

# Approaching high shear measurement precision on the noisy images

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## ABSTRACT

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### 1. INTRODUCTION

### 2. THE FOURIER\_Quad METHOD

Fourier\_Quad method measures the shear estimators on the 2D power spectrum of the galaxy image in Fourier space. The shear estimators are defined as:

$$\begin{aligned} G_1 &= -\frac{1}{2} \int d^2\vec{k} (k_x^2 - k_y^2) T(\vec{k}) M(\vec{k}) \\ G_2 &= - \int d^2\vec{k} k_x k_y T(\vec{k}) M(\vec{k}) \\ N &= \int d^2\vec{k} \left[ k^2 - \frac{\beta^2}{2} k^4 \right] T(\vec{k}) M(\vec{k}) \end{aligned} \quad (1)$$

where  $\vec{k}$  is the wave vector.

$$\begin{aligned} M(\vec{k}) &= \left| \tilde{f}^S(\vec{k}) \right|^2 - F^S - \left| \tilde{f}_N^B(\vec{k}) \right|^2 + F^B \\ F^S &= \frac{\int_{|\vec{k}| > k_c} d^2\vec{k} \left| \tilde{f}^S(\vec{k}) \right|^2}{\int_{|\vec{k}| > k_c} d^2\vec{k}}, \quad F^B = \frac{\int_{|\vec{k}| > k_c} d^2\vec{k} \left| \tilde{f}_N^B(\vec{k}) \right|^2}{\int_{|\vec{k}| > k_c} d^2\vec{k}}, \end{aligned} \quad (2)$$

average & PDF\_SYM approach

### 3. THE PDF\_SYM APPROACH IN FOURIER\_Quad METHOD

#### 3.1. Noise bias from the faint galaxy

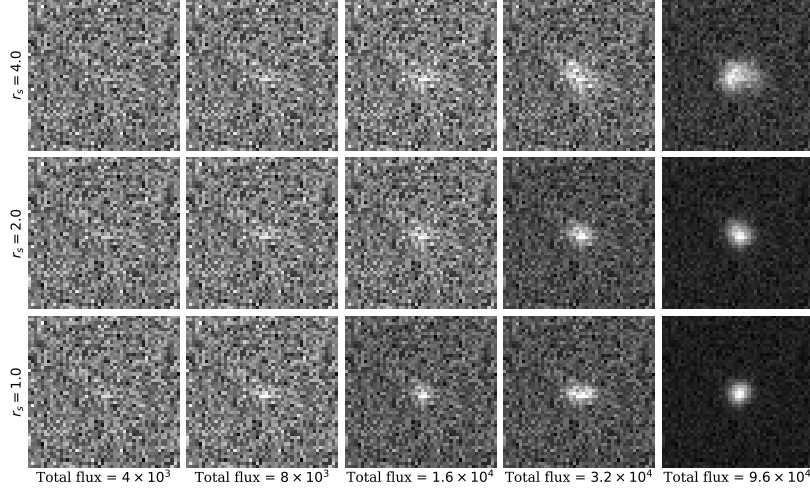
##### 3.1.1. Galaxy simulation

We use two types of galactic profiles in our image simulation to represent the regular galaxies and the irregular ones. We use Galsim (Rowe et al. 2015), an open source image simulation toolkit, to simulate the regular galaxies. The irregular galaxies are generated by the random walk method (Zhang 2008). We use 40 shear points range from  $-0.04$  to  $0.04$ , and generate  $8 \times 10^6$  galaxies for each shear point. For both type of galaxies, the stamp size is  $44 \times 44$  pixels.

##### 3.1.2. Point-source galaxies

##### 3.1.3. Galsim galaxies

We adopt a pure deVaucouleurs profile for the Galsim galaxies.



**Figure 1.** Sample of point-source galaxies. We fix the standard deviation of the background noise at 60.

#### 3.1.4. Multiplicative bias & Additive bias

We generate 15 datasets, including 5 SNRs and 3 galactic radii, for each type of galaxy to investigate the bias of shear measurement at different SNR and galactic size. We change the total flux of galaxy to achieve different SNRs. To test the additive bias, we generate the galaxy sample using isotropic and anisotropic PSF ( $e_1 = 0.1$ ,  $e_2 = 0$ ) respectively.

