

# 1 Variables

## 2 root

|     | var        | symbol   | documentation                | type     | units | eqs |
|-----|------------|----------|------------------------------|----------|-------|-----|
| 8   | $F_{N,A}$  | F_N_A    | fundamental incidence matrix | network  |       |     |
| 216 | $\Delta t$ | dt_pulse | lenth of pulse               | frame    | $s$   |     |
| 217 | $pulse$    | pulse    | pulse function               | frame    |       | 180 |
| 5   | $t$        | t        | time                         | frame    | $s$   |     |
| 6   | $t^o$      | to       | starting time                | frame    | $s$   | 4   |
| 7   | $t^e$      | te       | end time                     | frame    | $s$   | 5   |
| 1   | #          | value    | numerical value              | constant |       |     |
| 2   | 1          | one      | numerical value one          | constant |       | 1   |
| 3   | 0          | zero     | numerical value zero         | constant |       | 2   |
| 4   | 0.5        | onehalf  | numerical value one half     | constant |       | 3   |

### 3 physical

|     | var         | symbol  | documentation                                    | type       | units                     | eqs         |
|-----|-------------|---------|--|------------|---------------------------|-------------|
| 162 | $P_{N,NS}$  | P_N_NS  | projection of nodes onto the node species        | projection |                           |             |
| 200 | $I_{NS,AS}$ | I_NS_AS | projection species to node species               | projection |                           |             |
| 201 | $I_{N,A}$   | I_N_A   | projection of nodes and arcs                     | projection |                           |             |
| 32  | $P_{NS,AS}$ | P_NS_AS | projection node species to arc species           | projection |                           |             |
| 33  | $P_{K,NK}$  | P_K_NK  | projection of conversion to node conversion      | projection |                           |             |
| 34  | $P_{S,NS}$  | P_S_NS  | projection species to node species               | projection |                           |             |
| 35  | $P_{N,NK}$  | P_N_NK  | projection node to node conversion               | projection |                           |             |
| 36  | $P_{NS,KS}$ | P_NS_KS | projection node species to conversion species    | projection |                           |             |
| 37  | $P_{A,NS}$  | P_A_NS  | projection arc to node species for conductivity  | projection |                           |             |
| 65  | $P_{NK,KS}$ | P_NK_KS | projection node conversion to conversion species | projection |                           |             |
| 9   | $P_{N,A}$   | P_N_A   | projection from node to arc for arc properties   | projection |                           |             |
| 10  | $r_{xN}$    | r_x     | x-coordinate                                     | frame      | $m$                       |             |
| 11  | $r_{yN}$    | r_y     | y-coordinate                                     | frame      | $m$                       |             |
| 12  | $r_{zN}$    | r_z     | z coordinate                                     | frame      | $m$                       |             |
| 13  | $U_N$       | U       | fundamental state – internal energy              | state      | $kg\,m^2\,s^{-2}$         |             |
| 14  | $S_N$       | S       | fundamental state – entropy                      | state      | $kg\,m^2\,K^{-1}\,s^{-2}$ |             |
| 15  | $V_N$       | V       | fundamental state – volume                       | state      | $m^3$                     |             |
| 16  | $n_{NS}$    | n       | fundamental state – molar mass                   | state      | $mol$                     | 86          |
| 20  | $H_N$       | H       | enthalpy   | state      | $kg\,m^2\,s^{-2}$         | 9 87<br>184 |
| 21  | $A_N$       | A       | Helmholtz energy                                 | state      | $kg\,m^2\,s^{-2}$         | 10          |
| 22  | $G_N$       | G       | Gibbs free energy                                | state      | $kg\,m^2\,s^{-2}$         | 11          |
| 23  | $C_N$       | charge  | fundamental state – charge                       | state      | $A\,s$                    |             |

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|     | var        | symbol   | documentation                  | type           | units                               | eqs   |
|-----|------------|----------|--------------------------------|----------------|-------------------------------------|-------|
| 165 | $B_N$      | boz      | Boltzmann constant             | constant       | $kg\,m^2\,K^{-1}\,s^{-2}$           | 132   |
| 166 | $R_N$      | R        | gas constant                   | constant       | $kg\,m^2\,mol^{-1}\,K^{-1}\,s^{-2}$ | 133   |
| 24  | $A^v$      | Avogadro | Avogadro number                | constant       | $mol^{-1}$                          |       |
| 17  | $p_N$      | p        | thermodynamic pressure         | effort         | $kg\,m^{-1}\,s^{-2}$                | 6     |
| 18  | $T_N$      | T        | temperature                    | effort         | $K$                                 | 7 185 |
| 19  | $\mu_{NS}$ | chemPot  | chemical potential             | effort         | $kg\,m^2\,mol^{-1}\,s^{-2}$         | 8 136 |
| 27  | $U^e_N$    | Ue       | electrical potential – voltage | effort         | $kg\,m^2\,A^{-1}\,s^{-3}$           | 14 95 |
| 28  | $v_{xN}$   | v_x      | velocity in x-direction        | secondaryState | $ms^{-1}$                           | 15    |
| 29  | $v_{yN}$   | v_y      | velocity in y-direction        | secondaryState | $ms^{-1}$                           | 16    |
| 30  | $v_{zN}$   | v_z      | velocity in z-direction        | secondaryState | $ms^{-1}$                           | 17    |

## 4 control

|     | var             | symbol             | documentation                                   | type      | units                   | eqs                 |
|-----|-----------------|--------------------|---|-----------|-------------------------|---------------------|
| 136 | $x_N$           | <b>x</b>           | state   | state     |                         | <a href="#">111</a> |
| 137 | $x_{oN}$        | <b>xo</b>          | initial state                                   | state     |                         | <a href="#">109</a> |
| 129 | $A_{N,D}$       | <b>A</b>           | dynamic matrix                                  | constant  | $s^{-1}$                |                     |
| 130 | $B_{A,D}$       | <b>B</b>           | input matrix                                    | constant  | $s^{-1}$                |                     |
| 131 | $C_{N,A}$       | <b>C</b>           | measurement matrix                              | constant  |                         |                     |
| 132 | $D_A$           | <b>D</b>           | diagonal event matrix (no dimensional problems) | constant  |                         |                     |
| 133 | $y^o_A$         | <b>setPoint</b>    | set point                                       | constant  |                         | <a href="#">119</a> |
| 134 | $m_A$           | <b>meas</b>        | measurements                                    | constant  |                         |                     |
| 135 | $e_A$           | <b>e</b>           | control error                                   | constant  |                         | <a href="#">108</a> |
| 139 | $1_{N,D}$       | <b>I_N_D</b>       | space transformation D to N                     | constant  |                         |                     |
| 219 | $T_{norm_N}$    | <b>T_norm</b>      | temprature transmitter constant                 | constant  | $K$                     | <a href="#">186</a> |
| 138 | $\dot{x}_D$     | <b>dxdt</b>        | differential state (ABCD) model                 | diffState | $s^{-1}$                | <a href="#">110</a> |
| 141 | $\tilde{I}_N$   | <b>Imeasured</b>   | measured current                                | algebraic | $A$                     | <a href="#">113</a> |
| 143 | $\tilde{U}^e_N$ | <b>UeMeasured</b>  | measured electrical potential                   | algebraic | $kg\,m^2\,A^{-1}s^{-3}$ | <a href="#">115</a> |
| 144 | $\tilde{\xi}$   | <b>addMeasured</b> | measured additive fraction                      | algebraic |                         | <a href="#">116</a> |
| 145 | $R_N$           | <b>RComputed</b>   | measured resistance                             | algebraic | $kg\,m^2\,A^{-2}s^{-3}$ | <a href="#">117</a> |
| 154 | $y_A$           | <b>y</b>           | output equation                                 | algebraic |                         | <a href="#">126</a> |
| 171 | $s$             | <b>switch</b>      | switches at to                                  | algebraic |                         | <a href="#">138</a> |

