

# What does formal language theory tell us about the nature of reduplication?

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# Reduplication

**Morpho-phonological “copying”** → identity-based patterns on the surface

- **Meaning-changing operations**

*Dyirbal plurals* (Pama-Nyungan; North Queensland)

midi → midi~midi

Glosses: *little; small* → *lots of little ones*

*Agta plurals* (Austronesian; Philippines)

labáng → lab~labáng

patch → *PL*-patch

# Reduplication

**Morpho-phonological “copying”** → identity-based patterns on the surface

- **Semantics-free**

*Tagalog pseudo-reduplication* (Austronesian; Philippines)

patpát

\*pat

*“N: stick; piece of split bamboo”*

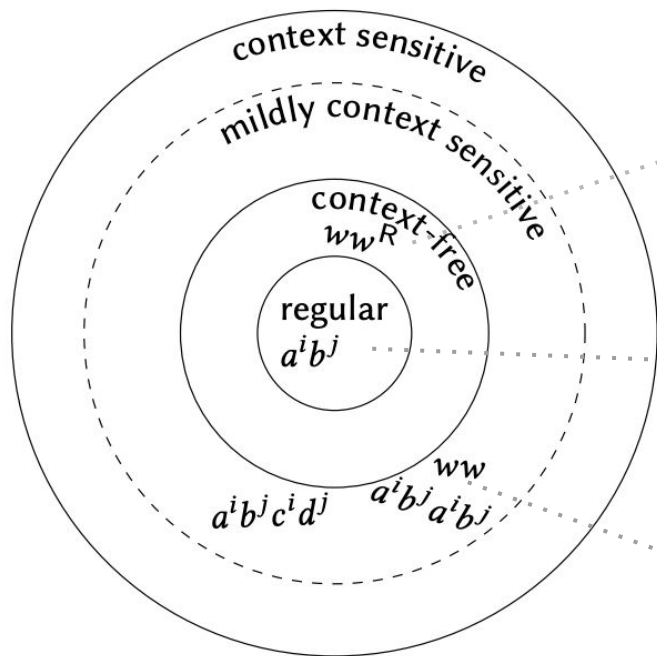
Reduplication-like representation for pseudo-reduplicated words (Zuraw, 2002)

→ supported by a MEG study on visual inputs (Wray et al., 2022)

# Why reduplication

- **Well-attested** in natural languages, typologically rich with many sub-types
  - ↪ Theoretical proposals for morpho-phonology (e.g., Marantz, 1982; McCarthy & Prince, 1986; Steriade, 1988; Gafos, 1998; Raimy, 2000; Inkelas & Zoll, 2005; Kiparsky, 2010; McCarthy et al., 2012; Zimmermann, 2021)
- Experimental works suggest humans are **highly sensitive** to identity-based patterns (e.g., Marcus et al., 1999; Gerken, 2006; Marcus et al., 2007; Kovács & Mehler, J., 2009a, 2009b; Gerken, 2010; Gervain et al., 2012; Wray et al., 2022; Gallagher, 2013; Berent et al., 2016, 2017; Moreton et al., 2021; Wang & Wilson, In prep) and reduplicative patterns aid speech segmentation (Ota & Skarabela, 2018) and facilitate lexical learning (Ota & Skarabela, 2016) .
- A **long-standing challenge** for formal languages theory and computational modeling (but see Frank & Tenenbaum, 2011; Berent et al, 2012; Prickett et al., 2022; Dolatian & Heinz, 2020; Beguš, 2021; Beguš & Zhou, 2022)

# The puzzle of reduplication



## String reversal

- ▶ rare, confined to language games (Marantz, 1982; Bagemihl, 1989)
- ▶ use explicit reasoning but not implicit linguistic knowledge (Moreton et al., 2021)

## Most phonology & morphology

(e.g., Johnson, 1972; Kaplan & Kay, 1994; Heinz, 2007; Chandlee, 2014; Chandlee, 2017)

## Unbounded copying & surface repetitions

- ▶ well-attested (e.g., Moravcsik, 1978; Rubino, 2013)
- ▶ use implicit linguistic knowledge (Moreton et al., 2021)

## **Question 1:**

How can we fit in reduplication with the rest of the (morpho-)phonology while excluding some unattested context-free patterns, such as reversals?

# Copying, but not reversal



As a **morphological generation** process,  $w \rightarrow ww$

(Dolatian & Heinz, 2018, 2019, 2020)

- Classifying the computation of the reduplicative typology based on **2-way (D-)Finite-state transducers**
  - ▶ **1-way** FST: only right movement along the input
  - ▶ **2-way** FST: move left and right along the input
  - ▶ **2-way rotating** FST: do not output anything while moving right-to-left  $\rightarrow$  no reversal

# Copying, but not reversal



As a morphological generation process,  $w \rightarrow ww$   
(Dolatian & Heinz, 2018, 2019, 2020)

- Classifying the computational properties of reduplicative typology based on **2-way (D-)Finite-state transducers**
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**Morphological analysis**  $ww \rightarrow w$ ?

## String-set problem

Namely, the computational properties of the surface phonological forms created by reduplication?



## Copying, but not reversal



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**Morphological analysis**  $ww \rightarrow w?$

### **String-set problem**

Namely, the computational properties of the surface phonological forms created?

**My proposal:** a formal characterization of regular languages (most phonology and morphophonology) and languages derived from them through a primitive copying operation.

# People wanted such a proposal long ago....

*We do not know whether there exists an independent characterization of **the class of languages that includes the regular sets and languages derivable from them through reduplication**, . . . this class might be relevant to the characterization of NL [natural language] word-sets.*

*(Gazdar and Pullum 1985, p 258).*

*Rather than grudgingly clambering up the Chomsky Hierarchy towards Context-sensitive Grammars, we should consider going back down to **Regular Grammars** and striking out in a different direction. The simplest alternative proposal is a class of grammars which intuitively have the same relation to **queues** that CFGs have to stacks.*

