location or country.

The constituent timescales are days (earth's rotations), months (moon's orbit around the earth), years (earth's orbit around the sun) and seconds determined by atomic clocks. To accommodate discrepancies, leap days and leap seconds are intercalated in some years. The commonest notations for the Gregorian calendar are ISO 8601 and its various restrictive profiles.

Example 2: The modern Islamic calendar is an observed lunar calendar, and the major religious dates progress throughout the year, year on year. The important months are determined by the observation of new moons from Mecca.

Example 3: The modern Jewish calendar is a calculated luni-solar calendar, and discrepancies in the solar year are addressed by adding 'leap months' every few years.

Example 4: The Ba'hai calendar is a calculated solar calendar, but without any other astronomical aspects. The year consists of 19 months of 19 days each, with 4 or 5 intercalated days for a new year holiday.

Example 5: The West African Yoruba traditional calendar is a solar calendar with months, but rather than subdividing a nominal month of 28 days into 4 weeks, 7 weeks of 4 days are used. This perhaps gave rise to the fortnightly (every 8 days) markets in many villages in the grasslands of north-west Cameroun.

Example 6: Teams controlling remote vehicles on Mars use a solar calendar, with Martian years and martian days (called sols). Months are not used because there are two moons, with different, rather short, orbital periods.



12

SYNCHRONISATION OF CLOCKS

If there are two or more clocks, stationary with respect to each other, and a practical method of communicating their times to each other, the clocks can be perfectly synchronized.

However, if the clocks are moving with respect to each other, they cannot be precisely coordinated (unless the communication is instantaneous). As communication speed is limited by the finite constant speed of light, perfect synchronisation is not possible, though repetitive protocols can be used to reduce the synchronization error to any practical desired level.

See A Brief History of Timekeeping, Page 187-191.



ANNEX A (NORMATIVE)

ANNEX TITLE



ANNEX A (NORMATIVE) ANNEX TITLE

<Insert annex content here>

NOTE: Place annex material in sequential order and set `obligation` attribute as “normative” (default) or “informative” according to the case.



B

ANNEX B (INFORMATIVE) ISO GLOSSARY

B

ANNEX B (INFORMATIVE) ISO GLOSSARY

The following concepts from the ISO TC211 Harmonized UML model are referenced by the Temporal Conceptual UML model but do not play a major role in its' definition. They are provided here to support a more complete understanding of the model.

Area

The measure of the physical extent of any topologically 2-D geometric object. Usually measured in “square” units of length.

[ISO 19103]

Boolean

Boolean is the mathematical datatype associated with two-valued logic

[ISO 19103]

CC_CoordinateOperation

A mathematical operation on coordinates that transforms or converts coordinates to another coordinate reference system.

[ISO 19111]

Character

A symbol from a standard character-set.

[ISO 19103]

CharacterString

Characterstring is a family of datatypes which represent strings of symbols from standard character-sets.

[ISO 19103]

CRS

Coordinate reference system which is usually single but may be compound.

[ISO 19111]

CV_DiscreteCoverage

A subclass of CV_Coverage that returns a single record of values for any direct position within a single geometric object in its spatiotemporal domain.

[[iso19123]]

CV_DomainObject

An element of the domain of the CV_Coverage. It is an aggregation of objects that may include any combination of GM_Objects (ISO 19107:2003), TM_GeometricPrimitives (ISO 10108), or spatial or temporal objects defined in other standards, such as the CV_GridPoint defined in this International Standard.

[[iso19123]]

CV_GridPointValuePair

A subtype of CV_GeometryValuePair that has a GM_GridPoint as the value of its geometry attribute.

[[iso19123]]

CV_GridValuesMatrix

The geometry represented by the various offset vectors is in the image plane of the grid.

[[iso19123]]

CV_ReferenceableGrid

A subclass of CV_Coverage that relates the grid coordinates to an external coordinate reference system.

[[iso19123]]

Date

Date gives values for year, month and day. Representation of Date is specified in ISO 8601. Principles for date and time are further discussed in ISO 19108.