## 5 reactions

|     | var              | symbol      | documentation   | type           | units                               | eqs |
|-----|------------------|-------------|---|----------------|-------------------------------------|-----|
| 147 | $P_{NK}$         | P_NK        | reactions per node  | projection     |                                     |     |
| 155 | $B$              | Boltzmann   | Boltzmann constant  | constant       | $kg\,m^2\,K^{-1}\,s^{-2}$           |     |
| 157 | $R$              | GasConstant | gas constant  | constant       | $kg\,m^2\,mol^{-1}\,K^{-1}\,s^{-2}$ | 127 |
| 158 | $N_{K,KS}$       | N_K_KS      | stoichiometry   | constant       |                                     |     |
| 159 | $N_{NK,KS}$      | N_NK_KS     | extended stoichiometric matrix                                  | constant       |                                     | 128 |
| 38  | $K^o_K$          | Ko          | Arrhenius frequency factor                                      | constant       | $m^{-3}\,mol\,s^{-1}$               |     |
| 62  | $E^a_{NK}$       | Ea          | Arrhenius activation energy                                     | constant       | $kg\,m^2\,mol^{-1}\,s^{-2}$         | 41  |
| 63  | $K_{NK}$         | K_NK        | Arrhenius reaction 'constant'                                   | constant       | $m^{-3}\,mol\,s^{-1}$               | 42  |
| 60  | $T_{NK}$         | T_NK        | temperature of the reactive system                              | effort         | $K$                                 | 39  |
| 151 | $c_{NK,KS}$      | c           | concentration matrix reaction per node and species per reaction | secondaryState | $m^{-3}\,mol$                       | 123 |
| 152 | $c^o_{NK,KS}$    | co          | norming concentration   | secondaryState | $m^{-3}\,mol$                       | 124 |
| 153 | $x_{NK,KS}$      | x           | matrix of normed, dimensionless mole fractions                  | secondaryState |                                     | 125 |
| 160 | $\phi_{NK}$      | phi         | probability function for reactions                              | secondaryState |                                     | 129 |
| 163 | $\tilde{n}_{NS}$ | nProd       | the species production term                                     | secondaryState | $mol\,s^{-1}$                       | 130 |

## 6 material

|     | var               | symbol       | documentation  | type     | units                       | eqs   |
|-----|-------------------|--------------|--|----------|-----------------------------|-------|
| 115 | $R_N^e$           | elResist     | electrical resistant   | property | $kg\,m^2\,A^{-2}\,s^{-3}$   | 91 92 |
| 116 | $k_N^{e,\xi}$     | elConductC   | simple model for the electrical conductivity as a function of the additive       | property | $kg^{-1}\,m^{-2}\,A^2\,s^3$ | 93    |
| 183 | $k_{NS}^{d,Fick}$ | k_d_Fick     | Fick's diffusivity   | property | $ms^{-1}$                   |       |
| 187 | $h_{AS}$          | h_A          | partial molar enthalpies (arc)   | property | $kg\,m^2\,mol^{-1}\,s^{-2}$ | 153   |
| 188 | $k_{AS}^{d,Fick}$ | k_d_Fick_A   | Fick's diffusivity (arc)   | property | $ms^{-1}$                   | 154   |
| 189 | $\rho_A$          | density_A    | density (arc)  | property | $kg\,m^{-3}$                | 155   |
| 190 | $k_A^{e,\xi}$     | elConductC_A | simple model for the electrical conductivity as a function of the additive (arc) | property | $kg^{-1}\,m^{-2}\,A^2\,s^3$ | 156   |
| 191 | $k_{xA}^c$        | kc_x_A       | convective mass conductivity in x-direction (arc)                                | property | $m^{-1}\,s$                 | 157   |
| 192 | $k_{yA}^c$        | kc_y_A       | convective mass conductivity in y-direction (arc)                                | property | $m^{-1}\,s$                 | 158   |
| 193 | $k_{zA}^c$        | kc_z_A       | convective mass conductivity in z-direction                                      | property | $m^{-1}\,s$                 | 159   |
| 194 | $k_{xAS}^d$       | kd_x_A       | diffusional mass conductivity in x-direction (arc)                               | property | $kg^{-1}\,m^{-4}\,mol^2\,s$ | 160   |
| 195 | $k_{yAS}^d$       | kd_y_A       | diffusional mass conductivity in y-direction (arc)                               | property | $kg^{-1}\,m^{-4}\,mol^2\,s$ | 161   |
| 196 | $k_{zAS}^d$       | kd_z_A       | diffusional mass conductivity in z-direction (arc)                               | property | $kg^{-1}\,m^{-4}\,mol^2\,s$ | 162   |
| 197 | $k_{xA}^q$        | kq_x_A       | thermal conductivity in x-direction (arc)  | property | $kg\,K^{-1}\,s^{-3}$        | 163   |
| 198 | $k_{yA}^q$        | kq_y_A       | thermal conductivity in y-direction (arc)  | property | $kg\,K^{-1}\,s^{-3}$        | 164   |
| 199 | $k_{zA}^q$        | kq_z_A       | thermal conductivity in z-direction (arc)  | property | $kg\,K^{-1}\,s^{-3}$        | 165   |
| 42  | $C_{pN}$          | Cp           | total heat capacity at constant pressure   | property | $kg\,m^2\,K^{-1}\,s^{-2}$   | 21    |
| 43  | $C_{VN}$          | Cv           | total heat capacity at constant volume   | property | $kg\,m^2\,K^{-1}\,s^{-2}$   | 22    |
| 44  | $k_{xN}^q$        | kq_x         | thermal conductivity in x-direction  | property | $kg\,K^{-1}\,s^{-3}$        | 23    |
| 45  | $k_{yN}^q$        | kq_y         | thermal conductivity in y-direction  | property | $kg\,K^{-1}\,s^{-3}$        | 24    |
| 46  | $k_{zN}^q$        | kq_z         | thermal conductivity in z-direction  | property | $kg\,K^{-1}\,s^{-3}$        | 25    |
| 48  | $k_{xN}^c$        | kc_x         | convective mass conductivity in x-direction                                      | property | $m^{-1}\,s$                 | 27    |

