1 Variables

2 root

	var	symbol	documentation	type	units	tokens	eqs
8	$F_{N,A}$	F	directed graph indicence matrix	network			
1	t	t	time	frame	s		
6	t_o	to	starting time	frame	s		3
7	t_e	te	end time	frame	s		4
3	#	value	numerical value	constant			
4	1	one	numerical value 1	constant			1
5	0	null	numerical value 0	constant		[]	2

3 System

	var	symbol	documentation	type	units	tokens	eqs
25	$\hat{x}^{A,\alpha}{}_N$	fx_A_alpha	netflow of token A due to mechanism alpha	transport	ms^{-1}		11
26	$\hat{x}^{A,\beta}{}_N$	fx_A_beta	net flow of token A due to mechanism beta	${ m transport}$	ms^{-1}		12
27	$\hat{y}^{B,\gamma}{}_N$	fy_B_gamma	netflow of token B due to mechanism gamma	transport	s^{-1}		14
28	$\hat{y}^{B,\delta}{}_N$	fy_B_delta	netflow of token B due to mechansim beta	transport	s^{-1}		15
36	$D_{N,A}$	D	difference operator	${\it difference Operator}$			
9	x_N	x	state token A	state	$\mid m \mid$		20
10	y_N	у	state token B	state			21
11	x^{o}_{N}	хо	initial condition for state x	state	$\mid m \mid$		5
12	$y^o{}_N$	уо	initial condition for state y	state			6
34	s	S	mixed state	state			31

	var	symbol	documentation	type	units	tokens	eqs
13	$K^{A,\alpha}{}_A$	K_A_alpha	conductivity token A mechanism alpha	constant	s^{-1}		
14	$K^{A,\beta}{}_A$	K_A_beta	conductivity token A mechanism beta	constant	s^{-1}		
15	$K^{B,\gamma}{}_A$	K_B_gamma	conductivity token B mechanism gamma	constant	s^{-1}		
16	$K^{B,\delta}{}_A$	K_B_delta	conductivity token B mechanism delta	constant	s^{-1}		
17	$M^{A,\alpha}{}_N$	M_A_alpha	norming factor token A mechanism alpha	constant			
18	$M^{A,eta}{}_N$	M_A_beta	norming factor token A mechanism beta	constant			
19	$M^{B,\gamma}{}_N$	M_B_gamma	norming factor token B mechanism gamma	constant			
20	$M^{B,\delta}{}_N$	M_B_delta	norming factor token B mechanism delta	constant			
21	$\pi^{A,\alpha}{}_N$	pi_A_alpha	effort for A mechanism alpha	secondaryState	$\mid m \mid$		7 27
22	$\pi^{A,\beta}{}_N$	pi_A_beta	effort for A mechanism beta	secondaryState	$\mid m \mid$		8 28
23	$\pi^{B,\gamma}{}_N$	pi_B_gamma	effort for B mechanism gamma	secondaryState			9 29
24	$\pi^{B,\delta}{}_N$	pi_B_delta	effort for B mechanism delta	secondaryState			10 30
31	$\underline{\pi}^{A}{}_{N}$	pi_A_stack	effort for token A stack	secondaryState	$\mid m \mid$		24
32	$\underline{\pi}^B{}_N$	pi_B_stack	effort for token B stack	secondaryState			25
33	$\underline{\pi}^{A,B}$	pi_stack	effort for token A, B stack	secondaryState			26
29	\dot{x}_N	dx	diferential balance for token A	differentialState	ms^{-1}		16 32
30	\dot{y}_N	dy	differential balance for token B	differentialState	s^{-1}		17 33
35	dxy	dxy	mixed stack of the two accumulation terms	differentialState			34

4 Properties

	var	symbol	documentation	type	units	tokens	eqs
37	$K_{Aa}lpha_{A}$	K_A_alpha	conductivity token A mechanism alpha	constant	s^{-1}		
38	$K_{Ab}eta_A$	K_A_beta	conductivity token A mechanism beta	constant	s^{-1}		
39	$K_{Bg}amma_A$	K_B_gamma	conductivity token B mechanism gamma	constant	s^{-1}		

	var	symbol	documentation	type	units	$_{ m tokens}$	eqs
40	$K_{Bd}elta_A$	K_B_delta	conductivity token B mechanism delta	constant	s^{-1}		
42	K_A	K	stack of conductivities	constant	s^{-1}		36

5 Control

	var	symbol	documentation	type	units	tokens	eqs
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6 System-Properties

	var	symbol	documentation	type	units	tokens	eqs
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7 Properties-System

	var	symbol	documentation	type	units	${ m tokens}$	eqs
41	$k_{Aa}lpha_{A}$	k_A_alpha	link	transform	s^{-1}	[]	35
43	$k_{Ab}eta_{A}$	k_A_beta	link	${ m transform}$	s^{-1}		37
44	$k_{Bd}elta_{A}$	k_B_delta	link	${ m transform}$	s^{-1}		38
45	$k_{Bg}amma_A$	k_B_gamma	link	${ m transform}$	s^{-1}	[]	39

