

# 1 Variables

## 2 root

|    | var        | symbol            | documentation                         | type       | units | eqs |
|----|------------|-------------------|---------------------------------------|------------|-------|-----|
| 10 | $F_{N,A}$  | <b>F</b>          | basic directed graph incidence matrix | network    |       |     |
| 48 | $I_{N,A}$  | <b>I_N_A</b>      | project node on arc                   | projection |       |     |
| 97 | $I_A$      | <b>I_A</b>        | vector of ones of length arcs         | projection |       |     |
| 96 | $I_N$      | <b>I_N</b>        | vector of ones of length nodes        | projection |       |     |
| 4  | $t$        | <b>t</b>          | time                                  | frame      | $s$   |     |
| 5  | $t^o$      | <b>to</b>         | time zero                             | frame      | $s$   | 3   |
| 9  | $\Delta$   | <b>pulse</b>      | pulse of length time interval         | frame      |       | 7   |
| 7  | $\Delta t$ | <b>t_interval</b> | time interval                         | frame      | $s$   | 5   |
| 6  | $t^e$      | <b>te</b>         | time end                              | frame      | $s$   | 4   |
| 1  | $\#$       | <b>value</b>      | numerical value                       | constant   |       |     |
| 2  | 1          | <b>one</b>        | numerical one                         | constant   |       | 1   |
| 8  | 0.5        | <b>onehalf</b>    | numerical one half                    | constant   |       | 6   |
| 3  | 0          | <b>zero</b>       | numerical value zero                  | constant   |       | 2   |

### 3 physical

|     | var         | symbol         | documentation                       | type       | units                               | eqs              |
|-----|-------------|----------------|-------------------------------------|------------|-------------------------------------|------------------|
| 170 | $S_S$       | <b>S_S</b>     | species selection                   | projection |                                     |                  |
| 98  | $I_S$       | <b>I_S</b>     | vector of ones of length sepecies   | projection |                                     |                  |
| 13  | $r_{yN}$    | <b>r_y</b>     | y-direction                         | frame      | $m$                                 | 9                |
| 11  | $\ell_N$    | <b>l</b>       | length                              | frame      | $m$                                 |                  |
| 14  | $r_{zN}$    | <b>r_z</b>     | z-direction                         | frame      | $m$                                 | 10               |
| 12  | $r_{xN}$    | <b>r_x</b>     | x-direction                         | frame      | $m$                                 | 8                |
| 189 | $h_N$       | <b>height</b>  | height                              | frame      | $m$                                 | 176              |
| 23  | $A_N$       | <b>A</b>       | Helmholts energy                    | state      | $kg\ m^2\ s^{-2}$                   | 17               |
| 22  | $H_N$       | <b>H</b>       | Enthalpy                            | state      | $kg\ m^2\ s^{-2}$                   | 15<br>128<br>161 |
| 17  | $S_N$       | <b>S</b>       | fundamental state - entropy         | state      | $kg\ m^2\ K^{-1}\ s^{-2}$           |                  |
| 25  | $C_N$       | <b>C</b>       | fundamental state - charge          | state      | $A\ s$                              |                  |
| 15  | $V_N$       | <b>V</b>       | fundamental state - volume          | state      | $m^3$                               | 11               |
| 24  | $G_N$       | <b>G</b>       | Gibbs free energy                   | state      | $kg\ m^2\ s^{-2}$                   | 18               |
| 16  | $U_N$       | <b>U</b>       | fundamental state - internal energy | state      | $kg\ m^2\ s^{-2}$                   |                  |
| 18  | $n_{N,S}$   | <b>n</b>       | fundamental state - molar mass      | state      | $mol$                               | 129              |
| 32  | $A^v$       | <b>Av</b>      | Avogadro number                     | constant   | $mol^{-1}$                          |                  |
| 190 | $g$         | <b>g</b>       | gravitational constant              | constant   | $ms^{-2}$                           |                  |
| 33  | $B_N$       | <b>Boltz</b>   | Boltzmann constant                  | constant   | $kg\ m^2\ K^{-1}\ s^{-2}$           | 24               |
| 34  | $R_N$       | <b>R</b>       | Gas constant                        | constant   | $kg\ m^2\ mol^{-1}\ K^{-1}\ s^{-2}$ | 25               |
| 35  | $U^e_N$     | <b>Ue</b>      | electrical potential – voltage      | effort     | $kg\ m^2\ A^{-1}\ s^{-3}$           | 26               |
| 21  | $\mu_{N,S}$ | <b>chemPot</b> | chemical potential                  | effort     | $kg\ m^2\ mol^{-1}\ s^{-2}$         | 14 88            |

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|    | var      | symbol     | documentation           | type           | units                | eqs                     |
|----|----------|------------|-------------------------|----------------|----------------------|-------------------------|
| 20 | $p_N$    | <b>p</b>   | pressure                | effort         | $kg\,m^{-1}\,s^{-2}$ | <b>13</b>               |
| 19 | $T_N$    | <b>T</b>   | temperature             | effort         | $K$                  | <b>16</b><br><b>162</b> |
| 28 | $v_{yN}$ | <b>v_y</b> | velocity in y-direction | secondaryState | $ms^{-1}$            | <b>20</b>               |
| 29 | $v_{zN}$ | <b>v_z</b> | velocity in z-direction | secondaryState | $ms^{-1}$            | <b>21</b>               |
| 27 | $v_{xN}$ | <b>v_x</b> | velocity in x-direction | secondaryState | $ms^{-1}$            | <b>19</b>               |

## 4 reactions

|     | var               | symbol                 | documentation   | type           | units                       | eqs |
|-----|-------------------|------------------------|---|----------------|-----------------------------|-----|
| 113 | $P_{N,K}$         | P_N_K                  | what node has what reaction   | projection     |                             |     |
| 114 | $T_{N,K}$         | T_K                    | temparature of the nodes with reactions   | effort         | $K$                         | 99  |
| 128 | $\bar{n}_{N,S}$   | cn                     | normed concentration  | secondaryState |                             | 112 |
| 129 | $\bar{n}_{N,S,K}$ | cn_NK                  | normed concentration – context node and conversion                                  | secondaryState |                             | 113 |
| 131 | $\phi_{N,K}$      | interactionProbability | probability for the species to meet to undergo reaction                             | properties     |                             | 115 |
| 115 | $E_{aN,K}$        | Ea                     | Arrhenius activation energy   | properties     | $kg\,m^2\,mol^{-1}\,s^{-2}$ | 100 |
| 134 | $K^o_K$           | Ko                     | Arrhenius frequency factor – a strange construction                                 | properties     | $m^{-3}\,mol\,s^{-1}$       | 118 |
| 135 | $K_{N,K}$         | K                      | reaction"constant   | properties     | $m^{-3}\,mol\,s^{-1}$       | 119 |
| 118 | $N_{S,K}$         | N                      | stoichiometric matrix   | properties     |                             |     |
| 126 | $c^n_{N,S}$       | c_norming              | norming concentration used in the definition of the species interaction probability | properties     | $m^{-3}\,mol$               | 110 |
| 136 | $\tilde{n}_{N,S}$ | nProd                  | production term for differential component mass balance                             | conversion     | $mol\,s^{-1}$               | 120 |

