Hazel PHI: 10-modules

July 3, 2021

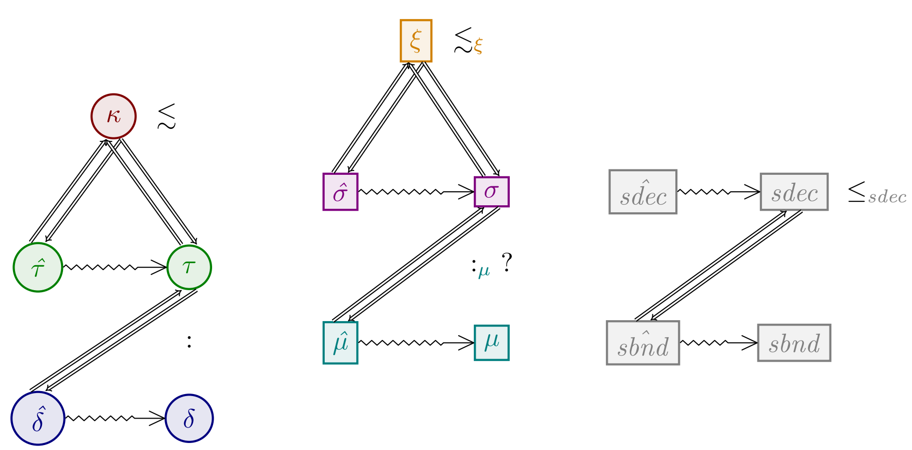
prerequisites

- Hazel PHI: 9-type-aliases-redux
  - github
  - current commit: 4410cd565ce717707e580e44f64868d3175fe2a6
- (optional) Hazel PHI: 1-labeled-tuples
  - github
  - current commit: 0a7d0b53ee7286d03ea3be13a7ac91a86f1c90b1

how to read

800000	kinds	D08000	signature kind
008000	types (constructors)	800080	signatures
000080	terms	008080	modules

notes



external typ/sig/mod syntax not written out yet (waiting for construction dust to settle); patterns not handled yet– will be left till end.

syntax

kind	κ	$::=$	$\mathtt{Type}$	kind of types
		$\mid$	$\mathtt{S}(\tau)$	singleton kind
		$\mid$	$\mathtt{KHole}$	kind hole
		$\mid$	$\Pi_{t::\kappa_1}.\kappa_2$	dependent function kind