[ISO 19103]

DateTime

A DateTime is a combination of a date and a time types. Representation of DateTime is specified in ISO 8601. Principles for date and time are further discussed in ISO 19108.

[ISO 19103]

Distance

Used as a type for returning distances and possibly lengths.

[ISO 19103]

Engineering CRS

A contextually local coordinate reference system which can be divided into two broad categories:

1. earth-fixed systems applied to engineering activities on or near the surface of the earth;
2. CRSs on moving platforms such as road vehicles, vessels, aircraft or spacecraft.

[ISO 19111]

Generic Name

Generic Name is the abstract class for all names in a Namespace. Each instance of a GenericName is either a LocalName or a ScopedName.

[ISO 19103]

Geometry

Geometry is the root class of the geometric object taxonomy and supports interfaces common to all geographically referenced geometric objects.

[ISO 19107]

GM_CompositePoint

A GM_Complex containing one and only one GM_Point.

[ISO 19107]

GM_CompositeSolid

A set of geometric solids adjoining one another along common boundary geometric surfaces
[ISO 19107]

GM_GenericSurface

GM_Surface and GM_SurfacePatch both represent sections of surface geometry, and therefore share a number of operation signatures. These are defined in the interface class GM_GenericSurface.
[ISO 19107]

GM_LineString

Consists of sequence of line segments, each having a parameterization like the one for GM_LineSegment
[ISO 19107]

GM_MultiPrimitive

The root class for all primitive aggregates. The association role “element” shall be the set of GM_Primitives contained in this GM_MultiPrimitive. The attribute declaration here specializes the one at GM_Aggregate to include only GM_Primitives in this type of aggregate.
[ISO 19107]

GM_OrientableSurface

A surface and an orientation inherited from GM_OrientablePrimitive. If the orientation is “+”, then the GM_OrientableSurface is a GM_Surface. If the orientation is “-”, then the GM_OrientableSurface is a reference to a GM_Surface with an upNormal that reverses the direction for this GM_OrientableSurface, the sense of “the top of the surface”.
[ISO 19107]

GM_PolyhedralSurface

A GM_Surface composed of polygon surfaces (GM_Polygon) connected along their common boundary curves.
[ISO 19107]

GM_Position

A union type consisting of either a DirectPosition or of a reference to a GM_Point from which a DirectPosition shall be obtained.
[ISO 19107]

GM_Primitive

The abstract root class of the geometric primitives. Its main purpose is to define the basic “boundary” operation that ties the primitives in each dimension together.
[ISO 19107]

Integer

An exact integer value, with no fractional part.
[ISO 19103]

Internet of Things

The network of physical objects—“things”—that are embedded with sensors, software, and other technologies for the purpose of connecting and exchanging data with other devices and systems over the Internet.

[Wikipedia](#)

IO_IdentifiedObjectBase

Supplementary identification and remarks information for a CRS or CRS-related object.

[ISO 19111]

Length

The measure of distance as an integral, i.e. the limit of an infinite sum of distances between points on a curve.

[ISO 19103]

Measure

The result from performing the act or process of ascertaining the extent, dimensions, or quantity of some entity.

[ISO 19103]

Number

The base type for all number data, giving the basic algebraic operations.

[ISO 19103]

Point

GM_Point is the basic data type for a geometric object consisting of one and only one point.

[ISO 19107]

Real

The common binary Real finite implementation using base 2.

[ISO 19103]

RS_ReferenceSystem

Description of a spatial and temporal reference system used by a dataset.

[ISO 19111]

Scoped Name

ScopedName is a composite of a LocalName for locating another NameSpace and a GenericName valid in that NameSpace. ScopedName contains a LocalName as head and a GenericName, which might be a LocalName or a ScopedName, as tail.

[ISO 19103]

Solid

GM_Solid, a subclass of GM_Primitive, is the basis for 3-dimensional geometry. The extent of a solid is defined by the boundary surfaces.

