## 1 Variables

#### 2 root

	var	symbol	documentation	type	units	tokens	eqs
13	$F_{N,A}$	F	directed graph incidence matrix	network			
1	$t_N$	t	time	frame	s		
3	$t^o{}_N$	to	starting time	frame	s		1
4	$t^e{}_N$	te	end time	frame	s		2
2	#	value	numerical value	constant			
18	0	null	numerical value 0	constant			16
19	1	one	numerical value 1	constant		[]	17

# 3 System

	var	symbol	documentation	type	units	tokens	eqs
37	$\hat{x}^{A,\alpha}{}_N$	fx_A_alpha	netflow of token A due to mechanism alpha	transport	$ms^{-1}$	[]	50 55
38	$\hat{x}^{A,eta}{}_N$	fx_A_beta	netflow of token A due to mechanism beta	transport	$ms^{-1}$		51 66
39	$\hat{y}^{B,\gamma}{}_N$	fy_B_gamma	netflow of token B due to mechanism gammma	transport	$s^{-1}$	[]	52 57
40	$\hat{y}^{B,\delta}{}_N$	fy_B_delta	netflow of token B due to mechanism delta	transport	$s^{-1}$		53 54
5	$x_N$	x	state token A	state	$\mid m \mid$		62
11	$\pi^{A,\alpha}{}_N$	pi_A_alpha	effort A mechanism alpha	state	$\mid m \mid$		7 14
12	$\pi^{A,eta}{}_N$	pi_A_beta	effort A mechanism beta	state	$\mid m \mid$		8 15
16	$\dot{x}_N$	dx	differential state	state	$ms^{-1}$		18 58
17	$x^o{}_N$	xo	initial condition for token A	state	$\mid m \mid$		12
20	$\underline{\pi}^{A}{}_{N}$	pi_A_stack	the stack of intensive variables token A	state	$\mid m \mid$		19

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	var	symbol	documentation	type	units	tokens	eqs
21	$y_N$	у	state token B	state			63
24	$\pi^{B,\gamma}{}_N$	pi_B_gamma	effort B mechanism gamma	state			23
26	$\dot{y}_N$	dy	differential state for token B	state	$s^{-1}$		36 59
27	$y^o{}_N$	уо	initial condition for token B	state			26
33	$\pi^{B,\delta}{}_N$	pi_B_delta	effort B mechansim delta	state			32
36	$\underline{\pi}^B{}_N$	pi_B_stack	the stack of intensive variables token B	state			44
41	$xy_stack$	xy_stack	mixed stack of both states	state			64
42	$pi_AB_stack$	pi_AB_stack	stack of both sets of intensives	state			67
7	$K^{A,lpha}{}_N$	K_A_alpha	frequency token A	constant	$s^{-1}$		40
8	$K^{A,eta}{}_N$	K_A_beta	frequency token B	constant	$s^{-1}$		41
9	$M^{A,lpha}$	M_A_alpha	norming factor token A mechanism alpha	constant			42
10	$M^{A,eta}$	M_A_beta	norming factor token A mechanism beta	constant			43
22	$M^{B,\gamma}$	M_B_gamma	norming factor token B mechanism gamma	constant			
23	$K^{B,\gamma}{}_N$	K_B_gamma	norming factor token A mechanism d	constant	$s^{-1}$		22
30	$K^{B,\delta}{}_N$	K_B_delta	frequency B delta	constant	$s^{-1}$		30
31	$M^{B,\delta}$	M_B_delta	norming factor token B mechanism delta	constant			

# 4 Properties

	var	symbol	documentation	type	units	tokens	eqs
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## 5 Control

	var	symbol	documentation	type	units	tokens	eqs		
6	6 System-Properties								
	var	symbol	documentation	type	units	tokens	eqs		
7	7 Properties-System								
	var	symbol	documentation	type	units	tokens	eqs		
8	System-Contro	ol							
	var	symbol	documentation	type	units	tokens	eqs		
9	9 Control-System								
	var	symbol	documentation	type	units	tokens	eqs		
10	10 Properties-Control								
	var	symbol	documentation	type	units	tokens	eqs		

# 11 Control-Properties

	var	symbol	documentation	type	units	tokens	eqs
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## 12 Equations

