1 Variables

2 root

| | var | symbol | documentation | type | units | tokens | eqs |
|---|-----------|--------|---------------------------------|----------|-------|--------|-----|
| 8 | $F_{N,A}$ | F | directed graph indicence matrix | network | | | |
| 1 | t | t | time | frame | s | | |
| 6 | t_o | to | starting time | frame | s | | 3 |
| 7 | t_e | te | end time | frame | s | | 4 |
| 3 | # | value | numerical value | constant | | | |
| 4 | 1 | one | numerical value 1 | constant | | | 1 |
| 5 | 0 | null | numerical value 0 | constant | | [] | 2 |

3 System

| | var | symbol | documentation | type | units | tokens | eqs |
|----|--------------------------|------------|---|-----------------------------|---------------|--------|-----|
| 25 | $\hat{x}^{A,\alpha}{}_N$ | fx_A_alpha | netflow of token A due to mechanism alpha | transport | ms^{-1} | | 11 |
| 26 | $\hat{x}^{A,\beta}{}_N$ | fx_A_beta | net flow of token A due to mechanism beta | ${ m transport}$ | ms^{-1} | | 12 |
| 27 | $\hat{y}^{B,\gamma}{}_N$ | fy_B_gamma | netflow of token B due to mechanism gamma | transport | s^{-1} | | 14 |
| 28 | $\hat{y}^{B,\delta}{}_N$ | fy_B_delta | netflow of token B due to mechansim beta | transport | s^{-1} | | 15 |
| 36 | $D_{N,A}$ | D | difference operator | ${\it difference Operator}$ | | | |
| 9 | x_N | x | state token A | state | $\mid m \mid$ | | 20 |
| 10 | y_N | у | state token B | state | | | 21 |
| 11 | x^{o}_{N} | хо | initial condition for state x | state | $\mid m \mid$ | | 5 |
| 12 | $y^o{}_N$ | уо | initial condition for state y | state | | | 6 |
| 34 | s | S | mixed state | state | | | 31 |

| | var | symbol | documentation | type | units | tokens | eqs |
|----|-----------------------------|------------|---|-------------------|---------------|--------|-------|
| 13 | $K^{A,\alpha}{}_A$ | K_A_alpha | conductivity token A mechanism alpha | constant | s^{-1} | | |
| 14 | $K^{A,\beta}{}_A$ | K_A_beta | conductivity token A mechanism beta | constant | s^{-1} | | |
| 15 | $K^{B,\gamma}{}_A$ | K_B_gamma | conductivity token B mechanism gamma | constant | s^{-1} | | |
| 16 | $K^{B,\delta}{}_A$ | K_B_delta | conductivity token B mechanism delta | constant | s^{-1} | | |
| 17 | $M^{A,lpha}{}_N$ | M_A_alpha | norming factor token A mechanism alpha | constant | | | |
| 18 | $M^{A,eta}{}_N$ | M_A_beta | norming factor token A mechanism beta | constant | | | |
| 19 | $M^{B,\gamma}{}_N$ | M_B_gamma | norming factor token B mechanism gamma | constant | | | |
| 20 | $M^{B,\delta}{}_N$ | M_B_delta | norming factor token B mechanism delta | constant | | | |
| 21 | $\pi^{A,\alpha}{}_N$ | pi_A_alpha | effort for A mechanism alpha | secondaryState | $\mid m \mid$ | | 7 27 |
| 22 | $\pi^{A,\beta}{}_N$ | pi_A_beta | effort for A mechanism beta | secondaryState | $\mid m \mid$ | | 8 28 |
| 23 | $\pi^{B,\gamma}{}_N$ | pi_B_gamma | effort for B mechanism gamma | secondaryState | | | 9 29 |
| 24 | $\pi^{B,\delta}{}_N$ | pi_B_delta | effort for B mechanism delta | secondaryState | | | 10 30 |
| 31 | $\underline{\pi}^{A}{}_{N}$ | pi_A_stack | effort for token A stack | secondaryState | $\mid m \mid$ | | 24 |
| 32 | $\underline{\pi}^B{}_N$ | pi_B_stack | effort for token B stack | secondaryState | | | 25 |
| 33 | $\underline{\pi}^{A,B}$ | pi_stack | effort for token A, B stack | secondaryState | | | 26 |
| 29 | \dot{x}_N | dx | diferential balance for token A | differentialState | ms^{-1} | | 16 32 |
| 30 | \dot{y}_N | dy | differential balance for token B | differentialState | s^{-1} | | 17 33 |
| 35 | \dot{xy} | dxy | mixed stack of the two accumulation terms | differentialState | | | 34 |

