1 Variables

2 root

	var	symbol	documentation	type	units	eqs
10	$F_{N,A}$	`F`	basic directed graph incidence matrix	network		
48	$I_{NAN,A}$	`I_N_A`	project node on arc	projection		
7	Δt	`t_interval`	time interval	frame	s	5
9	Δ	`pulse`	pulse of length time interval	frame		7
4	t	`t`	time	frame	s	
5	t^o	`to`	time zero	frame	s	3
6	t^e	`te`	time end	frame	s	4
3	0	`zero`	numerical value zero	constant		2
8	0.5	`onehalf`	numerical one half	constant		6
1	#	`value`	numerical value	constant		
2	1	`one`	numerical one	constant		1

3 physical

	var	symbol	documentation	type	units	eqs
14	r_{zN}	`r_z`	z-direction	frame	m	10
11	ℓ_N	`l`	length	frame	m	
12	r_{xN}	`r_x`	x-direction	frame	m	8
13	r_{yN}	`r_y`	y-direction	frame	m	9
17	S_N	`S`	fundamental state - entropy	state	$kg\,m^2\,K^{-1}\,s^{-2}$	
23	A_N	`A`	Helmholts energy	state	$kg\,m^2\,s^{-2}$	17
16	U_N	`U`	fundamental state - internal energy	state	$kg\,m^2\,s^{-2}$	
24	G_N	`G`	Gibbs free energy	state	$kg\,m^2\,s^{-2}$	18
22	H_N	`H`	Enthalpy	state	$kg\,m^2\,s^{-2}$	15
18	$n_{N,S}$	`n`	fundamental state - molar mass	state	mol	
15	V_N	`V`	fundamental state - volume	state	m^3	11
25	C_N	`C`	fundamental state - charge	state	$A\,s$	
33	B_N	`Boltz`	Boltzmann constant	constant	$kg\,m^2\,K^{-1}\,s^{-2}$	24
32	A^v	`Av`	Avogadro number	constant	mol^{-1}	
34	R_N	`R`	Gas constant	constant	$kg\,m^2\,mol^{-1}\,K^{-1}\,s^{-2}$	25
21	$\mu_{N,S}$	`chemPot`	chemical potential	effort	$kg\,m^2\,mol^{-1}\,s^{-2}$	14
19	T_N	`T`	temperature	effort	K	16
20	p_N	`p`	pressure	effort	$kg\,m^{-1}\,s^{-2}$	13
35	${U^e}_N$	`Ue`	electrical potential – voltage	effort	$kg\,m^2\,A^{-1}s^{-3}$	26
27	v_{xN}	`v_x`	velocity in x-direction	secondaryState	ms^{-1}	19
29	v_{zN}	`v_z`	velocity in z-direction	secondaryState	ms^{-1}	21
28	v_{yN}	`v_y`	velocity in y-direction	secondaryState	ms^{-1}	20