## 5 material

|    | var                    | symbol    | documentation                                       | type     | units                       | eqs |
|----|------------------------|-----------|---|----------|-----------------------------|-----|
| 36 | $C_{pN}$               | Cp        | total heat capacity at constant pressure            | property | $kg\ m^2\ K^{-1}\ s^{-2}$   | 27  |
| 49 | $k_{xA}^c$             | kc_x_A    | convective mass conductivity in x-direction in arc  | property | $m^{-1}\ s$                 | 39  |
| 89 | $\rho_A$               | density_A | density of arc material                             | property | $kg\ m^{-3}$                | 78  |
| 38 | $k_{xN}^q$             | kq_x      | thermal conductivity in x-direction                 | property | $kg\ K^{-1}\ s^{-3}$        | 29  |
| 52 | $k_{xA,S}^d$           | kd_x_A    | diffusional mass conductivity in x-direction in arc | property | $kg^{-1}\ m^{-4}\ mol^2\ s$ | 42  |
| 56 | $k_{yA}^q$             | kq_y_A    | thermal conductivity in y-direction in arc          | property | $kg\ K^{-1}\ s^{-3}$        | 46  |
| 45 | $k_{yN}^c$             | kc_y      | convective mass conductivity in y-direction         | property | $m^{-1}\ s$                 | 36  |
| 63 | $k_z^{d,Fick}{}_{A,S}$ | kd_z_Fick | Fick's diffusivity in arc and z-direction           | property | $ms^{-1}$                   | 53  |
| 47 | $h_{N,S}$              | h         | partial molar enthalpies                            | property | $kg\ m^2\ mol^{-1}\ s^{-2}$ | 38  |
| 58 | $m_N$                  | m         | mass  | property | $kg$                        | 48  |
| 54 | $k_{zA,S}^d$           | kd_z_A    | diffusional mass conductivity in z-direction in arc | property | $kg^{-1}\ m^{-4}\ mol^2\ s$ | 44  |
| 62 | $k_y^{d,Fick}{}_{A,S}$ | kd_y_Fick | Fick's diffusivity in arc and y-direction           | property | $ms^{-1}$                   | 52  |
| 46 | $k_{zN}^c$             | kc_z      | convective mass conductivity in z-direction         | property | $m^{-1}\ s$                 | 37  |
| 37 | $C_{vN}$               | Cv        | total heat capacity at constant volume              | property | $kg\ m^2\ K^{-1}\ s^{-2}$   | 28  |
| 55 | $k_{xA}^q$             | kq_x_A    | thermal conductivity in x-direction in arc          | property | $kg\ K^{-1}\ s^{-3}$        | 45  |
| 57 | $k_{zA}^q$             | kq_z_A    | thermal conductivity in z-direction in arc          | property | $kg\ K^{-1}\ s^{-3}$        | 47  |
| 43 | $k_{zN,S}^d$           | kd_z      | diffusional mass conductivity in z-direction        | property | $kg^{-1}\ m^{-4}\ mol^2\ s$ | 34  |
| 61 | $k_x^{d,Fick}{}_{A,S}$ | kd_x_Fick | Fick's diffusivity in arc and x-direction           | property | $ms^{-1}$                   | 51  |
| 51 | $k_{zA}^c$             | kc_z_A    | convective mass conductivity in z-direction in arc  | property | $m^{-1}\ s$                 | 41  |
| 42 | $k_{yN,S}^d$           | kd_y      | diffusional mass conductivity in z-direction        | property | $kg^{-1}\ m^{-4}\ mol^2\ s$ | 33  |
| 50 | $k_{yA}^c$             | kc_y_A    | convective mass conductivity in y-direction in arc  | property | $m^{-1}\ s$                 | 40  |
| 44 | $k_{xN}^c$             | kc_x      | convective mass conductivity in x-direction         | property | $m^{-1}\ s$                 | 35  |
| 41 | $k_{xN,S}^d$           | kd_x      | diffusional mass conductivity in x-direction        | property | $kg^{-1}\ m^{-4}\ mol^2\ s$ | 32  |

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|     | var           | symbol           | documentation  | type     | units                    | eqs        |
|-----|---------------|------------------|--|----------|--------------------------|------------|
| 53  | $k_{yA,S}^d$  | <b>kd_y_A</b>    | diffusional mass conductivity in y-direction in arc                                    | property | $kg^{-1} m^{-4} mol^2 s$ | <b>43</b>  |
| 59  | $\rho_N$      | <b>density</b>   | density  | property | $kg m^{-3}$              | <b>49</b>  |
| 171 | $k^{e,x}_N$   | <b>kex</b>       | electrical conductivity – a simple model being a function of a selected set of species | property | $kg^{-1} m^{-2} A^2 s^3$ | <b>155</b> |
| 60  | $v_S$         | <b>v</b>         | molar volume of species  | property | $m^3 mol^{-1}$           | <b>50</b>  |
| 107 | $h_{A,S}$     | <b>h_A</b>       | partial molar enthalpies of transport system   | property | $kg m^2 mol^{-1} s^{-2}$ | <b>93</b>  |
| 40  | $k_z^q$       | <b>kq_z</b>      | thermal conductivity in z-direction  | property | $kg K^{-1} s^{-3}$       | <b>31</b>  |
| 168 | $R_N^e$       | <b>Re</b>        | electrical resistance  | property | $kg m^2 A^{-2} s^{-3}$   | <b>154</b> |
| 39  | $k_y^q$       | <b>kq_y</b>      | thermal conductivity in y-direction  | property | $kg K^{-1} s^{-3}$       | <b>30</b>  |
| 172 | $cp_N$        | <b>cp</b>        | specific heat capacity at constant pressure  | property | $m^2 K^{-1} s^{-2}$      | <b>156</b> |
| 26  | $\lambda_S$   | <b>Mm</b>        | species' molecular mass  | property | $kg mol^{-1}$            |            |
| 102 | $\mu_{N,S}^o$ | <b>chemPot_o</b> | standard chemical potential  | effort   | $kg m^2 mol^{-1} s^{-2}$ | <b>86</b>  |

