

Q1 Adjacency Matrix

A	B	C	D	E	F	G	H	I
0	1	1	1	0	0	0	0	0
1	0	1	0	0	1	0	1	0
2	1	1	0	1	1	2	0	0
3	1	0	2	0	1	0	0	2
4	0	0	1	1	0	1	2	0
5	0	1	1	0	1	0	1	0
6	0	0	0	1	1	0	2	1
7	0	1	0	0	0	1	2	0
8	0	0	1	0	0	1	1	0

Q2 Find the shortest path from A to all other vertices using Dijkstra's Algorithm

$$\text{1. } A \left\{ \begin{array}{l} A-B: 22 \\ A-C: 9 \\ A-D: 12 \end{array} \right.$$

$$\text{2. } C \left\{ \begin{array}{l} C-B: 13 \\ C-E: 24 \\ C-F: 51 \end{array} \right.$$

$$\text{6. } F \left\{ \begin{array}{l} F-G: 30 \\ F-H: 25 \end{array} \right.$$

$$\text{4. } B \left\{ \begin{array}{l} B-C: 57 \\ B-F: 58 \\ B-H: 56 \end{array} \right.$$

$$\text{3. } D \left\{ \begin{array}{l} D-E: 45 \\ D-I: 42 \end{array} \right.$$

$$\text{8. } G \left\{ \begin{array}{l} G-H: 33 \\ G-I: 89 \end{array} \right.$$

$$\text{5. } E \left\{ \begin{array}{l} E-F: 63 \\ E-G: 68 \end{array} \right.$$

$$\text{7. } H \left\{ \begin{array}{l} H-I: 75 \end{array} \right.$$

(4) • I

dis:

A	B	C	D	E	F	G	H	I
0	22	9	12	45	51	68	56	42

path: A → B → C → D → E → F → G → H → I
 $\{ \}$ {A-B} {A-C} {A-D} {A-E} {A-F} {A-G} {A-H} {A-I}

Q3 What is the time complexity?

Q4 Find a minimum spanning tree using Kruskal's Algorithm

L-₂ $\left\{ \begin{array}{l} (c, g)_{2}, (A, C), (E, F), (H, I), (\cancel{G, I})^{21}, (G, I)^{22}, (A, B)^{23}, (E, G)^{24}, (F, H)^{25} \\ (B, I)^{20}, (B, E)^{21}, (B, H)^{24}, (B, C)^{25}, (B, F)^{23}, (F, G)^{22}, (C, F)^{25}, (C, E)^{25} \end{array} \right.$

Union-Final: {A}, {B}, {C}, {D}, {E}, {F}, {G}, {H}, {I}

$$\Rightarrow n = 9 \\ MST \text{ edges} = 9 - 1 = 8$$

pick(C, D) \Rightarrow find(C) \neq find(D). Union(C, D)

{A}, {B}, {C, D}, {E}, {F}, {G}, {H}, {I}

pick(A, C) \Rightarrow find(A) \neq find(C). Union(A, C)

{A, C, D}, {B}, {E}, {F}, {G}, {H}, {I}

pick(E, F) \Rightarrow find(E) \neq find(F). Union(E, F)

{A, C, D}, {B}, {E, F}, {G}, {H}, {I}

pick(H, I) \Rightarrow find(H) \neq find(I). Union(H, I)

{A, C, D}, {B}, {E, F}, {G}, {H, I}

pick(G, I) \Rightarrow find(G) \neq find(I). Union(G, I)

{A, C, D}, {B}, {E, F}, {G, H, I}

pick(A, B) \Rightarrow find(A) \neq find(B). Union(A, B)

{A, B, C, D}, {E, F}, {G, H, I}

pick(E, G) \Rightarrow find(E) \neq find(G). Union(E, G)

{A, B, C, D}, {E, F, G, H, I}

pick(B, I) \Rightarrow find(B) \neq find(I). Union(B, I)

{A, B, C, D, E, F, G, H, I} // we can stop here since we have $n-1$ edges