

# 1 Variables

## 2 root

|    | var        | symbol            | documentation                         | type       | units    | eqs      |
|----|------------|-------------------|---------------------------------------|------------|----------|----------|
| 10 | $F_{N,A}$  | <b>F</b>          | basic directed graph incidence matrix | network    |          |          |
| 97 | $I_A$      | <b>I_A</b>        | vector of ones of length arcs         | projection |          |          |
| 96 | $I_N$      | <b>I_N</b>        | vector of ones of length nodes        | projection |          |          |
| 48 | $I_{N,A}$  | <b>I_N_A</b>      | project node on arc                   | projection |          |          |
| 4  | $t$        | <b>t</b>          | time                                  | frame      | <i>s</i> |          |
| 5  | $t^o$      | <b>to</b>         | time zero                             | frame      | <i>s</i> | <b>3</b> |
| 6  | $t^e$      | <b>te</b>         | time end                              | frame      | <i>s</i> | <b>4</b> |
| 7  | $\Delta t$ | <b>t_interval</b> | time interval                         | frame      | <i>s</i> | <b>5</b> |
| 9  | $\Delta$   | <b>pulse</b>      | pulse of length time interval         | frame      |          | <b>7</b> |
| 8  | 0.5        | <b>onehalf</b>    | numerical one half                    | constant   |          | <b>6</b> |
| 1  | #          | <b>value</b>      | numerical value                       | constant   |          |          |
| 3  | 0          | <b>zero</b>       | numerical value zero                  | constant   |          | <b>2</b> |
| 2  | 1          | <b>one</b>        | numerical one                         | constant   |          | <b>1</b> |

### 3 physical

|    | var         | symbol  | documentation                       | type           | units                               | eqs       |
|----|-------------|---------|-------------------------------------|----------------|-------------------------------------|-----------|
| 98 | $I_S$       | I_S     | vector of ones of length sepecies   | projection     |                                     |           |
| 13 | $r_{yN}$    | r_y     | y-direction                         | frame          | $m$                                 | 9         |
| 11 | $\ell_N$    | l       | length                              | frame          | $m$                                 |           |
| 12 | $r_{xN}$    | r_x     | x-direction                         | frame          | $m$                                 | 8         |
| 14 | $r_{zN}$    | r_z     | z-direction                         | frame          | $m$                                 | 10        |
| 15 | $V_N$       | V       | fundamental state - volume          | state          | $m^3$                               | 11        |
| 23 | $A_N$       | A       | Helmholts energy                    | state          | $kg\,m^2\,s^{-2}$                   | 17        |
| 17 | $S_N$       | S       | fundamental state - entropy         | state          | $kg\,m^2\,K^{-1}\,s^{-2}$           |           |
| 22 | $H_N$       | H       | Enthalpy                            | state          | $kg\,m^2\,s^{-2}$                   | 15<br>128 |
| 18 | $n_{N,S}$   | n       | fundamental state - molar mass      | state          | $mol$                               | 129       |
| 24 | $G_N$       | G       | Gibbs free energy                   | state          | $kg\,m^2\,s^{-2}$                   | 18        |
| 25 | $C_N$       | C       | fundamental state - charge          | state          | $A\,s$                              |           |
| 16 | $U_N$       | U       | fundamental state - internal energy | state          | $kg\,m^2\,s^{-2}$                   |           |
| 32 | $A^v$       | Av      | Avogadro number                     | constant       | $mol^{-1}$                          |           |
| 34 | $R_N$       | R       | Gas constant                        | constant       | $kg\,m^2\,mol^{-1}\,K^{-1}\,s^{-2}$ | 25        |
| 33 | $B_N$       | Boltz   | Boltzmann constant                  | constant       | $kg\,m^2\,K^{-1}\,s^{-2}$           | 24        |
| 21 | $\mu_{N,S}$ | chemPot | chemical potential                  | effort         | $kg\,m^2\,mol^{-1}\,s^{-2}$         | 14 88     |
| 19 | $T_N$       | T       | temperature                         | effort         | $K$                                 | 16        |
| 20 | $p_N$       | p       | pressure                            | effort         | $kg\,m^{-1}\,s^{-2}$                | 13        |
| 35 | $U^e_N$     | Ue      | electrical potential – voltage      | effort         | $kg\,m^2\,A^{-1}\,s^{-3}$           | 26        |
| 29 | $v_{zN}$    | v_z     | velocity in z-direction             | secondaryState | $ms^{-1}$                           | 21        |
| 27 | $v_{xN}$    | v_x     | velocity in x-direction             | secondaryState | $ms^{-1}$                           | 19        |

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|    | var      | symbol     | documentation           | type           | units     | eqs |
|----|----------|------------|-------------------------|----------------|-----------|-----|
| 28 | $v_{yN}$ | <b>v_y</b> | velocity in y-direction | secondaryState | $ms^{-1}$ | 20  |