## 6 macroscopic

|     | var                         | symbol                       | documentation                                     | type      | units             | eqs              |
|-----|-----------------------------|------------------------------|---|-----------|-------------------|------------------|
| 195 | $fE_{potential_A}$          | <b>fE_potential</b>          | flow of potential energy                          | transport | $kg\ m^2\ s^{-3}$ | 180              |
| 104 | $\dot{n}_{N,S}^d$           | <b>and</b>                   | accumulation due to diffusional mass transfer     | transport | $mol\ s^{-1}$     | 90               |
| 101 | $\hat{n}_{A,S}^d$           | <b>fnd</b>                   | diffusional mass flow in arc                      | transport | $mol\ s^{-1}$     | 85 89            |
| 196 | $length_{pipe_A}$           | <b>length_pipe</b>           | length of pipe                                    | transport | $m$               | 181              |
| 87  | $c_{A,S}$                   | <b>c_A</b>                   | concentration in convective mass flow             | transport | $m^{-3}\ mol$     | 76               |
| 86  | $d_A$                       | <b>d</b>                     | flow direction of convective flow                 | transport |                   | 75               |
| 199 | $\hat{E}_A^k$               | <b>fE_kinetic</b>            | flow of kinetic energy                            | transport | $kg\ m^2\ s^{-3}$ | 184              |
| 188 | $\hat{m}_A$                 | <b>fm</b>                    | mass flow rate                                    | transport | $kg\ s^{-1}$      | 174              |
| 141 | $\hat{w}_A$                 | <b>fw</b>                    | just an numerical work flow term – as a starter   | transport | $kg\ m^2\ s^{-3}$ | 125              |
| 92  | $\hat{n}_{A,S}^c$           | <b>fnc</b>                   | convective mass flow in an arc                    | transport | $mol\ s^{-1}$     | 81               |
| 111 | $\dot{H}_N^c$               | <b>aHc</b>                   | enthalpy accumulation due to convective mass flow | transport | $kg\ m^2\ s^{-3}$ | 97               |
| 93  | $\dot{n}_{N,S}^c$           | <b>anc</b>                   | accumulation due to convective mass flow          | transport | $mol\ s^{-1}$     | 82               |
| 200 | $\hat{w}_A^f$               | <b>fw_friction</b>           | work flow due to linear friction                  | transport | $kg\ m^2\ s^{-3}$ | 185              |
| 91  | $\dot{V}_A$                 | <b>fV</b>                    | volumetric flow                                   | transport | $m^3\ s^{-1}$     | 80<br>172<br>175 |
| 83  | $\hat{q}_{xA}$              | <b>fq_x</b>                  | heat flow in arc and x-direction                  | transport | $kg\ m^2\ s^{-3}$ | 72               |
| 112 | $\dot{H}_N^d$               | <b>aHd</b>                   | enthalpy accumulation due to diffusive mass flow  | transport | $kg\ m^2\ s^{-3}$ | 98               |
| 142 | $\dot{w}_N$                 | <b>aw</b>                    | enthalpy accumulation due to work flows           | transport | $kg\ m^2\ s^{-3}$ | 126              |
| 109 | $\hat{H}_A^c$               | <b>fHc</b>                   | enthalpy flow due to convective mass flow         | transport | $kg\ m^2\ s^{-3}$ | 95               |
| 166 | $I_N$                       | <b>I</b>                     | electric current definition                       | transport | $A$               | 152              |
| 197 | $friction_{coeff_{linear}}$ | <b>friction_coeff_linear</b> | friction factor for linear friction model         | transport | $kg\ ms^{-3}$     | 182              |
| 194 | $height_{AA}$               | <b>height_A</b>              | height in arc node                                | transport | $m$               | 179              |

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|     | var                 | symbol        | documentation  | type               | units                     | eqs |
|-----|---------------------|---------------|--|--------------------|---------------------------|-----|
| 110 | $\hat{H}^d_A$       | fHd           | enthalpy flow due to diffusive mass flow                   | transport          | $kg\,m^2\,s^{-3}$         | 96  |
| 201 | $aE_{mechanical}_A$ | aE_mechanical | accumulation of mechanical energy                          | transport          | $kg\,m^2\,s^{-3}$         | 186 |
| 84  | $\dot{q}_N$         | aq            | accumulation due to conductive heat flow                   | transport          | $kg\,m^2\,s^{-3}$         | 73  |
| 66  | $A_{xzN}$           | A_xz          | cross sectional area xz                                    | geometry           | $m^2$                     | 55  |
| 65  | $A_{xyN}$           | A_xy          | cross sectional area xy                                    | geometry           | $m^2$                     | 54  |
| 70  | $A_{yzA}$           | A_yz_A        | cross sectional area yz of arc                             | geometry           | $m^2$                     | 59  |
| 68  | $A_{xyA}$           | A_xy_A        | cross sectional area yz of arc                             | geometry           | $m^2$                     | 57  |
| 69  | $A_{xzA}$           | A_xz_A        | cross sectional area xz of arc                             | geometry           | $m^2$                     | 58  |
| 67  | $A_{yzN}$           | A_yz          | cross sectional area yz                                    | geometry           | $m^2$                     | 56  |
| 186 | $k^{valve}_A$       | valveConstant | valve constant – pressure difference must be dimensionless | properties         | $m^3\,s^{-1}$             | 171 |
| 191 | $f$                 | f             | friction factor  | properties         |                           |     |
| 64  | $D_{N,A}$           | D             | difference operator  | differenceOperator |                           |     |
| 145 | $n^o_{N,S}$         | no            | initial species masses                                     | state              | $mol$                     | 131 |
| 144 | $H^o_N$             | Ho            | initial enthalpy   | state              | $kg\,m^2\,s^{-2}$         | 130 |
| 100 | $x_{N,S}$           | x             | concentration mole fraction                                | secondaryState     |                           | 84  |
| 99  | $n^t_N$             | nt            | total amount   | secondaryState     | $mol$                     | 83  |
| 148 | $c^o_{N,S}$         | c_norming     | norming concentration                                      | secondaryState     | $m^{-3}\,mol$             | 134 |
| 85  | $c_{N,S}$           | c             | molar concentration  | secondaryState     | $m^{-3}\,mol$             | 74  |
| 151 | $\bar{c}^o_{N,S}$   | c_normed      | normed concentration                                       | secondaryState     |                           | 137 |
| 192 | $v_{xA}$            | v_x_A         | velocity in arc  | secondaryState     | $ms^{-1}$                 | 177 |
| 146 | $T^o_N$             | T_norming     | norming temperature  | secondaryState     | $K$                       | 132 |
| 175 | $C_{pN}$            | Cp            | total heat capacity  | secondaryState     | $kg\,m^2\,K^{-1}\,s^{-2}$ | 159 |
| 150 | $\bar{p}^o_N$       | p_normed      | normed pressure  | secondaryState     |                           | 136 |
| 147 | $p^o_N$             | p_norming     | normed pressure  | secondaryState     | $kg\,m^{-1}\,s^{-2}$      | 133 |

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|     | var               | symbol              | documentation                 | type           | units             | eqs                 |
|-----|-------------------|---------------------|-------------------------------|----------------|-------------------|---------------------|
| 174 | $m_N$             | <b>m</b>            | mass                          | secondaryState | $kg$              | <a href="#">158</a> |
| 149 | $\bar{T}^o_N$     | <b>T_normed</b>     | normed temperature            | secondaryState |                   | <a href="#">135</a> |
| 176 | $T^{ref}_N$       | <b>T_ref</b>        | reference temperature         | secondaryState | $K$               | <a href="#">160</a> |
| 138 | $\dot{n}^p_{N,S}$ | <b>anProduction</b> | production term               | conversion     | $mol\ s^{-1}$     | <a href="#">122</a> |
| 143 | $\dot{H}_N$       | <b>aH</b>           | differential enthalpy balance | diffState      | $kg\ m^2\ s^{-3}$ | <a href="#">127</a> |
| 139 | $\dot{n}_{N,S}$   | <b>an</b>           | differential species balance  | diffState      | $mol\ s^{-1}$     | <a href="#">123</a> |