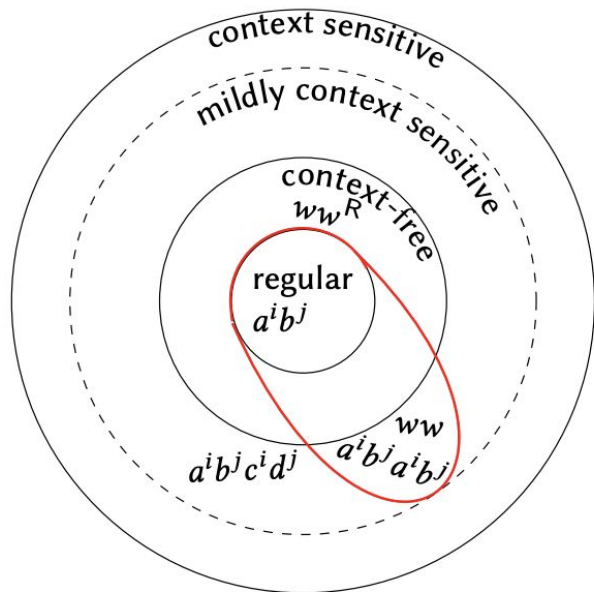
*(Manaster-Ramer 1986, p 87)*

# Proposal: Finite-state buffered machines

**A finite-state automata + a copying mechanism** (Wang & Hunter, 2023)

- Unbounded memory buffer, with queue storage and restricted ways of interaction with the input
  - same alphabet
  - once one symbol is removed, everything else must also be emptied
- Two modalities
  - Normal mode: similar to a normal FSA
  - Buffering mode: storing a copy of input symbols to the buffer
- Two special sets of states (indicating when to copy, and when to end)

# A proposed formal class (Wang 2021 a, b; Wang & Hunter, 2023)



Surveyed closure properties	Closed ?
union	✓
concatenation	✓
Kleene star	✓
homomorphism	✓
<b>Intersection with regular languages</b>	✓
Inverse homomorphism	✗
Recursive copying	✗
intersection	✗
complementation	✗

# On regular copying languages

*Yang Wang and Tim Hunter*  
University of California, Los Angeles

## ABSTRACT

This paper proposes a formal model of regular languages enriched with unbounded copying. We augment finite-state machinery with the ability to recognize copied strings by adding an unbounded memory buffer with a restricted form of first-in-first-out storage. The newly introduced computational device, finite-state buffered machines (FS-BMs), characterizes the class of regular languages and languages derived from them through a primitive copying operation. We name this language class *regular copying languages* (RCLs). We prove a pumping lemma and examine the closure properties of this language class. As suggested by previous literature (Gazdar and Pullum 1985, p.278), regular copying languages should approach the correct characterization of natural language word sets.

*Keywords:*  
*reduplication,*  
*copying,*  
*finite-state*  
*machinery,*  
*queue automata*



## **Question 2:**

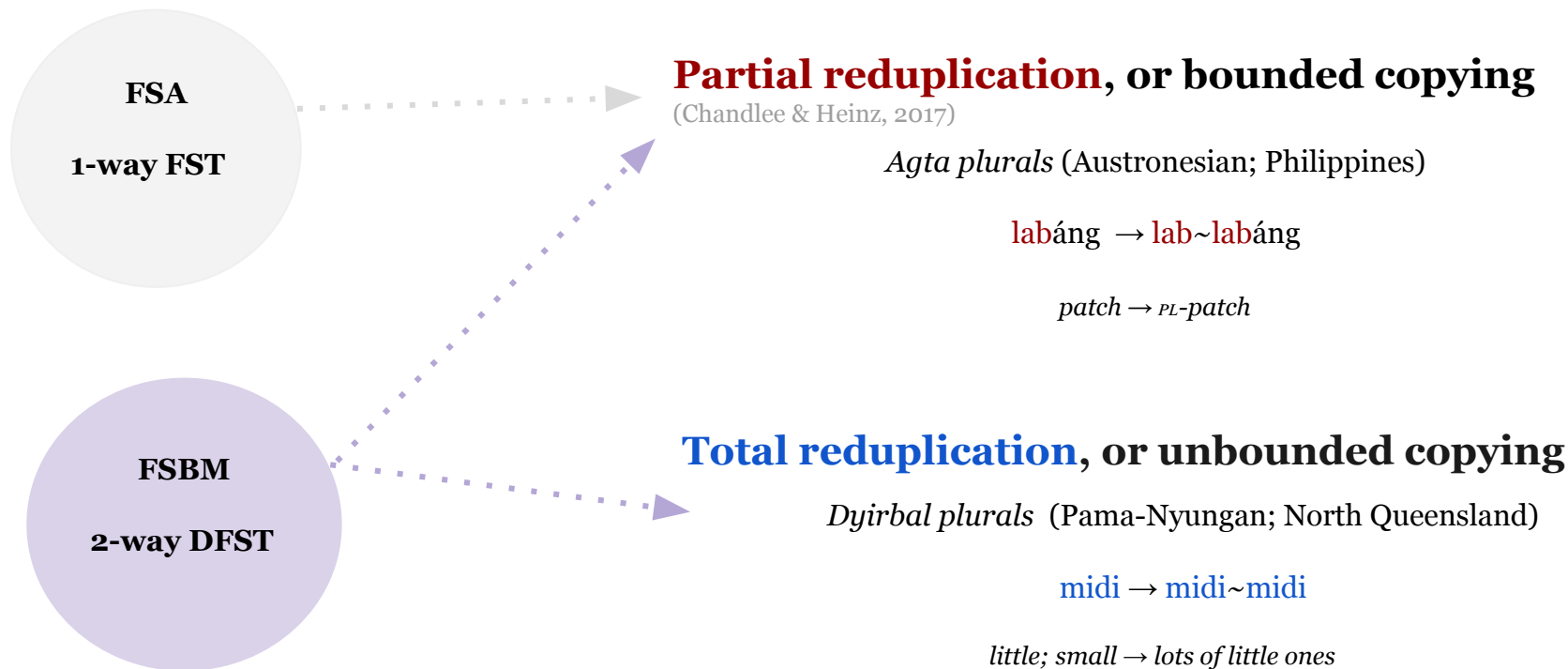
Now that reversals are excluded, does the enriched power overshoot? Should “regular” be sufficient?

# Copying, or not?

**Typology** says **yes** for the enriched power.

Now let us see some **evidence** from a **learning** experiment.

# Partial vs. total reduplication





# Hypotheses and predictions

	Total	Partial
FSA    1-way FST	✗	✓
FSBM    2-way FST	✓	✓

When people are prompted with input data that conform to both **total reduplication** and **partial reduplication**....