4 material

	var	symbol	documentation	type	units	eqs
46	k^c_{zN}	kc_z	convective mass conductivity in z-direction	property	$m^{-1}\,s$	37
44	k^c_{xN}	kc_x	convective mass conductivity in x-direction	property	$m^{-1}\,s$	35
53	$k^d_{yA,S}$	kd_y_A	diffusional mass conductivity in y-direction in arc	property	$kg^{-1}\,m^{-4}\,mol^2\,s$	43
37	C_{vN}	Cv	total heat capacity at constant volume	property	$kg\,m^2\,K^{-1}\,s^{-2}$	28
43	$k^d_{zN,S}$	kd_z	diffusional mass conductivity in z-direction	property	$kg^{-1}\,m^{-4}\,mol^2\,s$	34
41	$k^d_{xN,S}$	kd_x	diffusional mass conductivity in x-direction	property	$kg^{-1}\,m^{-4}\,mol^2\,s$	32
47	$h_{N,S}$	h	partial molar enthalpies	property	$kg\,m^2\,mol^{-1}\,s^{-2}$	38
54	$k^d_{zA,S}$	kd_z_A	diffusional mass conductivity in z-direction in arc	property	$kg^{-1}\,m^{-4}\,mol^2\,s$	44
36	C_{pN}	Cp	total heat capacity at constant pressure	property	$kg\,m^2\,K^{-1}\,s^{-2}$	27
45	k^c_{yN}	kc_y	convective mass conductivity in y-direction	property	$m^{-1}\,s$	36
55	k^q_{xA}	kq_x_A	thermal conductivity in x-direction in arc	property	$kg\,K^{-1}\,s^{-3}$	45
26	λ_S	Mm	species' molecular mass	property	$kg\,mol^{-1}$	
39	k^q_{yN}	kq_y	thermal conductivity in y-direction	property	$kg\,K^{-1}\,s^{-3}$	30
40	k^q_{zN}	kq_z	thermal conductivity in z-direction	property	$kg\,K^{-1}\,s^{-3}$	31
52	$k^d_{xA,S}$	kd_x_A	diffusional mass conductivity in x-direction in arc	property	$kg^{-1}\,m^{-4}\,mol^2\,s$	42
49	k^c_{xA}	kc_x_A	convective mass conductivity in x-direction in arc	property	$m^{-1}\,s$	39
56	k^q_{yA}	kq_y_A	thermal conductivity in y-direction in arc	property	$kg\,K^{-1}\,s^{-3}$	46
57	k^q_{zA}	kq_z_A	thermal conductivity in z-direction in arc	property	$kg\,K^{-1}\,s^{-3}$	47
42	$k^d_{yN,S}$	kd_y	diffusional mass conductivity in z-direction	property	$kg^{-1}\,m^{-4}\,mol^2\,s$	33
38	k^q_{xN}	kq_x	thermal conductivity in x-direction	property	$kg\,K^{-1}\,s^{-3}$	29
51	k^c_{zA}	kc_z_A	convective mass conductivity in z-direction in arc	property	$m^{-1}\,s$	41
50	k^c_{yA}	kc_y_A	convective mass conductivity in y-direction in arc	property	$m^{-1}\,s$	40

5 macroscopic

	var	symbol	documentation	type	units	eqs
31	m_N	`m`	mass	secondaryState	kg	23

6 material–macroscopic

	var	symbol	documentation	type	units	eqs
30	$\_\lambda_S$	`_Mm`	link variable Mm to interface material »> macroscopic	get	$kg\,mol^{-1}$	22

7 Equations

8 Generic

no	equation	documentation	layer
1	$1 := \text{Instantiate}(\#, \#)$	numerical one	root
2	$0 := \text{Instantiate}(\#, \#)$	numerical value zero	root
3	$t^o := \text{Instantiate}(t, 0)$	time zero	root
4	$t^e := \text{Instantiate}(t, \#)$	time end	root
5	$\Delta t := \text{Instantiate}(t, \#)$	time interval	root
6	$0.5 := \text{Instantiate}(\#, \#)$	numerical one half	root
7	$\Delta := \text{sign}\,(t - t^o) - \text{sign}\,(t - (t^o - \Delta t))$	pulse of length time interval	root
8	$r_{xN} := \text{Instantiate}(\ell_N, \#)$	x-direction	physical
9	$r_{yN} := \text{Instantiate}(\ell_N, \#)$	y-direction	physical
10	$r_{zN} := \text{Instantiate}(\ell_N, \#)$	z-direction	physical
11	$V_N := r_{xN} \,.\, r_{yN} \,.\, r_{zN}$	volume	physical
13	$p_N := \frac{\partial U_N}{\partial V_N}$	pressure	physical
14	$\mu_{N,S} := \frac{\partial U_N}{\partial n_{N,S}}$	chemical potential	physical
15	$H_N := U_N - p_N \,.\, V_N$	Enthalpy	physical
16	$T_N := \frac{\partial U_N}{\partial S_N}$	temperature	physical
17	$A_N := U_N - T_N \,.\, S_N$	Helmholts energy	physical