8 System-Control

	var	symbol	documentation	type	units	tokens	eqs
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9 Control-System

	var	symbol	documentation	type	units	tokens	eqs
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10 Properties-Control

	var	symbol	documentation	type	units	tokens	eqs
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11 Control-Properties

var	symbol	documentation	type	units	tokens	eqs

12 Equations

12.1 Model equations

no	equation	documentation	layer
1	1 := Instantiate(#, #)	numerical value 1	root
2	0 := Instantiate(#, #)	numerical value 0	root
3	$t_o := \text{Instantiate}(t, \#)$	starting time	root
4	$t_e := \text{Instantiate}(t, \#)$	end time	root
5	$x^o_N := \text{Instantiate}(x_N, \#)$	initial condition for state x	System
6	$y^o_N := \text{Instantiate}(y_N, \#)$	initial condition for state y	System
7	$\pi^{A,\alpha}{}_N := M^{A,\alpha}{}_N \cdot x_N$	effort for B mechanism alpha	System
8	$\pi^{A,\beta}{}_N := M^{A,\beta}{}_N \cdot x_N$	effort for A mechanism beta	System
9	$\pi^{B,\gamma}{}_N := M^{B,\gamma}{}_N . y_N$	effort for B mechanism gamma	System
10	$\pi^{B,\delta}{}_N := M^{B,\delta}{}_N \cdot y_N$	effort for B mechanism delta	System
11	$\hat{x}^{A,\alpha}{}_{N} := F_{N,A} \stackrel{A}{\star} \left(k_{Aa}lpha_{A} \cdot D_{N,A} \stackrel{N}{\star} \pi^{A,\alpha}{}_{N} \right)$	netflow of token A due to mechanism alpha	System
12	$\hat{x}^{A,\beta}{}_{N} := F_{N,A} \stackrel{A}{\star} \left(k_{Ab}eta_{A} . D_{N,A} \stackrel{N}{\star} \pi^{A,\beta}{}_{N} \right)$	net flow of token A due to mechanism beta	System
14	$\hat{y}^{B,\gamma}{}_{N} := F_{N,A} \stackrel{A}{\star} \left(k_{Bg} amm a_{A} . D_{N,A} \stackrel{N}{\star} \pi^{B,\gamma}{}_{N} \right)$	netflow of token B due to mechanism gamma	System
15	$\hat{y}^{B,\delta}{}_{N} := F_{N,A} \stackrel{A}{\star} \left(k_{Bd}elta_{A} . D_{N,A} \stackrel{N}{\star} \pi^{B,\delta}{}_{N} \right)$	netflow of token B due to mechansim beta	System

no	equation	documentation	layer
16	$\dot{x}_N := \hat{x}^{A,\alpha}{}_N + \hat{x}^{A,\beta}{}_N$	diferential balance for token A	System
17	$\dot{y}_N := \hat{y}^{B,\gamma}{}_N + \hat{y}^{B,\delta}{}_N$	differential balance for token B	System
20	$x_N := \int_{t_o}^{t_e} \dot{x}_N \ dt + x^o_N$	state token A	System
21	$y_N := \int_{t_o}^{t_e} \dot{y}_N dt + y^o{}_N$	state token B	System
24	$igg \underline{\pi}^{A}{}_{N} := \operatorname{Stack} \left(\pi^{A,lpha}{}_{N}, \pi^{A,eta}{}_{N} ight)$	effort for token A stack	System
25	$igg \underline{\pi}^B{}_N := \operatorname{Stack} \left(\pi^{B,\gamma}{}_N, \pi^{B,\delta}{}_N ight)$	effort for token B stack	System
26	$oxed{\pi^{A,B}} := \operatorname{MixedStack}\left(\overline{\pi}^{A}{}_{N}, \overline{\pi}^{B}{}_{N} ight)$	effort for token A, B stack	System
27	$\pi^{A,\alpha}{}_N := \text{Instantiate}(\pi^{A,\alpha}{}_N, \#)$	effort for B mechanism alpha	System
28	$\pi^{A,\beta}{}_{N} := \operatorname{Instantiate}(\pi^{A,\beta}{}_{N}, \#)$	effort for A mechanism beta	System
29	$\pi^{B,\gamma}{}_N := \text{Instantiate}(\pi^{B,\gamma}{}_N, \#)$	effort for B mechanism gamma	System
30	$\pi^{B,\delta}{}_N := \text{Instantiate}(\pi^{B,\delta}{}_N, \#)$	effort for B mechanism delta	System
31	$s := \text{MixedStack}(x_N, y_N)$	mixed state	System
32	$\dot{x}_N := \text{Instantiate}(\dot{x}_N, 0)$	diferential balance for token A	System
33	$\dot{y}_N := \operatorname{Instantiate}(\dot{y}_N, 0)$	differential balance for token B	System
34	$dxy := \operatorname{MixedStack}\left(\dot{x}_N, \dot{y}_N ight)$	mixed stack of the two accumulation terms	System
35	$egin{aligned} k_{Aa}lpha_A := K_{Aa}lpha_A \end{aligned}$	var doc : link	Properties »> System
36	$K_A := \operatorname{Stack}\left(K_{Aa}lpha_A, K_{Ab}eta_A, K_{Bg}amma_A, K_{Bd}elta_A\right)$	stack of conductivities	Properties

no	equation	documentation	layer
37	$k_{Ab}eta_A := K_{Ab}eta_A$	link	Properties »> System
38	$k_{Bd}elta_A := K_{Bd}elta_A$	link	Properties »> System
39	$k_{Bg}amma_A := K_{Bg}amma_A$	link	Properties »> System