

(37)  
(24)

## \* Assignment - 6

Title:- Curve and fractals.

Aim:- write C++ program to generate fractal pattern by using Koch curves.

Co. Mapped:-

CO<sub>5</sub>

Learning objectives:-

To learn curves and fractals.

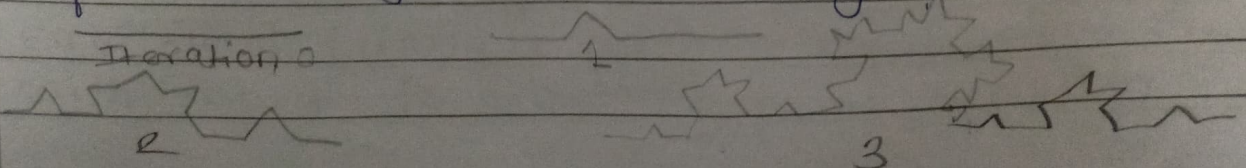
Theory:-

Koch curves:-

The Koch curves fractal was first introduced 1904 by Helye Von Koch. It was one of the first fractal object to be described. To create Koch curve.

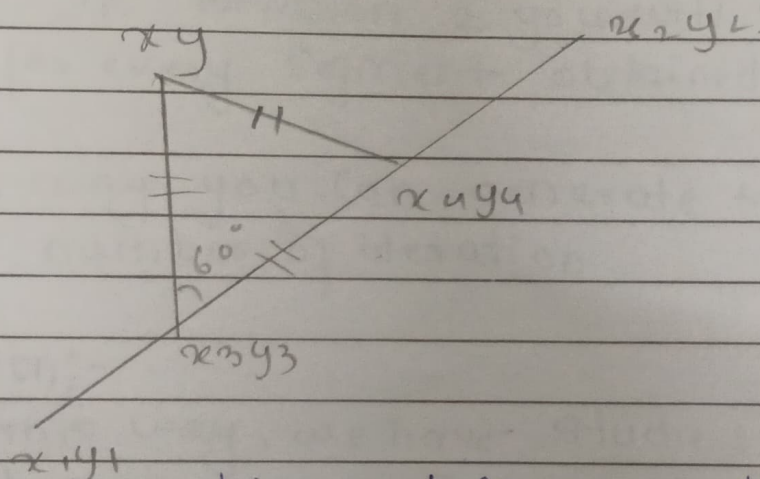
- ① Create a line and divide it into 3 parts.
- ② The second part is now rotate by  $60^\circ$ .
- ③ Add another part which goes from the end of one part 2 to the beginning of part 1.
- ④ Repeat above steps with each part of the line.

We will get following Koch curve as number of iteration goes on increasing



Step 1:- In iteration 0, we have a horizontal line.

Step 2:- In iteration 1, the line is divided into 3 equal parts. Middle part of a line is rotated in  $60^\circ$  because it forms a perfect equilateral triangle.



Here  $(x_1, y_1)$  and  $(x_2, y_2)$  is accepted from user. Now, we can see line is divided into 3 equal segments. Co-ordinates of middle two points will be calculated as follows:

$$x_3 = (x_1 + x_2) / 3;$$

$$y_3 = (y_1 + y_2) / 3;$$

$$x_4 = (x_1 + 2x_2) / 3;$$

$$y_4 = (y_1 + 2y_2) / 3;$$

In our curve, middle segment  $(x_3, y_3)$   $(x_2, y_2)$  will not be drawn. Now, in order to find out co-ordinates of the top vertex  $(x, y)$  of equilateral triangle we have rotate point  $(x_4, y_4)$  with respect to arbitrary point  $(x_3, y_3)$  by



angle of  $60^\circ$  in anticlockwise direction.  
After performing this rotation we will get rotated co-ordinates  $(x, y)$  as.

$$x = x_3 + (x_4 - x_3) \cos \theta + (y_4 - y_3) \sin \theta$$

$$y = y_3 - (x_4 - x_3) \sin \theta + (y_4 - y_3) \cos \theta$$

Step 3 - In iteration 2 you will repeat step 2 for every segment obtained in iteration 1.

In this way you can generate Koch curve for any number of iteration.

Conclusion:-

In this way, we have studied and implemented Koch curve.