HTyp	τ	$::=$	t	type variable
		$\mid$	bse	base type
		$\mid$	$\tau_1 \oplus \tau_2$	type binop
		$\mid$	$[\tau]$	list type
		$\mid$	$\lambda t{::}\kappa.\tau$	type function
		$\mid$	$\tau_1\ \tau_2$	type application
		$\mid$	$\{lab_1 \hookrightarrow \tau_1, \ldots\ lab_n \hookrightarrow \tau_n\}$	labelled product type (record)
		$\mid$	$\mu.lab$	module type projection
		$\mid$	$\llparenthesis\rrparenthesis$	empty type hole
		$\mid$	$\llparenthesis\tau\rrparenthesis$	nonempty type hole
base type	bse	$::=$	$\texttt{Int}$	
		$\mid$	$\texttt{Float}$	
		$\mid$	$\texttt{Bool}$	
HTyp BinOp	$\oplus$	$::=$	$\times$	
		$\mid$	$+$	
		$\mid$	$\rightarrow$	
external expression	$\hat{\delta}$	$::=$	$\ldots$	
		$\mid$	x	
		$\mid$	$\texttt{signature}\ s = \hat{\sigma}\ \texttt{in}\ \hat{\delta}$	
		$\mid$	$\texttt{module}\ m = \hat{\mu}\ \texttt{in}\ \hat{\delta}$	
		$\mid$	$\texttt{module}\ m{:}_{\mu} s = \hat{\mu}\ \texttt{in}\ \hat{\delta}$	
		$\mid$	$\texttt{functor something} = \texttt{something in}\ \hat{\delta}$	
		$\mid$	$\hat{\mu}.lab$	module term projection
internal expression	δ	$::=$	$\ldots$	
		$\mid$	x	
		$\mid$	$\texttt{signature}\ s = \sigma\ \texttt{in}\ \delta$	
		$\mid$	$\texttt{module}\ m{:}_{\mu} s = \mu\ \texttt{in}\ \delta$	
		$\mid$	$\texttt{functor something} = \texttt{something in}\ \delta$	
		$\mid$	$\mu.lab$	module term projection
signature kind	ξ	$::=$	$\texttt{SSigKind}(\sigma)$	
		$\mid$	$\texttt{SigKHole}$	
external signature	$\hat{\sigma}$	$::=$	s	signature variable
		$\mid$	$\{\widehat{sdecs}\}$	structure signature
		$\mid$	$\Pi_{m:_{\mu}\hat{\sigma_1}}.\hat{\sigma_2}$	functor signature
		$\mid$	$\llparenthesis\rrparenthesis^{\texttt{u}}$	empty signature hole
		$\mid$	$\llparenthesis s\rrparenthesis^{\texttt{u}}$	nonempty signature hole
signature	σ	$::=$	s	signature variable
		$\mid$	$\{sdecs\}$	structure signature
		$\mid$	$\Pi_{m:_{\mu}\sigma_1}.\sigma_2$	functor signature
		$\mid$	$\llparenthesis\rrparenthesis^{\texttt{u}}$	empty signature hole
		$\mid$	$\llparenthesis s\rrparenthesis^{\texttt{u}}$	nonempty signature hole
		$\mid$	$\underset{\sim\sim}{s}$	unbound signature variable
module	μ	$::=$	m	module variable
		$\mid$	$\{sbnds\}$	structure
		$\mid$	$\lambda m{:}_{\mu}\sigma.\mu$	functor
		$\mid$	$\mu_1\ \mu_2$	functor application
		$\mid$	$\mu.lab$	submodule projection
		$\mid$	$\llparenthesis\rrparenthesis$	empty module hole
		$\mid$	$\llparenthesis\mu\rrparenthesis$	nonempty module hole
signature declarations	$sdecs$	$::=$	$\cdot$	
		$\mid$	$sdec, sdecs$	
signature declaration	$sdec$	$::=$	$\texttt{type}\ lab{::}\kappa$	
		$\mid$	$\texttt{val}\ lab{:}\tau$	
		$\mid$	$\texttt{module}\ lab{:}_{\mu}\sigma$	
		$\mid$	$\texttt{functor}\ lab{:}_{\mu}\sigma$	
structure bindings	$sbnds$	$::=$	$\cdot$	

		$\mid$	$sbnd, sbnds$
structure binding	$sbnd$	$::=$	$\texttt{type}\ t = \tau$
		$\mid$	$\texttt{let}\ x{:}\tau = \delta$
		$\mid$	$\texttt{module}\ m = \mu$
		$\mid$	$\texttt{module}\ m{:}_{\mu}s = \mu$
		$\mid$	$\texttt{functor}\ m{:}_{\mu}s = \mu$

context definitions

$\Delta;, ?; \Gamma;, x{:}\tau; \Phi;, t{::}\kappa; \Xi;, m{:}_{\mu}\sigma; \Psi;, s{::}_{\sigma}\xi$

declarative statics

scratch

$\boxed{\Delta; \Phi; \Xi; \Psi; \vdash \Delta;; \Phi; \lesssim \kappa_1 \kappa_2}$ κ_1 is a consistent subkind of κ_2

KCSubsumption
$$\frac{test}{test}$$

$\boxed{\Delta;; \Phi;; \Xi;; \Psi; \vdash \xi_1 \lesssim_{\xi} \xi_2}$ ξ_1 is a consistent sub signature kind of ξ_2

nameMe
$$\frac{\exists sdec_x \in sdecs_1\ st\ \Delta;; \Phi;; \Xi;; \Psi; \vdash \texttt{SSigKind}(\{sdec_x\}) \lesssim_{\xi} \texttt{SSigKind}(\{sdec_2\}) \quad \Delta;; \Phi;, \mathsf{type}(\Delta;; \Phi;; \Xi;; \Psi;, sdec_2); \Xi;, \mathsf{submodule}(sdec_2); \Psi; \vdash \{sdecs_1\} \lesssim_{\xi} \{sdecs_2\}}{\Delta;; \Phi;; \Xi;; \Psi; \vdash \texttt{SSigKind}(\{sdec_{11}, sdec_{12}, sdecs_{13}\ \texttt{as}\ sdecs_1\}) \lesssim_{\xi} \texttt{SSigKind}(\{sdec_2, sdecs_2\})}$$