If we see people choose **total** over **partial**  $\Rightarrow$  yes for the extra copying operation

If we see people choose **partial** over **total**  $\Rightarrow$  inconclusive

# Extrapolation paradigm (aka. Poverty of the stimulus paradigm; Wilson, 2006)

**Training phase:** impoverished inputs, compatible with many possible hypotheses.

4 singular-plural pairs, where singulars are monosyllabic CVC nominals

**dug → dug~dug**

**Copy the full word?**

..... (e.g., feature-based  
template based on shared  
features at each slot; listed  
allomorphy, etc)

**Copy a CVC form?**

# Extrapolation paradigm (aka. Poverty of the stimulus paradigm; Wilson, 2006)

**Testing phase:** trials that can tease apart these different hypotheses

**20 novel singulars** (5 testing types; 4 for each type)

- |    |                 |                |                    |
|----|-----------------|----------------|--------------------|
| 1. | CVC             | Familiar       | 'nouɡ              |
| 2. | CV.CVC          | Disyllabic CV  | 'pa.diʃ            |
| 3. | CVC.CVC         | Disyllabic CVC | 'dɛb.gɪv           |
| 4. | CV.CV.CVC       | Trisyllabic    | 'teɪ.pə.gæb        |
| 5. | CV.CV.CV.CV.CVC | Five syllables | ,ɡɛ.zə.'seɪ.kə.dɪv |

# Procedure

## Training phase

- Participants were instructed to learn plural formation (pictures for semantic support)
- Listen to 4 singular ~ plural pairs
- Repeat the singular and the plural form

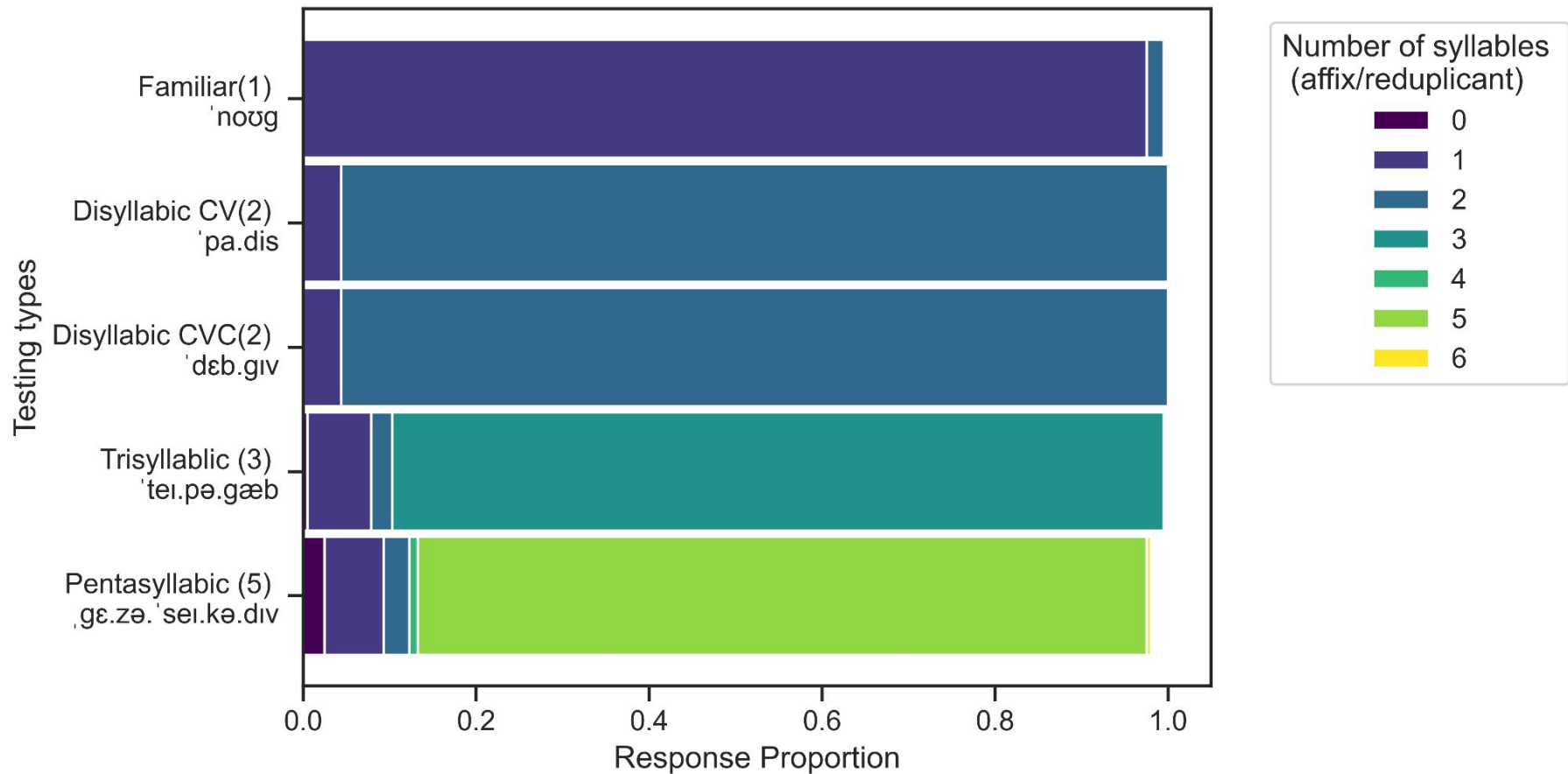
## Testing phase:

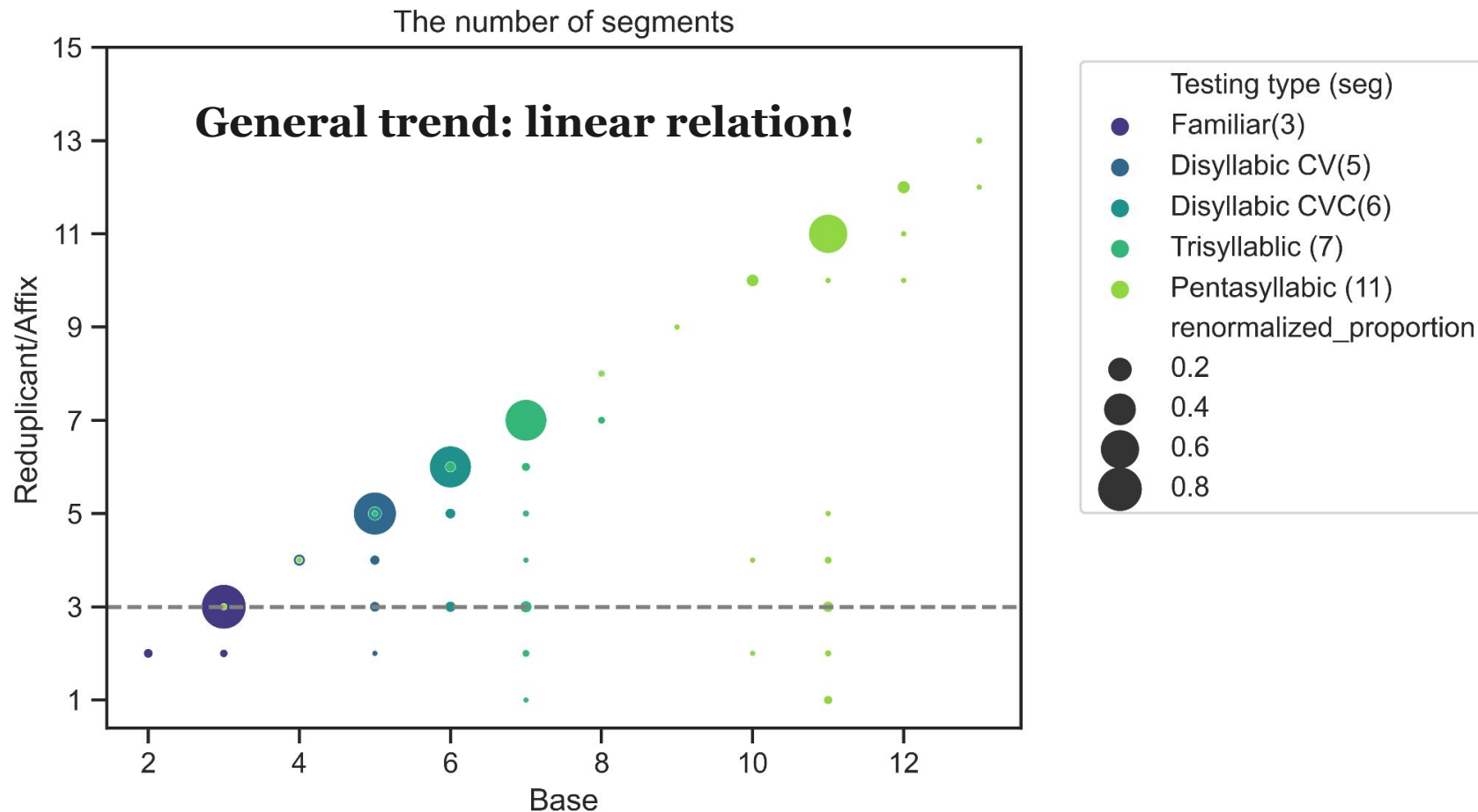
- Listen to a novel singular, repeat back, and produce the plural form
- All trial types tested together, order randomized

