### 1 Variables

#### 2 root

|    | var       | symbol | documentation                   | type     | units | tokens | eqs |
|----|-----------|--------|---------------------------------|----------|-------|--------|-----|
| 13 | $F_{N,A}$ | F      | directed graph incidence matrix | network  |       |        |     |
| 1  | $t_N$     | t      | time                            | frame    | s     |        |     |
| 3  | $t^o{}_N$ | to     | starting time                   | frame    | s     |        | 1   |
| 4  | $t^e{}_N$ | te     | end time                        | frame    | s     |        | 2   |
| 2  | #         | value  | numerical value                 | constant |       |        |     |
| 18 | 0         | null   | numerical value 0               | constant |       |        | 16  |
| 19 | 1         | one    | numerical value 1               | constant |       |        | 17  |

# 3 System

|    | var                         | symbol     | documentation                            | type      | units         | tokens | eqs   |
|----|-----------------------------|------------|--|-----------|---------------|--------|-------|
| 28 | $\hat{x}^{A,\alpha}{}_A$    | fx_A_alpha | flow of A mechanism alpha                | transport | $ms^{-1}$     | []     | 28    |
| 29 | $\hat{x}^{A,\beta}{}_A$     | fx_A_beta  | flow of A mechanism beta                 | transport | $ms^{-1}$     |        | 29    |
| 32 | $\hat{y}^{B,\gamma}{}_A$    | fy_B_gamma | flow of B mechanism gamma                | transport | $s^{-1}$      |        | 31    |
| 35 | $\hat{y}^{B,\delta}{}_A$    | fy_B_delta | flow of B mechanism delta                | transport | $s^{-1}$      |        | 34    |
| 5  | $x_N$                       | x          | state token A                            | state     | $\mid m \mid$ |        | 38    |
| 11 | $\pi^{A,\alpha}{}_N$        | pi_A_alpha | effort A mechanism alpha                 | state     | $\mid m \mid$ |        | 7 14  |
| 12 | $\pi^{A,eta}{}_N$           | pi_A_beta  | effort A mechanism beta                  | state     | $\mid m \mid$ |        | 8 15  |
| 16 | $\dot{x}_N$                 | dx         | differential state                       | state     | $ms^{-1}$     | []     | 18 37 |
| 17 | $x^o{}_N$                   | xo         | initial condition for token A            | state     | $\mid m \mid$ |        | 12    |
| 20 | $\underline{\pi}^{A}{}_{N}$ | pi_A_stack | the stack of intensive variables token A | state     | $\mid m \mid$ |        | 19    |

Continued on next page

|    | var                  | symbol     | documentation                  | type     | units    | tokens | eqs   |
|----|----------------------|------------|--------------------------------|----------|----------|--------|-------|
| 21 | $y_N$                | у          | state token B                  | state    |          | []     | 39    |
| 24 | ${\pi^{B,\gamma}}_N$ | pi_B_gamma | effort B mechanism gamma       | state    |          |        | 23    |
| 26 | $\dot{y}_N$          | dy         | differential state for token B | state    | $s^{-1}$ |        | 35 36 |
| 27 | $y^o{}_N$            | уо         | initial condition for token B  | state    |          |        | 26    |
| 33 | ${\pi^{B,\delta}}_N$ | pi_B_delta | effort B mechansim delta       | state    |          |        | 32    |
| 7  | $K^{A,lpha}{}_N$     | K_A_alpha  | frequency A alpha              | constant | $s^{-1}$ |        | 3     |
| 8  | $K^{A,eta}{}_N$      | K_A_beta   | frequency A beta               | constant | $s^{-1}$ |        | 4     |
| 9  | $M^{A,lpha}$         | M_A_alpha  | gain a                         | constant |          |        | 5     |
| 10 | $M^{A,eta}$          | M_A_beta   | gain b                         | constant |          |        | 6     |
| 22 | $M^{B,\gamma}$       | M_B_gamma  | gain B gamma                   | constant |          |        |       |
| 23 | $K^{B,\gamma}{}_N$   | K_B_gamma  | frequency B gamma              | constant | $s^{-1}$ |        | 22    |
| 30 | $K^{B,\delta}{}_N$   | K_B_delta  | frequency B delta              | constant | $s^{-1}$ |        | 30    |
| 31 | $M^{B,\delta}$       | M_B_delta  | gain B delta                   | constant |          |        |       |

# 4 Properties

| var symbol documentation type | rpe units tokens eqs |
|-------------------------------|----------------------|
|-------------------------------|----------------------|

## 5 Control

|  | var | symbol | documentation | type | units | tokens | eqs |
|--|-----|--------|---------------|------|-------|--------|-----|
|--|-----|--------|---------------|------|-------|--------|-----|