## 4 reactions

|     | var                | symbol                 | documentation   | type           | units                       | eqs |
|-----|--------------------|------------------------|---|----------------|-----------------------------|-----|
| 113 | $P_{N,CS}$         | P_N_K                  | what node has what reaction   | projection     |                             |     |
| 114 | $T_{N,CS}$         | T_K                    | temparature of the nodes with reactions   | effort         | $K$                         | 99  |
| 129 | $\bar{n}_{N,S,CS}$ | cn_NK                  | normed concentration – context node and conversion                                  | secondaryState |                             | 113 |
| 128 | $\bar{n}_{N,S}$    | cn                     | normed concentration  | secondaryState |                             | 112 |
| 115 | $E_{aN,CS}$        | Ea                     | Arrhenius activation energy   | properties     | $kg\,m^2\,mol^{-1}\,s^{-2}$ | 100 |
| 131 | $\phi_{N,CS}$      | interactionProbability | probability for the species to meet to undergo reaction                             | properties     |                             | 115 |
| 118 | $N_{S,CS}$         | N                      | stoichiometric matrix   | properties     |                             |     |
| 134 | $K^o_{CS}$         | Ko                     | Arrhenius frequency factor – a strange construction                                 | properties     | $m^{-3}\,mol\,s^{-1}$       | 118 |
| 135 | $K_{N,CS}$         | K                      | reaction"constant   | properties     | $m^{-3}\,mol\,s^{-1}$       | 119 |
| 126 | $c^n_{N,S}$        | c_norming              | norming concentration used in the definition of the species interaction probability | properties     | $m^{-3}\,mol$               | 110 |
| 136 | $\tilde{n}_{N,S}$  | nProd                  | production term for differential component mass balance                             | conversion     | $mol\,s^{-1}$               | 120 |

## 5 material

|     | var                    | symbol    | documentation                                       | type     | units                       | eqs |
|-----|------------------------|-----------|---|----------|-----------------------------|-----|
| 38  | $k_{xN}^q$             | kq_x      | thermal conductivity in x-direction                 | property | $kg\ K^{-1}\ s^{-3}$        | 29  |
| 60  | $v_S$                  | v         | molar volume of species                             | property | $m^3\ mol^{-1}$             | 50  |
| 55  | $k_{xA}^q$             | kq_x_A    | thermal conductivity in x-direction in arc          | property | $kg\ K^{-1}\ s^{-3}$        | 45  |
| 40  | $k_{zN}^q$             | kq_z      | thermal conductivity in z-direction                 | property | $kg\ K^{-1}\ s^{-3}$        | 31  |
| 62  | $k_y^{d,Fick}{}_{A,S}$ | kd_y_Fick | Fick's diffusivity in arc and y-direction           | property | $ms^{-1}$                   | 52  |
| 36  | $C_{pN}$               | Cp        | total heat capacity at constant pressure            | property | $kg\ m^2\ K^{-1}\ s^{-2}$   | 27  |
| 56  | $k_{yA}^q$             | kq_y_A    | thermal conductivity in y-direction in arc          | property | $kg\ K^{-1}\ s^{-3}$        | 46  |
| 49  | $k_{xA}^c$             | kc_x_A    | convective mass conductivity in x-direction in arc  | property | $m^{-1}\ s$                 | 39  |
| 58  | $m_N$                  | m         | mass  | property | $kg$                        | 48  |
| 107 | $h_{AA,S}$             | h_A       | partial molar enthalpies of transport system        | property | $kg\ m^2\ mol^{-1}\ s^{-2}$ | 93  |
| 54  | $k_{zA,S}^d$           | kd_z_A    | diffusional mass conductivity in z-direction in arc | property | $kg^{-1}\ m^{-4}\ mol^2\ s$ | 44  |
| 51  | $k_{zA}^c$             | kc_z_A    | convective mass conductivity in z-direction in arc  | property | $m^{-1}\ s$                 | 41  |
| 26  | $\lambda_S$            | Mm        | species' molecular mass                             | property | $kg\ mol^{-1}$              |     |
| 37  | $C_{vN}$               | Cv        | total heat capacity at constant volume              | property | $kg\ m^2\ K^{-1}\ s^{-2}$   | 28  |
| 63  | $k_z^{d,Fick}{}_{A,S}$ | kd_z_Fick | Fick's diffusivity in arc and z-direction           | property | $ms^{-1}$                   | 53  |
| 47  | $h_{N,S}$              | h         | partial molar enthalpies                            | property | $kg\ m^2\ mol^{-1}\ s^{-2}$ | 38  |
| 44  | $k_{xN}^c$             | kc_x      | convective mass conductivity in x-direction         | property | $m^{-1}\ s$                 | 35  |
| 61  | $k_x^{d,Fick}{}_{A,S}$ | kd_x_Fick | Fick's diffusivity in arc and x-direction           | property | $ms^{-1}$                   | 51  |
| 39  | $k_{yN}^q$             | kq_y      | thermal conductivity in y-direction                 | property | $kg\ K^{-1}\ s^{-3}$        | 30  |
| 43  | $k_{zN,S}^d$           | kd_z      | diffusional mass conductivity in z-direction        | property | $kg^{-1}\ m^{-4}\ mol^2\ s$ | 34  |
| 42  | $k_{yN,S}^d$           | kd_y      | diffusional mass conductivity in z-direction        | property | $kg^{-1}\ m^{-4}\ mol^2\ s$ | 33  |
| 50  | $k_{yA}^c$             | kc_y_A    | convective mass conductivity in y-direction in arc  | property | $m^{-1}\ s$                 | 40  |
| 46  | $k_{zN}^c$             | kc_z      | convective mass conductivity in z-direction         | property | $m^{-1}\ s$                 | 37  |

