1 Variables

2 root

	var	symbol	documentation	type	units	tokens	eqs
8	$F_{N,A}$	F	directed graph indicence matrix	network			
1	t	t	time	frame	s		
6	t_o	to	starting time	frame	s		3
7	t_e	te	end time	frame	s		4
3	#	value	numerical value	constant			
4	1	one	numerical value 1	constant			1
5	0	null	numerical value 0	constant		[]	2

3 Properties

	var	symbol	documentation	type	units	tokens	eqs
57	$M^{A,lpha}{}_N$	M_A_alpha	norming factor token A mechanism alpha	constant		[]	51
58	$M^{A,eta}{}_N$	M_A_beta	norming factor token A mechanism beta	constant			52
59	$M^{B,\gamma}{}_N$	M_B_gamma	norming factor token B mechanism gamma	constant			53
60	$M^{B,\delta}{}_N$	M_B_delta	norming factor token B mechanism delta	constant			54
69	$M^A{}_N$	M_A	stack of M matrices token A	constant			55
70	$M^B{}_N$	M_B	stack of M matrices token B	constant			56
71	M_N	М	stack of M matrices token A and B	constant			57

4 Control

	var	symbol	documentation	type	units	tokens	eqs
67	y_A	У	controller output	$\operatorname{controlOut}$		[]	49 50
61	m_A	m	measurement	${ m measure In}$			61 62
65	$I_{N,D}$	I_N_D	Identity to shift from differential space to integral space	network			
66	$I_{A,D}$	I_A_D	identity to shift from differential space to arc	network			
55	x_N	x	controller state	state			48
56	$x^{o}{}_{N}$	xo	controller state initial condition	state			44
50	$A_{N,D}$	A	dynamic matrix A	constant	s^{-1}		
51	$B_{A,D}$	В	input matrix C	constant	s^{-1}		
52	$C_{N,A}$	С	output matrix C	constant			
53	$D_{N,A}$	D	event matrix D	constant			
62	y_{sA}	setpoint	set point	constant			45
63	e_A	e	control error	constant			46
68	D_A	D_A	event diagonal matrix D	constant			
64	\dot{x}_D	dx	differential state	${\it differential State}$	s^{-1}		47

5 System

	var	symbol	documentation	type	units	tokens	eqs
76	u_A	u	[0-1]-normed control signal	$\operatorname{controlIn}$		[]	
74	z_N	measure	normed measurement of pi A alpha	measureOut			59
75	\mathbf{Z}_A	measure_set_A	measurement vector for A	measureOut			60
25	$\hat{x}^{A,lpha}{}_N$	fx_A_alpha	netflow of token A due to mechanism alpha	transport	ms^{-1}		11
26	$\hat{x}^{A,\beta}{}_N$	fx_A_beta	net flow of token A due to mechanism beta	transport	ms^{-1}		12
27	$\hat{y}^{B,\gamma}{}_N$	fy_B_gamma	netflow of token B due to mechanism gamma	transport	s^{-1}		14
28	$\hat{y}^{B,\delta}{}_N$	fy_B_delta	netflow of token B due to mechansim beta	transport	s^{-1}		15
73	$I_{zN,A}$	I_measure	unidirectional graph for interface connection	network			
36	$D_{N,A}$	D	difference operator	${\it difference Operator}$			
9	x_N	x	state token A	state	$\mid m \mid$		20
10	y_N	у	state token B	state			21
11	$x^{o}{}_{N}$	хо	initial condition for state x	state	$\mid m \mid$		5
12	$y^o{}_N$	уо	initial condition for state y	state			6
34	s	S	mixed state	state			31
13	$K^{A,\alpha}{}_A$	K_A_alpha	conductivity token A mechanism alpha	constant	s^{-1}		
14	$K^{A,\beta}{}_A$	K_A_beta	conductivity token A mechanism beta	$\operatorname{constant}$	s^{-1}		
15	$K^{B,\gamma}{}_A$	K_B_gamma	conductivity token B mechanism gamma	$\operatorname{constant}$	s^{-1}		
16	$K^{B,\delta}{}_A$	K_B_delta	conductivity token B mechanism delta	$\operatorname{constant}$	s^{-1}		
17	$M^{A,lpha}{}_N$	M_A_alpha	norming factor token A mechanism alpha	constant			
18	$M^{A,eta}{}_N$	M_A_beta	norming factor token A mechanism beta	constant			
19	$M^{B,\gamma}{}_N$	M_B_gamma	norming factor token B mechanism gamma	$\operatorname{constant}$			
20	$M^{B,\delta}{}_N$	M_B_delta	norming factor token B mechanism delta	$\operatorname{constant}$			
72	$\pi^{A,\alpha,o}{}_N$	pi_A_alpha_norm	norming factor for pi A alpha	constant	$\mid m \mid$		58