[ISO 19107]

Time

Time is the designation of an instant on a selected time scale, astronomical or atomic. It is used in the sense of time of day.

[ISO 19103]

TM_Duration

A data type to be used for describing length or distance in the temporal dimension.
[ISO 19108]

TM_TemporalPosition

The position of a TM_Instant relative to a TM_ReferenceSystem.
[ISO 19108]

Unit of Measure

Any of the systems devised to measure some physical quantity such distance or area or a system devised to measure such things as the passage of time.
[ISO 19103]

URI

Uniform Resource Identifier (URI), is a compact string of characters used to identify or name a resource
[ISO 19103]

Volume

Volume is the measure of the physical space of any 3-D geometric object.
[ISO 19103]



ANNEX C (INFORMATIVE) GLOSSARY



ANNEX C (INFORMATIVE) GLOSSARY

C.1. conceptual model

description of common concepts and their relationships, particularly in order to facilitate exchange of information between parties within a specific domain. A conceptual model is explicitly chosen to be independent of design or implementation concerns.

[SOURCE:]

C.2. compound coordinate reference system

coordinate reference system using at least two independent coordinate reference systems

Note 1 to entry: Coordinate reference systems are independent of each other if coordinate values in one cannot be converted or transformed into coordinate values in the other.

[SOURCE: ISO 19111]

C.3. coordinate

one of a sequence of numbers designating the position of a point

Note 1 to entry: In a spatial coordinate reference system, the coordinate numbers are qualified by units.

[SOURCE: ISO 19111]

C.4. coordinate epoch

epoch to which coordinates in a dynamic coordinate reference system are referenced

[SOURCE: ISO 19111]

C.5. coordinate reference system

coordinate system that is related to an object by a datum

Note 1 to entry: Geodetic and vertical datums are referred to as reference frames.

Note 2 to entry: For geodetic and vertical reference frames, the object will be the Earth. In planetary applications, geodetic and vertical reference frames may be applied to other celestial bodies.

[SOURCE: ISO 19111]

C.6. coordinate system

set of mathematical rules for specifying how coordinates are to be assigned to points

[SOURCE: ISO 19111]

C.7. datum

reference frame **ADMITTED**

parameter or set of parameters that realize the position of the origin, the scale, and the orientation of a coordinate system

[SOURCE: ISO 19111]

C.8. derived coordinate reference system

coordinate reference system that is defined through the application of a specified coordinate conversion to the coordinates within a previously established coordinate reference system

Note 1 to entry: The previously established coordinate reference system is referred to as the base coordinate reference system.

Note 2 to entry: A derived coordinate reference system inherits its datum or reference frame from its base coordinate reference system.

Note 3 to entry: The coordinate conversion between the base and derived coordinate reference system is implemented using the parameters and formula(s) specified in the definition of the coordinate conversion.

[SOURCE: ISO 19111]

C.9. dynamic coordinate reference system

coordinate reference system that has a dynamic reference frame

Note 1 to entry: Coordinates of points on or near the crust of the Earth that are referenced to a dynamic coordinate reference system may change with time, usually due to crustal deformations such as tectonic motion and glacial isostatic adjustment.

Note 2 to entry: Metadata for a dataset referenced to a dynamic coordinate reference system should include coordinate epoch information.

[SOURCE: ISO 19111]

C.10. dynamic reference frame

dynamic datum ADMITTED

reference frame in which the defining parameters include time evolution

Note 1 to entry: The defining parameters that have time evolution are usually a coordinate set.

[SOURCE: ISO 19111]

C.11.engineering coordinate reference system

coordinate reference system based on an engineering datum

Example 1 System for identifying relative positions within a few kilometres of the reference point, such as a building or construction site.

Example 2 Coordinate reference system local to a moving object such as a ship or an orbiting spacecraft.

Example 3 Internal coordinate reference system for an image. This has continuous axes. It may be the foundation for a grid.