## 7 control

|     | var            | symbol                          | documentation                        | type      | units    | eqs  |
|-----|----------------|---------------------------------|--------------------------------------|-----------|----------|--|
| 185 | $t_{sA}$       | <code>t_switch_A</code>         | switching times                      | frame     | $s$      | <a href="#">169</a>                        |
| 183 | $x_N^o$        | <code>xo</code>                 | initial controller state             | state     |          | <a href="#">166</a>                        |
| 179 | $x_N$          | <code>x</code>                  | controller state                     | state     |          | <a href="#">165</a>                        |
| 178 | $B_{A,D}$      | <code>B</code>                  | LTIS B-matrix                        | constant  | $s^{-1}$ |  |
| 159 | $P$            | <code>P</code>                  | gain                                 | constant  |          |  |
| 158 | $m^{m*}_{A,S}$ | <code>setpoint_matrix</code>    | setpoint for measurment matrix       | constant  |          | <a href="#">145</a>                        |
| 181 | $I_{N,D}$      | <code>I_N_D</code>              | map differential space to node space | constant  |          |  |
| 177 | $A_{N,D}$      | <code>A</code>                  | LTIS A-matrix                        | constant  | $s^{-1}$ |  |
| 157 | $m^{v*}_A$     | <code>setpoint_vector</code>    | setpoint for measurement vector      | constant  |          | <a href="#">144</a>                        |
| 182 | $\dot{x}_D$    | <code>dxdt</code>               | differential controller state        | diffState | $s^{-1}$ | <a href="#">164</a>                        |
| 160 | $e^v_A$        | <code>error_vector</code>       | output error vector                  | algebraic |          | <a href="#">146</a>                        |
| 155 | $m_A$          | <code>measurement_vector</code> | normed measurements of temperatures  | algebraic |          | <a href="#">141</a><br><a href="#">142</a> |
| 163 | $u^m_{A,S}$    | <code>u_matrix</code>           | control output matrix                | algebraic |          | <a href="#">149</a>                        |
| 156 | $m_{A,S}$      | <code>measurement_matrix</code> | normed measurment of concentration   | algebraic |          | <a href="#">143</a>                        |
| 162 | $u^v_A$        | <code>u_vector</code>           | control ouput vector                 | algebraic |          | <a href="#">148</a><br><a href="#">170</a> |
| 161 | $e^m_{A,S}$    | <code>error_matrix</code>       | output error matrix                  | algebraic |          | <a href="#">147</a>                        |

## 8 material–macroscopic

|     | var                    | symbol           | documentation  | type | units                       | eqs |
|-----|------------------------|------------------|--|------|-----------------------------|-----|
| 108 | $_{h_{A,S}}$           | $_{h\_A}$        | link variable h A to interface material »> macroscopic       | get  | $kg\,m^2\,mol^{-1}\,s^{-2}$ | 94  |
| 71  | $_{k_{xA}^c}$          | $_{kc\_x\_A}$    | link variable kc x A to interface material »> macroscopic    | get  | $m^{-1}\,s$                 | 60  |
| 88  | $_{\rho_N}$            | $_{density}$     | link variable density to interface material »> macroscopic   | get  | $kg\,m^{-3}$                | 77  |
| 78  | $_{k_{zA,S}^d}$        | $_{kd\_z\_A}$    | link variable kd z A to interface material »> macroscopic    | get  | $kg^{-1}\,m^{-4}\,mol^2\,s$ | 67  |
| 76  | $_{k_{yA,S}^{d,Fick}}$ | $_{kd\_y\_Fick}$ | link variable kd y Fick to interface material »> macroscopic | get  | $ms^{-1}$                   | 65  |
| 72  | $_{k_{yA}^c}$          | $_{kc\_y\_A}$    | link variable kc y A to interface material »> macroscopic    | get  | $m^{-1}\,s$                 | 61  |
| 75  | $_{k_{xA}^{d,Fick}}$   | $_{kd\_x\_Fick}$ | link variable kd x Fick to interface material »> macroscopic | get  | $ms^{-1}$                   | 64  |
| 77  | $_{k_{yA,S}^d}$        | $_{kd\_y\_A}$    | link variable kd y A to interface material »> macroscopic    | get  | $kg^{-1}\,m^{-4}\,mol^2\,s$ | 66  |
| 30  | $_{\lambda_S}$         | $_{Mm}$          | link variable Mm to interface material »> macroscopic        | get  | $kg\,mol^{-1}$              | 22  |
| 79  | $_{k_{zA,S}^{d,Fick}}$ | $_{kd\_z\_Fick}$ | link variable kd z Fick to interface material »> macroscopic | get  | $ms^{-1}$                   | 68  |
| 73  | $_{k_{zA}^c}$          | $_{kc\_z\_A}$    | link variable kc z A to interface material »> macroscopic    | get  | $m^{-1}\,s$                 | 62  |
| 81  | $_{k_{yA}^q}$          | $_{kq\_y\_A}$    | link variable kq y A to interface material »> macroscopic    | get  | $kg\,K^{-1}\,s^{-3}$        | 70  |
| 80  | $_{k_{xA}^q}$          | $_{kq\_x\_A}$    | link variable kq x A to interface material »> macroscopic    | get  | $kg\,K^{-1}\,s^{-3}$        | 69  |
| 173 | $_{c_{pN}}$            | $_{cp}$          | link variable cp to interface material »> macroscopic        | get  | $m^2\,K^{-1}\,s^{-2}$       | 157 |

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|     | var               | symbol                  | documentation  | type | units                    | eqs       |
|-----|-------------------|-------------------------|--|------|--------------------------|-----------|
| 74  | $_{k_{x A, S}^d}$ | <code>_kd_x_A</code>    | link variable kd x A to interface material »> macroscopic    | get  | $kg^{-1} m^{-4} mol^2 s$ | <b>63</b> |
| 90  | $_{\rho A}$       | <code>_density_A</code> | link variable density A to interface material »> macroscopic | get  | $kg m^{-3}$              | <b>79</b> |
| 82  | $_{k_{z A}^q}$    | <code>_kq_z_A</code>    | link variable kq z A to interface material »> macroscopic    | get  | $kg K^{-1} s^{-3}$       | <b>71</b> |
| 106 | $_{h_{N, S}}$     | <code>_h</code>         | link variable h to interface material »> macroscopic         | get  | $kg m^2 mol^{-1} s^{-2}$ | <b>92</b> |

## 9 macroscopic-material

|     | var          | symbol          | documentation  | type | units | eqs |
|-----|--------------|-----------------|--|------|-------|-----|
| 103 | $_{x_{N,S}}$ | $_{\mathbf{x}}$ | link variable x to interface macroscopic »> material | get  |       | 87  |
| 167 | $_{I N}$     | $_{\mathbf{I}}$ | link variable I to interface macroscopic »> material | get  | $A$   | 153 |