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|     | var               | symbol       | documentation  | type     | units                    | eqs   |
|-----|-------------------|--------------|--|----------|--------------------------|-------|
| 49  | $k_{yN}^c$        | kc_y         | convective mass conductivity in y-direction                                      | property | $m^{-1} s$               | 28    |
| 50  | $k_{zN}^c$        | kc_z         | convective mass conductivity in z-direction                                      | property | $m^{-1} s$               | 29    |
| 52  | $k_{xNS}^d$       | kd_x         | diffusional mass conductivity in x-direction                                     | property | $kg^{-1} m^{-4} mol^2 s$ | 31    |
| 53  | $k_{yNS}^d$       | kd_y         | diffusional mass conductivity in y-direction                                     | property | $kg^{-1} m^{-4} mol^2 s$ | 32    |
| 54  | $k_{zNS}^d$       | kd_z         | diffusional mass conductivity in z-direction                                     | property | $kg^{-1} m^{-4} mol^2 s$ | 33    |
| 56  | $h_{NS}$          | h            | partial molar enthalpies   | property | $kg m^2 mol^{-1} s^{-2}$ | 35    |
| 59  | $\rho_N$          | density      | density  | property | $kg m^{-3}$              | 38    |
| 115 | $R_N^e$           | elResist     | electrical resistant   | property | $kg m^2 A^{-2} s^{-3}$   | 91 92 |
| 116 | $k^{e,\xi}_N$     | elConductC   | simple model for the electrical conductivity as a function of the additive       | property | $kg^{-1} m^{-2} A^2 s^3$ | 93    |
| 183 | $k^{d,Fick}_{NS}$ | k_d_Fick     | Fick's diffusivity   | property | $ms^{-1}$                |       |
| 187 | $h_{AS}$          | h_A          | partial molar enthalpies (arc)   | property | $kg m^2 mol^{-1} s^{-2}$ | 153   |
| 188 | $k^{d,Fick}_{AS}$ | k_d_Fick_A   | Fick's diffusivity (arc)   | property | $ms^{-1}$                | 154   |
| 189 | $\rho_A$          | density_A    | density (arc)  | property | $kg m^{-3}$              | 155   |
| 190 | $k^{e,\xi}_A$     | elConductC_A | simple model for the electrical conductivity as a function of the additive (arc) | property | $kg^{-1} m^{-2} A^2 s^3$ | 156   |
| 191 | $k_{xA}^c$        | kc_x_A       | convective mass conductivity in x-direction (arc)                                | property | $m^{-1} s$               | 157   |
| 192 | $k_{yA}^c$        | kc_y_A       | convective mass conductivity in y-direction (arc)                                | property | $m^{-1} s$               | 158   |
| 193 | $k_{zA}^c$        | kc_z_A       | convective mass conductivity in z-direction                                      | property | $m^{-1} s$               | 159   |
| 194 | $k_{xAS}^d$       | kd_x_A       | diffusional mass conductivity in x-direction (arc)                               | property | $kg^{-1} m^{-4} mol^2 s$ | 160   |
| 195 | $k_{yAS}^d$       | kd_y_A       | diffusional mass conductivity in y-direction (arc)                               | property | $kg^{-1} m^{-4} mol^2 s$ | 161   |
| 196 | $k_{zAS}^d$       | kd_z_A       | diffusional mass conductivity in z-direction (arc)                               | property | $kg^{-1} m^{-4} mol^2 s$ | 162   |
| 197 | $k_{xA}^q$        | kq_x_A       | thermal conductivity in x-direction (arc)  | property | $kg K^{-1} s^{-3}$       | 163   |
| 198 | $k_{yA}^q$        | kq_y_A       | thermal conductivity in y-direction (arc)  | property | $kg K^{-1} s^{-3}$       | 164   |
| 199 | $k_{zA}^q$        | kq_z_A       | thermal conductivity in z-direction (arc)  | property | $kg K^{-1} s^{-3}$       | 165   |

Continued on next page

|     | var         | symbol   | documentation                                | type     | units                       | eqs                |
|-----|-------------|----------|--|----------|-----------------------------|--------------------|
| 42  | $C_{pN}$    | Cp       | total heat capacity at constant pressure     | property | $kg\,m^2\,K^{-1}\,s^{-2}$   | <a href="#">21</a> |
| 43  | $C_{VN}$    | Cv       | total heat capacity at constant volume       | property | $kg\,m^2\,K^{-1}\,s^{-2}$   | <a href="#">22</a> |
| 44  | $k_{xN}^q$  | kq_x     | thermal conductivity in x-direction          | property | $kg\,K^{-1}\,s^{-3}$        | <a href="#">23</a> |
| 45  | $k_{yN}^q$  | kq_y     | thermal conductivity in y-direction          | property | $kg\,K^{-1}\,s^{-3}$        | <a href="#">24</a> |
| 46  | $k_{zN}^q$  | kq_z     | thermal conductivity in z-direction          | property | $kg\,K^{-1}\,s^{-3}$        | <a href="#">25</a> |
| 48  | $k_{xN}^c$  | kc_x     | convective mass conductivity in x-direction  | property | $m^{-1}\,s$                 | <a href="#">27</a> |
| 49  | $k_{yN}^c$  | kc_y     | convective mass conductivity in y-direction  | property | $m^{-1}\,s$                 | <a href="#">28</a> |
| 50  | $k_{zN}^c$  | kc_z     | convective mass conductivity in z-direction  | property | $m^{-1}\,s$                 | <a href="#">29</a> |
| 52  | $k_{xNS}^d$ | kd_x     | diffusional mass conductivity in x-direction | property | $kg^{-1}\,m^{-4}\,mol^2\,s$ | <a href="#">31</a> |
| 53  | $k_{yNS}^d$ | kd_y     | diffusional mass conductivity in y-direction | property | $kg^{-1}\,m^{-4}\,mol^2\,s$ | <a href="#">32</a> |
| 54  | $k_{zNS}^d$ | kd_z     | diffusional mass conductivity in z-direction | property | $kg^{-1}\,m^{-4}\,mol^2\,s$ | <a href="#">33</a> |
| 56  | $h_{NS}$    | h        | partial molar enthalpies                     | property | $kg\,m^2\,mol^{-1}\,s^{-2}$ | <a href="#">35</a> |
| 59  | $\rho_N$    | density  | density                                      | property | $kg\,m^{-3}$                | <a href="#">38</a> |
| 112 | $\xi$       | additive | fraction of additives                        | constant |                             | <a href="#">88</a> |
| 40  | $\lambda_S$ | Mm       | species molecular mass                       | constant | $kg\,mol^{-1}$              |                    |



## 7 macroscopic

|     | var                           | symbol            | documentation                                    | type               | units             | eqs        |
|-----|-------------------------------|-------------------|--|--------------------|-------------------|------------|
| 100 | $\hat{n}_{NS}^c$              | fnc               | net molar convectional mass flow                 | transport          | $mol\ s^{-1}$     | 75         |
| 102 | $\hat{H}_A^c$                 | fHc_A             | convective enthalpy flow for given stream        | transport          | $kg\ m^2\ s^{-3}$ | 77         |
| 103 | $\hat{H}_N^c$                 | fHc               | net convectional enthalpy stream                 | transport          | $kg\ m^2\ s^{-3}$ | 78         |
| 104 | $\hat{w}_A$                   | fw_A              | sample work stream                               | transport          | $kg\ m^2\ s^{-3}$ | 79         |
| 105 | $\hat{w}_N$                   | fw                | net work stream                                  | transport          | $kg\ m^2\ s^{-3}$ | 80         |
| 106 | $\hat{q}_{xA}$                | fq_A_x            | heat flow in x-direction for given stream        | transport          | $kg\ m^2\ s^{-3}$ | 81         |
| 107 | $\hat{q}_N$                   | fq                | net heat flow                                    | transport          | $kg\ m^2\ s^{-3}$ | 82         |
| 173 | $\hat{n}_{AS}^{c,controlled}$ | fnc_AS_controlled | switched flow                                    | transport          | $mol\ s^{-1}$     | 141<br>181 |
| 92  | $\hat{V}_A$                   | fV                | volumetric flow                                  | transport          | $m^3\ s^{-1}$     | 67<br>140  |
| 93  | $\hat{n}_{AS}^d$              | fnd_AS            | diffusional mass flow in a given stream          | transport          | $mol\ s^{-1}$     | 68<br>152  |
| 94  | $\hat{n}_{NS}^d$              | fnd               | net diffusional mass flow                        | transport          | $mol\ s^{-1}$     | 69         |
| 95  | $\hat{H}_A^d$                 | fHd_A             | enthalpy flow per diffusional mass stream        | transport          | $kg\ m^2\ s^{-3}$ | 70         |
| 96  | $\hat{H}_N^d$                 | fHd               | net enthalpy stream due to diffusion             | transport          | $kg\ m^2\ s^{-3}$ | 71         |
| 97  | $d_A$                         | d                 | flow direction of convectional flow              | transport          |                   | 72         |
| 99  | $\hat{n}_{AS}^c$              | fnc_AS            | molar convectional mass flow in the given stream | transport          | $mol\ s^{-1}$     | 74         |
| 215 | $A_{yzA}$                     | Ayz_A             | cross sectional area yz (arc)                    | geometry           | $m^2$             | 179        |
| 71  | $A_{yzN}$                     | Ayz               | cross sectional area yz                          | geometry           | $m^2$             | 48         |
| 70  | $F_{NS,AS}$                   | F_NS_AS           | species related incidence matrix                 | network            |                   |            |
| 90  | $D_{N,A}$                     | D                 | difference operator                              | differenceOperator |                   |            |
| 91  | $D_{NS,AS}$                   | D_NS_AS           | difference operator for species topology         | differenceOperator |                   |            |
| 109 | $H_N^o$                       | Ho                | initial enthalpy                                 | state              | $kg\ m^2\ s^{-2}$ | 84         |

