## 1 Variables

#### 2 root

	var	symbol	documentation	type	units	tokens	eqs
8	$F_{N,A}$	F	directed graph indicence matrix	network			
1	$t_N$	t	time	frame	s		
6	$t_{oN}$	to	starting time	frame	s		3
7	$t_{eN}$	te	end time	frame	s		4
3	#	value	numerical value	constant			
4	1	one	numerical value 1	constant			1
5	0	null	numerical value 0	constant			2

# 3 System

	var	symbol	documentation	type	units	tokens	eqs
25	$\hat{x}^{A,\alpha}{}_N$	fx_A_alpha	netflow of token A due to mechanism alpha	transport	$ms^{-1}$		11
26	$\hat{x}^{A,\beta}{}_N$	fx_A_beta	net flow of token A due to mechanism beta	${ m transport}$	$ms^{-1}$		12
27	$\hat{y}^{B,\gamma}{}_N$	fy_B_gamma	netflow of token B due to mechanism gamma	transport	$s^{-1}$		14
28	$\hat{y}^{B,\delta}{}_N$	fy_B_delta	netflow of token B due to mechansim beta	transport	$s^{-1}$		15
36	$D_{N,A}$	D	difference operator	${\it difference Operator}$			
9	$x_N$	x	state token A	state	$\mid m \mid$		20
10	$y_N$	у	state token B	state			21
11	$x^{o}_{N}$	хо	initial condition for state x	state	$\mid m \mid$		5
12	$y^o{}_N$	уо	initial condition for state y	state			6
34	s	S	mixed state	state			31

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	var	symbol	documentation	type	units	tokens	eqs
13	$K^{A,\alpha}{}_A$	K_A_alpha	conductivity token A mechanism alpha	constant	$s^{-1}$		
14	$K^{A,eta}{}_A$	K_A_beta	conductivity token A mechanism beta	constant	$s^{-1}$		
15	$K^{B,\gamma}{}_A$	K_B_gamma	conductivity token B mechanism gamma	constant	$s^{-1}$		
16	$K^{B,\delta}{}_A$	K_B_delta	conductivity token B mechanism delta	constant	$s^{-1}$		
17	$M^{A,\alpha}{}_N$	M_A_alpha	norming factor token A mechanism alpha	constant			
18	$M^{A,eta}{}_N$	M_A_beta	norming factor token A mechanism beta	constant			
19	$M^{B,\gamma}{}_N$	M_B_gamma	norming factor token B mechanism gamma	constant			
20	$M^{B,\delta}{}_N$	M_B_delta	norming factor token B mechanism delta	constant			
21	$\pi^{A,lpha}{}_N$	pi_A_alpha	effort for A mechanism alpha	secondaryState	$\mid m \mid$		7 27
22	$\pi^{A,eta}{}_N$	pi_A_beta	effort for A mechanism beta	secondaryState	$\mid m \mid$		8 28
23	$\pi^{B,\gamma}{}_N$	pi_B_gamma	effort for B mechanism gamma	secondaryState			9 29
24	$\pi^{B,\delta}{}_N$	pi_B_delta	effort for B mechanism delta	secondaryState			10 30
31	$\underline{\pi}^{A}{}_{N}$	pi_A_stack	effort for token A stack	secondaryState	$\mid m \mid$		24
32	$\underline{\pi}^B{}_N$	pi_B_stack	effort for token B stack	secondaryState			25
33	$\underline{\pi}^{A,B}$	pi_stack	effort for token A, B stack	secondaryState			26
29	$\dot{x}_N$	dx	diferential balance for token A	differentialState	$ms^{-1}$		16 32
30	$\dot{y}_N$	dy	differential balance for token B	differentialState	$s^{-1}$		17 33
35	dxy	dxy	mixed stack of the two accumulation terms	differentialState			34

# 4 Properties

	var	symbol	documentation	type	units	tokens	eqs
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#### 5 Control

	var	symbol	documentation	type	units	tokens	eqs			
6	6 System-Properties									
	var	symbol	documentation	type	units	tokens	eqs			
7	7 Properties-System									
	var	symbol	documentation	type	units	tokens	eqs			
8	8 System-Control									
	var	symbol	documentation	type	units	tokens	eqs			
9	9 Control-System									
	var	symbol	documentation	type	units	tokens	eqs			
10	10 Properties-Control									
	var	symbol	documentation	type	units	tokens	eqs			

# 11 Control-Properties

	var	symbol	documentation	type	units	tokens	eqs
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## 12 Equations