4 Properties

| | var | symbol | documentation | type | units | tokens | eqs |
|----|--------------------|-----------|--------------------------------------|---------------------------|----------|--------|-----|
| 37 | $K^{A,\alpha}{}_A$ | K_A_alpha | conductivity token A mechanism alpha | constant | s^{-1} | | |
| 38 | $K^{A,\beta}{}_A$ | K_A_beta | conductivity token A mechanism beta | $\operatorname{constant}$ | s^{-1} | | |
| 39 | $K^{B,\gamma}{}_A$ | K_B_gamma | conductivity token B mechanism gamma | $\operatorname{constant}$ | s^{-1} | | |

| | var | symbol | documentation | type | units | $_{ m tokens}$ | eqs |
|----|--------------------|-----------|--------------------------------------|----------|----------|----------------|-----|
| 40 | $K^{B,\delta}{}_A$ | K_B_delta | conductivity token B mechanism delta | constant | s^{-1} | [] | |
| 42 | K_A | K | stack of conductivities | constant | s^{-1} | | 36 |

5 Control

| | var | symbol | documentation | type | units | tokens | eqs |
|--|-----|--------|---------------|------|-------|--------|-----|
|--|-----|--------|---------------|------|-------|--------|-----|

6 System-Properties

| | var | symbol | documentation | type | units | tokens | eqs |
|--|-----|--------|---------------|------|-------|--------|-----|
|--|-----|--------|---------------|------|-------|--------|-----|

7 Properties-System

| | var | symbol | ${\it documentation}$ | type | units | $_{ m tokens}$ | eqs |
|----|--------------------|-----------|-----------------------|------------------|----------|----------------|-----|
| 41 | $k^{A,\alpha}{}_A$ | k_A_alpha | link | transform | s^{-1} | [] | 35 |
| 43 | $k^{A,\beta}{}_A$ | k_A_beta | link | ${ m transform}$ | s^{-1} | | 37 |
| 44 | $k^{B,\delta}{}_A$ | k_B_delta | link | ${ m transform}$ | s^{-1} | | 38 |
| 45 | $k^{B,\gamma}{}_A$ | k_B_gamma | link | ${ m transform}$ | s^{-1} | | 39 |

8 System-Control

| | var | symbol | documentation | type | units | tokens | eqs |
|--|-----|--------|---------------|------|-------|--------|-----|
|--|-----|--------|---------------|------|-------|--------|-----|

9 Control-System

| | var | symbol | documentation | type | units | tokens | eqs |
|--|-----|--------|---------------|------|-------|--------|-----|
|--|-----|--------|---------------|------|-------|--------|-----|

10 Properties-Control

| | var | symbol | documentation | type | units | tokens | eqs |
|--|-----|--------|---------------|------|-------|--------|-----|
|--|-----|--------|---------------|------|-------|--------|-----|

11 Control-Properties

| var | symbol | documentation | type | units | tokens | eqs |
|-----|--------|---------------|------|-------|--------|-----|

12 Equations

12.1 Model equations

| no | equation | documentation | layer |
|----|--|---|--------|
| 1 | 1 := Instantiate(#, #) | numerical value 1 | root |
| 2 | 0 := Instantiate(#, #) | numerical value 0 | root |
| 3 | $t_o := \text{Instantiate}(t, \#)$ | starting time | root |
| 4 | $t_e := \text{Instantiate}(t, \#)$ | end time | root |
| 5 | $x^o_N := \text{Instantiate}(x_N, \#)$ | initial condition for state x | System |
| 6 | $y^o_N := \text{Instantiate}(y_N, \#)$ | initial condition for state y | System |
| 7 | $\pi^{A,\alpha}{}_N := M^{A,\alpha}{}_N \cdot x_N$ | effort for B mechanism alpha | System |
| 8 | $\pi^{A,\beta}{}_N := M^{A,\beta}{}_N \cdot x_N$ | effort for A mechanism beta | System |
| 9 | $\pi^{B,\gamma}{}_N := M^{B,\gamma}{}_N . y_N$ | effort for B mechanism gamma | System |
| 10 | $\pi^{B,\delta}{}_N := M^{B,\delta}{}_N \cdot y_N$ | effort for B mechanism delta | System |
| 11 | $\hat{x}^{A,\alpha}{}_{N} := F_{N,A} \stackrel{A}{\star} \left(k^{A,\alpha}{}_{A} \cdot D_{N,A} \stackrel{N}{\star} \pi^{A,\alpha}{}_{N} \right)$ | netflow of token A due to mechanism alpha | System |
| 12 | $\hat{x}^{A,\beta}{}_{N} := F_{N,A} \stackrel{A}{\star} \left(k^{A,\beta}{}_{A} \cdot D_{N,A} \stackrel{N}{\star} \pi^{A,\beta}{}_{N} \right)$ | net flow of token A due to mechanism beta | System |
| 14 | $\hat{y}^{B,\gamma}{}_{N} := F_{N,A} \stackrel{A}{\star} \left(k^{B,\gamma}{}_{A} \cdot D_{N,A} \stackrel{N}{\star} \pi^{B,\gamma}{}_{N} \right)$ | netflow of token B due to mechanism gamma | System |
| 15 | $\hat{y}^{B,\delta}{}_{N} := F_{N,A} \stackrel{A}{\star} \left(k^{B,\delta}{}_{A} \cdot D_{N,A} \stackrel{N}{\star} \pi^{B,\delta}{}_{N} \right)$ | netflow of token B due to mechansim beta | System |