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|     | var              | symbol        | documentation   | type              | units                  | eqs                              |
|-----|------------------|---------------|---|-------------------|------------------------|----------------------------------|
| 110 | $n^o_{NS}$       | <b>no</b>     | initial species   | state             | $mol$                  | <b>85</b>                        |
| 127 | $1_S$            | <b>one_S</b>  | a vector of ones with the length of the ordinal number of S | constant          |                        |                                  |
| 218 | $T^{ref}_N$      | <b>T_ref</b>  | reference temperature                                       | effort            | $K$                    | <b>183</b>                       |
| 128 | $n^t_N$          | <b>nTotal</b> | total number of moles                                       | secondaryState    | $mol$                  | <b>107</b>                       |
| 168 | $n_{tN}$         | <b>nt</b>     | total number of species in a node                           | secondaryState    | $mol$                  | <b>134</b>                       |
| 169 | $\xi_{NS}$       | <b>xi</b>     | mole fraction   | secondaryState    |                        | <b>135</b>                       |
| 176 | $g_{NS}$         | <b>g</b>      |   | secondaryState    | $mol$                  | <b>145</b>                       |
| 57  | $m_N$            | <b>m</b>      | total mass  | secondaryState    | $kg$                   | <b>36</b>                        |
| 66  | $c_{NS}$         | <b>c</b>      | molar composition   | secondaryState    | $m^{-3} mol$           | <b>44</b>                        |
| 98  | $c_{AS}$         | <b>c_AS</b>   | concentration in convectonal flow                           | secondaryState    | $m^{-3} mol$           | <b>73</b>                        |
| 170 | $\tilde{n}_{NS}$ | <b>nProd</b>  | production term   | conversion        | $mol s^{-1}$           | <b>137</b>                       |
| 101 | $\dot{n}_{NS}$   | <b>dndt</b>   | differential species balance                                | diffState         | $mol s^{-1}$           | <b>76</b><br><b>182</b>          |
| 108 | $\dot{H}_N$      | <b>dHdt</b>   | differential enthalpy balance                               | diffState         | $kg m^2 s^{-3}$        | <b>83</b>                        |
| 118 | $\dot{U}^e_N$    | <b>dUedt</b>  | Kirkhoffs first law   | diffState         | $kg m^2 A^{-1} s^{-3}$ | <b>96</b> <b>97</b><br><b>98</b> |
| 113 | $I_N$            | <b>i</b>      | electrical current definition                               | internalTransport | $A$                    | <b>89</b>                        |

## 8 solid

|  | var | symbol | documentation | type | units | eqs |
|--|-----|--------|---------------|------|-------|-----|
|--|-----|--------|---------------|------|-------|-----|

## 9 fluid

|  | var | symbol | documentation | type | units | eqs |
|--|-----|--------|---------------|------|-------|-----|
|--|-----|--------|---------------|------|-------|-----|

## 10 energy

|  | var | symbol | documentation | type | units | eqs |
|--|-----|--------|---------------|------|-------|-----|
|--|-----|--------|---------------|------|-------|-----|

## 11 liquid

|  | var | symbol | documentation | type | units | eqs |
|--|-----|--------|---------------|------|-------|-----|
|--|-----|--------|---------------|------|-------|-----|

## 12 gas

|  | var | symbol | documentation | type | units | eqs |
|--|-----|--------|---------------|------|-------|-----|
|--|-----|--------|---------------|------|-------|-----|

## 13 control-control

|  | var | symbol | documentation | type | units | eqs |
|--|-----|--------|---------------|------|-------|-----|
|--|-----|--------|---------------|------|-------|-----|



## 14 energy–gas

|  | var | symbol | documentation | type | units | eqs |
|--|-----|--------|---------------|------|-------|-----|
|--|-----|--------|---------------|------|-------|-----|

## 15 energy–energy

|  | var | symbol | documentation | type | units | eqs |
|--|-----|--------|---------------|------|-------|-----|
|--|-----|--------|---------------|------|-------|-----|

## 16 gas–gas

|  | var | symbol | documentation | type | units | eqs |
|--|-----|--------|---------------|------|-------|-----|
|--|-----|--------|---------------|------|-------|-----|

## 17 energy–liquid

|  | var | symbol | documentation | type | units | eqs |
|--|-----|--------|---------------|------|-------|-----|
|--|-----|--------|---------------|------|-------|-----|

## 18 liquid–liquid

|  | var | symbol | documentation | type | units | eqs |
|--|-----|--------|---------------|------|-------|-----|
|--|-----|--------|---------------|------|-------|-----|

## 19 energy–solid

|  | var | symbol | documentation | type | units | eqs |
|--|-----|--------|---------------|------|-------|-----|
|--|-----|--------|---------------|------|-------|-----|

## 20 solid-solid

|  | var | symbol | documentation | type | units | eqs |
|--|-----|--------|---------------|------|-------|-----|
|--|-----|--------|---------------|------|-------|-----|

## 21 gas–liquid

|  | var | symbol | documentation | type | units | eqs |
|--|-----|--------|---------------|------|-------|-----|
|--|-----|--------|---------------|------|-------|-----|



## 22 gas-solid

|  | var | symbol | documentation | type | units | eqs |
|--|-----|--------|---------------|------|-------|-----|
|--|-----|--------|---------------|------|-------|-----|

## 23 liquid–solid

|  | var | symbol | documentation | type | units | eqs |
|--|-----|--------|---------------|------|-------|-----|
|--|-----|--------|---------------|------|-------|-----|

## 24 material–material

|  | var | symbol | documentation | type | units | eqs |
|--|-----|--------|---------------|------|-------|-----|
|--|-----|--------|---------------|------|-------|-----|

## 25 reactions-reactions

|  | var | symbol | documentation | type | units | eqs |
|--|-----|--------|---------------|------|-------|-----|
|--|-----|--------|---------------|------|-------|-----|

## 26 control-reactions

|  | var | symbol | documentation | type | units | eqs |
|--|-----|--------|---------------|------|-------|-----|
|--|-----|--------|---------------|------|-------|-----|

## 27 reactions-control

|  | var | symbol | documentation | type | units | eqs |
|--|-----|--------|---------------|------|-------|-----|
|--|-----|--------|---------------|------|-------|-----|

## 28 control-material

|  | var | symbol | documentation | type | units | eqs |
|--|-----|--------|---------------|------|-------|-----|
|--|-----|--------|---------------|------|-------|-----|

## 29 material-control

|     | var             | symbol                 | documentation  | type | units | eqs |
|-----|-----------------|------------------------|--|------|-------|-----|
| 124 | <code>_ξ</code> | <code>_additive</code> | link variable additive to interface material » > control | get  |       | 104 |



## 30 control-macroscopic

|     | var      | symbol               | documentation  | type | units | eqs |
|-----|----------|----------------------|----------------|------|-------|-----|
| 172 | <i>s</i> | <code>_switch</code> | switches at to | get  |       | 139 |

## 31 macroscopic-control

|     | var      | symbol | documentation  | type | units                   | eqs |
|-----|----------|--------|--|------|-------------------------|-----|
| 119 | $_I_N$   | $_i$   | link variable i to interface macroscopic »> control  | get  | $A$                     | 99  |
| 125 | $_T_N$   | $_T$   | link variable T to interface macroscopic »> control  | get  | $K$                     | 105 |
| 142 | $_U^e_N$ | $_Ue$  | link variable Ue to interface macroscopic »> control | get  | $kg\,m^2\,A^{-1}s^{-3}$ | 114 |