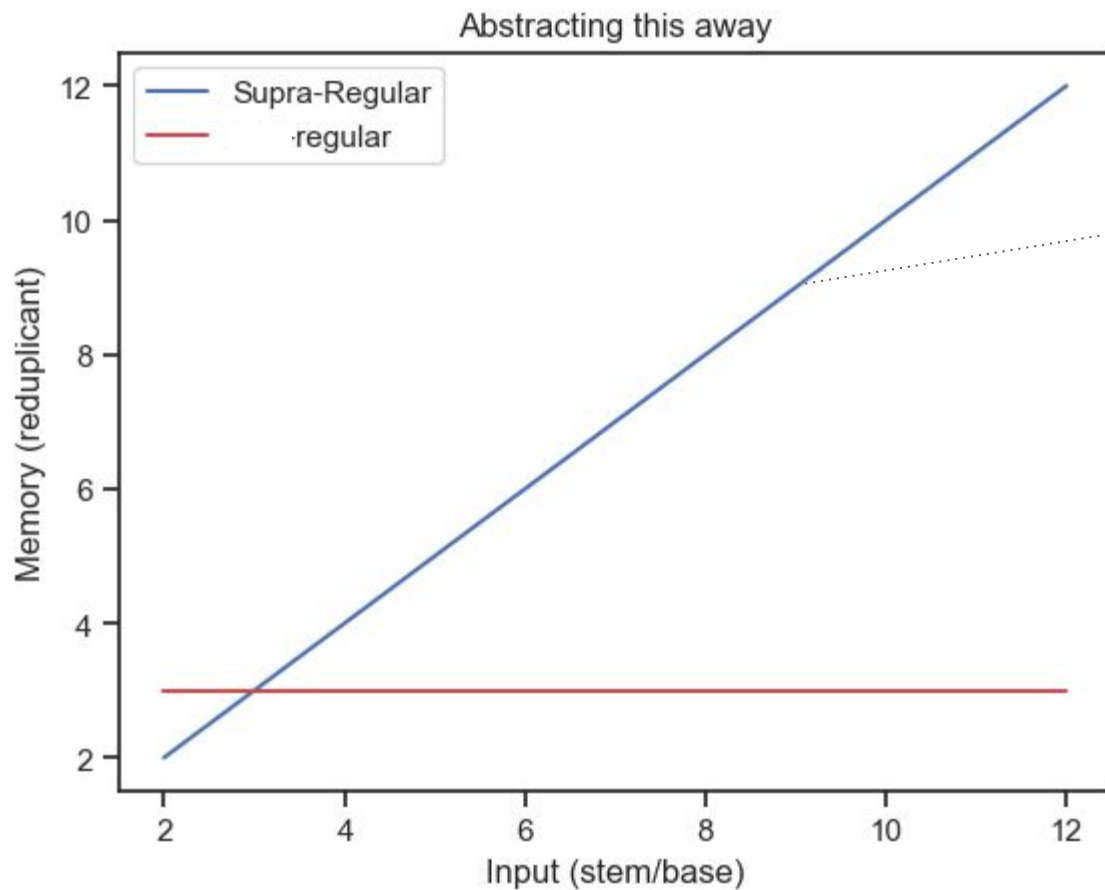
# Participants

52 US-based English speakers were recruited from Prolific (51 were analyzed)

- ▶ 1 exclusion due to silent responses for all training trials and 90% of the testing trials
- ▶ 29 Female; 21 Male; 1 Other
- ▶ Age: mean = 42.48; max = 72; min = 19
- ▶ Screening on prolific: English monolingual; primary language: English; no language-related disorders.







This is what has been learned!



## Hypotheses and predictions

	<b>Total</b>	<b>Partial</b>
FSA    1-way FST	✗	✓
FSBM    2-way FST	✓	✓

When people are prompted with input data that conform to both **total reduplication** and **partial reduplication**....

! If we see people choose **total** over **partial**  $\Rightarrow$  yes for the extra copying operation

If we see people choose **partial** over **total**  $\Rightarrow$  inconclusive

## **Question 3:**

How is reduplication learned?

# From grammatical knowledge to learning biases

The presented experiment addresses two levels of questions.