| no | equation | documentation | layer |
|----|---|---|----------------------|
| 16 | $\dot{x}_N := \hat{x}^{A,\alpha}{}_N + \hat{x}^{A,\beta}{}_N$ | diferential balance for token A | System |
| 17 | $\dot{y}_N := \hat{y}^{B,\gamma}{}_N + \hat{y}^{B,\delta}{}_N$ | differential balance for token B | System |
| 20 | $x_N := \int_{t_o}^{t_e} \dot{x}_N \ dt + x^o_N$ | state token A | System |
| 21 | $y_N := \int_{t_o}^{t_e} \dot{y}_N dt + y^o{}_N$ | state token B | System |
| 24 | $igg \underline{\pi}^{A}{}_{N} := \operatorname{Stack} \left(\pi^{A,lpha}{}_{N}, \pi^{A,eta}{}_{N} ight)$ | effort for token A stack | System |
| 25 | $igg \underline{\pi}^B{}_N := \operatorname{Stack} \left(\pi^{B,\gamma}{}_N, \pi^{B,\delta}{}_N ight)$ | effort for token B stack | System |
| 26 | $oxed{\pi^{A,B}} := \operatorname{MixedStack}\left(\overline{\pi}^{A}{}_{N}, \overline{\pi}^{B}{}_{N} ight)$ | effort for token A, B stack | System |
| 27 | $\pi^{A,\alpha}{}_N := \text{Instantiate}(\pi^{A,\alpha}{}_N, \#)$ | effort for B mechanism alpha | System |
| 28 | $\pi^{A,\beta}{}_{N} := \operatorname{Instantiate}(\pi^{A,\beta}{}_{N}, \#)$ | effort for A mechanism beta | System |
| 29 | $\pi^{B,\gamma}{}_N := \text{Instantiate}(\pi^{B,\gamma}{}_N, \#)$ | effort for B mechanism gamma | System |
| 30 | $\pi^{B,\delta}{}_N := \text{Instantiate}(\pi^{B,\delta}{}_N, \#)$ | effort for B mechanism delta | System |
| 31 | $s := \text{MixedStack}(x_N, y_N)$ | mixed state | System |
| 32 | $\dot{x}_N := \text{Instantiate}(\dot{x}_N, 0)$ | diferential balance for token A | System |
| 33 | $\dot{y}_N := \operatorname{Instantiate}(\dot{y}_N, 0)$ | differential balance for token B | System |
| 34 | $\dot{xy} := 	ext{MixedStack}\left(\dot{x}_N, \dot{y}_N ight)$ | mixed stack of the two accumulation terms | System |
| 35 | $k^{A,\alpha}{}_A := K^{A,\alpha}{}_A$ | var doc : link | Properties »> System |
| 36 | $K_{A} := \operatorname{Stack}\left(K^{A,\alpha}{}_{A}, K^{A,\beta}{}_{A}, K^{B,\gamma}{}_{A}, K^{B,\delta}{}_{A}\right)$ | stack of conductivities | Properties |

| no | equation | documentation | layer |
|----|--------------------------------------|---------------|----------------------|
| 37 | $k^{A,\beta}{}_A:=K^{A,\beta}{}_A$ | link | Properties »> System |
| 38 | $k^{B,\delta}{}_A:=K^{B,\delta}{}_A$ | link | Properties »> System |
| 39 | $k^{B,\gamma}{}_A:=K^{B,\gamma}{}_A$ | link | Properties »> System |