## 32 reactions-material

|  | var | symbol | documentation | type | units | eqs |
|--|-----|--------|---------------|------|-------|-----|
|--|-----|--------|---------------|------|-------|-----|

### 33 material-reactions

|  | var | symbol | documentation | type | units | eqs |
|--|-----|--------|---------------|------|-------|-----|
|--|-----|--------|---------------|------|-------|-----|

### 34 reactions-macroscopic

|     | var              | symbol | documentation   | type | units         | eqs |
|-----|------------------|--------|---|------|---------------|-----|
| 164 | $\tilde{n}_{NS}$ | _nProd | link variable nProd to interface reactions »> macroscopic | get  | $mol\ s^{-1}$ | 131 |

## 35 macroscopic-reactions

|    | var               | symbol          | documentation   | type | units        | eqs |
|----|-------------------|-----------------|---|------|--------------|-----|
| 67 | <code>_cNS</code> | <code>_c</code> | link variable c to interface macroscopic »> reactions | get  | $m^{-3} mol$ | 45  |

### 36 material–macroscopic

|     | var                    | symbol                     | documentation   | type | units                    | eqs                 |
|-----|------------------------|----------------------------|---|------|--------------------------|---------------------|
| 117 | $_{R^e_N}$             | <code>_elConductC</code>   | link variable elConductC to interface material »> macroscopic   | get  | $kg^{-1} m^{-2} A^2 s^3$ | <a href="#">94</a>  |
| 140 | $_{\xi}$               | <code>_additive</code>     | link variable additive to interface material »> macroscopic     | get  |                          | <a href="#">112</a> |
| 184 | $_{k^{d,Fick}_{NS}}$   | <code>_k_d_Fick</code>     | link variable k d Fick to interface material »> macroscopic     | get  | $ms^{-1}$                | <a href="#">151</a> |
| 202 | $_{\rho_A}$            | <code>_density_A</code>    | link variable density A to interface material »> macroscopic    | get  | $kg m^{-3}$              | <a href="#">166</a> |
| 203 | $_{R^e_A}$             | <code>_elConductC_A</code> | link variable elConductC A to interface material »> macroscopic | get  | $kg^{-1} m^{-2} A^2 s^3$ | <a href="#">167</a> |
| 204 | $_{h_{AS}}$            | <code>_h_A</code>          | link variable h A to interface material »> macroscopic          | get  | $kg m^2 mol^{-1} s^{-2}$ | <a href="#">168</a> |
| 205 | $_{k^{d,Fick,A}_{AS}}$ | <code>_k_d_Fick_A</code>   | link variable k d Fick A to interface material »> macroscopic   | get  | $ms^{-1}$                | <a href="#">169</a> |
| 206 | $_{k^c_{xA}}$          | <code>_kc_x_A</code>       | link variable kc x A to interface material »> macroscopic       | get  | $m^{-1} s$               | <a href="#">170</a> |
| 207 | $_{k^c_{yA}}$          | <code>_kc_y_A</code>       | link variable kc y A to interface material »> macroscopic       | get  | $m^{-1} s$               | <a href="#">171</a> |
| 208 | $_{k^c_{zA}}$          | <code>_kc_z_A</code>       | link variable kc z A to interface material »> macroscopic       | get  | $m^{-1} s$               | <a href="#">172</a> |
| 209 | $_{k^d_{xAS}}$         | <code>_kd_x_A</code>       | link variable kd x A to interface material »> macroscopic       | get  | $kg^{-1} m^{-4} mol^2 s$ | <a href="#">173</a> |
| 210 | $_{k^d_{yAS}}$         | <code>_kd_y_A</code>       | link variable kd y A to interface material »> macroscopic       | get  | $kg^{-1} m^{-4} mol^2 s$ | <a href="#">174</a> |
| 211 | $_{k^d_{zAS}}$         | <code>_kd_z_A</code>       | link variable kd z A to interface material »> macroscopic       | get  | $kg^{-1} m^{-4} mol^2 s$ | <a href="#">175</a> |
| 212 | $_{k^c_{xA}}$          | <code>_kq_x_A</code>       | link variable kq x A to interface material »> macroscopic       | get  | $kg K^{-1} s^{-3}$       | <a href="#">176</a> |

*Continued on next page*

|     | var            | symbol        | documentation  | type | units                       | eqs |
|-----|----------------|---------------|--|------|-----------------------------|-----|
| 213 | $_{k_y^c A}$   | $_{kq\_y\_A}$ | link variable kq y A to interface material »> macroscopic  | get  | $kg\ K^{-1}\ s^{-3}$        | 177 |
| 214 | $_{k_z^c A}$   | $_{kq\_z\_A}$ | link variable kq z A to interface material »> macroscopic  | get  | $kg\ K^{-1}\ s^{-3}$        | 178 |
| 41  | $_{\lambda_S}$ | $_{Mm}$       | link variable Mm to interface material »> macroscopic      | get  | $kg\ mol^{-1}$              | 20  |
| 74  | $_{\rho_N}$    | $_{density}$  | link variable density to interface material »> macroscopic | get  | $kg\ m^{-3}$                | 51  |
| 75  | $_{h_{NS}}$    | $_{h}$        | link variable h to interface material »> macroscopic       | get  | $kg\ m^2\ mol^{-1}\ s^{-2}$ | 52  |
| 76  | $_{k_x^q N}$   | $_{kq\_x}$    | link variable kq x to interface material »> macroscopic    | get  | $kg\ K^{-1}\ s^{-3}$        | 53  |
| 77  | $_{Cv_N}$      | $_{Cv}$       | link variable Cv to interface material »> macroscopic      | get  | $kg\ m^2\ K^{-1}\ s^{-2}$   | 54  |
| 78  | $_{k_y^q N}$   | $_{kq\_y}$    | link variable kq y to interface material »> macroscopic    | get  | $kg\ K^{-1}\ s^{-3}$        | 55  |
| 79  | $_{k_z^q N}$   | $_{kq\_z}$    | link variable kq z to interface material »> macroscopic    | get  | $kg\ K^{-1}\ s^{-3}$        | 56  |
| 81  | $_{k_x^c N}$   | $_{kc\_x}$    | link variable kc x to interface material »> macroscopic    | get  | $m^{-1}\ s$                 | 58  |
| 82  | $_{Cp_N}$      | $_{Cp}$       | link variable Cp to interface material »> macroscopic      | get  | $kg\ m^2\ K^{-1}\ s^{-2}$   | 59  |
| 83  | $_{k_y^c N}$   | $_{kc\_y}$    | link variable kc y to interface material »> macroscopic    | get  | $m^{-1}\ s$                 | 60  |
| 84  | $_{k_z^c N}$   | $_{kc\_z}$    | link variable kc z to interface material »> macroscopic    | get  | $m^{-1}\ s$                 | 61  |
| 86  | $_{k_x^d NS}$  | $_{kd\_x}$    | link variable kd x to interface material »> macroscopic    | get  | $kg^{-1}\ m^{-4}\ mol^2\ s$ | 63  |
| 87  | $_{k_y^d NS}$  | $_{kd\_y}$    | link variable kd y to interface material »> macroscopic    | get  | $kg^{-1}\ m^{-4}\ mol^2\ s$ | 64  |
| 88  | $_{k_z^d NS}$  | $_{kd\_z}$    | link variable kd z to interface material »> macroscopic    | get  | $kg^{-1}\ m^{-4}\ mol^2\ s$ | 65  |



## 37 macroscopic-material

|     | var    | symbol | documentation  | type | units | eqs |
|-----|--------|--------|--|------|-------|-----|
| 114 | $_I_N$ | $_i$   | link variable i to interface macroscopic »> material | get  | $A$   | 90  |
| 58  | $_m_N$ | $_m$   | link variable m to interface macroscopic »> material | get  | $kg$  | 37  |