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|     | var           | symbol           | documentation                                       | type     | units                    | eqs       |
|-----|---------------|------------------|---|----------|--------------------------|-----------|
| 45  | $k_{yN}^c$    | <b>kc_y</b>      | convective mass conductivity in y-direction         | property | $m^{-1} s$               | <b>36</b> |
| 89  | $\rho_A$      | <b>density_A</b> | density of arc material                             | property | $kg m^{-3}$              | <b>78</b> |
| 53  | $k_{yA,S}^d$  | <b>kd_y_A</b>    | diffusional mass conductivity in y-direction in arc | property | $kg^{-1} m^{-4} mol^2 s$ | <b>43</b> |
| 52  | $k_{xA,S}^d$  | <b>kd_x_A</b>    | diffusional mass conductivity in x-direction in arc | property | $kg^{-1} m^{-4} mol^2 s$ | <b>42</b> |
| 59  | $\rho_N$      | <b>density</b>   | density   | property | $kg m^{-3}$              | <b>49</b> |
| 57  | $k_z^q A$     | <b>kq_z_A</b>    | thermal conductivity in z-direction in arc          | property | $kg K^{-1} s^{-3}$       | <b>47</b> |
| 41  | $k_{xN,S}^d$  | <b>kd_x</b>      | diffusional mass conductivity in x-direction        | property | $kg^{-1} m^{-4} mol^2 s$ | <b>32</b> |
| 102 | $\mu_{N,S}^o$ | <b>chemPot_o</b> | standard chemical potential                         | effort   | $kg m^2 mol^{-1} s^{-2}$ | <b>86</b> |

## 6 macroscopic

|     | var               | symbol | documentation                                     | type               | units             | eqs   |
|-----|-------------------|--------|---|--------------------|-------------------|-------|
| 142 | $\dot{w}_N$       | aw     | enthalpy accumulation due to work flows           | transport          | $kg\,m^2\,s^{-3}$ | 126   |
| 110 | $\hat{H}^d_A$     | fHd    | enthalpy flow due to diffusive mass flow          | transport          | $kg\,m^2\,s^{-3}$ | 96    |
| 104 | $\dot{n}^d_{N,S}$ | and    | accumulation due to diffusional mass transfer     | transport          | $mol\,s^{-1}$     | 90    |
| 91  | $\dot{V}_A$       | fV     | volumetric flow                                   | transport          | $m^3\,s^{-1}$     | 80    |
| 111 | $\dot{H}^c_N$     | aHc    | enthalpy accumulation due to convective mass flow | transport          | $kg\,m^2\,s^{-3}$ | 97    |
| 101 | $\hat{n}^d_{A,S}$ | fnd    | diffusional mass flow in arc                      | transport          | $mol\,s^{-1}$     | 85 89 |
| 84  | $\dot{q}_N$       | aq     | accumulation due to conductive heat flow          | transport          | $kg\,m^2\,s^{-3}$ | 73    |
| 92  | $\hat{n}^c_{A,S}$ | fnc    | convective mass flow in an arc                    | transport          | $mol\,s^{-1}$     | 81    |
| 87  | $c_{A,S}$         | c_A    | concentration in convective mass flow             | transport          | $m^{-3}\,mol$     | 76    |
| 93  | $\dot{n}^c_{N,S}$ | anc    | accumulation due to convective mass flow          | transport          | $mol\,s^{-1}$     | 82    |
| 112 | $\dot{H}^d_N$     | aHd    | enthalpy accumulation due to diffusive mass flow  | transport          | $kg\,m^2\,s^{-3}$ | 98    |
| 83  | $\hat{q}_{xA}$    | fq_x   | heat flow in arc and x-direction                  | transport          | $kg\,m^2\,s^{-3}$ | 72    |
| 86  | $d_A$             | d      | flow direction of convective flow                 | transport          |                   | 75    |
| 141 | $\hat{w}_A$       | fw     | just an numerical work flow term – as a starter   | transport          | $kg\,m^2\,s^{-3}$ | 125   |
| 109 | $\hat{H}^c_A$     | fHc    | enthalpy flow due to convective mass flow         | transport          | $kg\,m^2\,s^{-3}$ | 95    |
| 65  | $A_{xyN}$         | A_xy   | cross sectional area xy                           | geometry           | $m^2$             | 54    |
| 66  | $A_{xzN}$         | A_xz   | cross sectional area xz                           | geometry           | $m^2$             | 55    |
| 70  | $A_{yzA}$         | A_yz_A | cross sectional area yz of arc                    | geometry           | $m^2$             | 59    |
| 68  | $A_{xyA}$         | A_xy_A | cross sectional area yz of arc                    | geometry           | $m^2$             | 57    |
| 69  | $A_{xzA}$         | A_xz_A | cross sectional area xz of arc                    | geometry           | $m^2$             | 58    |
| 67  | $A_{yzN}$         | A_yz   | cross sectional area yz                           | geometry           | $m^2$             | 56    |
| 64  | $D_{N,A}$         | D      | difference operator                               | differenceOperator |                   |       |
| 145 | $n^o_{N,S}$       | no     | initial species masses                            | state              | $mol$             | 131   |