## 10 control–macroscopic

|     | var            | symbol                        | documentation   | type | units | eqs                 |
|-----|----------------|-------------------------------|---|------|-------|---------------------|
| 165 | ${}_A^v m$     | <code>_setpoint_vector</code> | link variable setpoint vector to interface control »> macroscopic | get  |       | <a href="#">151</a> |
| 187 | ${}_A^v u$     | <code>_u_vector</code>        | link variable u vector to interface control »> macroscopic        | get  |       | <a href="#">173</a> |
| 164 | ${}_{A,S}^m m$ | <code>_setpoint_matrix</code> | link variable setpoint matrix to interface control »> macroscopic | get  |       | <a href="#">150</a> |

## 11 reactions–macroscopic

|     | var                  | symbol              | documentation   | type | units                       | eqs        |
|-----|----------------------|---------------------|---|------|-----------------------------|------------|
| 122 | $_{NS,K}$            | <code>_N</code>     | link variable N to interface reactions »> macroscopic     | get  |                             | <b>106</b> |
| 137 | $_{\tilde{n}_{N,S}}$ | <code>_nProd</code> | link variable nProd to interface reactions »> macroscopic | get  | $mol\ s^{-1}$               | <b>121</b> |
| 119 | $_{E^a_{N,K}}$       | <code>_Ea</code>    | link variable Ea to interface reactions »> macroscopic    | get  | $kg\ m^2\ mol^{-1}\ s^{-2}$ | <b>103</b> |
| 123 | $_{T_{N,K}}$         | <code>_T_K</code>   | link variable T K to interface reactions »> macroscopic   | get  | $K$                         | <b>107</b> |

## 12 macroscopic-reactions

|     | var                           | symbol          | documentation   | type | units        | eqs |
|-----|-------------------------------|-----------------|---|------|--------------|-----|
| 125 | <code>_c<sub>N,S</sub></code> | <code>_c</code> | link variable c to interface macroscopic »> reactions | get  | $m^{-3} mol$ | 109 |



## 13 macroscopic-control

|     | var                | symbol                 | documentation  | type | units | eqs                 |
|-----|--------------------|------------------------|--|------|-------|---------------------|
| 153 | $_{\bar{T}_N}$     | <code>_T_normed</code> | link variable T normed to interface macroscopic »> control | get  |       | <a href="#">139</a> |
| 152 | $_{\bar{p}_N}$     | <code>_p_normed</code> | link variable p normed to interface macroscopic »> control | get  |       | <a href="#">138</a> |
| 154 | $_{\bar{c}_{N,S}}$ | <code>_c_normed</code> | link variable c normed to interface macroscopic »> control | get  |       | <a href="#">140</a> |

## 14 Equations

## 15 Generic

| no | equation   | documentation                 | layer    |
|----|--|-------------------------------|----------|
| 1  | $1 := \text{Instantiate}(\#, \#)$                                    | numerical one                 | root     |
| 2  | $0 := \text{Instantiate}(\#, \#)$                                    | numerical value zero          | root     |
| 3  | $t^o := \text{Instantiate}(t, 0)$                                    | time zero                     | root     |
| 4  | $t^e := \text{Instantiate}(t, \#)$                                   | time end                      | root     |
| 5  | $\Delta t := \text{Instantiate}(t, \#)$                              | time interval                 | root     |
| 6  | $0.5 := \text{Instantiate}(\#, \#)$                                  | numerical one half            | root     |
| 7  | $\Delta := \text{sign}(t - t^o) - \text{sign}(t - (t^o - \Delta t))$ | pulse of length time interval | root     |
| 8  | $r_{xN} := \text{Instantiate}(\ell_N, \#)$                           | x-direction                   | physical |
| 9  | $r_{yN} := \text{Instantiate}(\ell_N, \#)$                           | y-direction                   | physical |
| 10 | $r_{zN} := \text{Instantiate}(\ell_N, \#)$                           | z-direction                   | physical |
| 11 | $V_N := r_{xN} \cdot r_{yN} \cdot r_{zN}$                            | volume                        | physical |
| 13 | $p_N := \frac{\partial U_N}{\partial V_N}$                           | pressure                      | physical |
| 14 | $\mu_{N,S} := \frac{\partial U_N}{\partial n_{N,S}}$                 | chemical potential            | physical |
| 15 | $H_N := U_N - p_N \cdot V_N$   | Enthalpy                      | physical |
| 16 | $T_N := \frac{\partial U_N}{\partial S_N}$                           | temperature                   | physical |
| 17 | $A_N := U_N - T_N \cdot S_N$   | Helmholts energy              | physical |

*Continued on next page*

| no | equation   | documentation                                | layer    |
|----|--|--|----------|
| 18 | $G_N := U_N + p_N \cdot V_N - T_N \cdot S_N$   | Gibbs free energy                            | physical |
| 19 | $v_{xN} := (t)^{-1} \cdot r_{xN}$  | velocity in x-direction                      | physical |
| 20 | $v_{yN} := (t)^{-1} \cdot r_{yN}$  | velocity in y-direction                      | physical |
| 21 | $v_{zN} := (t)^{-1} \cdot r_{zN}$  | velocity in z-direction                      | physical |
| 24 | $B_N := \mathbf{Instantiate}(S_N, \#)$   | Boltzmann constant                           | physical |
| 25 | $R_N := A^v \cdot B_N$   | Gas constant                                 | physical |
| 26 | $U_N^e := (C_N)^{-1} \cdot U_N$  | electrical potential – voltage               | physical |
| 27 | $C_{pN} := \frac{\partial H_N}{\partial T_N}$  | total heat capacity at constant pressure     | material |
| 28 | $C_{vN} := \frac{\partial U_N}{\partial T_N}$  | total heat capacity at constant volume       | material |
| 29 | $k_{xN}^q := (V_N)^{-1} \cdot C_{pN} \cdot v_{xN}$   | thermal conductivity in x-direction          | material |
| 30 | $k_{yN}^q := (V_N)^{-1} \cdot C_{pN} \cdot v_{yN}$   | thermal conductivity in y-direction          | material |
| 31 | $k_{zN}^q := (V_N)^{-1} \cdot C_{pN} \cdot v_{zN}$   | thermal conductivity in z-direction          | material |
| 32 | $k_{xN,S}^d := (\mu_{N,S})^{-1} \cdot \left( v_{xN} \cdot \left( (V_N)^{-1} \cdot \frac{\partial U_N}{\partial \mu_{N,S}} \right) \right)$ | diffusional mass conductivity in x-direction | material |
| 33 | $k_{yN,S}^d := (\mu_{N,S})^{-1} \cdot \left( v_{yN} \cdot \left( (V_N)^{-1} \cdot \frac{\partial U_N}{\partial \mu_{N,S}} \right) \right)$ | diffusional mass conductivity in y-direction | material |
| 34 | $k_{zN,S}^d := (\mu_{N,S})^{-1} \cdot \left( v_{zN} \cdot \left( (V_N)^{-1} \cdot \frac{\partial U_N}{\partial \mu_{N,S}} \right) \right)$ | diffusional mass conductivity in z-direction | material |
| 35 | $k_{xN}^c := \left( \lambda_S \star (\mu_{N,S})^{-1} \right) \cdot (V_N)^{-1} \cdot \frac{\partial U_N}{\partial p_N} \cdot v_{xN}$        | convective mass conductivity in x-direction  | material |