single
$$\frac{\Delta;; \Phi;; \Xi;; \Psi; \vdash sdec_1 \leq_{sdec} sdec_2}{\Delta;; \Phi;; \Xi;; \Psi; \vdash \texttt{SSigKind}(\{sdec_1\}) \lesssim_{\xi} \texttt{SSigKind}(\{sdec_2\})}$$

nil
$$\frac{}{\Delta;; \Phi;; \Xi;; \Psi; \vdash \texttt{SSigKind}(\{sdecs\}) \lesssim_{\xi} \texttt{SSigKind}(\{\cdot\})}$$

varprop
$$\frac{s{::}_{\sigma}\xi \in \Psi;}{\Delta;; \Phi;; \Xi;; \Psi; \vdash \texttt{SSigKind}(s) \lesssim_{\xi} \xi}$$

nameMe?delete?
$$\frac{\sigma_1 \neq s \quad \Delta;; \Phi;; \Xi;; \Psi; \vdash \sigma_1 \Leftarrow \texttt{SSigKind}(\sigma_2)}{\Delta;; \Phi;; \Xi;; \Psi; \vdash \texttt{SSigKind}(\sigma_1) \lesssim_{\xi} \texttt{SSigKind}(\sigma_2)}$$

funct
$$\frac{\Delta;; \Phi;; \Xi;; \Psi; \vdash \texttt{SSigKind}(\sigma_{21}) \lesssim_{\xi} \texttt{SSigKind}(\sigma_{11}) \quad \Delta;; \Phi;; \Xi;, m{:}_{\mu}\sigma_{11}; \Psi; \vdash \texttt{SSigKind}(\sigma_{12}) \lesssim_{\xi} \texttt{SSigKind}(\sigma_{22})}{\Delta;; \Phi;; \Xi;; \Psi; \vdash \texttt{SSigKind}(\Pi_{m:_{\mu}\sigma_{11}}.\sigma_{12}) \lesssim_{\xi} \texttt{SSigKind}(\Pi_{m:_{\mu}\sigma_{21}}.\sigma_{22})}$$

holes
$$\frac{\Delta;; \Phi;; \Xi;; \Psi; \vdash (\!|\,|\!)^{\mathsf{uu}} \Leftarrow \xi}{\Delta;; \Phi;; \Xi;; \Psi; \vdash \texttt{SSigKind}((\!|\,|\!)^{\mathsf{uu}}) \lesssim_{\xi} \xi}$$

neholes
$$\frac{\Delta;; \Phi;; \Xi;; \Psi; \vdash (\!|\mathsf{s}|\!)^{\mathsf{uu}} \Leftarrow \xi}{\Delta;; \Phi;; \Xi;; \Psi; \vdash \texttt{SSigKind}((\!|\mathsf{s}|\!)^{\mathsf{uu}}) \lesssim_{\xi} \xi}$$

CSubSigKindHoleL
$$\frac{}{\Delta;; \Phi;; \Xi;; \Psi; \vdash \texttt{SigKHole} \lesssim_{\xi} \xi}$$

CSubSigKindHoleR
$$\frac{}{\Delta;; \Phi;; \Xi;; \Psi; \vdash \xi \lesssim_{\xi} \texttt{SigKHole}}$$

$\boxed{\Delta;; \Phi;; \Xi;; \Psi; \vdash \sigma \Rightarrow \xi}$ σ synthesizes signature kind ξ

SynSigKndVar
$$\frac{s{::}_{\sigma}\xi \in \Psi;}{\Delta;; \Phi;; \Xi;; \Psi; \vdash s \Rightarrow \texttt{SSigKind}(s)}$$

SynSigKndVarFail
$$\frac{s \notin \mathsf{dom}(\Psi;)}{\Delta;; \Phi;; \Xi;; \Psi; \vdash s \Rightarrow \texttt{SigKHole}}$$

$$\frac{\{sdecs\} wellformed?}{\vdash \{sdecs\} \Rightarrow \texttt{SSigKind}(\{sdecs\})}$$

$$\frac{\Delta;; \Phi;; \Xi;, m{:}_{\mu}\sigma_1; \Psi; \vdash \sigma_2 \Rightarrow \xi}{\Delta;; \Phi;; \Xi;; \Psi; \vdash \Pi_{m:_{\mu}\sigma_1}.\sigma_2 \Rightarrow \texttt{SSigKind}(\Pi_{m:_{\mu}\sigma_1}.\sigma_2)}$$