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|     | var             | symbol              | documentation                 | type           | units             | eqs        |
|-----|-----------------|---------------------|-------------------------------|----------------|-------------------|------------|
| 144 | $H^o_N$         | <b>Ho</b>           | initial enthalpy              | state          | $kg\,m^2\,s^{-2}$ | <b>130</b> |
| 100 | $x_{N,S}$       | <b>x</b>            | concentration mole fraction   | secondaryState |                   | <b>84</b>  |
| 99  | $n^t_N$         | <b>nt</b>           | total amount                  | secondaryState | $mol$             | <b>83</b>  |
| 85  | $c_{N,S}$       | <b>c</b>            | molar concentration           | secondaryState | $m^{-3}\,mol$     | <b>74</b>  |
| 138 | $\dot{n}_{N,S}$ | <b>anProduction</b> | production term               | conversion     | $mol\,s^{-1}$     | <b>122</b> |
| 143 | $\dot{H}_N$     | <b>aH</b>           | differential enthalpy balance | diffState      | $kg\,m^2\,s^{-3}$ | <b>127</b> |
| 139 | $\dot{n}_{N,S}$ | <b>an</b>           | differential species balance  | diffState      | $mol\,s^{-1}$     | <b>123</b> |



## 7 macroscopic-reactions

|     | var                           | symbol          | documentation   | type | units        | eqs |
|-----|-------------------------------|-----------------|---|------|--------------|-----|
| 125 | <code>_c<sub>N,S</sub></code> | <code>_c</code> | link variable c to interface macroscopic »> reactions | get  | $m^{-3} mol$ | 109 |

## 8 material–macroscopic

|     | var                   | symbol           | documentation  | type | units                    | eqs |
|-----|-----------------------|------------------|--|------|--------------------------|-----|
| 77  | $_{k_y^d A,S}$        | $_{kd\_y\_A}$    | link variable kd y A to interface material »> macroscopic    | get  | $kg^{-1} m^{-4} mol^2 s$ | 66  |
| 88  | $_{\rho N}$           | $_{density}$     | link variable density to interface material »> macroscopic   | get  | $kg m^{-3}$              | 77  |
| 75  | $_{k_x^{d,Fick} A,S}$ | $_{kd\_x\_Fick}$ | link variable kd x Fick to interface material »> macroscopic | get  | $ms^{-1}$                | 64  |
| 71  | $_{k_x^c A}$          | $_{kc\_x\_A}$    | link variable kc x A to interface material »> macroscopic    | get  | $m^{-1} s$               | 60  |
| 74  | $_{k_x^d A,S}$        | $_{kd\_x\_A}$    | link variable kd x A to interface material »> macroscopic    | get  | $kg^{-1} m^{-4} mol^2 s$ | 63  |
| 90  | $_{\rho A}$           | $_{density\_A}$  | link variable density A to interface material »> macroscopic | get  | $kg m^{-3}$              | 79  |
| 108 | $_{h_{A,S}}$          | $_{h\_A}$        | link variable h A to interface material »> macroscopic       | get  | $kg m^2 mol^{-1} s^{-2}$ | 94  |
| 76  | $_{k_y^{d,Fick} A,S}$ | $_{kd\_y\_Fick}$ | link variable kd y Fick to interface material »> macroscopic | get  | $ms^{-1}$                | 65  |
| 30  | $_{\lambda_S}$        | $_{Mm}$          | link variable Mm to interface material »> macroscopic        | get  | $kg mol^{-1}$            | 22  |
| 80  | $_{k_x^q A}$          | $_{kq\_x\_A}$    | link variable kq x A to interface material »> macroscopic    | get  | $kg K^{-1} s^{-3}$       | 69  |
| 106 | $_{h_{N,S}}$          | $_{h}$           | link variable h to interface material »> macroscopic         | get  | $kg m^2 mol^{-1} s^{-2}$ | 92  |
| 73  | $_{k_z^c A}$          | $_{kc\_z\_A}$    | link variable kc z A to interface material »> macroscopic    | get  | $m^{-1} s$               | 62  |
| 82  | $_{k_z^q A}$          | $_{kq\_z\_A}$    | link variable kq z A to interface material »> macroscopic    | get  | $kg K^{-1} s^{-3}$       | 71  |
| 81  | $_{k_y^q A}$          | $_{kq\_y\_A}$    | link variable kq y A to interface material »> macroscopic    | get  | $kg K^{-1} s^{-3}$       | 70  |