In figure 4, we present the multiplicative and additive bias from both average and PDF\_SYM approach. We find that the average approach, as the Eq() shows, gives an unbiased shear estimate. The multiplicative and additive bias are well consistent with zero even in the faintest sample of which the galaxies are hardly identified. However, we find the bias from PDF\_SYM approach varies with SNR and galactic morphology. The bias will be enlarged by the lower SNR or small galaxy size. Both multiplicative and additive bias vanish in the brightest sample. It should be noted that both approaches give unbiased shear estimate for the noise free image.

To find the origin of the bias in PDF\_SYM approach, we divide the noisy galaxy image into two components, *i.e.*, the noise free galaxy image (GI, hereafter) and the background noise image (NI, hereafter). Therefore, the power spectrum of the galaxy image can be written as

$$\left| \tilde{f}^S(\vec{k}) \right|^2 = \left| \tilde{f}_G^S(\vec{k}) \right|^2 + \left| \tilde{f}_N^S(\vec{k}) \right|^2 + \tilde{f}_G^S(\vec{k}) \tilde{f}_N^S(\vec{k})^* + \tilde{f}_G^S(\vec{k})^* \tilde{f}_N^S(\vec{k}), \quad (3)$$

where the  $\tilde{f}_G^S(\vec{k})$  is the Fourier transform of GI, and the  $\tilde{f}_N^S(\vec{k})$  is the Fourier transform of NI. Then, we re-write the modified galaxy image power as the summation of three parts, the power spectrum of the GI ( $\left| \tilde{f}_G^S(\vec{k}) \right|^2$ , FGI), the difference between the power spectrum of NI and that of the neighboring background noise image ( $\left| \tilde{f}_N^S(\vec{k}) \right|^2 - \left| \tilde{f}_N^B(\vec{k}) \right|^2$ , DNI), and the mixture term ( $\tilde{f}_G^S(\vec{k}) \tilde{f}_N^S(\vec{k})^* + \tilde{f}_G^S(\vec{k})^* \tilde{f}_N^S(\vec{k})$ , FMI) due to the Fourier transform.

$$M(\vec{k}) = \left| \tilde{f}_G^S(\vec{k}) \right|^2 + \Delta \left| \tilde{f}_N(\vec{k}) \right|^2 + \tilde{f}_G^S(\vec{k}) \tilde{f}_N^S(\vec{k})^* + \tilde{f}_G^S(\vec{k})^* \tilde{f}_N^S(\vec{k}), \quad (4)$$

where  $\Delta \left| \tilde{f}_N(\vec{k}) \right|^2$  is DNI term. We have dropped the terms estimates the Poission noise power spectrum of the source and noise image ( $F_S$  and  $F_B$ ), because we find the Poission noise here would not change the result. Then, we run measurement on FGI, FGI+DNI, and FGI+FMI respectively. The FMI term is found to bias the measurement in the noisy samples significantly. Figure 3 shows the results from the PDF\_SYM approach.