SynSigKndSigHole
$$\frac{u{::}_{\sigma}\xi \in \Delta;}{\Delta;; \Phi;; \Xi;; \Psi; \vdash (\!|\,|\!)^{\mathsf{uu}} \Rightarrow \xi}$$

SynSigKndSigHole
$$\frac{u{::}_{\sigma}\xi \in \Delta; \quad \Delta;; \Phi;; \Xi;; \Psi; \vdash s \Rightarrow \xi_1}{\Delta;; \Phi;; \Xi;; \Psi; \vdash (\!|s|\!)^{\mathsf{uu}} \Rightarrow \xi}$$

$\boxed{\Delta;;\Phi;;\Xi;;\Psi;\vdash \sigma \Leftarrow \xi}$ σ analyzes against signature kind ξ

Sub
$$\frac{\Delta;;\Phi;;\Xi;;\Psi;\vdash \sigma \Rightarrow \xi_1 \qquad \Delta;;\Phi;;\Xi;;\Psi;\vdash \xi_1 \lesssim_\xi \xi}{\Delta;;\Phi;;\Xi;;\Psi;\vdash \sigma \Leftarrow \xi}$$

$\boxed{\Delta;;\Phi;;\Xi;;\Psi;\vdash sdec_1 \leq_{sdec} sdec_2}$ $sdec_1$ is a subsdec of $sdec_2$

singleType
$$\frac{\Delta;\Phi;\Xi;\Psi;\vdash\lesssim \kappa_1\kappa_2}{\Delta;;\Phi;;\Xi;;\Psi;\vdash \texttt{type}\ lab{::}\kappa_1 \leq_{sdec} \texttt{type}\ lab{::}\kappa_2}$$

singleVa
$$\frac{\Delta;\Phi;\Xi;\Psi \vdash \Delta;;\Phi;;\Xi;;\Psi;\overset{\kappa}{\equiv} \tau_1\tau_2}{\Delta;;\Phi;;\Xi;;\Psi;\vdash \texttt{val}\ lab{:}\tau_1 \leq_{sdec} \texttt{val}\ lab{:}\tau_2}$$

singleMod
$$\frac{\Delta;;\Phi;;\Xi;;\Psi;\vdash \sigma_1 \Leftarrow \texttt{SSigKind}(\sigma_2)}{\Delta;;\Phi;;\Xi;;\Psi;\vdash \texttt{module}\ lab{:}_\mu\sigma_1 \leq_{sdec} \texttt{module}\ lab{:}_\mu\sigma_2}$$

elaboration

$\boxed{\Gamma;;\Phi;;\Xi;\vdash \hat{\delta} \Rightarrow \tau \rightsquigarrow \delta \dashv \Delta;}$ $\hat{\delta}$ synthesizes type τ and elaborates to δ with hole context $\Delta;$

...

SynElabLetMod
$$\frac{\Gamma;;\Phi;;\Xi;\vdash \hat{\mu} \Rightarrow \sigma \rightsquigarrow \mu \dashv \Delta;_1 \qquad \Gamma;;\Phi;;\Xi;,m{:}_\mu\sigma \vdash \hat{\delta} \Rightarrow \tau \rightsquigarrow \delta \dashv \Delta;_2}{\Gamma;;\Phi;;\Xi;\vdash \texttt{module}\ m = \hat{\mu}\ \texttt{in}\ \hat{\delta} \Rightarrow \tau \rightsquigarrow \texttt{module}\ m = \mu\ \texttt{in}\ \delta \dashv \Delta;_1 \cup \Delta;_2}$$

SynElabLetModAnn
$$\frac{\Phi;;\Xi;\vdash \hat{\sigma} \Rightarrow \xi \rightsquigarrow \sigma \dashv \Delta;_1 \qquad \Gamma;;\Phi;;\Xi;\vdash \hat{\mu} \Leftarrow \sigma \rightsquigarrow \mu \dashv \Delta;_2 \qquad \Gamma;;\Phi;;\Xi;,m{:}_\mu\sigma \vdash \hat{\delta} \Rightarrow \tau \rightsquigarrow \delta \dashv \Delta;_3}{\Gamma;;\Phi;;\Xi;\vdash \texttt{module}\ m{:}_\mu\hat{\sigma} = \hat{\mu}\ \texttt{in}\ \hat{\delta} \Rightarrow \tau \rightsquigarrow \texttt{module}\ m{:}_\mu\sigma = \mu\ \texttt{in}\ \delta \dashv \Delta;_1 \cup \Delta;_2 \cup \Delta;_3}$$