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	var	symbol	documentation	type	units	tokens	eqs
29	\dot{x}_N	dx	diferential balance for token A	differentialState	ms^{-1}		16 32
30	\dot{y}_N	dy	differential balance for token B	differentialState	s^{-1}		17 33
35	\dot{xy}	dxy	mixed stack of the two accumulation terms	differentialState			34
21	$\pi^{A,lpha}{}_N$	pi_A_alpha	effort for A mechanism alpha	secondaryState	$\mid m \mid$		7 27
22	$\pi^{A,eta}{}_N$	pi_A_beta	effort for A mechanism beta	secondaryState	$\mid m \mid$		8 28
23	$\pi^{B,\gamma}{}_N$	pi_B_gamma	effort for B mechanism gamma	secondaryState			9 29
24	$\pi^{B,\delta}{}_N$	pi_B_delta	effort for B mechanism delta	secondaryState			10 30
31	$\underline{\pi}^{A}{}_{N}$	pi_A_stack	effort for token A stack	secondaryState	$\mid m \mid$		24
32	$\underline{\pi}^B{}_N$	pi_B_stack	effort for token B stack	secondaryState			25
33	$\underline{\pi}^{A,B}$	pi_stack	effort for token A, B stack	secondaryState			26

6 Equations

7 Generic

no	equation	documentation	layer
1	1 := Instantiate(#, #)	numerical value 1	root
2	0 := Instantiate(#, #)	numerical value 0	root
3	$t_o := \text{Instantiate}(t, \#)$	starting time	root
4	$t_e := \text{Instantiate}(t, \#)$	end time	root
5	$x^o{}_N := \text{Instantiate}(x_N, \#)$	initial condition for state x	System
6	$y^o{}_N := \text{Instantiate}(y_N, \#)$	initial condition for state y	System
7	$\pi^{A,\alpha}{}_N := M^{A,\alpha}{}_N \cdot x_N$	effort for B mechanism alpha	System
8	$\pi^{A,\beta}{}_N := M^{A,\beta}{}_N \cdot x_N$	effort for A mechanism beta	System
9	$\pi^{B,\gamma}{}_N := M^{B,\gamma}{}_N . y_N$	effort for B mechanism gamma	System
10	$\pi^{B,\delta}{}_N := M^{B,\delta}{}_N \cdot y_N$	effort for B mechanism delta	System
11	$\hat{x}^{A,\alpha}{}_{N} := F_{N,A} \stackrel{A}{\star} \left(K^{A,\alpha}{}_{A} \cdot D_{N,A} \stackrel{N}{\star} \pi^{A,\alpha}{}_{N} \right)$	netflow of token A due to mechanism alpha	System
12	$\hat{x}^{A,\beta}{}_{N} := F_{N,A} \stackrel{A}{\star} \left(K^{A,\beta}{}_{A} \cdot D_{N,A} \stackrel{N}{\star} \pi^{A,\beta}{}_{N} \right)$	net flow of token A due to mechanism beta	System
14	$\hat{y}^{B,\gamma}{}_{N} := F_{N,A} \stackrel{A}{\star} \left(K^{B,\gamma}{}_{A} \cdot D_{N,A} \stackrel{N}{\star} \pi^{B,\gamma}{}_{N} \right)$	netflow of token B due to mechanism gamma	System
15	$\hat{y}^{B,\delta}{}_{N} := F_{N,A} \stackrel{A}{\star} \left(K^{B,\delta}{}_{A} \cdot D_{N,A} \stackrel{N}{\star} \pi^{B,\delta}{}_{N} \right)$	netflow of token B due to mechansim beta	System

