

## 4 Trigonometry and Euclid

### 4.1 Tues., Mar. 19: Representative triangles

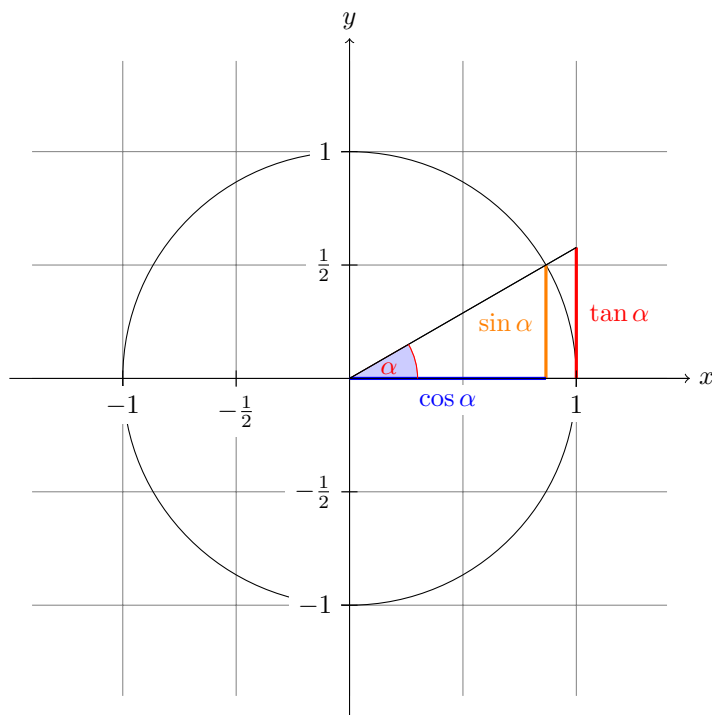
In calc we turn from degree measure to radian measure... as we learned from deriving  $\pi$ , there are 6.28 radius lengths in a circle and so we have the formula:

$$s = 2\pi r \quad (40)$$

So  $\frac{2\pi}{2}$  is a half revolution, or 180 degrees. It's also useful to know that  $\frac{\pi}{6} = 30^\circ$ ,  $\frac{\pi}{4} = 45^\circ$ ,  $\frac{\pi}{2} = 90^\circ$ . We can convert from degrees to radians easily by observing:

$$360^\circ = 2\pi \text{ rad} \quad (41)$$

$\frac{\pi}{180^\circ}$  is the conversion you most often want to multiply by.



The trig ratios are:

$$\begin{aligned} \sin(\theta) &= \frac{\text{opposite}}{\text{hypotenuse}} & \csc(\theta) &= \frac{h}{o} \\ \sin(\theta) &= \frac{\text{opposite}}{\text{hypotenuse}} & \csc(\theta) &= \frac{h}{a} \\ \sin(\theta) &= \frac{\text{opposite}}{\text{hypotenuse}} & \csc(\theta) &= \frac{a}{o} \end{aligned}$$

**Exercise 44.** Find the trig ratios for the representative triangles 45 – 45 – 90 and 30 – 60 – 90 in each quadrant.

**Exercise 45.** Compute  $\sin(\theta)$  for three  $\theta$  you choose... then compute  $\cos(\theta - 90^\circ)$  for the same three  $\theta$  values. What is their relationship? Why?

### 4.2 Thurs., Mar. 21

### 4.3 Fri., Mar. 22