SynElabModTermPrj
$$\frac{\Gamma;;\Phi;;\Xi;\vdash \hat{\mu} \Rightarrow \sigma \rightsquigarrow \mu \dashv \Delta; \qquad \Phi;;\Xi;\vdash \sigma \Rightarrow \xi}{\Gamma;;\Phi;;\Xi;\vdash \hat{\mu}.lab \Rightarrow \tau \rightsquigarrow \mu.lab \dashv \Delta;}$$

$\boxed{\Phi;;\Xi;\vdash \hat{\tau} \Rightarrow \kappa \rightsquigarrow \tau \dashv \Delta;}$ $\hat{\tau}$ synthesizes kind κ and elaborates to τ with hole context $\Delta;$

...

SynElabModTypPrj
$$\frac{\Phi;;\Xi;\vdash m \Rightarrow \sigma \rightsquigarrow m \dashv \Delta; \qquad something\sigma\kappa}{\Phi;;\Xi;\vdash m.lab \Rightarrow \kappa \rightsquigarrow m.lab \dashv \Delta;}$$

$\boxed{\Phi;;\Xi;\vdash \hat{\tau} \Leftarrow \kappa \rightsquigarrow \tau \dashv \Delta;}$ $\hat{\tau}$ analyzes against kind κ and elaborates to τ with hole context $\Delta;$

$\boxed{\Gamma;;\Phi;;\Xi;\vdash \hat{\mu} \Rightarrow \sigma \rightsquigarrow \mu \dashv \Delta;}$ $\hat{\mu}$ synthesizes signature σ and elaborates to μ with hole context $\Delta;$

SynElabModVar
$$\frac{m{:}_\mu\sigma \in \Xi;}{\Gamma;;\Phi;;\Xi;\vdash m \Rightarrow \sigma \rightsquigarrow m \dashv \cdot}$$

SynElabModVarFail
$$\frac{m \notin \mathsf{dom}(\Xi;)}{\Gamma;;\Phi;;\Xi;\vdash m \Rightarrow (\!|\!)^{\mathtt{u}} \rightsquigarrow (\!|m|\!)^{\mathtt{u}} \dashv u{:}_\mu(\!|\!)^{\mathtt{u}}}$$

SynElabConsStruct
$$\frac{\begin{array}{c}\Gamma;;\Phi;;\Xi;\vdash \widehat{sbnd} \Rightarrow sdec \rightsquigarrow sbnd \dashv \Delta;_1 \\ \Gamma;,\mathsf{val}(sdec);\Phi;,\mathsf{type}(\Delta;_1;\Phi;;\Xi;;\Psi;,sdec);\Xi;,\mathsf{submodule}(sdec) \vdash \{\widehat{sbnds}\} \Rightarrow \{sdecs\} \rightsquigarrow \{sbnds\} \dashv \Delta;_2\end{array}}{\Gamma;;\Phi;;\Xi;\vdash \{\widehat{sbnd},\widehat{sbnds}\} \Rightarrow \{sdec, sdecs\} \rightsquigarrow \{sbnd, sbnds\} \dashv \Delta;_1 \cup \Delta;_2}$$

SynElabNilStruct
$$\frac{}{\Gamma;;\Phi;;\Xi;\vdash \{\cdot\} \Rightarrow \{\cdot\} \rightsquigarrow \{\cdot\} \dashv \cdot}$$

SynElabEmptyModHole
$$\frac{}{\Gamma;;\Phi;;\Xi;\vdash (\!|\!)^{\mathtt{u}} \Rightarrow (\!|\!)^{\mathtt{u}} \rightsquigarrow (\!|\!)^{\mathtt{u}} \dashv u{:}_\mu(\!|\!)^{\mathtt{u}}}$$

SynElabNonemptyModHole
$$\frac{}{\Gamma;;\Phi;;\Xi;\vdash (\!|m|\!)^{\mathtt{u}} \Rightarrow (\!|\!)^{\mathtt{u}} \rightsquigarrow (\!|m|\!)^{\mathtt{u}} \dashv u{:}_\mu(\!|\!)^{\mathtt{u}}}$$

functor stuff

$\boxed{\Gamma;;\Phi;;\Xi;\vdash \hat{\mu} \;\Leftarrow\; \sigma \rightsquigarrow \mu \dashv \Delta;}$ $\hat{\mu}$ analyzes against signature σ and elaborates to μ with hole context Δ;