1. Whether the extra power to copy should be there in the grammatical knowledge?

**Answer: yes**

2. Is there any biases that guide the learner through the learning process?

**Answer: An inductive bias that prefers total reduplication over a segment-based length restricting hypothesis (at least for pluralization)**

**What about other attested patterns?**

# Extrapolation paradigm (aka. Poverty of the stimulus paradigm; Wilson, 2006)

**Training phase:** “impoverished” inputs, compatible with many possible hypotheses.

4 singular-plural pairs, where singular are monosyllabic CVC nominals

**dug → du~dug**

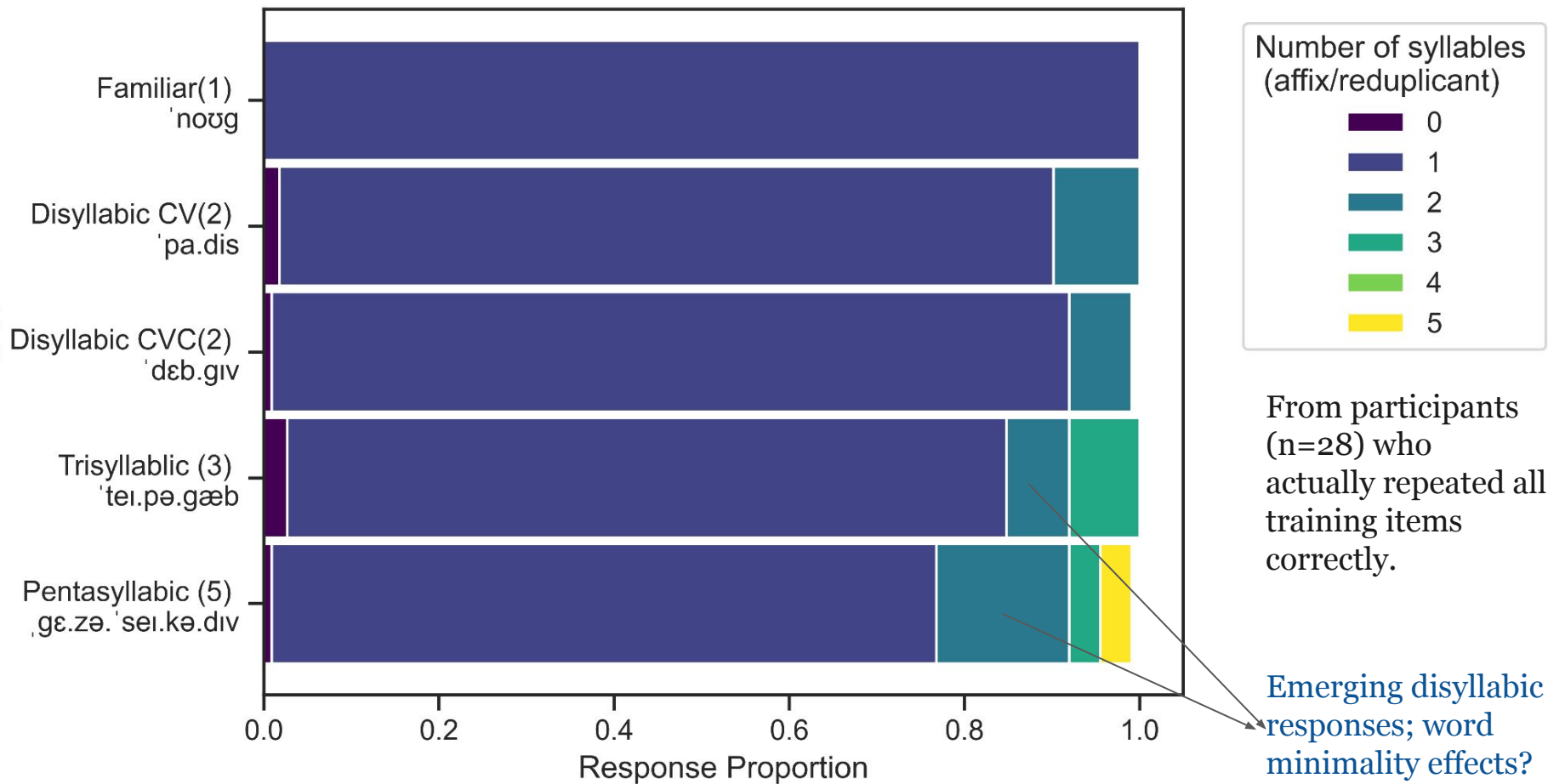
**Delete the last coda?**

.....(e.g., copy a CV of a final syllable/stressed syllable)

