

Question 2.

(a) $A = \{1, 2, 3, 4, 5, 6, 7, 8, 9\}$

Steps:

- Triple $\{1, 5, 9\} \rightarrow \text{pivot} = 5$
- Partition: $L = [1, 2, 3, 4] \mid E = [5] \mid G = [6, 7, 8, 9]$
- Recursion: $\text{QuickSort}(L)$ and $\text{QuickSort}(G)$

Sub-Array $L = [1, 2, 3, 4]$

- Triple $\{1, 2, 4\} \rightarrow \text{pivot} = 2$

• Partition:

$$L = [1] \mid E = [2] \mid G = [3, 4]$$

left side solved, recurse in $G([3, 4])$

- $G([3, 4])$: triple $\{3, 3, 4\} \rightarrow \text{pivot} = 3$

$$[] \mid [3] \mid G = [4] \rightarrow \text{done}$$

Subtree $G = [6, 7, 8, 9]$:

- Triple $\{6, 7, 9\} \rightarrow \text{pivot} = 7$

• Partition:

$$[6] \mid [7] \mid G = [8, 9]$$

recurse in $G([8, 9])$

- Triple $\{8, 8, 9\} \rightarrow \text{pivot} = 8$

$$[] \mid [8] \mid [9]$$

Result: $[1, 2, 3, 4, 5, 6, 7, 8, 9]$

Question 2

(b) $A = \{8, 7, 6, 5, 4, 3, 2, 1, 9\}$

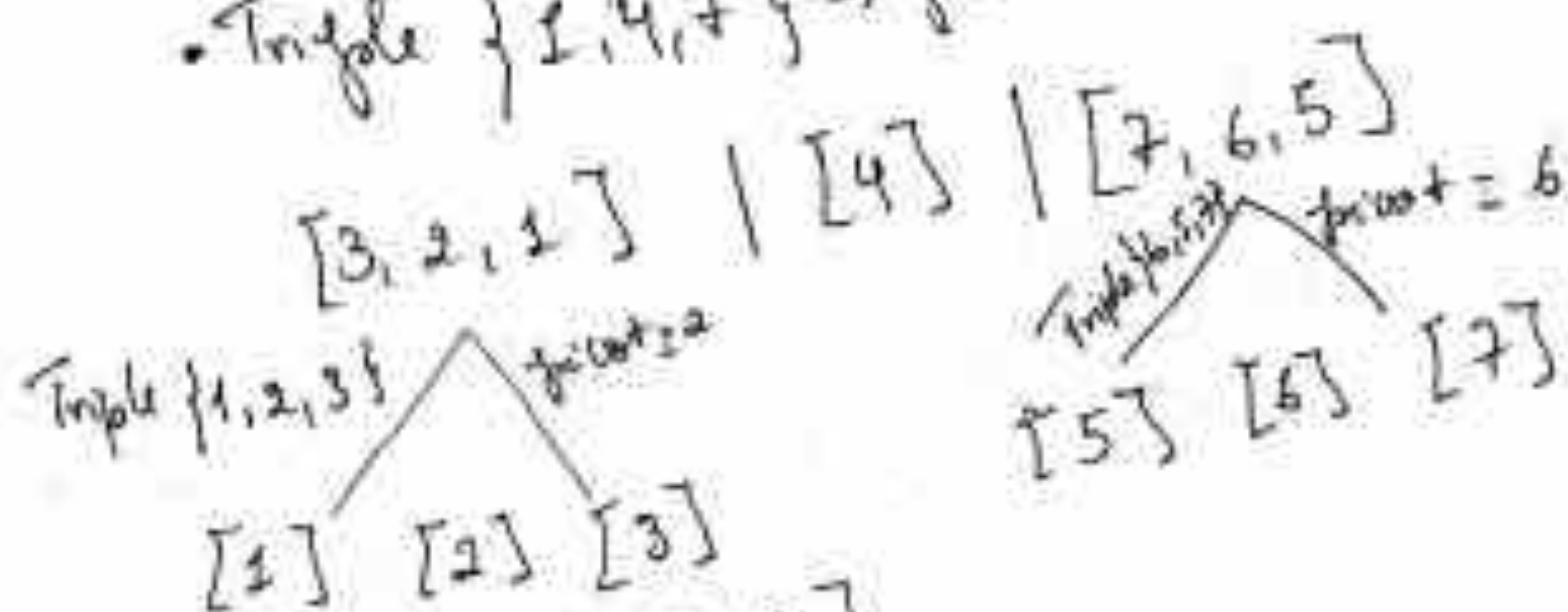
• triple $\{4, 8, 9\}$ pivot = 8

• Partition:

$L = [7, 6, 5, 4, 3, 2, 1] \mid E = [8] \mid G = [9]$

• Recursion: QuickSort $L([7, 6, 5, 4, 3, 2, 1])$

• Triple $\{1, 4, 7\} \rightarrow \text{pivot} = 4$



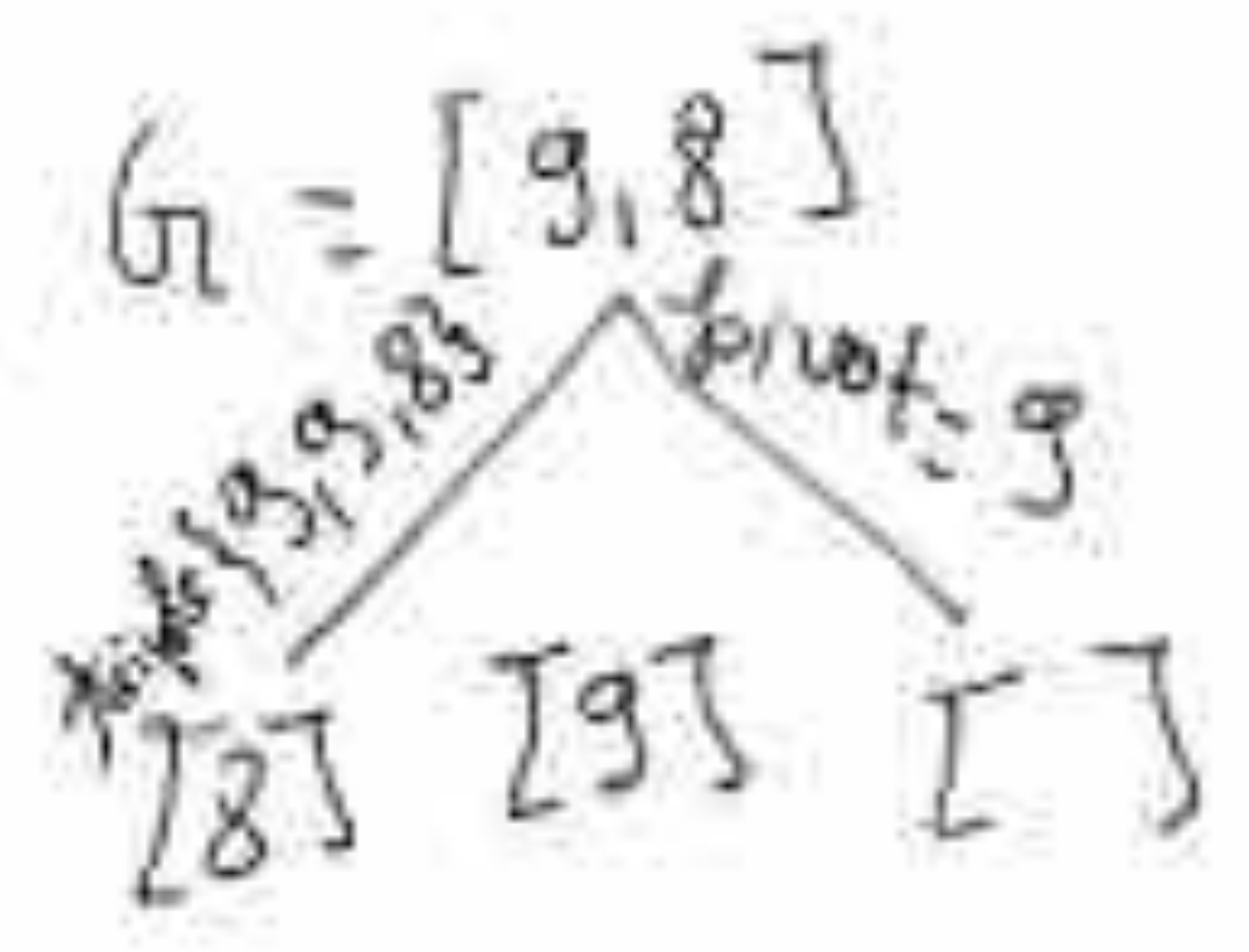
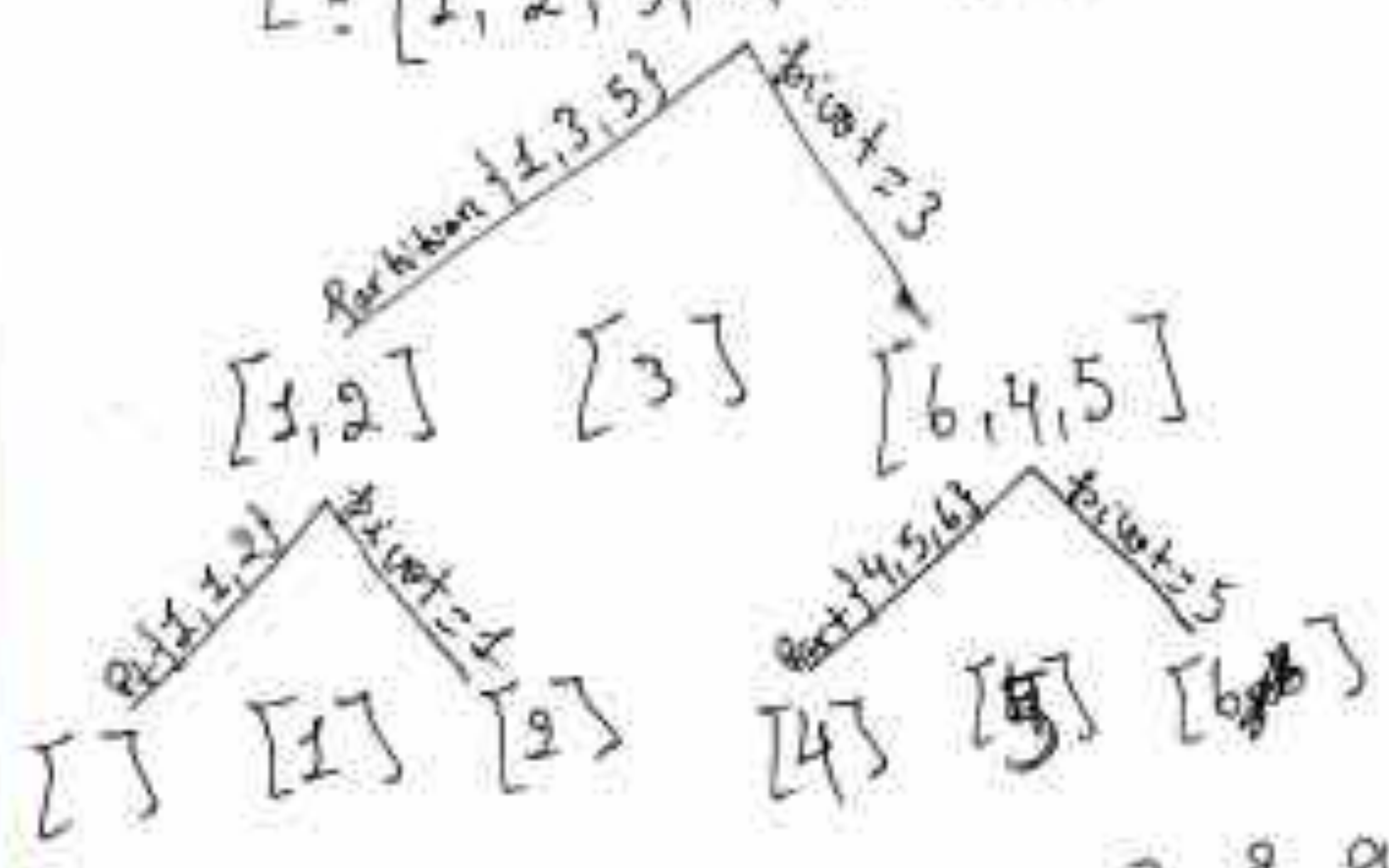
Result: $[1, 2, 3, 4, 5, 6, 7, 8, 9]$

Question 2

(c) $A = \{9, 1, 8, 2, 7, 3, 6, 4, 5\}$

triple $\{5, 7, 9\} \rightarrow \text{pivot} = 7$

$L = [1, 2, 3, 6, 4, 5] \mid E = [7] \mid G = [9, 8]$



Result: $[1, 2, 3, 4, 5, 6, 7, 8, 9]$