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no	equation	documentation	layer
16	$\dot{x}_N := \hat{x}^{A,\alpha}{}_N + \hat{x}^{A,\beta}{}_N$	diferential balance for token A	System
17	$\dot{y}_N := \hat{y}^{B,\gamma}{}_N + \hat{y}^{B,\delta}{}_N$	differential balance for token B	System
20	$x_N := \int_{t_o}^{t_e} \dot{x}_N \ dt + x^o{}_N$	state token A	System
21	$y_N := \int_{t_o}^{t_e} \dot{y}_N \ dt + y^o{}_N$	state token B	System
24	$\underline{\pi}^{A}{}_{N} := \operatorname{Stack}\left(\pi^{A,\alpha}{}_{N}, \pi^{A,\beta}{}_{N}\right)$	effort for token A stack	System
25	$\underline{\pi}^{B}{}_{N} := \operatorname{Stack}\left(\pi^{B,\gamma}{}_{N}, \pi^{B,\delta}{}_{N}\right)$	effort for token B stack	System
26	$\underline{\pi}^{A,B} := \operatorname{MixedStack}\left(\underline{\pi}^{A}{}_{N},\underline{\pi}^{B}{}_{N}\right)$	effort for token A, B stack	System
27	$\pi^{A,\alpha}{}_N := \text{Instantiate}(\pi^{A,\alpha}{}_N, \#)$	effort for B mechanism alpha	System
28	${\pi^{A,\beta}}_N := \text{Instantiate}({\pi^{A,\beta}}_N, \#)$	effort for A mechanism beta	System
29	$\pi^{B,\gamma}{}_N := \text{Instantiate}(\pi^{B,\gamma}{}_N,\#)$	effort for B mechanism gamma	System
30	${\pi^{B,\delta}}_N := \text{Instantiate}({\pi^{B,\delta}}_N, \#)$	effort for B mechanism delta	System
31	$s := \text{MixedStack}\left(x_N, y_N\right)$	mixed state	System
32	$\dot{x}_N := \operatorname{Instantiate}(\dot{x}_N, 0)$	diferential balance for token A	System
33	$\dot{y}_N := \operatorname{Instantiate}(\dot{y}_N, 0)$	differential balance for token B	System
34	$\dot{xy} := ext{MixedStack}\left(\dot{x}_N, \dot{y}_N ight)$	mixed stack of the two accumulation terms	System
44	$x^o_N := \text{Instantiate}(x_N, \#)$	controller state initial condition	Control
45	$y_{sA} := \text{Instantiate}(m_A, \#)$	set point	Control
46	$e_A := m_A - y_{sA}$	control error	Control

no	equation	${\it documentation}$	layer
47	$\dot{x}_D := A_{N,D} \overset{N}{\star} x_N + B_{A,D} \overset{A}{\star} e_A$	differential state	Control
48	$x_N := \int_{t_o}^{t_e} I_{N,D} \stackrel{D}{\star} \dot{x}_D \ dt$	controller state	Control
49	$y_A := C_{N,A} \overset{N}{\star} x_N + I_{A,D} \overset{D}{\star} \left(I_{N,D} \overset{N}{\star} D_{N,A} \overset{A}{\star} e_A \right)$	controller output	Control
50	$y_A := C_{N,A} \overset{N}{\star} x_N + D_A \cdot e_A$	controller output	Control
51	$M^{A,\alpha}{}_N := \operatorname{Instantiate}(M^{A,\alpha}{}_N, \#)$	norming factor token A mechanism alpha	Properties
52	$M^{A,\beta}{}_N := \operatorname{Instantiate}(M^{A,\beta}{}_N,\#)$	norming factor token A mechanism beta	Properties
53	$M^{B,\gamma}{}_N := \operatorname{Instantiate}(M^{B,\gamma}{}_N, \#)$	norming factor token B mechanism gamma	Properties
54	$M^{B,\delta}{}_N := \operatorname{Instantiate}(M^{B,\delta}{}_N, \#)$	norming factor token B mechanism delta	Properties
55	$M^{A}{}_{N}:=\operatorname{Stack}\left(M^{A,lpha}{}_{N},M^{A,eta}{}_{N} ight)$	stack of M matrices token A	Properties
56	$M^{B}{}_{N} := \operatorname{Stack}\left(M^{B,\gamma}{}_{N}, M^{B,\delta}{}_{N}\right)$	stack of M matrices token B	Properties
57	$M_N := \operatorname{Stack}\left(M^A{}_N, M^B{}_N ight)$	stack of M matrices token A and B	Properties
58	$\pi^{A,\alpha,o}{}_N := \text{Instantiate}(\pi^{A,\alpha}{}_N,\#)$	norming factor for pi A alpha	System
59	$z_N := \left(\pi^{A,\alpha,o}{}_N\right)^{-1} \cdot \pi^{A,\alpha}{}_N$	normed measurement of pi A alpha	System
60	$\underline{\mathbf{z}}_A := I_{zN,A} \overset{N}{\star} z_N$	measurement vector for A	System
61	$m_A := \operatorname{Instantiate}(m_A, \#)$	measurement	Control

8 Interface Link Equation

no	equation	documentation	layer
62	$m_A := \mathbf{\underline{z}}_A$	interface equation	System »> Control