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|    | var                   | symbol                  | documentation  | type | units                    | eqs |
|----|-----------------------|-------------------------|--|------|--------------------------|-----|
| 72 | $_{k_y^c A}$          | <code>_kc_y_A</code>    | link variable kc y A to interface material »> macroscopic    | get  | $m^{-1} s$               | 61  |
| 78 | $_{k_z^d A,S}$        | <code>_kd_z_A</code>    | link variable kd z A to interface material »> macroscopic    | get  | $kg^{-1} m^{-4} mol^2 s$ | 67  |
| 79 | $_{k_z^{d,Fick} A,S}$ | <code>_kd_z_Fick</code> | link variable kd z Fick to interface material »> macroscopic | get  | $ms^{-1}$                | 68  |

## 9 reactions–macroscopic

|     | var               | symbol              | documentation   | type | units                       | eqs                 |
|-----|-------------------|---------------------|---|------|-----------------------------|---------------------|
| 119 | $_E^a_{N,CS}$     | <code>_Ea</code>    | link variable Ea to interface reactions »> macroscopic    | get  | $kg\,m^2\,mol^{-1}\,s^{-2}$ | <a href="#">103</a> |
| 137 | $_{\tilde{n}N,S}$ | <code>_nProd</code> | link variable nProd to interface reactions »> macroscopic | get  | $mol\,s^{-1}$               | <a href="#">121</a> |
| 122 | $_{NS,CS}$        | <code>_N</code>     | link variable N to interface reactions »> macroscopic     | get  |                             | <a href="#">106</a> |
| 123 | $_T_{N,CS}$       | <code>_T_K</code>   | link variable T K to interface reactions »> macroscopic   | get  | $K$                         | <a href="#">107</a> |

## 10 macroscopic-material

|     | var        | symbol        | documentation  | type | units | eqs |
|-----|------------|---------------|--|------|-------|-----|
| 103 | $_x_{N,S}$ | $\mathbf{-x}$ | link variable x to interface macroscopic »> material | get  |       | 87  |

## 11 Equations

## 12 Generic

| no | equation   | documentation                 | layer    |
|----|--|-------------------------------|----------|
| 1  | $1 := \text{Instantiate}(\#, \#)$                                    | numerical one                 | root     |
| 2  | $0 := \text{Instantiate}(\#, \#)$                                    | numerical value zero          | root     |
| 3  | $t^o := \text{Instantiate}(t, 0)$                                    | time zero                     | root     |
| 4  | $t^e := \text{Instantiate}(t, \#)$                                   | time end                      | root     |
| 5  | $\Delta t := \text{Instantiate}(t, \#)$                              | time interval                 | root     |
| 6  | $0.5 := \text{Instantiate}(\#, \#)$                                  | numerical one half            | root     |
| 7  | $\Delta := \text{sign}(t - t^o) - \text{sign}(t - (t^o - \Delta t))$ | pulse of length time interval | root     |
| 8  | $r_{xN} := \text{Instantiate}(\ell_N, \#)$                           | x-direction                   | physical |
| 9  | $r_{yN} := \text{Instantiate}(\ell_N, \#)$                           | y-direction                   | physical |
| 10 | $r_{zN} := \text{Instantiate}(\ell_N, \#)$                           | z-direction                   | physical |
| 11 | $V_N := r_{xN} \cdot r_{yN} \cdot r_{zN}$                            | volume                        | physical |
| 13 | $p_N := \frac{\partial U_N}{\partial V_N}$                           | pressure                      | physical |
| 14 | $\mu_{N,S} := \frac{\partial U_N}{\partial n_{N,S}}$                 | chemical potential            | physical |
| 15 | $H_N := U_N - p_N \cdot V_N$   | Enthalpy                      | physical |
| 16 | $T_N := \frac{\partial U_N}{\partial S_N}$                           | temperature                   | physical |
| 17 | $A_N := U_N - T_N \cdot S_N$   | Helmholts energy              | physical |

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| no | equation   | documentation                                | layer    |
|----|--|--|----------|
| 18 | $G_N := U_N + p_N \cdot V_N - T_N \cdot S_N$   | Gibbs free energy                            | physical |
| 19 | $v_{xN} := (t)^{-1} \cdot r_{xN}$  | velocity in x-direction                      | physical |
| 20 | $v_{yN} := (t)^{-1} \cdot r_{yN}$  | velocity in y-direction                      | physical |
| 21 | $v_{zN} := (t)^{-1} \cdot r_{zN}$  | velocity in z-direction                      | physical |
| 24 | $B_N := \text{Instantiate}(S_N, \#)$   | Boltzmann constant                           | physical |
| 25 | $R_N := A^v \cdot B_N$   | Gas constant                                 | physical |
| 26 | $U_N^e := (C_N)^{-1} \cdot U_N$  | electrical potential – voltage               | physical |
| 27 | $C_{pN} := \frac{\partial H_N}{\partial T_N}$  | total heat capacity at constant pressure     | material |
| 28 | $C_{vN} := \frac{\partial U_N}{\partial T_N}$  | total heat capacity at constant volume       | material |
| 29 | $k_{xN}^q := (V_N)^{-1} \cdot C_{pN} \cdot v_{xN}$   | thermal conductivity in x-direction          | material |
| 30 | $k_{yN}^q := (V_N)^{-1} \cdot C_{pN} \cdot v_{yN}$   | thermal conductivity in y-direction          | material |
| 31 | $k_{zN}^q := (V_N)^{-1} \cdot C_{pN} \cdot v_{zN}$   | thermal conductivity in z-direction          | material |
| 32 | $k_{xN,S}^d := (\mu_{N,S})^{-1} \cdot \left( v_{xN} \cdot \left( (V_N)^{-1} \cdot \frac{\partial U_N}{\partial \mu_{N,S}} \right) \right)$ | diffusional mass conductivity in x-direction | material |
| 33 | $k_{yN,S}^d := (\mu_{N,S})^{-1} \cdot \left( v_{yN} \cdot \left( (V_N)^{-1} \cdot \frac{\partial U_N}{\partial \mu_{N,S}} \right) \right)$ | diffusional mass conductivity in y-direction | material |
| 34 | $k_{zN,S}^d := (\mu_{N,S})^{-1} \cdot \left( v_{zN} \cdot \left( (V_N)^{-1} \cdot \frac{\partial U_N}{\partial \mu_{N,S}} \right) \right)$ | diffusional mass conductivity in z-direction | material |
| 35 | $k_{xN}^c := \left( \lambda_S \star (\mu_{N,S})^{-1} \right) \cdot (V_N)^{-1} \cdot \frac{\partial U_N}{\partial p_N} \cdot v_{xN}$        | convective mass conductivity in x-direction  | material |