*Continued on next page*

| no | equation  | documentation                                       | layer    |
|----|---|---|----------|
| 36 | $k_{yN}^c := \left( \lambda_S \star (\mu_{N,S})^{-1} \right) \cdot (V_N)^{-1} \cdot \frac{\partial U_N}{\partial p_N} \cdot v_{yN}$ | convective mass conductivity in y-direction         | material |
| 37 | $k_{zN}^c := \left( \lambda_S \star (\mu_{N,S})^{-1} \right) \cdot (V_N)^{-1} \cdot \frac{\partial U_N}{\partial p_N} \cdot v_{zN}$ | convective mass conductivity in z-direction         | material |
| 38 | $h_{N,S} := H_N \cdot (n_{N,S})^{-1}$   | partial molar enthalpies                            | material |
| 39 | $k_{xA}^c := I_{N,A} \star k_{xN}^c$  | convective mass conductivity in x-direction in arc  | material |
| 40 | $k_{yA}^c := I_{N,A} \star k_{yN}^c$  | convective mass conductivity in y-direction in arc  | material |
| 41 | $k_{zA}^c := I_{N,A} \star k_{zN}^c$  | convective mass conductivity in z-direction in arc  | material |
| 42 | $k_{xA,S}^d := I_{N,A} \star k_{xN,S}^d$  | diffusional mass conductivity in x-direction in arc | material |
| 43 | $k_{yA,S}^d := I_{N,A} \star k_{yN,S}^d$  | diffusional mass conductivity in z-direction in arc | material |
| 44 | $k_{zA,S}^d := I_{N,A} \star k_{zN,S}^d$  | diffusional mass conductivity in z-direction in arc | material |
| 45 | $k_{xA}^q := I_{N,A} \star k_{xN}^q$  | thermal conductivity in x-direction in arc          | material |
| 46 | $k_{yA}^q := I_{N,A} \star k_{yN}^q$  | thermal conductivity in y-direction in arc          | material |
| 47 | $k_{zA}^q := I_{N,A} \star k_{zN}^q$  | thermal conductivity in z-direction in arc          | material |
| 48 | $m_N := \lambda_S \star n_{N,S}$  | mass  | material |

*Continued on next page*

| no | equation   | documentation                             | layer       |
|----|--|---|-------------|
| 49 | $\rho_N := (V_N)^{-1} \cdot m_N$   | density                                   | material    |
| 50 | $v_S := V_N \star (n_{N,S})^{-1}$  | molar volume of species                   | material    |
| 51 | $k_{x,A,S}^{d,Fick} := I_{N,A} \star \left( v_{xN} \cdot \frac{\partial U_N}{\partial \mu_{N,S}} \cdot (n_{N,S})^{-1} \right)$ | Fick's diffusivity in arc and x-direction | material    |
| 52 | $k_{y,A,S}^{d,Fick} := I_{N,A} \star \left( v_{yN} \cdot \frac{\partial U_N}{\partial \mu_{N,S}} \cdot (n_{N,S})^{-1} \right)$ | Fick's diffusivity in arc and y-direction | material    |
| 53 | $k_{z,A,S}^{d,Fick} := I_{N,A} \star \left( v_{zN} \cdot \frac{\partial U_N}{\partial \mu_{N,S}} \cdot (n_{N,S})^{-1} \right)$ | Fick's diffusivity in arc and z-direction | material    |
| 54 | $A_{xyN} := r_{xN} \cdot r_{yN}$   | cross sectional area xy                   | macroscopic |
| 55 | $A_{xzN} := r_{xN} \cdot r_{zN}$   | cross sectional area xz                   | macroscopic |
| 56 | $A_{yzN} := r_{yN} \cdot r_{zN}$   | cross sectional area yz                   | macroscopic |
| 57 | $A_{xyA} := I_{N,A} \star A_{xyN}$   | cross sectional area yz of arc            | macroscopic |
| 58 | $A_{xzA} := I_{N,A} \star A_{xzN}$   | cross sectional area xz of arc            | macroscopic |
| 59 | $A_{yzA} := I_{N,A} \star A_{yzN}$   | cross sectional area yz of arc            | macroscopic |
| 72 | $\hat{q}_{xA} := A_{yzA} \cdot \_k_{xA}^q \cdot (D_{N,A} \star T_N)$   | heat flow in arc and x-direction          | macroscopic |
| 73 | $\dot{q}_N := F_{N,A} \star \hat{q}_{xA}$  | accumulation due to conductive heat flow  | macroscopic |
| 74 | $c_{N,S} := (V_N)^{-1} \cdot n_{N,S}$  | molar concentration                       | macroscopic |
| 75 | $d_A := \mathbf{sign}(D_{N,A} \star p_N)$  | flow direction of convective flow         | macroscopic |
| 76 | $c_{A,S} := (0.5 \cdot (D_{N,A} - d_A \cdot  D_{N,A} )) \star c_{N,S}$   | concentration in convective mass flow     | macroscopic |
| 78 | $\rho_A := I_{N,A} \star \rho_N$   | density of arc material                   | material    |
| 80 | $\dot{V}_A := (\_ \rho_A)^{-1} \cdot \_k_{xA}^c \cdot A_{yzA} \cdot (D_{N,A} \star p_N)$                                       | volumetric flow                           | macroscopic |

Continued on next page

| no | equation  | documentation  | layer       |
|----|---|--|-------------|
| 81 | $\hat{n}_{A,S}^c := \dot{V}_A \cdot c_{A,S}$  | convective mass flow in an arc                       | macroscopic |
| 82 | $\dot{n}_{N,S}^c := F_{N,A} \star \hat{n}_{A,S}^c$                                      | accumulation due to convective mass flow             | macroscopic |
| 83 | $n_N^t := I_S \star n_{N,S}$  | total amount   | macroscopic |
| 84 | $x_{N,S} := (n_N^t)^{-1} \cdot n_{N,S}$   | concentration mole fraction                          | macroscopic |
| 85 | $\hat{n}_{A,S}^d := A_{yzA} \cdot (-_x k_{A,S}^{d,Fick}) \cdot (D_{N,A} \star c_{N,S})$ | diffusional mass flow in arc                         | macroscopic |
| 86 | $\mu_{N,S}^o := \text{Instantiate}(\mu_{N,S}, \#)$                                      | standard chemical potential                          | material    |
| 88 | $\mu_{N,S} := \mu_{N,S}^o + R_N \cdot T_N \cdot \ln(_x x_{N,S})$                        | chemical potential standard model with mole fraction | material    |
| 89 | $\hat{n}_{A,S}^d := A_{yzA} \cdot (-_x k_{A,S}^d) \cdot (D_{N,A} \star \mu_{N,S})$      | diffusional mass flow in arc                         | macroscopic |
| 90 | $\dot{n}_{N,S}^d := F_{N,A} \star \hat{n}_{A,S}^d$                                      | accumulation due to diffusional mass transfer        | macroscopic |
| 93 | $h_{A,S} := I_{N,A} \star h_{N,S}$  | partial molar enthalpies of transport system         | material    |
| 95 | $\hat{H}_A^c := I_S \star (_h h_{A,S} \cdot \hat{n}_{A,S}^c)$                           | enthalpy flow due to convective mass flow            | macroscopic |
| 96 | $\hat{H}_A^d := I_S \star (_h h_{A,S} \cdot \hat{n}_{A,S}^d)$                           | enthalpy flow due to diffusive mass flow             | macroscopic |
| 97 | $\dot{H}_N^c := F_{N,A} \star \hat{H}_A^c$  | enthalpy accumulation due to convective mass flow    | macroscopic |
| 98 | $\dot{H}_N^d := F_{N,A} \star \hat{H}_A^d$  | enthalpy accumulation due to diffusive mass flow     | macroscopic |
| 99 | $T_{N,K} := T_N \cdot P_{N,K}$  | temparature of the nodes with reactions              | reactions   |