AnaElabModSubsumption
$$\frac{\Gamma;;\Phi;;\Xi;\vdash \hat{\mu} \;\Rightarrow\; \sigma \rightsquigarrow \mu \dashv \Delta;}{\Gamma;;\Phi;;\Xi;\vdash \hat{\mu} \;\Leftarrow\; \sigma \rightsquigarrow \mu \dashv \Delta;}$$

$\boxed{\Gamma;;\Phi;;\Xi;\vdash \hat{sbnd} \;\Rightarrow\; sdec \rightsquigarrow sbnd \dashv \Delta;}$ $\hat{sbnd}$ synthesizes declaration $sdec$ and elaborates to $sbnd$ with hole context Δ;

SynElabTypeSbnd
$$\frac{\Phi;;\Xi;\vdash \hat{\tau} \;\Rightarrow\; \kappa \rightsquigarrow \tau \dashv \Delta;}{\Gamma;;\Phi;;\Xi;\vdash \texttt{type}\ t = \hat{\tau} \;\Rightarrow\; \texttt{type}\ t{::}\kappa \rightsquigarrow \texttt{type}\ t = \tau \dashv \Delta;}$$

SynElabValSbnd
$$\frac{\Phi;;\Xi;\vdash \hat{\tau} \;\Rightarrow\; \kappa \rightsquigarrow \tau \dashv \Delta;_1 \qquad \Gamma;;\Phi;;\Xi;\vdash \hat{\delta} \;\Leftarrow\; \tau \rightsquigarrow \delta \dashv \Delta;_2}{\Gamma;;\Phi;;\Xi;\vdash \texttt{let}\ x{:}\hat{\tau} = \hat{\delta} \;\Rightarrow\; \texttt{val}\ x{:}\tau \rightsquigarrow \texttt{let}\ x{:}\tau = \delta \dashv \Delta;_1 \cup \Delta;_2}$$

SynElabModSbnd
$$\frac{\Gamma;;\Phi;;\Xi;\vdash \hat{\mu} \;\Rightarrow\; \sigma \rightsquigarrow \mu \dashv \Delta;}{\Gamma;;\Phi;;\Xi;\vdash \texttt{module}\ m = \hat{\mu} \;\Rightarrow\; \texttt{module}\ m{:}_{\mu}\sigma \rightsquigarrow \texttt{module}\ m{:}_{\mu}\sigma = \mu \dashv \Delta;}$$

SynElabModAnnSbnd
$$\frac{\Phi;;\Xi;\vdash \hat{\sigma} \;\Rightarrow\; \xi \rightsquigarrow \sigma_1 \dashv \Delta;_1 \qquad \Gamma;;\Phi;;\Xi;\vdash \hat{\mu} \;\Rightarrow\; \sigma_2 \rightsquigarrow \mu \dashv \Delta;_2 \qquad \Phi;;\Xi;;\Psi;\vdash \sigma_2 \;\Leftarrow\; \xi}{\Gamma;;\Phi;;\Xi;\vdash \texttt{module}\ m{:}_{\mu}\hat{\sigma} = \hat{\mu} \;\Rightarrow\; \texttt{module}\ m{:}_{\mu}\sigma_1 \rightsquigarrow \texttt{module}\ m{:}_{\mu}\sigma_1 = \mu \dashv \Delta;_1 \cup \Delta;_2}$$

$\boxed{\Gamma;;\Phi;;\Xi;\vdash \hat{sbnd} \;\Leftarrow\; sdec \rightsquigarrow sbnd \dashv \Delta;}$ $\hat{sbnd}$ analyzes against declaration $sdec$ and elaborates to $sbnd$ with hole context Δ;

subsump
$$\frac{\Gamma;;\Phi;;\Xi;;l\Psi;\vdash \hat{sbnd} \;\Rightarrow\; sdec_1 \rightsquigarrow sbnd \dashv \Delta; \qquad \Delta;;\Phi;;\Xi;;\Psi;\vdash sdec_1 \leq_{sdec} sdec}{\Gamma;;\Phi;;\Xi;;\Psi;\vdash \hat{sbnd} \;\Leftarrow\; sdec \rightsquigarrow sbnd \dashv \Delta;}$$