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| no | equation  | documentation                                       | layer    |
|----|---|---|----------|
| 36 | $k_{yN}^c := \left( \lambda_S \star (\mu_{N,S})^{-1} \right) \cdot (V_N)^{-1} \cdot \frac{\partial U_N}{\partial p_N} \cdot v_{yN}$ | convective mass conductivity in y-direction         | material |
| 37 | $k_{zN}^c := \left( \lambda_S \star (\mu_{N,S})^{-1} \right) \cdot (V_N)^{-1} \cdot \frac{\partial U_N}{\partial p_N} \cdot v_{zN}$ | convective mass conductivity in z-direction         | material |
| 38 | $h_{N,S} := H_N \cdot (n_{N,S})^{-1}$   | partial molar enthalpies                            | material |
| 39 | $k_{xA}^c := I_{N,A} \star k_{xN}^c$  | convective mass conductivity in x-direction in arc  | material |
| 40 | $k_{yA}^c := I_{N,A} \star k_{yN}^c$  | convective mass conductivity in y-direction in arc  | material |
| 41 | $k_{zA}^c := I_{N,A} \star k_{zN}^c$  | convective mass conductivity in z-direction in arc  | material |
| 42 | $k_{xA,S}^d := I_{N,A} \star k_{xN,S}^d$  | diffusional mass conductivity in x-direction in arc | material |
| 43 | $k_{yA,S}^d := I_{N,A} \star k_{yN,S}^d$  | diffusional mass conductivity in z-direction in arc | material |
| 44 | $k_{zA,S}^d := I_{N,A} \star k_{zN,S}^d$  | diffusional mass conductivity in z-direction in arc | material |
| 45 | $k_{xA}^q := I_{N,A} \star k_{xN}^q$  | thermal conductivity in x-direction in arc          | material |
| 46 | $k_{yA}^q := I_{N,A} \star k_{yN}^q$  | thermal conductivity in y-direction in arc          | material |
| 47 | $k_{zA}^q := I_{N,A} \star k_{zN}^q$  | thermal conductivity in z-direction in arc          | material |
| 48 | $m_N := \lambda_S \star n_{N,S}$  | mass  | material |

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| no | equation   | documentation                             | layer       |
|----|--|---|-------------|
| 49 | $\rho_N := (V_N)^{-1} \cdot m_N$   | density                                   | material    |
| 50 | $v_S := V_N \star (n_{N,S})^{-1}$  | molar volume of species                   | material    |
| 51 | $k_{x,A,S}^{d,Fick} := I_{N,A} \star \left( v_{xN} \cdot \frac{\partial U_N}{\partial \mu_{N,S}} \cdot (n_{N,S})^{-1} \right)$ | Fick's diffusivity in arc and x-direction | material    |
| 52 | $k_{y,A,S}^{d,Fick} := I_{N,A} \star \left( v_{yN} \cdot \frac{\partial U_N}{\partial \mu_{N,S}} \cdot (n_{N,S})^{-1} \right)$ | Fick's diffusivity in arc and y-direction | material    |
| 53 | $k_{z,A,S}^{d,Fick} := I_{N,A} \star \left( v_{zN} \cdot \frac{\partial U_N}{\partial \mu_{N,S}} \cdot (n_{N,S})^{-1} \right)$ | Fick's diffusivity in arc and z-direction | material    |
| 54 | $A_{xyN} := r_{xN} \cdot r_{yN}$   | cross sectional area xy                   | macroscopic |
| 55 | $A_{xzN} := r_{xN} \cdot r_{zN}$   | cross sectional area xz                   | macroscopic |
| 56 | $A_{yzN} := r_{yN} \cdot r_{zN}$   | cross sectional area yz                   | macroscopic |
| 57 | $A_{xyA} := I_{N,A} \star A_{xyN}$   | cross sectional area yz of arc            | macroscopic |
| 58 | $A_{xzA} := I_{N,A} \star A_{xzN}$   | cross sectional area xz of arc            | macroscopic |
| 59 | $A_{yzA} := I_{N,A} \star A_{yzN}$   | cross sectional area yz of arc            | macroscopic |
| 72 | $\hat{q}_{xA} := A_{yzA} \cdot \_k_{xA}^q \cdot (D_{N,A} \star T_N)$   | heat flow in arc and x-direction          | macroscopic |
| 73 | $\dot{q}_N := F_{N,A} \star \hat{q}_{xA}$  | accumulation due to conductive heat flow  | macroscopic |
| 74 | $c_{N,S} := (V_N)^{-1} \cdot n_{N,S}$  | molar concentration                       | macroscopic |
| 75 | $d_A := \text{sign}(D_{N,A} \star p_N)$  | flow direction of convective flow         | macroscopic |
| 76 | $c_{A,S} := (0.5 \cdot (D_{N,A} - d_A \cdot  D_{N,A} )) \star c_{N,S}$   | concentration in convective mass flow     | macroscopic |
| 78 | $\rho_A := I_{N,A} \star \rho_N$   | density of arc material                   | material    |
| 80 | $\dot{V}_A := (\_ \rho_A)^{-1} \cdot \_k_{xA}^c \cdot A_{yzA} \cdot (D_{N,A} \star p_N)$                                       | volumetric flow                           | macroscopic |