Continued on next page

| no  | equation   | documentation   | layer       |
|-----|--|---|-------------|
| 100 | $E_{aN,K} := \mathbf{Instantiate}(R_N . T_{N,K}, \#)$  | Arrhenius activation energy   | reactions   |
| 110 | $c^n_{N,S} := \mathbf{Instantiate}(_c c_{N,S}, \#)$  | norming concentration used in the definition of the species interaction probability | reactions   |
| 112 | $\bar{n}_{N,S} := (c^n_{N,S})^{-1} . _c c_{N,S}$   | normed concentration  | reactions   |
| 113 | $\bar{n}_{N,S,K} := P_{N,K} . \bar{n}_{N,S}$   | normed concentration – context node and conversion                                  | reactions   |
| 115 | $\phi_{N,K} := \prod_S \bar{n}_{N,S,K}^{(N_{S,K})}$  | probability for the species to meet to undergo reaction                             | reactions   |
| 118 | $K^o_K := \mathbf{Instantiate}(I_S \star (P_{N,K} \star ((t)^{-1} . (V_N)^{-1} . n_{N,S})), \#)$ | Arrhenius frequency factor – a strange construction                                 | reactions   |
| 119 | $K_{N,K} := K^o_K . \mathbf{exp}((-E_{aN,K}) . (R_N . T_{N,K})^{-1})$                            | reaction"constant   | reactions   |
| 120 | $\tilde{n}_{N,S} := V_N . (N_{S,K} \star (K_{N,K} . \phi_{N,K}))$                                | production term for differential component mass balance                             | reactions   |
| 122 | $\dot{n}^p_{N,S} := _n \tilde{n}_{N,S}$  | production term   | macroscopic |
| 123 | $\dot{n}_{N,S} := \dot{n}^c_{N,S} + \dot{n}^d_{N,S} + \dot{n}^p_{N,S}$                           | differential species balance  | macroscopic |
| 125 | $\hat{w}_A := \mathbf{Instantiate}(\hat{H}^c_A, \#)$   | just an numerical work flow term – as a starter                                     | macroscopic |
| 126 | $\dot{w}_N := F_{N,A} \star \hat{w}_A$   | enthalpy accumulation due to work flows   | macroscopic |
| 127 | $\dot{H}_N := \dot{H}^c_N + \dot{H}^d_N + \dot{q}_N + \dot{w}_N$                                 | differential enthalpy balance   | macroscopic |
| 128 | $H_N := \int_{t^o}^{t^e} \dot{H}_N dt + H^o_N$   | Enthalpy  | macroscopic |

*Continued on next page*

| no  | equation   | documentation                       | layer       |
|-----|--|-------------------------------------|-------------|
| 129 | $n_{N,S} := \int_{t^o}^{t^e} \dot{n}_{N,S} dt + n_{N,S}^o$ | fundamental state - molar mass      | macroscopic |
| 130 | $H_N^o := \text{Instantiate}(H_N, \#)$                     | initial enthalpy                    | macroscopic |
| 131 | $n_{N,S}^o := \text{Instantiate}(n_{N,S}, \#)$             | initial species masses              | macroscopic |
| 132 | $T_N^o := \text{Instantiate}(T_N, \#)$                     | norming temperature                 | macroscopic |
| 133 | $p_N^o := \text{Instantiate}(p_N, \#)$                     | normed pressure                     | macroscopic |
| 134 | $c_{N,S}^o := \text{Instantiate}(c_{N,S}, \#)$             | norming concentration               | macroscopic |
| 135 | $\bar{T}_N^o := T_N \cdot (T_N^o)^{-1}$                    | normed temperature                  | macroscopic |
| 136 | $\bar{p}_N^o := (p_N)^{-1} \cdot p_N$                      | normed pressure                     | macroscopic |
| 137 | $\bar{c}_{N,S}^o := (c_{N,S}^o)^{-1} \cdot c_{N,S}$        | normed concentration                | macroscopic |
| 141 | $m_A := F_{N,A} \star \bar{T}_N$                           | normed measurements of temperatures | control     |
| 142 | $m_A := F_{N,A} \star \bar{p}_N$                           | normed measurements of pressures    | control     |
| 143 | $m_{A,S} := F_{N,A} \star \bar{c}_{N,S}$                   | normed measurment of concentration  | control     |
| 144 | $m^{v\star}_A := \text{Instantiate}(m_A, \#)$              | setpoint for measurement vector     | control     |
| 145 | $m^{m\star}_{A,S} := \text{Instantiate}(m_{A,S}, \#)$      | setpoiint for measurment matrix     | control     |
| 146 | $e^v_A := m^{v\star}_A - m_A$                              | output error vector                 | control     |
| 147 | $e^m_{A,S} := m^{m\star}_{A,S} - m_{A,S}$                  | output error matrix                 | control     |
| 148 | $u^v_A := P \cdot e^v_A$                                   | control ouput vector                | control     |
| 149 | $u^m_{A,S} := P \cdot e^m_{A,S}$                           | control output matrix               | control     |