$\boxed{\Gamma;;\Phi;;\Xi;;\Psi;\vdash \hat{sdec} \rightsquigarrow sdec \dashv \Delta;}$ $\hat{sdec}$ elaborates to $sdec$ with hole context Δ;

opq
$$\frac{}{\Gamma;;\Phi;;\Xi;;\Psi;\vdash \texttt{type}\ lab \rightsquigarrow \texttt{type}\ lab{::}\texttt{Type} \dashv \cdot}$$

trn
$$\frac{\Gamma;;\Phi;;\Xi;;\Psi;\vdash \hat{\tau} \;\Rightarrow\; \kappa \rightsquigarrow \tau \dashv \Delta;}{\Gamma;;\Phi;;\Xi;;\Psi;\vdash \texttt{type}\ lab{::}\hat{\tau} \rightsquigarrow \texttt{type}\ lab{::}\kappa \dashv \Delta;}$$

val
$$\frac{\Gamma;;\Phi;;\Xi;;\Psi;\vdash \hat{\tau} \;\Rightarrow\; \kappa \rightsquigarrow \tau \dashv \Delta;}{\Gamma;;\Phi;;\Xi;;\Psi;\vdash \texttt{val}\ lab{:}\hat{\tau} \rightsquigarrow \texttt{val}\ lab{:}\tau \dashv \Delta;}$$

mod
$$\frac{\Gamma;;\Phi;;\Xi;;\Psi;\vdash \hat{\sigma} \;\Rightarrow\; \xi \rightsquigarrow \sigma \dashv \Delta;}{\Gamma;;\Phi;;\Xi;;\Psi;\vdash \texttt{module}\ lab{:}_{\mu}\hat{\sigma} \rightsquigarrow \texttt{module}\ lab{:}_{\mu}\sigma \dashv \Delta;}$$

`we're going to need HOFunctors so we don't need to preclude users from typing a functor into a module and vice versa`

$\boxed{\Phi;;\Xi;;\Psi;\vdash \hat{\sigma} \;\Rightarrow\; \xi \rightsquigarrow \sigma \dashv \Delta;}$ $\hat{\sigma}$ synthesizes signature kind ξ and elaborates to σ with hole context Δ;

SynSigEmptyHole
$$\frac{}{\Phi;;\Xi;;\Psi;\vdash (\!|\,|\!)^{\mathtt{uu}} \;\Rightarrow\; \texttt{SigKHole} \rightsquigarrow (\!|\,|\!)^{\mathtt{uu}} \dashv u{::}_{\sigma}\texttt{SigKHole}}$$

SynSigNonEmptyHole

$\boxed{\Phi;;\Xi;\vdash \hat{\sigma} \;\Leftarrow\; \xi \rightsquigarrow \sigma \dashv \Delta;}$ $\hat{\sigma}$ analyzes against signature kind ξ and elaborates to σ with hole context Δ;

misc functions

$$\mathsf{val}(sdec) = \begin{cases} lab{:}\tau & sdec = \texttt{val}\ lab{:}\tau \\ \cdot & \text{otherwise} \end{cases}$$

$$\mathsf{type}(cntxts, sdec) = \begin{cases} lab{::}\kappa & sdec = \texttt{type}\ lab{::}\kappa \\ \cdot & \text{otherwise} \end{cases}$$

$$\mathsf{submodule}(sdec) = \begin{cases} lab{:}_{\mu}\sigma & sdec = \texttt{module}\ lab{:}_{\mu}\sigma \\ \cdot & \text{otherwise} \end{cases}$$

$$\mathtt{S}_{\mathtt{Type}}(\tau) := \mathtt{S}(\tau)$$
$$\mathtt{S}_{\mathtt{S}(\tau_1)}(\tau) := \mathtt{S}(\tau)$$
$$\mathtt{S}_{\mathtt{KHole}}(\tau) := \mathtt{KHole}$$

theorems

Kind Synthesis Precision

If cntxts $\vdash \tau \;\Rightarrow\; \kappa$ then $\forall \kappa_1 . \Delta; \Phi; \Xi; \Psi \vdash$ cntxts::$\kappa \tau \kappa_1 \implies \Delta; \Phi; \Xi; \Psi; \vdash$ cntxts $\lesssim \kappa \kappa_1$