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| no | equation  | documentation  | layer       |
|----|---|--|-------------|
| 81 | $\hat{n}_{A,S}^c := \dot{V}_A \cdot c_{A,S}$  | convective mass flow in an arc                       | macroscopic |
| 82 | $\dot{n}_{N,S}^c := F_{N,A} \star \hat{n}_{A,S}^c$                                      | accumulation due to convective mass flow             | macroscopic |
| 83 | $n_N^t := I_S \star n_{N,S}$  | total amount   | macroscopic |
| 84 | $x_{N,S} := (n_N^t)^{-1} \cdot n_{N,S}$   | concentration mole fraction                          | macroscopic |
| 85 | $\hat{n}_{A,S}^d := A_{yzA} \cdot (-_x k_{A,S}^{d,Fick}) \cdot (D_{N,A} \star c_{N,S})$ | diffusional mass flow in arc                         | macroscopic |
| 86 | $\mu_{N,S}^o := \text{Instantiate}(\mu_{N,S}, \#)$                                      | standard chemical potential                          | material    |
| 88 | $\mu_{N,S} := \mu_{N,S}^o + R_N \cdot T_N \cdot \ln(_x x_{N,S})$                        | chemical potential standard model with mole fraction | material    |
| 89 | $\hat{n}_{A,S}^d := A_{yzA} \cdot (-_x k_{A,S}^d) \cdot (D_{N,A} \star \mu_{N,S})$      | diffusional mass flow in arc                         | macroscopic |
| 90 | $\dot{n}_{N,S}^d := F_{N,A} \star \hat{n}_{A,S}^d$                                      | accumulation due to diffusional mass transfer        | macroscopic |
| 93 | $h_{AA,S} := I_{N,A} \star h_{N,S}$   | partial molar enthalpies of transport system         | material    |
| 95 | $\hat{H}_A^c := I_S \star (_h h_{A,S} \cdot \hat{n}_{A,S}^c)$                           | enthalpy flow due to convective mass flow            | macroscopic |
| 96 | $\hat{H}_A^d := I_S \star (_h h_{A,S} \cdot \hat{n}_{A,S}^d)$                           | enthalpy flow due to diffusive mass flow             | macroscopic |
| 97 | $\dot{H}_N^c := F_{N,A} \star \hat{H}_A^c$  | enthalpy accumulation due to convective mass flow    | macroscopic |
| 98 | $\dot{H}_N^d := F_{N,A} \star \hat{H}_A^d$  | enthalpy accumulation due to diffusive mass flow     | macroscopic |
| 99 | $T_{N,CS} := T_N \cdot P_{N,CS}$  | temparature of the nodes with reactions              | reactions   |

