1 Variables

2 root

| | var | symbol | documentation | type | units | tokens | eqs |
|----|-----------|--------|---------------------------------|----------|-------|--------|-----|
| 13 | $F_{N,A}$ | F | directed graph incidence matrix | network | | | |
| 1 | t_N | t | time | frame | s | | |
| 3 | $t^o{}_N$ | to | starting time | frame | s | | 1 |
| 4 | $t^e{}_N$ | te | end time | frame | s | | 2 |
| 2 | # | value | numerical value | constant | | | |
| 18 | 0 | null | numerical value 0 | constant | | | 16 |
| 19 | 1 | one | numerical value 1 | constant | | | 17 |

3 System

| | var | symbol | documentation | type | units | tokens | eqs |
|----|-----------------------------|------------|--|------------------|---------------|--------|-------|
| 37 | $\hat{x}^{A,\alpha}{}_N$ | fx_A_alpha | netflow of token A due to mechanism alpha | transport | ms^{-1} | | 50 55 |
| 38 | $\hat{x}^{A,eta}{}_N$ | fx_A_beta | netflow of token A due to mechanism beta | ${ m transport}$ | ms^{-1} | | 51 56 |
| 39 | $\hat{y}^{B,\gamma}{}_N$ | fy_B_gamma | netflow of token B due to mechanism gammma | transport | s^{-1} | | 52 57 |
| 40 | $\hat{y}^{B,\delta}{}_N$ | fy_B_delta | netflow of token B due to mechanism delta | transport | s^{-1} | | 53 54 |
| 5 | x_N | x | state token A | state | $\mid m \mid$ | | 60 |
| 11 | $\pi^{A,\alpha}{}_N$ | pi_A_alpha | effort A mechanism alpha | state | $\mid m \mid$ | | 7 14 |
| 12 | $\pi^{A,eta}{}_N$ | pi_A_beta | effort A mechanism beta | state | $\mid m \mid$ | | 8 15 |
| 16 | \dot{x}_N | dx | differential state | state | ms^{-1} | | 18 58 |
| 17 | $x^o{}_N$ | xo | initial condition for token A | state | $\mid m \mid$ | | 12 |
| 20 | $\underline{\pi}^{A}{}_{N}$ | pi_A_stack | the stack of intensive variables token A | state | $\mid m \mid$ | [] | 19 |

Continued on next page

| | var | symbol | documentation | type | units | tokens | eqs |
|----|-----------------------------|------------|--|----------|------------|--------|-------|
| 21 | y_N | у | state token B | state | | | 61 |
| 24 | $\pi^{B,\gamma}{}_N$ | pi_B_gamma | effort B mechanism gamma | state | | | 23 |
| 26 | \dot{y}_N | dy | differential state for token B | state | s^{-1} | | 36 59 |
| 27 | $y^o{}_N$ | уо | initial condition for token B | state | | | 26 |
| 33 | $\pi^{B,\delta}{}_N$ | pi_B_delta | effort B mechansim delta | state | | | 32 |
| 36 | $\underline{\pi}^{B}{}_{N}$ | pi_B_stack | the stack of intensive variables token B | state | | | 44 |
| 7 | $K^{A,lpha}{}_N$ | K_A_alpha | frequency token A | constant | $ s^{-1} $ | | 40 |
| 8 | $K^{A,eta}{}_N$ | K_A_beta | frequency token B | constant | $ s^{-1} $ | | 41 |
| 9 | $M^{A,lpha}$ | M_A_alpha | norming factor token A mechanism alpha | constant | | | 42 |
| 10 | $M^{A,eta}$ | M_A_beta | norming factor token A mechanism beta | constant | | | 43 |
| 22 | $M^{B,\gamma}$ | M_B_gamma | norming factor token B mechanism gamma | constant | | | |
| 23 | $K^{B,\gamma}{}_N$ | K_B_gamma | norming factor token A mechanism d | constant | s^{-1} | | 22 |
| 30 | $K^{B,\delta}{}_N$ | K_B_delta | frequency B delta | constant | s^{-1} | | 30 |
| 31 | $M^{B,\delta}$ | M_B_delta | norming factor token B mechanism delta | constant | | | |

4 Properties

| | var | symbol | documentation | type | units | tokens | eqs |
|--|-----|--------|---------------|------|-------|--------|-----|
|--|-----|--------|---------------|------|-------|--------|-----|

5 Control

| | T. | | | Т | | |
|-----|--------|---------------|------|-------|----------------|-----|
| var | symbol | documentation | type | units | $_{ m tokens}$ | eqs |

6 System-Properties

| | var | symbol | documentation | type | units | tokens | eqs | |
|---|-------------|--------|---------------|------|-------|--------|-----|--|
| $7 	ext{Properties-System}$ | | | | | | | | |
| | var | symbol | documentation | type | units | tokens | eqs | |
| 8 System-Control | | | | | | | | |
| | var | symbol | documentation | type | units | tokens | eqs | |
| 9 | Control-Sys | stem | documentation | type | units | tokens | ons | |
| var symbol documentation type units tokens eqs 10 Properties-Control | | | | | | | | |
| | var | symbol | documentation | type | units | tokens | eqs | |
| 11 Control-Properties | | | | | | | | |
| l 1 | | - | | | | | | |