C.12.engineering datum

local datum ADMITTED

datum describing the relationship of a coordinate system to a local reference

Note 1 to entry: Engineering datum excludes both geodetic and vertical reference frames.

[SOURCE: ISO 19111]

C.13.epoch

<geodesy> point in time

Note 1 to entry: In this document an epoch is expressed in the Gregorian calendar as a decimal year.

Example 2017-03-25 in the Gregorian calendar is epoch 2017.23.

[SOURCE: ISO 19111]

C.14.frame reference epoch

epoch of coordinates that define a dynamic reference frame

[SOURCE: ISO 19111]

C.15.linear coordinate system

one-dimensional coordinate system in which a linear feature forms the axis

Example 1 Distances along a pipeline.

Example 2 Depths down a deviated oil well bore.

[SOURCE: ISO 19111]

C.16.parameter reference epoch

epoch at which the parameter values of a time-dependent coordinate transformation are valid

Note 1 to entry: The transformation parameter values first need to be propagated to the epoch of the coordinates before the coordinate transformation can be applied.

[SOURCE: ISO 19111]

C.17.parametric coordinate reference system

coordinate reference system based on a parametric datum

[SOURCE: ISO 19111]

C.18.parametric coordinate system

one-dimensional coordinate system where the axis units are parameter values which are not inherently spatial

[SOURCE: ISO 19111]

C.19.parametric datum

datum describing the relationship of a parametric coordinate system to an object

Note 1 to entry: The object is normally the Earth.

[SOURCE: ISO 19111]

C.20.point motion operation

coordinate operation that changes coordinates within one coordinate reference system due to the motion of the point

Note 1 to entry: The change of coordinates is from those at an initial epoch to those at another epoch.

Note 2 to entry: In this document the point motion is due to tectonic motion or crustal deformation.

[SOURCE: ISO 19111]

C.21.reference frame

datum ADMITTED

parameter or set of parameters that realize the position of the origin, the scale, and the orientation of a coordinate system

[SOURCE: ISO 19111]

C.22.spatio-parametric coordinate reference system

compound coordinate reference system in which one constituent coordinate reference system is a spatial coordinate reference system and one is a parametric coordinate reference system

Note 1 to entry: Normally the spatial component is “horizontal” and the parametric component is “vertical”.

[SOURCE: ISO 19111]

C.23.spatio-parametric-temporal coordinate reference system

compound coordinate reference system comprised of spatial, parametric and temporal coordinate reference systems

[SOURCE: ISO 19111]

C.24.spatio-temporal coordinate reference system

compound coordinate reference system in which one constituent coordinate reference system is a spatial coordinate reference system and one is a temporal coordinate reference system

[SOURCE: ISO 19111]

C.25.static coordinate reference system

coordinate reference system that has a static reference frame

Note 1 to entry: Coordinates of points on or near the crust of the Earth that are referenced to a static coordinate reference system do not change with time.

Note 2 to entry: Metadata for a dataset referenced to a static coordinate reference system does not require coordinate epoch information.

[SOURCE: ISO 19111]

C.26.static reference frame

static datum

reference frame in which the defining parameters exclude time evolution

[SOURCE: ISO 19111]

C.27.temporal coordinate reference system

coordinate reference system based on a temporal datum

[SOURCE: ISO 19111]

C.28.temporal coordinate system

<geodesy> one-dimensional coordinate system where the axis is time

[SOURCE: ISO 19111]

C.29.temporal datum

datum describing the relationship of a temporal coordinate system to an object

Note 1 to entry: The object is normally time on the Earth.

[SOURCE: ISO 19111]

C.30.terrestrial reference system

TRS ADMITTED

set of conventions defining the origin, scale, orientation and time evolution of a spatial reference system co-rotating with the Earth in its diurnal motion in space

Note 1 to entry: The abstract concept of a TRS is realised through a terrestrial reference frame that usually consists of a set of physical points with precisely determined coordinates and optionally their rates of change. In this document terrestrial reference frame is included within the geodetic reference frame element of the data model

[SOURCE: ISO 19111]



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