## 38 Equations

## 39 Generic

| no  | equation   | documentation                                  | layer       |
|-----|--|--|-------------|
| 10  | $A_N := U_N - T_N \cdot S_N$   | Helmholtz energy                               | physical    |
| 107 | $n_N^t := 1_S \overset{S \in NS}{\star} n_{NS}$                                | total number of moles                          | macroscopic |
| 108 | $e_A := m_A - y_A^o$   | control error                                  | control     |
| 11  | $G_N := U_N + p_N \cdot V_N - T_N \cdot S_N$                                   | Gibbs free energy                              | physical    |
| 110 | $\dot{x}_D := A_{N,D} \overset{N}{\star} x_N + B_{A,D} \overset{A}{\star} e_A$ | differential state (ABCD) model                | control     |
| 111 | $x_N := \int_{t^o}^{t^e} 1_{N,D} \overset{D}{\star} \dot{x}_D dt$              | state  | control     |
| 113 | $\check{I}_N := \_I_N$   | measured current                               | control     |
| 115 | $\check{U}_N^e := \_U_N^e$   | measured electrical potential                  | control     |
| 116 | $\check{\xi} := \_\xi$   | measured additive fraction                     | control     |
| 117 | $R_N := (\check{I}_N)^{-1} \cdot \check{U}_N^e$                                | measured resistance                            | control     |
| 123 | $c_{NK,KS} := P_{NK} \cdot (P_{NS,KS} \overset{NS}{\star} \_c_{NS})$           | var doc :                                      | reactions   |
| 125 | $x_{NK,KS} := (c_{NK,KS}^o)^{-1} \cdot c_{NK,KS}$                              | matrix of normed, dimensionless mole fractions | reactions   |
| 126 | $y_A := C_{N,A} \overset{N}{\star} x_N + D_A \cdot e_A$                        | output equation                                | control     |
| 127 | $R := A^v \cdot B$   | gas constant                                   | reactions   |
| 128 | $N_{NK,KS} := P_{K,NK} \overset{K}{\star} N_{K,KS}$                            | extended stoichiometrix matrix                 | reactions   |

*Continued on next page*

| no  | equation   | documentation                           | layer                             |
|-----|--|---|-----------------------------------|
| 129 | $\phi_{NK} := \prod_{KS} x_{NK,KS}^{N_{NK,KS}}$  | probability function for reactions      | reactions                         |
| 130 | $\tilde{n}_{NS} := V_N \star^N \left( P_{N,NK} \star^{NK} \left( (K_{NK} \cdot \phi_{NK}) \cdot \left( P_{NS,KS} \star^{KS} N_{NK,KS} \right) \right) \right)$ | the species production term             | reactions                         |
| 132 | $B_N := \text{Instantiate}(S_N, \#)$   | Boltzmann constant                      | physical                          |
| 133 | $R_N := A^v \cdot B_N$   | gas constant                            | physical                          |
| 134 | $n_{tN} := 1_S \star^{S \in NS} n_{NS}$  | total number of species in a node       | macroscopic                       |
| 135 | $\xi_{NS} := (n_{tN})^{-1} \odot n_{NS}$   | mole fraction                           | macroscopic                       |
| 136 | $\mu_{NS} := (R_N \cdot T_N) \odot \ln(\xi_{NS})$  | chemical potential                      | macroscopic                       |
| 137 | $\tilde{n}_{NS} := \_ \tilde{n}_{NS}$  | production term                         | macroscopic                       |
| 138 | $s := 0.5 \cdot (1 + \text{sign}(t^o))$  | switches at to                          | control                           |
| 139 | $s := s$   | switches at to                          | control $\rightarrow$ macroscopic |
| 14  | $U^e_N := (C_N)^{-1} \cdot U_N$  | electrical potential – voltage          | physical                          |
| 141 | $\hat{n}^{c,controlled}_{AS} := s \cdot \hat{n}^c_{AS}$  | switched flow                           | macroscopic                       |
| 145 | $g_{NS} := n_{NS} + n_{NS}$  |   | macroscopic                       |
| 15  | $v_{xN} := \frac{\partial r_{xN}}{\partial t}$   | velocity in x-direction                 | physical                          |
| 152 | $\hat{n}^d_{AS} := A_{yZA} \odot \left( \_ k^{d,Fick,A}_{AS} \right) \cdot D_{NS,AS} \star^{NS} c_{NS}$  | diffusional mass flow in a given stream | macroscopic                       |
| 153 | $h_{AS} := I_{NS,AS} \star^{NS} h_{NS}$  | partial molar enthalpies (arc)          | material                          |
| 154 | $k^{d,Fick}_{AS} := I_{NS,AS} \star^{NS} k^{d,Fick}_{NS}$  | Fick's diffusivity (arc)                | material                          |
| 155 | $\rho_A := I_{N,A} \star^N \rho_N$   | density (arc)                           | material                          |

Continued on next page

| no  | equation  | documentation  | layer       |
|-----|---|--|-------------|
| 156 | $k^{e,\xi}_A := I_{N,A} \stackrel{N}{\star} k^{e,\xi}_N$            | simple model for the electrical conductivity as a function of the additive (arc) | material    |
| 157 | $k^c_{xA} := I_{N,A} \stackrel{N}{\star} k^c_{xN}$                  | convective mass conductivity in x-direction (arc)                                | material    |
| 158 | $k^c_{yA} := I_{N,A} \stackrel{N}{\star} k^c_{yN}$                  | convective mass conductivity in y-direction (arc)                                | material    |
| 159 | $k^c_{zA} := I_{N,A} \stackrel{N}{\star} k^c_{zN}$                  | convective mass conductivity in z-direction                                      | material    |
| 16  | $v_{yN} := \frac{\partial r_{yN}}{\partial t}$                      | velocity in y direction  | physical    |
| 160 | $k^d_{xAS} := I_{NS,AS} \stackrel{NS}{\star} k^d_{xNS}$             | diffusional mass conductivity in x-direction (arc)                               | material    |
| 161 | $k^d_{yAS} := I_{NS,AS} \stackrel{NS}{\star} k^d_{yNS}$             | diffusional mass conductivity in y-direction (arc)                               | material    |
| 162 | $k^d_{zAS} := I_{NS,AS} \stackrel{NS}{\star} k^d_{zNS}$             | diffusional mass conductivity in z-direction (arc)                               | material    |
| 163 | $k^q_{xA} := I_{N,A} \stackrel{N}{\star} k^q_{xN}$                  | thermal conductivity in x-direction  | material    |
| 164 | $k^q_{yA} := I_{N,A} \stackrel{N}{\star} k^q_{yN}$                  | thermal conductivity in y-direction (arc)  | material    |
| 165 | $k^q_{zA} := I_{N,A} \stackrel{N}{\star} k^q_{zN}$                  | thermal conductivity in z-direction (arc)  | material    |
| 17  | $v_{zN} := \frac{\partial r_{zN}}{\partial t}$                      | velocity in z-direction  | macroscopic |
| 179 | $A_{yzA} := I_{N,A} \stackrel{N}{\star} A_{yzN}$                    | cross sectional area yz (arc)  | macroscopic |
| 180 | $pulse := \text{sign}(t - t^o) - \text{sign}(t - (t^o + \Delta t))$ | pulse function   | root        |