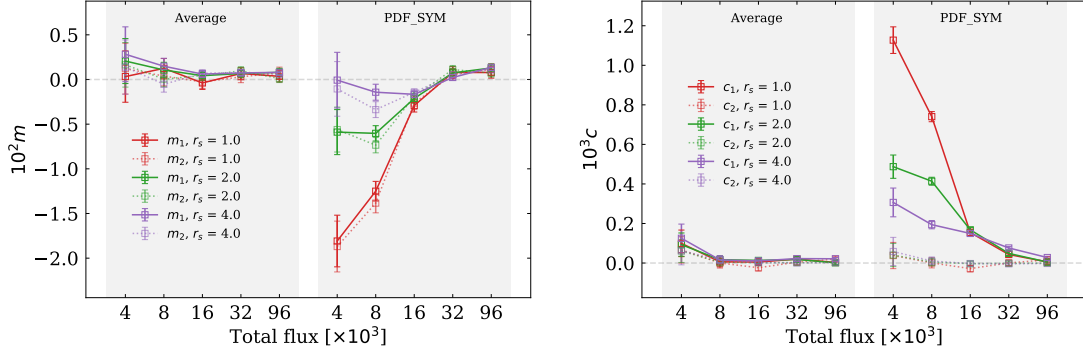
The FMI term,  $\tilde{f}_G^S(\vec{k}) \tilde{f}_N^S(\vec{k})^* + \tilde{f}_G^S(\vec{k})^* \tilde{f}_N^S(\vec{k})$ , contains the Fourier transform of galaxy image,  $\tilde{f}_G^S(\vec{k})$ , rather than the power spectrum,  $\left| \tilde{f}_G^S(\vec{k}) \right|^2$ . Therefore, the shear estimators measured from FMI compared with that from FGI would become negligible in the shear estimation when the galaxy has very high SNR. However, when the brightness of the galaxy decreases to a certain level, the bias due to FMI would become significant. In the deconvolution process, the image power spectrum is divided by the power spectrum of PSF,  $\left| \tilde{W}_{PSF}(\vec{k}) \right|^2$ . For the FMI term, the deconvolution

operation would leave the imprint of the anisotropy of PSF on the image power spectrum. Therefore, the asisotropic PSF would give rise to the additive bias in the faint sample.

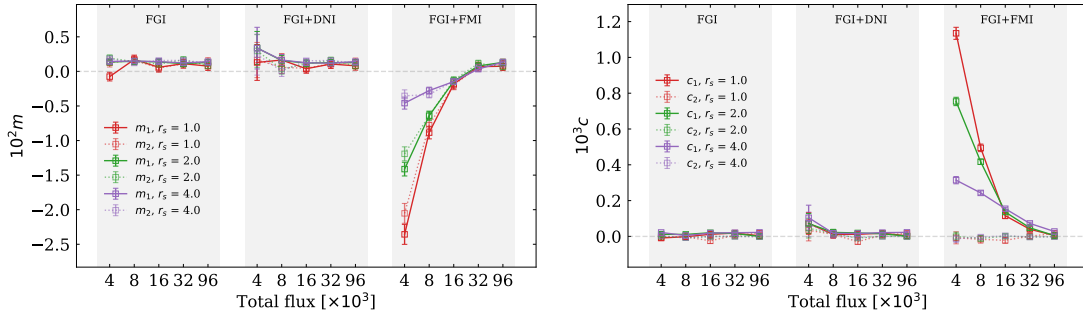
show the bias & origin of the bias

average method & PDF\_SYM method

Galsim & point source galaxy



**Figure 2.** The shaded areas show the multiplicative and additive bias measured by average and PDF\_SYM approach respectively. We use a slightly sheared PSF ( $e_1 = 0.1, e_2 = 0$ ) to show the effect of the PSF anisotropy. The measurement of the PDF\_SYM approach would be biased by the small and faint galaxies.



**Figure 3.** Multiplicative and additive bias measured from different components of the galaxy power spectrum by the PDF\_SYM approach. The measurement is biased by FMI which is the mixture of the power spectrum of galaxy image and that of the background noise.

power of the galaxy, the noise residual and the galaxy-noise crossing term.