#### 12.1 Model equations

no	equation	documentation	layer
1	1 := Instantiate(#, #)	numerical value 1	root
2	0 := Instantiate(#, #)	numerical value 0	root
3	$t_{oN} := \text{Instantiate}(t_N, \#)$	starting time	root
4	$t_{eN} := \text{Instantiate}(t_N, \#)$	end time	root
5	$x^o_N := \text{Instantiate}(x_N, \#)$	initial condition for state x	System
6	$y^o_N := \text{Instantiate}(y_N, \#)$	initial condition for state y	System
7	$\pi^{A,\alpha}{}_N := M^{A,\alpha}{}_N \cdot x_N$	effort for B mechanism alpha	System
8	$\pi^{A,\beta}{}_N := M^{A,\beta}{}_N \cdot x_N$	effort for A mechanism beta	System
9	$\pi^{B,\gamma}{}_N := M^{B,\gamma}{}_N \cdot y_N$	effort for B mechanism gamma	System
10	$\pi^{B,\delta}{}_N := M^{B,\delta}{}_N \cdot y_N$	effort for B mechanism delta	System
11	$\hat{x}^{A,\alpha}{}_{N} := F_{N,A} \stackrel{A}{\star} \left( K^{A,\alpha}{}_{A} . D_{N,A} \stackrel{N}{\star} \pi^{A,\alpha}{}_{N} \right)$	netflow of token A due to mechanism alpha	System
12	$\hat{x}^{A,\beta}{}_{N} := F_{N,A} \stackrel{A}{\star} \left( K^{A,\beta}{}_{A} \cdot D_{N,A} \stackrel{N}{\star} \pi^{A,\beta}{}_{N} \right)$	net flow of token A due to mechanism beta	System
14	$\hat{y}^{B,\gamma}{}_{N} := F_{N,A} \stackrel{A}{\star} \left( K^{B,\gamma}{}_{A} \cdot D_{N,A} \stackrel{N}{\star} \pi^{B,\gamma}{}_{N} \right)$	netflow of token B due to mechanism gamma	System
15	$\hat{y}^{B,\delta}{}_{N} := F_{N,A} \stackrel{A}{\star} \left( K^{B,\delta}{}_{A} \cdot D_{N,A} \stackrel{N}{\star} \pi^{B,\delta}{}_{N} \right)$	netflow of token B due to mechansim beta	System

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no	equation	documentation	layer
16	$\dot{x}_N := \hat{x}^{A,\alpha}{}_N + \hat{x}^{A,\beta}{}_N$	diferential balance for token A	System
17	$\dot{y}_N := \hat{y}^{B,\gamma}{}_N + \hat{y}^{B,\delta}{}_N$	differential balance for token B	System
20	$x_N := \int_{t_{o_N}}^{t_{e_N}} \dot{x}_N \ dt_N + x^o{}_N$	state token A	System
21	$y_N := \int_{t_{oN}}^{t_{eN}} \dot{y}_N \ dt_N + y^o{}_N$	state token B	System
24	$\underline{\pi}^{A}{}_{N} := \operatorname{Stack}\left(\pi^{A,\alpha}{}_{N}, \pi^{A,\beta}{}_{N}\right)$	effort for token A stack	System
25	$\underline{\pi}^{B}{}_{N} := \operatorname{Stack}\left(\pi^{B,\gamma}{}_{N}, \pi^{B,\delta}{}_{N}\right)$	effort for token B stack	System
26	$\underline{\pi}^{A,B} := \operatorname{MixedStack}\left(\underline{\pi}^{A}{}_{N},\underline{\pi}^{B}{}_{N}\right)$	effort for token A, B stack	System
27	$\pi^{A,\alpha}{}_N := \text{Instantiate}(\pi^{A,\alpha}{}_N, \#)$	effort for B mechanism alpha	System
28	${\pi^{A,\beta}}_N := \operatorname{Instantiate}({\pi^{A,\beta}}_N, \#)$	effort for A mechanism beta	System
29	$\pi^{B,\gamma}{}_N := \text{Instantiate}(\pi^{B,\gamma}{}_N,\#)$	effort for B mechanism gamma	System
30	$\pi^{B,\delta}{}_N := \text{Instantiate}(\pi^{B,\delta}{}_N, \#)$	effort for B mechanism delta	System
31	$s := \operatorname{MixedStack}(x_N, y_N)$	mixed state	System
32	$\dot{x}_N := \operatorname{Instantiate}(\dot{x}_N, 0)$	diferential balance for token A	System
33	$\dot{y}_N := \operatorname{Instantiate}(\dot{y}_N, 0)$	differential balance for token B	System
34	$dxy := \operatorname{MixedStack}\left(\dot{x}_N, \dot{y}_N\right)$	mixed stack of the two accumulation terms	System