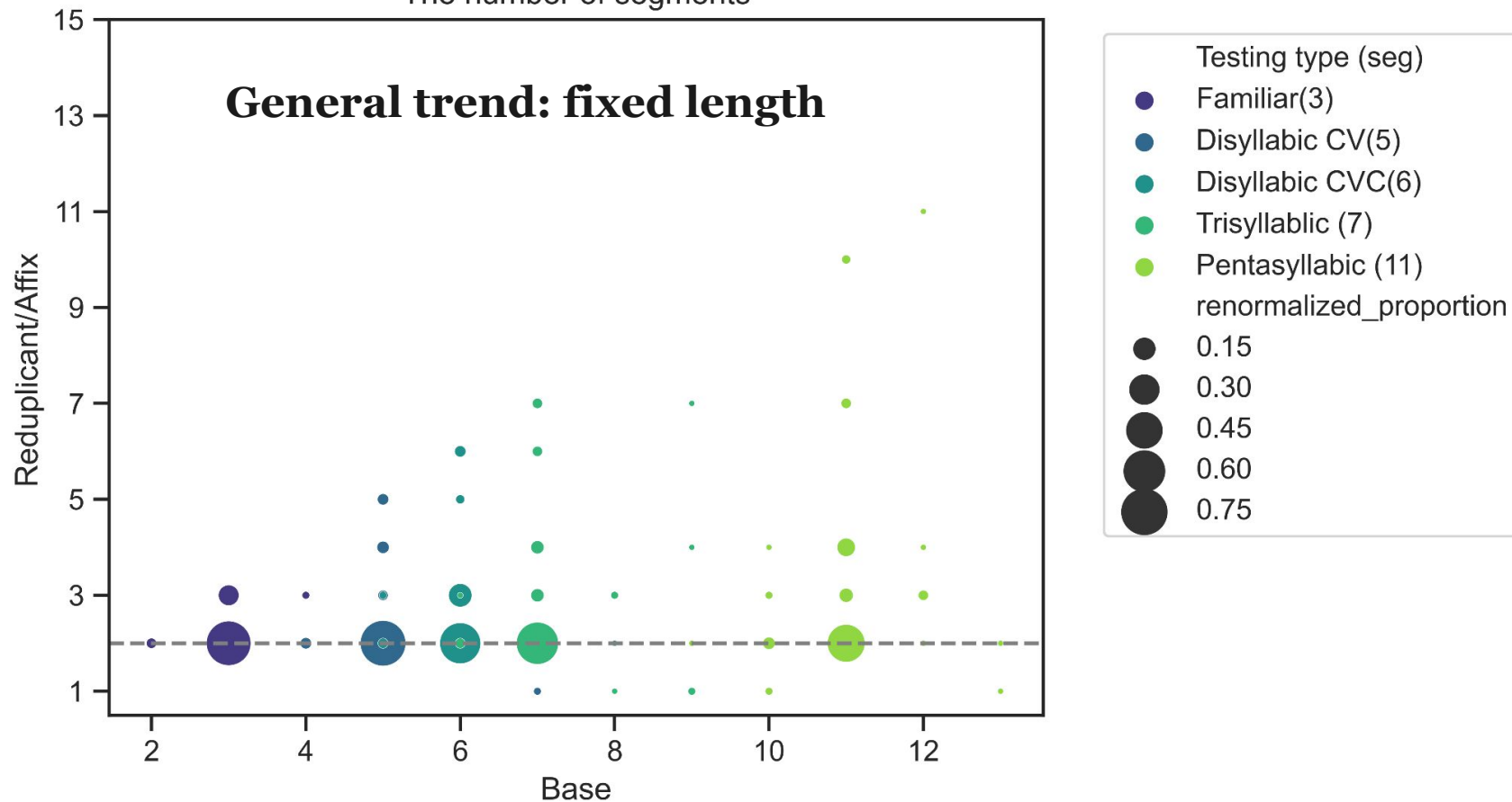
**Copy an initial CV?**

# Participants

- 36 US-based English speakers were recruited from Prolific (more replication in progress)
  - ▶ 1 participant were excluded due to failure to follow the experimental instruction by giving English words of the pictures
  - ▶ 2 participants were excluded because of exposure to languages with attested grammatical reduplication (Hebrew and Japanese)
- Data from 33 participants were analyzed
  - ▶ 20 Female; 12 Male; 1 Other
  - ▶ Age: mean = 39.30; max = 68; min = 18
  - ▶ Screening on prolific: English monolingual; primary language: English; no language-related disorders



The number of segments

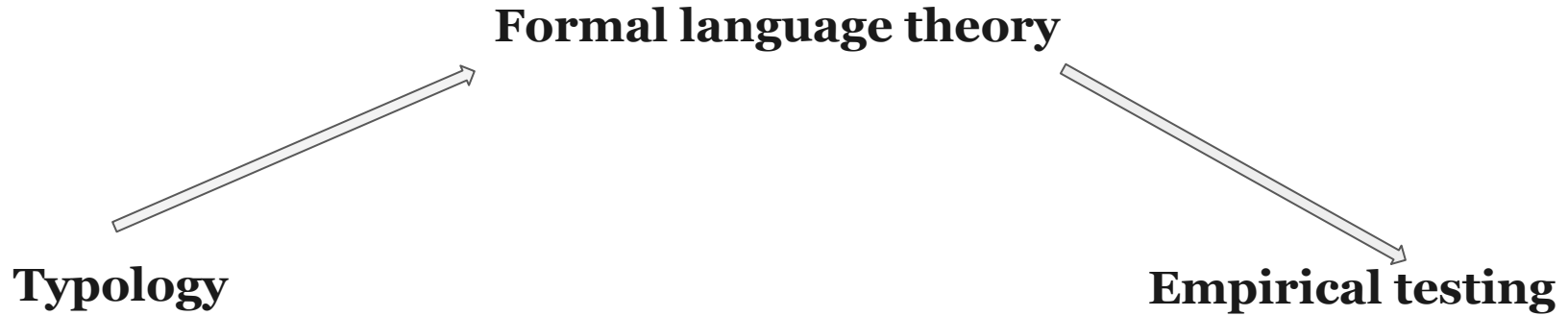


# Take-home message

- A computational device for natural language morphology and phonology requires a kind of the **primitive copying** operation.
- When trained with complete monosyllabic copying, people generalize total reduplication to longer forms, but not heavy syllable copying.
- Incomplete copying leads to more responses of invariant shapes (the one that gets trained on), with some emerging typological variations.
  - ▶ (ask me about this if you want to hear more!)



# Concluding remarks



# Thank you!

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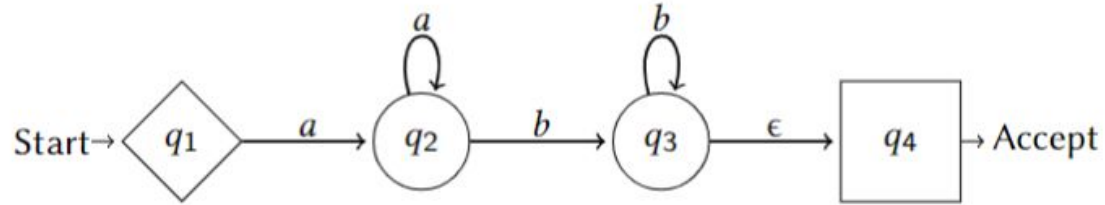
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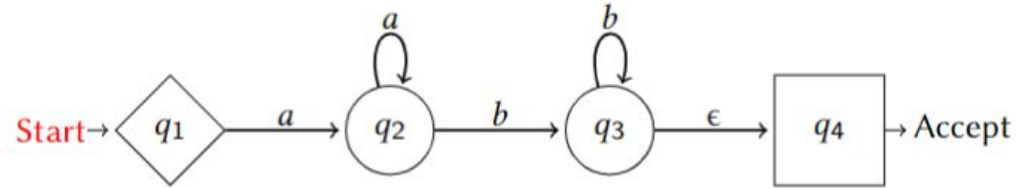
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# Appendix: A worked example



**Figure:** An FSBM  $M_2$  with  $G = \{q_1\}$  and  $H = \{q_4\}$ .  $L(M_2) = \{a^i b^j a^i b^j \mid i, j \geq 1\}$

# Appendix: A worked example

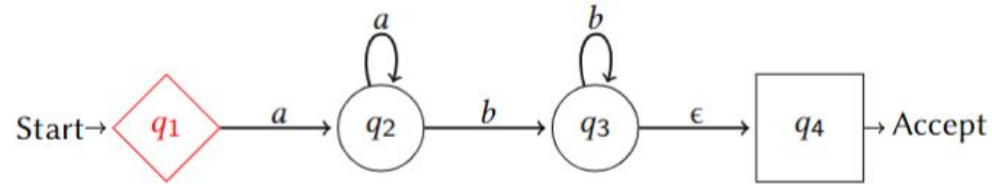


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input	state	buffer	mode
abbabb	$q_1$	$\epsilon$	N



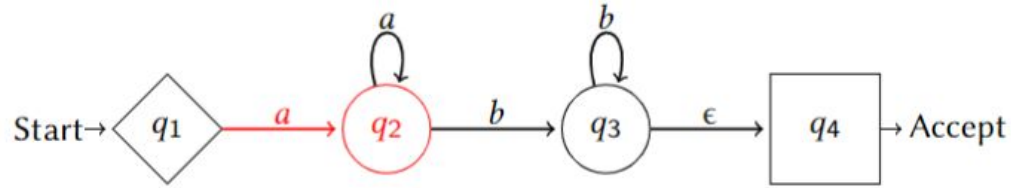
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input	state	buffer	mode
abbabb	$q_1$	$\epsilon$	N
abbabb	$q_1$	$\epsilon$	<b>B</b>