#### 12.1 Model equations

no	equation	documentation	layer
1	$t^o{}_N := \operatorname{Instantiate}(t_N, \#)$	starting time	root
2	$t^e{}_N := \operatorname{Instantiate}(t_N, \#)$	end time	root
7	$\pi^{A,\alpha}{}_N := M^{A,\alpha} \cdot x_N$	effort a	System
8	$\pi^{A,\beta}{}_N := M^{A,\beta} \cdot x_N$	effort b	System
12	$x^o_N := \text{Instantiate}(x_N, \#)$	initial condition	System
14	$\pi^{A,\alpha}{}_N := \text{Instantiate}(\pi^{A,\alpha}{}_N, \#)$	effort a	System
15	${\pi^{A,\beta}}_N := \operatorname{Instantiate}({\pi^{A,\beta}}_N, \#)$	effort b	System
16	0 := Instantiate(#, #)	numerical value 0	root
17	1 := Instantiate(#, #)	numerical value 1	root
18	$\dot{x}_N := \text{Instantiate}(\dot{x}_N, 0)$	differential state	System
19	$\underline{\pi}^{A}{}_{N} := \operatorname{Stack}\left(\pi^{A,\alpha}{}_{N}, \pi^{A,\beta}{}_{N}\right)$	the stack of intensive variables	System
22	$K^{B,\gamma}{}_{N} := \operatorname{Instantiate}((t_{N})^{-1}, \#)$	frequency B alpha	System
23	$\pi^{B,\gamma}{}_N := M^{B,\gamma} \cdot y_N$	transport of B mechanism gamma	System
26	$y^o{}_N := \text{Instantiate}(y_N, \#)$	initial condition for token B	System
30	$K^{B,\delta}{}_{N} := \operatorname{Instantiate}((t_{N})^{-1}, \#)$	var doc : frequency B delta	System
32	$\pi^{B,\delta}{}_N := M^{B,\delta} \cdot y_N$	effort B mechansim delta	System

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no	equation	documentation	layer
36	$\dot{y}_N := \text{Instantiate}(\dot{y}_N, \#)$	differential state for token B	System
40	$K^{A,\alpha}{}_{N} := \operatorname{Instantiate}(\left(t_{N}\right)^{-1}, \#)$	frequency token A	System
41	$K^{A,\beta}{}_{N} := \operatorname{Instantiate}(\left(t_{N}\right)^{-1}, \#)$	frequency token B	System
42	$M^{A,lpha}:=\operatorname{Instantiate}(\#,\#)$	norming factor token A mechanism alpha	System
43	$M^{A,\beta} := \text{Instantiate}(\#, \#)$	norming factor token A mechanism beta	System
44	$\underline{\pi}^{B}{}_{N} := \operatorname{Stack}\left(\pi^{B,\gamma}{}_{N}, \pi^{B,\delta}{}_{N}\right)$	the stack of intensive variables token B	System
50	$\hat{x}^{A,\alpha}{}_{N} := F_{N,A} \stackrel{A}{\star} \left( K^{A,\alpha}{}_{N} . F_{N,A} \stackrel{N}{\star} \pi^{A,\alpha}{}_{N} \right)$	netflow of token A due to mechanism alpha	System
51	$\hat{x}^{A,\beta}{}_{N} := F_{N,A} \stackrel{A}{\star} \left( K^{A,\beta}{}_{N} \cdot F_{N,A} \stackrel{N}{\star} \pi^{A,\beta}{}_{N} \right)$	netflow of token A due to mechanism beta	System
52	$\hat{y}^{B,\gamma}{}_{N} := F_{N,A} \stackrel{A}{\star} \left( K^{B,\gamma}{}_{N} . F_{N,A} \stackrel{N}{\star} \pi^{B,\gamma}{}_{N} \right)$	netflow of token B due to mechanism gammma	System
53	$\hat{y}^{B,\delta}{}_{N} := F_{N,A}  \stackrel{A}{\star}  \left( K^{B,\delta}{}_{N}  .  F_{N,A}  \stackrel{N}{\star}  \pi^{B,\delta}{}_{N} \right)$	netflow of token B due to mechanism delta	System
54	$\hat{\boldsymbol{y}}^{B,\delta}{}_{N} := \text{Instantiate}(\hat{\boldsymbol{y}}^{B,\delta}{}_{N}, \#)$	netflow of token B due to mechanism delta	System
55	$\hat{x}^{A,\alpha}{}_N := \text{Instantiate}(\hat{x}^{A,\alpha}{}_N, \#)$	netflow of token A due to mechanism alpha	System
57	$\hat{y}^{B,\gamma}{}_N := \text{Instantiate}(\hat{y}^{B,\gamma}{}_N, \#)$	netflow of token B due to mechanism gammma	System
58	$\dot{x}_N := \hat{x}^{A,\alpha}{}_N + \hat{x}^{A,\beta}{}_N$	differential state	System

no	equation	documentation	layer
59	$\dot{y}_N := \hat{y}^{B,\gamma}{}_N + \hat{y}^{B,\delta}{}_N$	differential state for token B	System
62	$x_N := \int_{t^o_N}^{t^e_N} \dot{x}_N \ dt_N + x^o_N$	state token A	System
63	$y_N := \int_{t^o_N}^{t^e_N} \dot{y}_N \ dt_N + y^o_N$	state token B	System
64	$xy_stack := MixedStack(x_N, y_N)$	mixed stack of both states	System
66	$\hat{\boldsymbol{x}}^{A,\beta}{}_{N} := \operatorname{Instantiate}(\hat{\boldsymbol{x}}^{A,\alpha}{}_{N}, \#)$	netflow of token A due to mechanism beta	System
67	$pi_A B_s tack := \text{MixedStack}\left(\underline{\pi}^A{}_N, \underline{\pi}^B{}_N\right)$	stack of both sets of intensives	System