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no	equation	documentation	layer
18	$G_N := U_N + p_N \,.\, V_N - T_N \,.\, S_N$	Gibbs free energy	physical
19	$v_{xN} := (t)^{-1} \,.\, r_{xN}$	velocity in x-direction	physical
20	$v_{yN} := (t)^{-1} \,.\, r_{yN}$	velocity in y-direction	physical
21	$v_{zN} := (t)^{-1} \,.\, r_{zN}$	velocity in z-direction	physical
23	$m_N := \_\lambda_S \star n_{N,S}$	mass	macroscopic
24	$B_N := \text{Instantiate}(S_N, \#)$	Boltzmann constant	physical
25	$R_N := A^v \,.\, B_N$	Gas constant	physical
26	$U^e{}_N := (C_N)^{-1} \,.\, U_N$	electrical potential – voltage	physical
27	$C_{pN} := \frac{\partial H_N}{\partial T_N}$	total heat capacity at constant pressure	material
28	$C_{vN} := \frac{\partial U_N}{\partial T_N}$	total heat capacity at constant volume	material
29	$k^q_{xN} := (V_N)^{-1} \,.\, C_{pN} \,.\, v_{xN}$	thermal conductivity in x-direction	material
30	$k^q_{yN} := (V_N)^{-1} \,.\, C_{pN} \,.\, v_{yN}$	thermal conductivity in y-direction	material
31	$k^q_{zN} := (V_N)^{-1} \,.\, C_{pN} \,.\, v_{zN}$	thermal conductivity in z-direction	material
32	$k^d_{xN,S} := (\mu_{N,S})^{-1} \,.\, \left(v_{xN} \,.\, \left((V_N)^{-1} \,.\, \frac{\partial U_N}{\partial \mu_{N,S}}\right)\right)$	diffusional mass conductivity in x-direction	material
33	$k^d_{yN,S} := (\mu_{N,S})^{-1} \,.\, \left(v_{yN} \,.\, \left((V_N)^{-1} \,.\, \frac{\partial U_N}{\partial \mu_{N,S}}\right)\right)$	diffusional mass conductivity in y-direction	material
34	$k^d_{zN,S} := (\mu_{N,S})^{-1} \,.\, \left(v_{zN} \,.\, \left((V_N)^{-1} \,.\, \frac{\partial U_N}{\partial \mu_{N,S}}\right)\right)$	diffusional mass conductivity in z-direction	material

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no	equation	documentation	layer
35	$k^c_{xN} := \left(\lambda_S \star (\mu_{N,S})^{-1}\right) . (V_N)^{-1} . \frac{\partial U_N}{\partial p_N} . v_{xN}$	convective mass conductivity in x-direction	material
36	$k^c_{yN} := \left(\lambda_S \star (\mu_{N,S})^{-1}\right) . (V_N)^{-1} . \frac{\partial U_N}{\partial p_N} . v_{yN}$	convective mass conductivity in y-direction	material
37	$k^c_{zN} := \left(\lambda_S \star (\mu_{N,S})^{-1}\right) . (V_N)^{-1} . \frac{\partial U_N}{\partial p_N} . v_{zN}$	convective mass conductivity in z-direction	material
38	$h_{N,S} := H_N . (n_{N,S})^{-1}$	partial molar enthalpies	material
39	$k^c_{xA} := I_{NAN,A} \star k^c_{xN}$	convective mass conductivity in x-direction in arc	material
40	$k^c_{yA} := I_{NAN,A} \star k^c_{yN}$	convective mass conductivity in y-direction in arc	material
41	$k^c_{zA} := I_{NAN,A} \star k^c_{zN}$	convective mass conductivity in z-direction in arc	material
42	$k^d_{xA,S} := I_{NAN,A} \star k^d_{xN,S}$	diffusional mass conductivity in x-direction in arc	material
43	$k^d_{yA,S} := I_{NAN,A} \star k^d_{yN,S}$	diffusional mass conductivity in z-direction in arc	material
44	$k^d_{zA,S} := I_{NAN,A} \star k^d_{zN,S}$	diffusional mass conductivity in z-direction in arc	material
45	$k^q_{xA} := I_{NAN,A} \star k^q_{xN}$	thermal conductivity in x-direction in arc	material
46	$k^q_{yA} := I_{NAN,A} \star k^q_{yN}$	thermal conductivity in y-direction in arc	material

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no	equation	documentation	layer
47	$k_{zA}^{q} := I_{NAN,A} \star k_{zN}^{q}$	thermal conductivity in z-direction in arc	material

9 Interface Link Equation

no	equation	documentation	layer
22	$\_\lambda_S := \lambda_S$	interface equation	material –> macroscopic