# 6 System-Properties

|   | var         | symbol | documentation | type | units | tokens | eqs |  |
|---|-------------|--------|---------------|------|-------|--------|-----|--|
| 7 Properties–System   |             |        |               |      |       |        |     |  |
|   | var         | symbol | documentation | type | units | tokens | eqs |  |
| 8 System-Control  |             |        |               |      |       |        |     |  |
|   | var         | symbol | documentation | type | units | tokens | eqs |  |
| 9   | Control-Sys | stem   | documentation | type | units | tokens | ons |  |
| var symbol documentation type units tokens eqs  10 Properties-Control |             |        |               |      |       |        |     |  |
|   | var         | symbol | documentation | type | units | tokens | eqs |  |
| 11 Control–Properties   |             |        |               |      |       |        |     |  |
| <b>l</b> 1  |             | -      |               |      |       |        |     |  |

## 12 Equations

#### 12.1 Model equations

| no | equation  | documentation                    | layer  |
|----|---|----------------------------------|--------|
| 1  | $t^o{}_N := Set(t_N, \#)$   | starting time                    | root   |
| 2  | $t^e{}_N := Set(t_N, \#)$   | end time                         | root   |
| 3  | $K^{A,\alpha}{}_{N} := Set((t_{N})^{-1}, \#)$   | frequency a                      | System |
| 4  | $K^{A,\beta}{}_N := Set((t_N)^{-1}, \#)$  | frequency b                      | System |
| 5  | $M^{A,lpha}:=Set(\#,\#)$  | gain a                           | System |
| 6  | $M^{A,eta}:=Set(\#,\#)$   | gain b                           | System |
| 7  | $\pi^{A,\alpha}{}_N := M^{A,\alpha} \cdot x_N$  | effort a                         | System |
| 8  | $\pi^{A,\beta}{}_N := M^{A,\beta} \cdot x_N$  | effort b                         | System |
| 12 | $x^o{}_N := Set(x_N, \#)$   | initial condition                | System |
| 14 | $\pi^{A,\alpha}{}_N := Set(\pi^{A,\alpha}{}_N,\#)$                                      | effort a                         | System |
| 15 | ${\pi^{A,\beta}}_N:=Set({\pi^{A,\beta}}_N,\#)$  | effort b                         | System |
| 16 | 0 := Set(#,#)   | numerical value 0                | root   |
| 17 | 1 := Set(#,#)   | numerical value 1                | root   |
| 18 | $\dot{x}_N := Set(\dot{x}_N, 0)$  | differential state               | System |
| 19 | $\underline{\pi}^{A}{}_{N}:=Stack\left(\pi^{A,\alpha}{}_{N},\pi^{A,\beta}{}_{N}\right)$ | the stack of intensive variables | System |
| 22 | $K^{B,\gamma}{}_N := Set((t_N)^{-1}, \#)$   | frequency B alpha                | System |

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| no | equation   | documentation                  | layer  |
|----|--|--------------------------------|--------|
| 23 | $\pi^{B,\gamma}{}_N := M^{B,\gamma} \cdot y_N$   | transport of B mechanism gamma | System |
| 26 | $y^o{}_N := Set(y_N, \#)$  | initial condition for token B  | System |
| 28 | $\hat{x}^{A,\alpha}{}_A := K^{A,\alpha}{}_N \cdot F_{N,A} \overset{N}{\star} \pi^{A,\alpha}{}_N$                     | flow of A mechanism alpha      | System |
| 29 | $\hat{x}^{A,\beta}{}_A := K^{A,\beta}{}_N \cdot F_{N,A} \stackrel{N}{\star} \pi^{A,\beta}{}_N$                       | flow of A mechanism beta       | System |
| 30 | $K^{B,\delta}{}_N := Set(\left(t_N\right)^{-1},\#)$  | var doc : frequency B delta    | System |
| 31 | $\hat{y}^{B,\gamma}{}_A := K^{B,\gamma}{}_N . F_{N,A}  \stackrel{N}{\star}  \pi^{B,\gamma}{}_N$                      | flow of B mechanism gamma      | System |
| 32 | $\pi^{B,\delta}{}_N := M^{B,\delta} \cdot y_N$   | effort B mechansim delta       | System |
| 34 | $\hat{y}^{B,\delta}{}_A := K^{B,\delta}{}_N . F_{N,A}  \stackrel{N}{\star}  \pi^{B,\delta}{}_N$                      | flow of B mechanism delta      | System |
| 35 | $\dot{y}_N := F_{N,A} \overset{A}{\star} \hat{y}^{B,\gamma}{}_A + F_{N,A} \overset{A}{\star} \hat{y}^{B,\delta}{}_A$ | differential state for token B | System |
| 36 | $\dot{y}_N := Set(\dot{y}_N, \#)$  | differential state for token B | System |
| 37 | $\dot{x}_N := F_{N,A} \overset{A}{\star} \hat{x}^{A,\alpha}{}_A + F_{N,A} \overset{A}{\star} \hat{x}^{A,\beta}{}_A$  | differential state             | System |
| 38 | $x_N := \int_{t^o_N}^{t^e_N} \dot{x}_N \ dt_N$   | state token A                  | System |
| 39 | $y_N := \int_{t^o_N}^{t^e_N} \dot{y}_N \ dt_N$   | state token B                  | System |