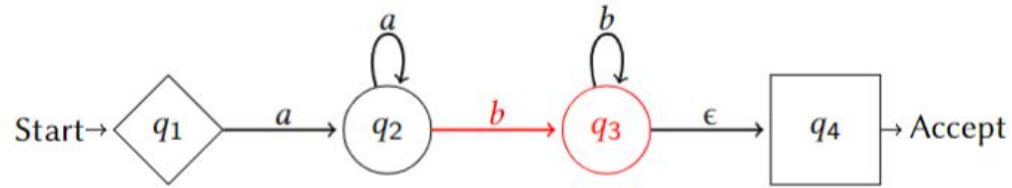
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input	state	buffer	mode
abbabb	$q_1$	$\epsilon$	N
abbabb	$q_1$	$\epsilon$	B
bbabb	$q_2$	a	B

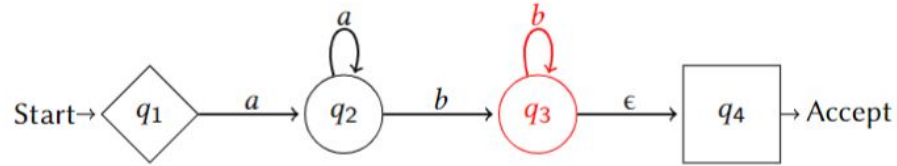
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input	state	buffer	mode
abbabb	$q_1$	$\epsilon$	N
abbabb	$q_1$	$\epsilon$	B
bbabb	$q_2$	a	B
babb	$q_3$	a <b>b</b>	B

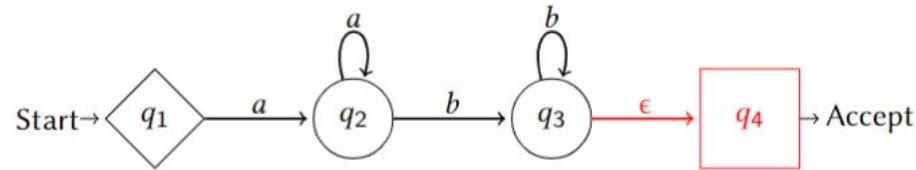
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input	state	buffer	mode
abbabb	$q_1$	$\epsilon$	N
abbabb	$q_1$	$\epsilon$	b
bbabb	$q_2$	a	B
babb	$q_3$	ab	B
abb	$q_3$	ab <b>b</b>	B

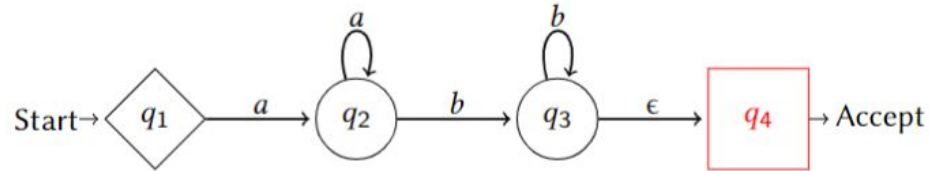
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abbabb	$q_1$	$\epsilon$	B
bbabb	$q_2$	a	B
babb	$q_3$	ab	B
abb	$q_3$	abb	B
abb	$q_4$	abb	B

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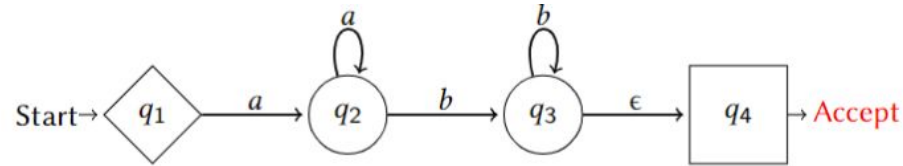


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input	state	buffer	mode
abbabb	$q_1$	$\epsilon$	N
abbabb	$q_1$	$\epsilon$	B
bbabb	$q_2$	a	B
babb	$q_3$	ab	B
abb	$q_3$	abb	B
abb	$q_4$	abb	B

input	state	buffer	mode
$\epsilon$	$q_4$	$\epsilon$	<span style="color:red">N</span>

# Appendix: A worked example



**Figure:** An FSBM  $M_2$  with  $G = \{q_1\}$  and  $H = \{q_4\}$ .  $L(M_2) = \{a^i b^j a^i b^j \mid i, j \geq 1\}$

input	state	buffer	mode
abbabb	$q_1$	$\epsilon$	N
abbabb	$q_1$	$\epsilon$	B
bbabb	$q_2$	a	B
babb	$q_3$	ab	B
abb	$q_3$	abb	B
abb	$q_4$	abb	B

input	state	buffer	mode
$\epsilon$	$q_4$	$\epsilon$	N
ACCEPT			

# Appendix: Emerging variation

- There are a lot of variations in terms of individual behaviors, which I did not have the time to show.
  - Quite a few instances of no-copying but listed allomorphy: ga-/da- prefixation; or deleting the last coda in the base;
  - Frequently, we observe “the emergence of the unmarked”: vowel reduction in the reduplicant
  - People vary in terms of which part to copy and where to place the reduplicant/affix (see slide 50)



# Appendix: Emerging variation

- ▶ One par variable total reduplication up to the disyllabic forms; for trisyllabic forms and five syllable word, copy the final syllable