12 Equations

12.1 Model equations

| no | equation | documentation | layer |
|----|--|----------------------------------|--------|
| 1 | $t^o{}_N := \operatorname{Instantiate}(t_N, \#)$ | starting time | root |
| 2 | $t^e{}_N := \operatorname{Instantiate}(t_N, \#)$ | end time | root |
| 7 | $\pi^{A,\alpha}{}_N := M^{A,\alpha} \cdot x_N$ | effort a | System |
| 8 | $\pi^{A,\beta}{}_N := M^{A,\beta} \cdot x_N$ | effort b | System |
| 12 | $x^o{}_N := \text{Instantiate}(x_N, \#)$ | initial condition | System |
| 14 | $\pi^{A,\alpha}{}_N := \operatorname{Instantiate}(\pi^{A,\alpha}{}_N, \#)$ | effort a | System |
| 15 | $\pi^{A,\beta}{}_{N} := \operatorname{Instantiate}(\pi^{A,\beta}{}_{N}, \#)$ | effort b | System |
| 16 | 0 := Instantiate(#, #) | numerical value 0 | root |
| 17 | 1 := Instantiate(#, #) | numerical value 1 | root |
| 18 | $\dot{x}_N := \text{Instantiate}(\dot{x}_N, 0)$ | differential state | System |
| 19 | $\boxed{\underline{\pi}^{A}{}_{N} := Stack\left(\pi^{A,\alpha}{}_{N}, \pi^{A,\beta}{}_{N}\right)}$ | the stack of intensive variables | System |
| 22 | $K^{B,\gamma}_{N} := \operatorname{Instantiate}((t_{N})^{-1}, \#)$ | frequency B alpha | System |
| 23 | $\pi^{B,\gamma}{}_N := M^{B,\gamma} \cdot y_N$ | transport of B mechanism gamma | System |
| 26 | $y^o{}_N := \operatorname{Instantiate}(y_N, \#)$ | initial condition for token B | System |
| 30 | $K^{B,\delta}_{N} := \operatorname{Instantiate}((t_{N})^{-1}, \#)$ | var doc : frequency B delta | System |
| 32 | $\pi^{B,\delta}{}_N := M^{B,\delta} \cdot y_N$ | effort B mechansim delta | System |

Continued on next page

| no | equation | documentation | layer |
|----|--|--|--------|
| 36 | $\dot{y}_N := \operatorname{Instantiate}(\dot{y}_N, \#)$ | differential state for token B | System |
| 40 | $K^{A,\alpha}_{N} := \text{Instantiate}((t_{N})^{-1}, \#)$ | frequency token A | System |
| 41 | $K^{A,\beta}{}_{N} := \operatorname{Instantiate}((t_{N})^{-1}, \#)$ | frequency token B | System |
| 42 | $M^{A,\alpha} := \text{Instantiate}(\#, \#)$ | norming factor token A mechanism alpha | System |
| 43 | $M^{A,eta} := \operatorname{Instantiate}(\#,\#)$ | norming factor token A mechanism beta | System |
| 44 | $\underline{\pi}^{B}{}_{N} := Stack\left(\pi^{B,\gamma}{}_{N}, \pi^{B,\delta}{}_{N}\right)$ | the stack of intensive variables token B | System |
| 50 | $\hat{x}^{A,\alpha}{}_{N} := F_{N,A} \overset{A}{\star} \left(K^{A,\alpha}{}_{N} . F_{N,A} \overset{N}{\star} \pi^{A,\alpha}{}_{N} \right)$ | netflow of token A due to mechanism alpha | System |
| 51 | $\hat{x}^{A,\beta}{}_{N} := F_{N,A} \stackrel{A}{\star} \left(K^{A,\beta}{}_{N} . F_{N,A} \stackrel{N}{\star} \pi^{A,\beta}{}_{N} \right)$ | netflow of token A due to mechanism beta | System |
| 52 | $\hat{y}^{B,\gamma}{}_{N} := F_{N,A} \stackrel{A}{\star} \left(K^{B,\gamma}{}_{N} . F_{N,A} \stackrel{N}{\star} \pi^{B,\gamma}{}_{N} \right)$ | netflow of token B due to mechanism gammma | System |
| 53 | $\hat{y}^{B,\delta}{}_{N} := F_{N,A} \stackrel{A}{\star} \left(K^{B,\delta}{}_{N} \cdot F_{N,A} \stackrel{N}{\star} \pi^{B,\delta}{}_{N} \right)$ | netflow of token B due to mechanism delta | System |
| 54 | $\hat{y}^{B,\delta}{}_N := \text{Instantiate}(\hat{y}^{B,\delta}{}_N, \#)$ | netflow of token B due to mechanism delta | System |
| 55 | $\hat{x}^{A,\alpha}{}_N := \text{Instantiate}(\hat{x}^{A,\alpha}{}_N, \#)$ | netflow of token A due to mechanism alpha | System |
| 56 | $\hat{\boldsymbol{x}}^{A,\beta}{}_{N} := \operatorname{Instantiate}(\hat{\boldsymbol{x}}^{A,\alpha}{}_{N}, \#)$ | netflow of token A due to mechanism beta | System |

Continued on next page

| no | equation | documentation | layer |
|----|--|--|--------|
| 57 | $\hat{y}^{B,\gamma}{}_N := \operatorname{Instantiate}(\hat{y}^{B,\gamma}{}_N, \#)$ | netflow of token B due to mechanism gammma | System |
| 58 | $\dot{x}_N := \hat{x}^{A,\alpha}{}_N + \hat{x}^{A,\beta}{}_N$ | differential state | System |
| 59 | $\dot{y}_N := \hat{y}^{B,\gamma}{}_N + \hat{y}^{B,\delta}{}_N$ | differential state for token B | System |
| 60 | $x_N := \int_{t^o_N}^{t^e_N} \dot{x}_N \ dt_N$ | state token A | System |
| 61 | $y_N := \int_{t^o_N}^{t^e_N} \dot{y}_N \ dt_N$ | state token B | System |