Continued on next page

| no  | equation  | documentation                                | layer       |
|-----|---|--|-------------|
| 181 | $\hat{n}^{c,controlled}_{AS} := pulse \cdot \hat{n}^c_{AS}$   | manipulate flow                              | macroscopic |
| 182 | $\dot{n}_{NS} := \text{Instantiate}(\dot{n}_{NS}, 0)$   | differential species balance – event dynamic | macroscopic |
| 183 | $T^{ref}_N := \text{Instantiate}(T_N, -)$   | reference temperature                        | macroscopic |
| 184 | $H_N := _Cp_N \cdot (T_N - T^{ref}_N)$  | enthalpy from constant heat capacity         | macroscopic |
| 185 | $T_N := \text{Root}(H_N)$   | temperature                                  | macroscopic |
| 186 | $T_{norm}_N := \text{Instantiate}(_T_N, \#)$  | temprature transmitter constant              | control     |
| 21  | $C_{pN} := \frac{\partial H_N}{\partial T_N}$   | total heat capacity at constant pressure     | material    |
| 22  | $C_{VN} := \frac{\partial U_N}{\partial T_N}$   | total heat capacity at constant volume       | material    |
| 23  | $k^q_{xN} := (V_N)^{-1} \cdot \frac{\partial U_N}{\partial T_N} \cdot v_{xN}$   | thermal conductivity in x-direction          | material    |
| 24  | $k^q_{yN} := (V_N)^{-1} \cdot \frac{\partial U_N}{\partial T_N} \cdot v_{yN}$   | thermal conductivity in y-direction          | material    |
| 25  | $k^q_{zN} := (V_N)^{-1} \cdot \frac{\partial U_N}{\partial T_N} \cdot v_{zN}$   | thermal conductivity in z-direction'         | material    |
| 27  | $k^c_{xN} := \left( \lambda_S^{S \in NS} \star (\mu_{NS})^{-1} \right) \cdot (V_N)^{-1} \cdot \frac{\partial U_N}{\partial p_N} \cdot v_{xN}$ | convecitve mass conductivity in x-direction  | material    |
| 28  | $k^c_{yN} := \left( \lambda_S^{S \in NS} \star (\mu_{NS})^{-1} \right) \cdot (V_N)^{-1} \cdot \frac{\partial U_N}{\partial p_N} \cdot v_{yN}$ | convecitve mass conductivity in y-direction  | material    |
| 29  | $k^c_{zN} := \left( \lambda_S^{S \in NS} \star (\mu_{NS})^{-1} \right) \cdot (V_N)^{-1} \cdot \frac{\partial U_N}{\partial p_N} \cdot v_{zN}$ | convecitve mass conductivity in z-direction  | material    |
| 31  | $k^d_{xNS} := (\mu_{NS})^{-1} \cdot \left( v_{xN} \odot \left( (V_N)^{-1} \odot \frac{\partial U_N}{\partial \mu_{NS}} \right) \right)$       | diffusional mass conductivity in x-direction | material    |

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| no | equation  | documentation                                | layer       |
|----|---|--|-------------|
| 32 | $k_{yNS}^d := (\mu_{NS})^{-1} \cdot \left( v_{yN} \odot \left( (V_N)^{-1} \odot \frac{\partial U_N}{\partial \mu_{NS}} \right) \right)$ | diffusional mass conductivity in y-direction | material    |
| 33 | $k_{zNS}^d := (\mu_{NS})^{-1} \cdot \left( v_{zN} \odot \left( (V_N)^{-1} \odot \frac{\partial U_N}{\partial \mu_{NS}} \right) \right)$ | diffusional mass conductivity in z-direction | material    |
| 35 | $h_{NS} := H_N \odot (n_{NS})^{-1}$   | partial molar enthalpies                     | material    |
| 36 | $m_N := \_ \lambda_S \overset{S \in NS}{\star} n_{NS}$  | total mass                                   | macroscopic |
| 38 | $\rho_N := \_ m_N \cdot (V_N)^{-1}$   | density                                      | material    |
| 39 | $T_{NK} := P_{N,NK} \overset{N}{\star} T_N$   | temperature of the reactive system           | reactions   |
| 42 | $K_{NK} := K^o_K \odot \exp((-E^a_{NK}) \cdot (R \cdot T_{NK})^{-1})$   | Arrhenius reaction 'constant'                | reactions   |
| 44 | $c_{NS} := (V_N)^{-1} \odot n_{NS}$   | molar composition                            | macroscopic |
| 48 | $A_{yzN} := r_{yN} \cdot r_{zN}$  | cross sectional area yz                      | macroscopic |
| 6  | $p_N := \left( -\frac{\partial U_N}{\partial V_N} \right)$  | thermodynamic pressure                       | physical    |
| 67 | $\hat{V}_A := (\_ \rho_N)^{-1} \cdot \_ k_{xN}^c \cdot A_{yzN} \cdot D_{N,A} \overset{N}{\star} p_N$                                    | volumetric flow                              | macroscopic |
| 68 | $\hat{n}_{AS}^d := A_{yzA} \odot \left( -\_ k_{xAS}^d \right) \cdot D_{NS,AS} \overset{NS}{\star} \mu_{NS}$                             | diffusional mass flow in a given stream      | macroscopic |
| 69 | $\hat{n}_{NS}^d := F_{NS,AS} \overset{AS}{\star} \hat{n}_{AS}^d$  | net diffusional mass flow                    | macroscopic |
| 7  | $T_N := \frac{\partial U_N}{\partial S_N}$  | temperature                                  | physical    |
| 70 | $\hat{H}_A^d := \left( F_{NS,AS} \overset{NS}{\star} \_ h_{NS} \right) \overset{S \in AS}{\star} \hat{n}_{AS}^d$                        | enthalpy flow per diffusional mass stream    | macroscopic |
| 71 | $\hat{H}_N^d := F_{N,A} \overset{A}{\star} \hat{H}_A^d$   | net enthaply stream due to diffusion         | macroscopic |
| 72 | $d_A := \text{sign} \left( F_{N,A} \overset{N}{\star} p_N \right)$  | flow direction of convectional flow          | macroscopic |

Continued on next page

| no | equation   | documentation  | layer       |
|----|--|--|-------------|
| 73 | $c_{AS} := (0.5 \cdot (F_{NS,AS} - d_A \odot  F_{NS,AS} )) \overset{NS}{\star} c_{NS}$                           | concentration in convectonal flow  | macroscopic |
| 74 | $\hat{n}^c_{AS} := \hat{V}_A \odot c_{AS}$   | molar convetional mass flow in the given stream                            | macroscopic |
| 75 | $\hat{n}^c_{NS} := F_{NS,AS} \overset{AS}{\star} \hat{n}^c_{AS}$   | net molar convectonal mass flow  | macroscopic |
| 76 | $\dot{n}_{NS} := \hat{n}^c_{NS} + \hat{n}^d_{NS} + \_ \tilde{n}_{NS}$  | differential species balance   | macroscopic |
| 77 | $\hat{H}^c_A := \left( F_{NS,AS} \overset{NS}{\star} \_ h_{NS} \right) \overset{S \in AS}{\star} \hat{n}^c_{AS}$ | convective enthalpy flow for given stream                                  | macroscopic |
| 78 | $\hat{H}^c_N := F_{N,A} \overset{A}{\star} \hat{H}^c_A$  | net convectonal enthalpy stream  | macroscopic |
| 8  | $\mu_{NS} := \frac{\partial U_N}{\partial n_{NS}}$   | chemical potential   | physical    |
| 80 | $\hat{w}_N := F_{N,A} \overset{A}{\star} \hat{w}_A$  | net work stream  | macroscopic |
| 81 | $\hat{q}_{xA} := A_{yzN} \cdot \_ k^q_{xN} \cdot D_{N,A} \overset{N}{\star} T_N$                                 | heat flow in x-direction for given stream                                  | macroscopic |
| 82 | $\hat{q}_N := F_{N,A} \overset{A}{\star} \hat{q}_{xA}$   | net heat flow  | macroscopic |
| 83 | $\dot{H}_N := \hat{H}^c_N + \hat{H}^d_N + \hat{q}_N + \hat{w}_N$   | differential enthalpy balance  | macroscopic |
| 86 | $n_{NS} := \int_{t^o}^{t^e} \dot{n}_{NS} dt + n^o_{NS}$  | fundamental state – molar mass   | macroscopic |
| 87 | $H_N := \int_{t^o}^{t^e} \dot{H}_N dt$   | enthalpy   | macroscopic |
| 89 | $I_N := \frac{dC_N}{dt}$   | electrical current definition  | macroscopic |
| 9  | $H_N := U_N - p_N \cdot V_N$   | enthalpy   | physical    |
| 93 | $k^{e,\xi}_N := (R^e_N)^{-1} \cdot \xi$  | simple model for the electrical conductivity as a function of the additive | material    |
| 95 | $U^e_N := (\_ R^e_N)^{-1} \cdot I_N$   | electrical potential – voltage   | macroscopic |