'dɛb.gɪv- 'dɛb.gɪv

'teɪ.pə.gæb-gæb

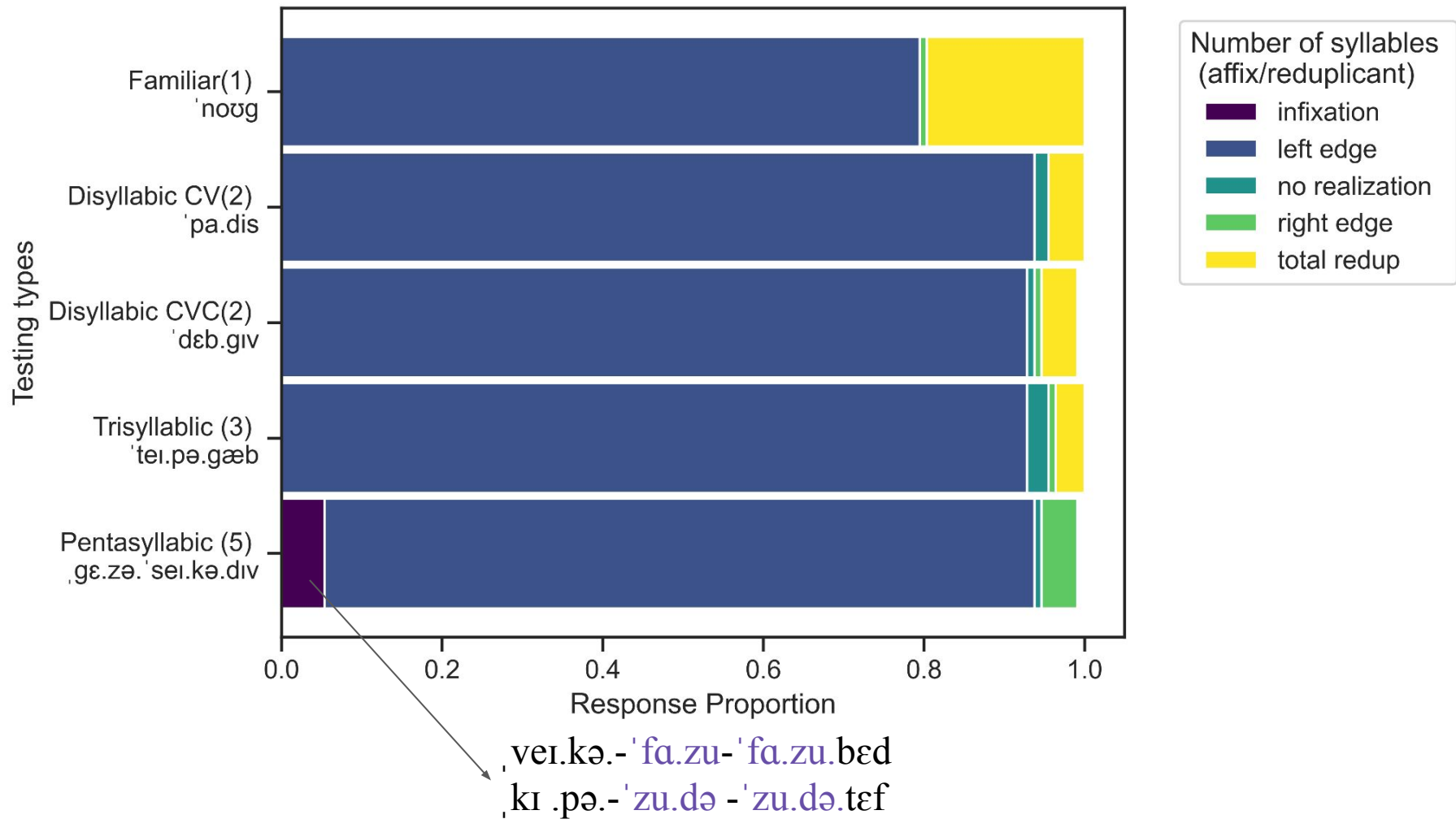
,gɛ.zə.'seɪ.kə.dɪv-dɪv

- ▶ One participant shows 3 instances of truncating both copies when the stem is long (templatic back-copying?)

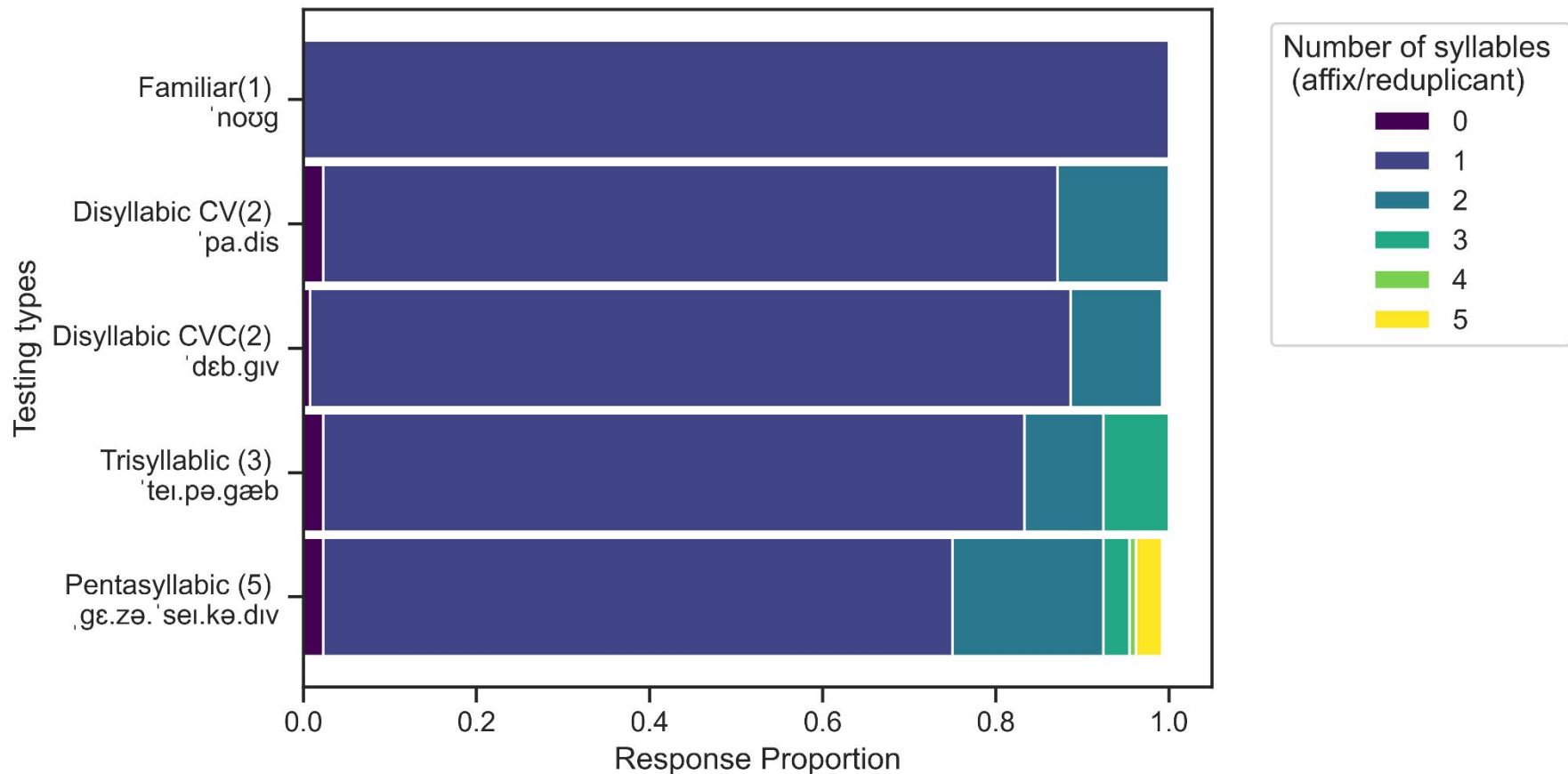
'di.zə.gɛd → diz-diz

,kɪpə'zudətɛf → kɪp-kɪp

,pi.sə.'gou.bɛ.kət → pis-pis



## Appendix: all participants in training without coda



The number of segments