*Continued on next page*



| no  | equation   | documentation  | layer       |
|-----|--|--|-------------|
| 152 | $I_N := \frac{dC_N}{dt}$   | electric current definition  | macroscopic |
| 154 | $R_N^e := (I_N)^{-1} \cdot U_N^e$  | electrical resistance  | material    |
| 155 | $k^{e,x}_N := (R_N^e)^{-1} \cdot (S_S \star \_x_{N,S})$  | electrical conductivity – a simple model being a function of a selected set of species | material    |
| 156 | $cp_N := C_{pN} \cdot (m_N)^{-1}$  | specific heat capacity at constant pressure  | material    |
| 158 | $m_N := \_ \lambda_S \star n_{N,S}$  | mass   | macroscopic |
| 159 | $C_{pN} := m_N \cdot \_ c_{pN}$  | total heat capacity  | macroscopic |
| 160 | $T_N^{ref} := \mathbf{Instantiate}(T_N, \#)$   | reference temperature  | macroscopic |
| 161 | $H_N := C_{pN} \cdot (T_N - T_N^{ref})$  | Enthalpy   | macroscopic |
| 162 | $T_N := \mathbf{Root}(H_N)$  | temperature  | macroscopic |
| 164 | $\dot{x}_D := A_{N,D} \star x_N + B_{A,D} \star m_A$   | differential controller state  | control     |
| 165 | $x_N := \int_{t^o}^{t^e} I_{N,D} \star \dot{x}_D \, dt + x_N^o$  | controller state   | control     |
| 166 | $x_N^o := \mathbf{Instantiate}(x_N, \#)$   | initial controller state   | control     |
| 169 | $t_{sA} := \mathbf{Instantiate}(I_A \cdot t, \#)$  | switching times  | control     |
| 170 | $u_A^v := 0.5 \cdot (I_A \cdot 1 - \mathbf{sign}((I_A \cdot t) - t_{sA}))$   | control output vector – switches   | control     |
| 171 | $k^{valve}_A := \mathbf{Instantiate}(\dot{V}_A, \#)$   | valve constant – pressure difference must be dimensionless                             | macroscopic |
| 172 | $\dot{V}_A := \_ u_A^v \cdot k^{valve}_A \cdot \mathbf{sqrt}\left(\left(D_{N,A} \star \left(p_N \cdot (p_N^o)^{-1}\right)\right)\right)$ | volumetric flow  | macroscopic |

Continued on next page

| no  | equation  | documentation                             | layer       |
|-----|---|---|-------------|
| 174 | $\hat{m}_A := \_ \rho_A \cdot \dot{V}_A$  | mass flow rate                            | macroscopic |
| 175 | $\dot{V}_A := (I_{N,A} \star v_{xN}) \cdot A_{yzA}$   | volumetric flow                           | macroscopic |
| 176 | $h_N := \mathbf{Instantiate}(\ell_N, \#)$   | height                                    | physical    |
| 177 | $v_{xA} := I_{N,A} \star v_{xN}$  | velocity in arc                           | macroscopic |
| 179 | $height_{AA} := I_{N,A} \star h_N$  | height in arc node                        | macroscopic |
| 180 | $fE_{potential}_A := \hat{m}_A \cdot g \cdot height_{AA}$   | flow of potential energy                  | macroscopic |
| 181 | $length_{pipe}_A := I_{N,A} \star \ell_N$   | length of pipe                            | macroscopic |
| 182 | $friction_{coefficient}_A := \mathbf{Instantiate}(fE_{potential}_A \cdot (length_{pipe}_A)^{-1}, \#)$ | friction factor for linear friction model | macroscopic |
| 184 | $\hat{E}^k_A := \hat{m}_A \cdot v_{xA} \cdot v_{xA}$  | flow of kinetic energy                    | macroscopic |
| 185 | $\hat{w}^f_A := (-friction_{coefficient}_A) \cdot length_{pipe}_A$                                    | work flow due to linear friction          | macroscopic |
| 186 | $aE_{mechanical}_A := \hat{E}^k_A + fE_{potential}_A + \hat{w}^f_A$                                   | accumulation of mechanical energy         | macroscopic |

## 16 Interface Link Equation

| no | equation                                       | documentation      | layer                   |
|----|--|--------------------|-------------------------|
| 22 | $_{-}\lambda_S := \lambda_S$                   | interface equation | material -> macroscopic |
| 60 | $_{-}k_{xA}^c := k_{xA}^c$                     | interface equation | material -> macroscopic |
| 61 | $_{-}k_{yA}^c := k_{yA}^c$                     | interface equation | material -> macroscopic |
| 62 | $_{-}k_{zA}^c := k_{zA}^c$                     | interface equation | material -> macroscopic |
| 63 | $_{-}k_{xA,S}^d := k_{xA,S}^d$                 | interface equation | material -> macroscopic |
| 64 | $_{-}k_{x,A,S}^{d,Fick} := k_{x,A,S}^{d,Fick}$ | interface equation | material -> macroscopic |
| 65 | $_{-}k_{y,A,S}^{d,Fick} := k_{y,A,S}^{d,Fick}$ | interface equation | material -> macroscopic |
| 66 | $_{-}k_{yA,S}^d := k_{yA,S}^d$                 | interface equation | material -> macroscopic |
| 67 | $_{-}k_{zA,S}^d := k_{zA,S}^d$                 | interface equation | material -> macroscopic |
| 68 | $_{-}k_{z,A,S}^{d,Fick} := k_{z,A,S}^{d,Fick}$ | interface equation | material -> macroscopic |
| 69 | $_{-}k_{xA}^q := k_{xA}^q$                     | interface equation | material -> macroscopic |

*Continued on next page*

| no  | equation                               | documentation      | layer                               |
|-----|--|--------------------|-------------------------------------|
| 70  | $\_k_{yA}^q := k_{yA}^q$               | interface equation | material $\rightarrow$ macroscopic  |
| 71  | $\_k_{zA}^q := k_{zA}^q$               | interface equation | material $\rightarrow$ macroscopic  |
| 77  | $\_\rho_N := \rho_N$                   | interface equation | material $\rightarrow$ macroscopic  |
| 79  | $\_\rho_A := \rho_A$                   | interface equation | material $\rightarrow$ macroscopic  |
| 87  | $\_x_{N,S} := x_{N,S}$                 | interface equation | macroscopic $\rightarrow$ material  |
| 92  | $\_h_{N,S} := h_{N,S}$                 | interface equation | material $\rightarrow$ macroscopic  |
| 94  | $\_h_{A,S} := h_{A,S}$                 | interface equation | material $\rightarrow$ macroscopic  |
| 103 | $\_E^a_{N,K} := E_{aN,K}$              | interface equation | reactions $\rightarrow$ macroscopic |
| 106 | $\_N_{S,K} := N_{S,K}$                 | interface equation | reactions $\rightarrow$ macroscopic |
| 107 | $\_T_{N,K} := T_{N,K}$                 | interface equation | reactions $\rightarrow$ macroscopic |
| 109 | $\_c_{N,S} := c_{N,S}$                 | interface equation | macroscopic $\rightarrow$ reactions |
| 121 | $\_\tilde{n}_{N,S} := \tilde{n}_{N,S}$ | interface equation | reactions $\rightarrow$ macroscopic |

*Continued on next page*

| no  | equation                              | documentation      | layer                  |
|-----|---------------------------------------|--------------------|------------------------|
| 138 | $_{\bar{p}N} := \bar{p}^o_N$          | interface equation | macroscopic control →  |
| 139 | $_{\bar{T}N} := \bar{T}^o_N$          | interface equation | macroscopic control →  |
| 140 | $_{\bar{c}_{N,S}} := \bar{c}^o_{N,S}$ | interface equation | macroscopic control →  |
| 150 | $_{m^m_{A,S}} := m^{m\star}_{A,S}$    | interface equation | control → macroscopic  |
| 151 | $_{m^v_A} := m^{v\star}_A$            | interface equation | control → macroscopic  |
| 153 | $_{IN} := I_N$                        | interface equation | macroscopic material → |
| 157 | $_{c_{pN}} := c_{pN}$                 | interface equation | material → macroscopic |
| 173 | $_{u^v_A} := u^v_A$                   | interface equation | control → macroscopic  |