Continued on next page

| no | equation                     | documentation      | layer       |
|----|------------------------------|--------------------|-------------|
| 96 | $\dot{U}^e_N := 1 . U^e_N$   | Kirkhoff first law | macroscopic |
| 97 | $\dot{U}^e_N := Root(U^e_N)$ | Kirkhoff first law | macroscopic |



## 40 Instantiate

| no  | equation  | documentation               | layer       |
|-----|---|-----------------------------|-------------|
| 1   | $1 := \text{Instantiate}(\#, \#)$                   | numerical value 1           | root        |
| 109 | $x_{oN} := \text{Instantiate}(x_N, \#)$             | initial state               | control     |
| 119 | $y^o_A := \text{Instantiate}(y^o_A, \#)$            | set point                   | control     |
| 124 | $c^o_{NK,KS} := \text{Instantiate}(c_{NK,KS}, \#)$  | norming concentration       | reactions   |
| 2   | $0 := \text{Instantiate}(\#, \#)$                   | numerical value zero        | root        |
| 3   | $0.5 := \text{Instantiate}(\#, \#)$                 | numerical value one half    | root        |
| 4   | $t^o := \text{Instantiate}(t, \#)$                  | starting time               | root        |
| 41  | $E^a_{NK} := \text{Instantiate}(R.T_{NK}, \#)$      | Arrhenius activation energy | reactions   |
| 5   | $t^e := \text{Instantiate}(t, \#)$                  | end time                    | root        |
| 79  | $\hat{w}_A := \text{Instantiate}(\hat{H}^c_A, \#)$  | sample work stream          | macroscopic |
| 84  | $H^o_N := \text{Instantiate}(H_N, \#)$              | initial enthalpy            | macroscopic |
| 85  | $n^o_{NS} := \text{Instantiate}(n_{NS}, \#)$        | initial species             | macroscopic |
| 88  | $\xi := \text{Instantiate}(\xi, \#)$                | fraction of additives       | material    |
| 91  | $R^e_N := (_I_N)^{-1} . U^e_N$                      | electrical resistant        | material    |
| 92  | $R^e_N := \text{Instantiate}(R^e_N, \#)$            | electrical resistant        | material    |
| 98  | $\dot{U}^e_N := \text{Instantiate}(\dot{U}^e_N, 0)$ | Kirkhoff first law          | macroscopic |

## 41 Instantiation Equation

| no  | equation   | documentation          | layer       |
|-----|--|------------------------|-------------|
| 140 | $\hat{V}_A := \text{Instantiate}(\hat{V}_A, \#)$ | instantiation equation | macroscopic |

## 42 Interface Link Equation

| no  | equation                                  | documentation      | layer                    |
|-----|---|--------------------|--------------------------|
| 104 | $\_ \xi := \xi$                           | interface equation | material -> control      |
| 105 | $\_ T_N := T_N$                           | interface equation | macroscopic -> control   |
| 112 | $\_ \xi := \xi$                           | interface equation | material -> macroscopic  |
| 114 | $\_ U_N^e := U_N^e$                       | interface equation | macroscopic -> control   |
| 131 | $\_ \tilde{n}_{NS} := \tilde{n}_{NS}$     | interface equation | reactions -> macroscopic |
| 151 | $\_ k_{NS}^{d,Fick} := k_{NS}^{d,Fick}$   | interface equation | material -> macroscopic  |
| 166 | $\_ \rho_A := \rho_A$                     | interface equation | material -> macroscopic  |
| 167 | $\_ R_A^e := k_{A}^{e,\xi}$               | interface equation | material -> macroscopic  |
| 168 | $\_ h_{AS} := h_{AS}$                     | interface equation | material -> macroscopic  |
| 169 | $\_ k_{AS}^{d,Fick,A} := k_{AS}^{d,Fick}$ | interface equation | material -> macroscopic  |
| 170 | $\_ k_{xA}^c := k_{xA}^c$                 | interface equation | material -> macroscopic  |

*Continued on next page*

| no  | equation                   | documentation      | layer                    |
|-----|----------------------------|--------------------|--------------------------|
| 171 | $\_k_{yA}^c := k_{yA}^c$   | interface equation | material -> macroscopic  |
| 172 | $\_k_{zA}^c := k_{zA}^c$   | interface equation | material -> macroscopic  |
| 173 | $\_k_{xAS}^d := k_{xAS}^d$ | interface equation | material -> macroscopic  |
| 174 | $\_k_{yAS}^d := k_{yAS}^d$ | interface equation | material -> macroscopic  |
| 175 | $\_k_{zAS}^d := k_{zAS}^d$ | interface equation | material -> macroscopic  |
| 176 | $\_k_{xA}^c := k_{xA}^q$   | interface equation | material -> macroscopic  |
| 177 | $\_k_{yA}^c := k_{yA}^q$   | interface equation | material -> macroscopic  |
| 178 | $\_k_{zA}^c := k_{zA}^q$   | interface equation | material -> macroscopic  |
| 20  | $\_\lambda_S := \lambda_S$ | interface equation | material -> macroscopic  |
| 37  | $\_m_N := m_N$             | interface equation | macroscopic -> material  |
| 45  | $\_c_{NS} := c_{NS}$       | interface equation | macroscopic -> reactions |
| 51  | $\_\rho_N := \rho_N$       | interface equation | material -> macroscopic  |

*Continued on next page*

| no | equation                   | documentation      | layer                              |
|----|----------------------------|--------------------|------------------------------------|
| 52 | $\_h_{NS} := h_{NS}$       | interface equation | material $\rightarrow$ macroscopic |
| 53 | $\_k_{xN}^q := k_{xN}^q$   | interface equation | material $\rightarrow$ macroscopic |
| 54 | $\_Cv_N := C_{VN}$         | interface equation | material $\rightarrow$ macroscopic |
| 55 | $\_k_{yN}^q := k_{yN}^q$   | interface equation | material $\rightarrow$ macroscopic |
| 56 | $\_k_{zN}^q := k_{zN}^q$   | interface equation | material $\rightarrow$ macroscopic |
| 58 | $\_k_{xN}^c := k_{xN}^c$   | interface equation | material $\rightarrow$ macroscopic |
| 59 | $\_Cp_N := C_{pN}$         | interface equation | material $\rightarrow$ macroscopic |
| 60 | $\_k_{yN}^c := k_{yN}^c$   | interface equation | material $\rightarrow$ macroscopic |
| 61 | $\_k_{zN}^c := k_{zN}^c$   | interface equation | material $\rightarrow$ macroscopic |
| 63 | $\_k_{xNS}^d := k_{xNS}^d$ | interface equation | material $\rightarrow$ macroscopic |
| 64 | $\_k_{yNS}^d := k_{yNS}^d$ | interface equation | material $\rightarrow$ macroscopic |
| 65 | $\_k_{zNS}^d := k_{zNS}^d$ | interface equation | material $\rightarrow$ macroscopic |

*Continued on next page*

| no | equation                 | documentation      | layer                              |
|----|--------------------------|--------------------|------------------------------------|
| 90 | $\_I_N := I_N$           | interface equation | macroscopic material $\rightarrow$ |
| 94 | $\_R^e_N := k^{e,\xi}_N$ | interface equation | material $\rightarrow$ macroscopic |
| 99 | $\_I_N := I_N$           | interface equation | macroscopic control $\rightarrow$  |