bias depends on SNR and morphology

### 3.2. Improving the statistics towards sub-percent precision

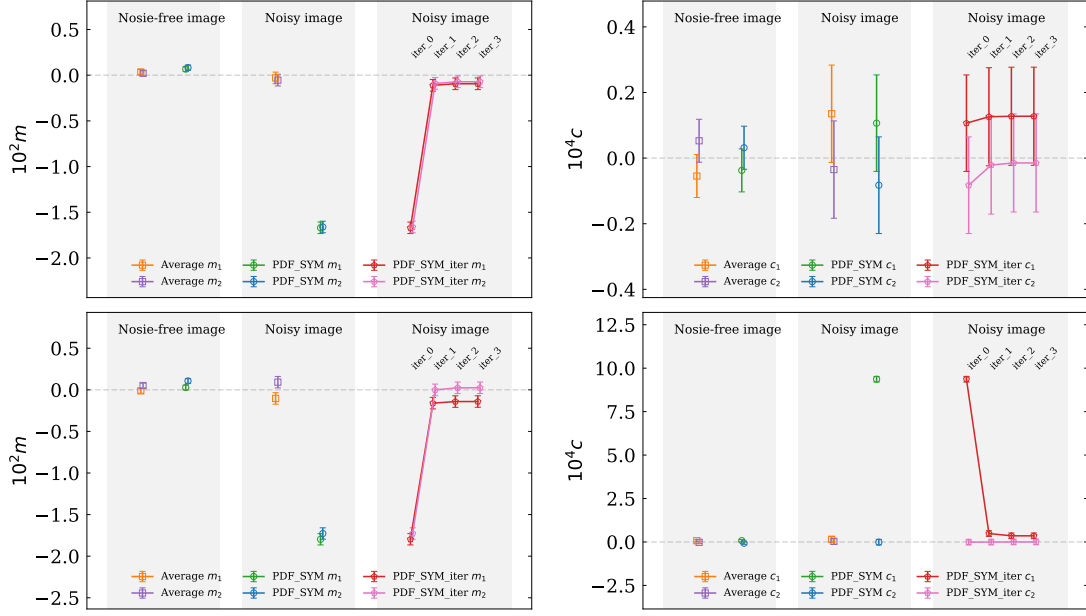
gN & gU

## 4. CONCLUSION

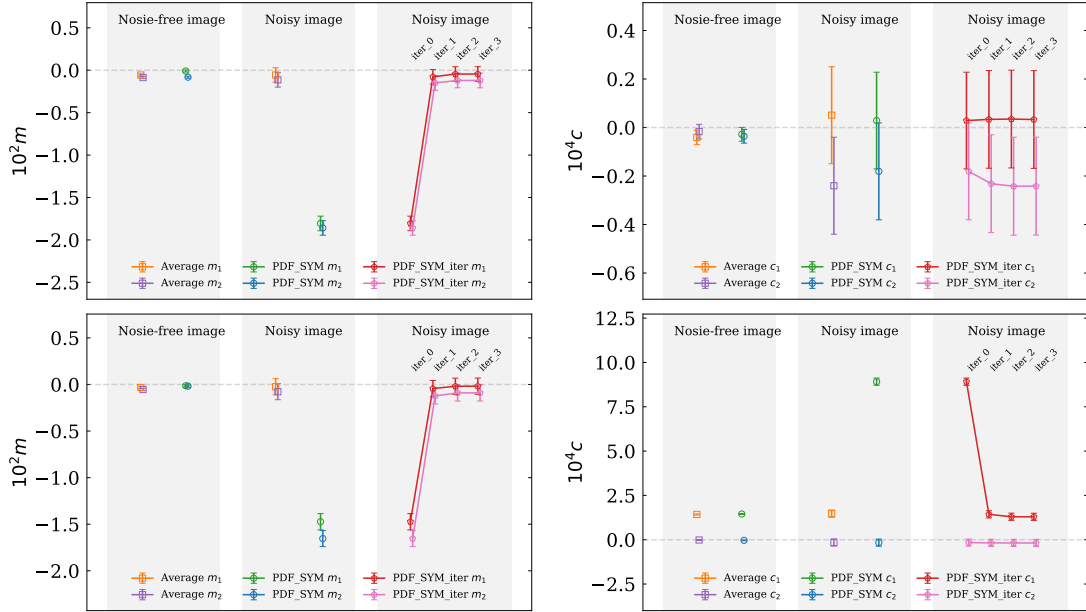
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**Figure 4.**  $8 \times 10^6$  Random walk galaxies. Aisotropic PSF ( $e_1 = 0.1, e_2 = 0$ )



**Figure 5.**  $4 \times 10^7$  galsim galaxies.