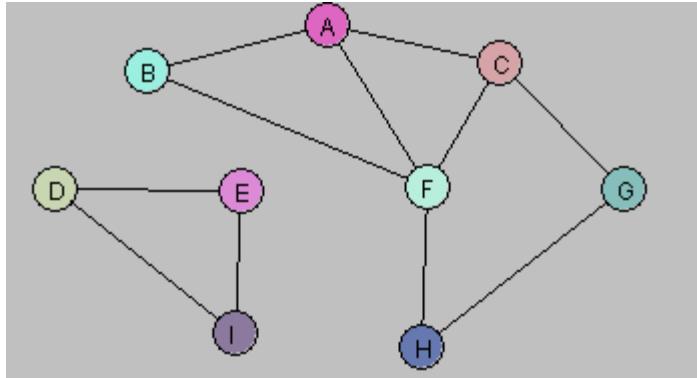


Lab W3D3

Question 1. Induced Graphs. Answer questions about the graph $G = (V, E)$ displayed below.



- A. Let $U = \{A, B\}$. Draw $G[U]$.

$$A \text{---} B$$

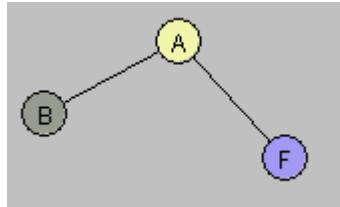
- B. Let $W = \{A, C, G, F\}$. Draw $G[W]$.

$$\begin{array}{c} A \\ \wedge \\ C \text{---} F \\ | \\ G \end{array}$$

- C. Let $Y = \{A, B, D, E\}$. Draw $G[Y]$.

$$A \text{---} B \qquad D \text{---} E$$

- D. Consider the following subgraph H of G :



Is there a subset X of the vertex set V so that $H = G[X]$? Explain.

A: There is no subset X of V such that $H = G[X]$. In the subgraph H , the vertices are $\{A, B, F\}$ and the only edges shown are $A \text{---} B$ and $A \text{---} F$. However, in the original graph G , there is also an edge between B and F .

E. Find a way to partition the vertex set V into two subsets V_1, V_2 so that each of the induced graphs $G[V_1]$ and $G[V_2]$ is connected and $G = G[V_1] \cup G[V_2]$.

Question 2. The following graph has a Hamiltonian cycle. Find it.