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| no  | equation   | documentation   | layer       |
|-----|--|---|-------------|
| 100 | $E_{aN,CS} := \text{Instantiate}(R_N \cdot T_{N,CS}, \#)$  | Arrhenius activation energy   | reactions   |
| 110 | $c^n_{N,S} := \text{Instantiate}(_c c_{N,S}, \#)$  | norming concentration used in the definition of the species interaction probability | reactions   |
| 112 | $\bar{n}_{N,S} := (c^n_{N,S})^{-1} \cdot _c c_{N,S}$   | normed concentration  | reactions   |
| 113 | $\bar{n}_{N,S,CS} := P_{N,CS} \cdot \bar{n}_{N,S}$   | normed concentration – context node and conversion                                  | reactions   |
| 115 | $\phi_{N,CS} := \prod_S \bar{n}_{N,S,CS}$  | probability for the species to meet to undergo reaction                             | reactions   |
| 118 | $K^o_{CS} := \text{Instantiate}(I_S \star (P_{N,CS} \star ((t)^{-1} \cdot (V_N)^{-1} \cdot n_{N,S})), \#)$ | Arrhenius frequency factor – a strange construction                                 | reactions   |
| 119 | $K_{N,CS} := K^o_{CS} \cdot \exp((-E_{aN,CS}) \cdot (R_N \cdot T_{N,CS})^{-1})$                            | reaction"constant   | reactions   |
| 120 | $\tilde{n}_{N,S} := V_N \cdot (N_{S,CS} \star (K_{N,CS} \cdot \phi_{N,CS}))$                               | production term for differential component mass balance                             | reactions   |
| 122 | $\dot{n}_{N,S} := _\dot{n}_{N,S}$  | production term   | macroscopic |
| 123 | $\dot{n}_{N,S} := \dot{n}^c_{N,S} + \dot{n}^d_{N,S} + \dot{n}_{N,S}$                                       | differential species balance  | macroscopic |
| 125 | $\hat{w}_A := \text{Instantiate}(\hat{H}^c_A, \#)$   | just an numerical work flow term – as a starter                                     | macroscopic |
| 126 | $\dot{w}_N := F_{N,A} \star \hat{w}_A$   | enthalpy accumulation due to work flows   | macroscopic |
| 127 | $\dot{H}_N := \dot{H}^c_N + \dot{H}^d_N + \dot{q}_N + \dot{w}_N$   | differential enthalpy balance   | macroscopic |
| 128 | $H_N := \int_{t^o}^{t^e} \dot{H}_N dt + H^o_N$   | Enthalpy  | macroscopic |

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| no  | equation   | documentation                  | layer       |
|-----|--|--------------------------------|-------------|
| 129 | $n_{N,S} := \int_{t^o}^{t^e} \dot{n}_{N,S} dt + n^o_{N,S}$ | fundamental state - molar mass | macroscopic |
| 130 | $H^o_N := \text{Instantiate}(H_N, \#)$                     | initial enthalpy               | macroscopic |
| 131 | $n^o_{N,S} := \text{Instantiate}(n_{N,S}, \#)$             | initial species masses         | macroscopic |

## 13 Interface Link Equation

| no | equation                                       | documentation      | layer                   |
|----|--|--------------------|-------------------------|
| 22 | $_{-}\lambda_S := \lambda_S$                   | interface equation | material -> macroscopic |
| 60 | $_{-}k_{xA}^c := k_{xA}^c$                     | interface equation | material -> macroscopic |
| 61 | $_{-}k_{yA}^c := k_{yA}^c$                     | interface equation | material -> macroscopic |
| 62 | $_{-}k_{zA}^c := k_{zA}^c$                     | interface equation | material -> macroscopic |
| 63 | $_{-}k_{xA,S}^d := k_{xA,S}^d$                 | interface equation | material -> macroscopic |
| 64 | $_{-}k_{x,A,S}^{d,Fick} := k_{x,A,S}^{d,Fick}$ | interface equation | material -> macroscopic |
| 65 | $_{-}k_{y,A,S}^{d,Fick} := k_{y,A,S}^{d,Fick}$ | interface equation | material -> macroscopic |
| 66 | $_{-}k_{yA,S}^d := k_{yA,S}^d$                 | interface equation | material -> macroscopic |
| 67 | $_{-}k_{zA,S}^d := k_{zA,S}^d$                 | interface equation | material -> macroscopic |
| 68 | $_{-}k_{z,A,S}^{d,Fick} := k_{z,A,S}^{d,Fick}$ | interface equation | material -> macroscopic |
| 69 | $_{-}k_{xA}^q := k_{xA}^q$                     | interface equation | material -> macroscopic |

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| no  | equation                               | documentation      | layer                               |
|-----|--|--------------------|-------------------------------------|
| 70  | $\_k_{yA}^q := k_{yA}^q$               | interface equation | material $\rightarrow$ macroscopic  |
| 71  | $\_k_{zA}^q := k_{zA}^q$               | interface equation | material $\rightarrow$ macroscopic  |
| 77  | $\_\rho_N := \rho_N$                   | interface equation | material $\rightarrow$ macroscopic  |
| 79  | $\_\rho_A := \rho_A$                   | interface equation | material $\rightarrow$ macroscopic  |
| 87  | $\_x_{N,S} := x_{N,S}$                 | interface equation | macroscopic $\rightarrow$ material  |
| 92  | $\_h_{N,S} := h_{N,S}$                 | interface equation | material $\rightarrow$ macroscopic  |
| 94  | $\_h_{A,S} := h_{AA,S}$                | interface equation | material $\rightarrow$ macroscopic  |
| 103 | $\_E^a_{N,CS} := E_{aN,CS}$            | interface equation | reactions $\rightarrow$ macroscopic |
| 106 | $\_N_{S,CS} := N_{S,CS}$               | interface equation | reactions $\rightarrow$ macroscopic |
| 107 | $\_T_{N,CS} := T_{N,CS}$               | interface equation | reactions $\rightarrow$ macroscopic |
| 109 | $\_c_{N,S} := c_{N,S}$                 | interface equation | macroscopic $\rightarrow$ reactions |
| 121 | $\_\tilde{n}_{N,S} := \tilde{n}_{N,S}$ | interface equation | reactions $\rightarrow$ macroscopic |