

## Day 3, Lecture 1

# Longitudinal data structures and time-dependent treatment decisions

# Overview of course: Day 3

Day 3: 8 – 10

Time-dependent treatment decisions. Causal inference in longitudinal data.

- ▷ Treatment-confounder feedback.

Day 3: 10 – 12

Longitudinal TMLE. Targeting for time-varying structures.

- ▷ Identification proofs and extension of the time-fixed setting.
- ▷ Software: `ltmle`.

Lunch.

Day 3: 13 – 15

Evaluation + "buffer".

# Longitudinal data structures

## Lecture 1 What are we targeting?

- ▶ Time-varying treatment interventions.
- ▶ Identification and time-dependent confounding.
- ▶ An introduction to get started with Lecture 2.

## Lecture 2 TMLE for estimation

- ▶ IP-weighting + G-formula.
- ▶ Iterated expectations representation.
- ▶ Targeting effects of time-varying treatment interventions.
- ▶ `ltmle` software package

## Observational studies analyzed like randomized experiments: an application to postmenopausal hormone therapy and coronary heart disease

Miguel A. Hernán<sup>1,2</sup>, Alvaro Alonso<sup>3</sup>, Roger Logan<sup>1</sup>, Francine Grodstein<sup>1,4</sup>, Karin B. Michels<sup>1,4,5</sup>, Meir J. Stampfer<sup>1,4,6</sup>, Walter C. Willett<sup>1,4,6</sup>, JoAnn E. Manson<sup>1,4,7</sup>, and James M. Robins<sup>1,8</sup>

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### Abstract

**Background**—The Women's Health Initiative randomized trial found greater coronary heart disease (CHD) risk in women assigned to estrogen/progestin therapy than in those assigned to placebo. Observational studies had previously suggested reduced CHD risk in hormone users.

**Methods**—Using data from the observational Nurses' Health Study, we emulated the design and intention-to-treat (ITT) analysis of the randomized trial. The observational study was conceptualized as a sequence of "trials" in which eligible women were classified as initiators or noninitiators of estrogen/progestin therapy.

## Hernán et al., 2008 (part 1/2)

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(and the general difficulties in analyzing observational studies).

### Background for the paper:

- ▶ An RCT found **greater** risk of coronary heart disease (CHD) in women assigned to hormone therapy than those assigned to placebo.
- ▶ Earlier observation studies had found **reduced** risk of CHD among hormone users.

The difference has been explained as due to unobserved confounding.

Conclusion: *Cannot use observational data for causal inference?*

The **RCT results** were based on an intention-to-treat (ITT)<sup>1</sup> analysis

- ▶ trial participants were randomized to hormone treatment initiation or placebo at baseline

---

<sup>1</sup>Subjects are analyzed irrespective of their actual adherence to their assigned randomization arm.

The **RCT results** were based on an intention-to-treat (ITT)<sup>1</sup> analysis

- ▶ trial participants were randomized to hormone treatment initiation or placebo at baseline

Whereas the **observational analyses** were based on a comparison of two groups:

- ▶ "Current users"
- ▶ "Never users"

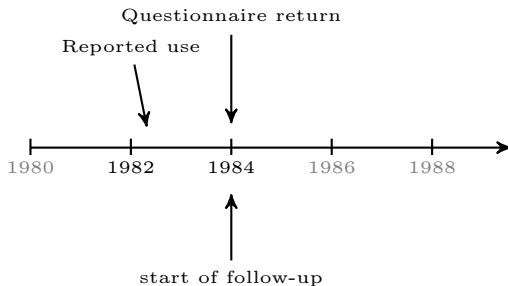
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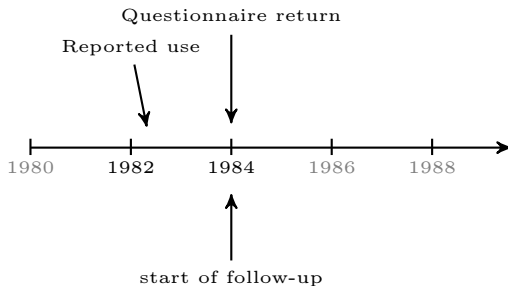
- ▶ In the observational study, women answered questionnaires every two years
  - ▶ updated information on use, duration, etc, of treatment



- ▶ The start of follow-up was defined as the return of the questionnaire
  - ▶ initiators who stopped/died before return were excluded (to define "current-users")

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**Selection bias:** Early (harmful) effect of treatment **not identified**.

## Hernán et al., 2008 (part 1/2)

Hernán et al. reanalyze the observational data and show in their paper that:

1. When using the current user design (including the selection bias), the result of a **beneficial** effect from earlier observational studies was reproduced.
2. *When imitating the analysis of the randomized trial*, targeting the ITT effect, the result that the treatment has a **harmful** effect was reproduced.

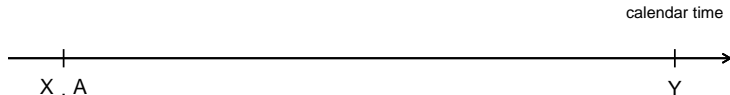
The discrepancy found in the previous analyses had nothing to do with confounding.

# Causal inference for longitudinal data structures

## New setting: Longitudinal data structure

Data structure considered so far:

- ▶  $O = (X, A, Y) \in \mathbb{R}^d \times \{0, 1\} \times \{0, 1\}$
- ▶ Covariates  $X$  are measured before treatment decision  $A$  is made
- ▶ After treatment decision  $A$ , the outcome  $Y$  is observed



## New setting: Longitudinal data structure

### Longitudinal data structure:

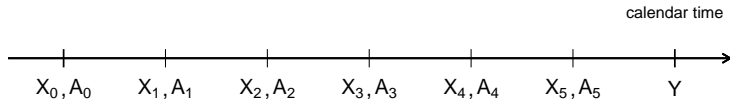
- ▶  $O = (X_0, A_0, X_1, A_1, \dots, X_K, A_K, Y = X_{K+1}) \in (\mathbb{R}^d \times \{0, 1\})^K \times \{0, 1\}$
- ▶ Covariates  $X = (X_0, X_1, \dots, X_K)$  change over time
- ▶ Treatment decisions  $A = (A_0, A_1, \dots, A_K)$  are updated over time
- ▶ Covariates and treatment decisions interact in complex ways



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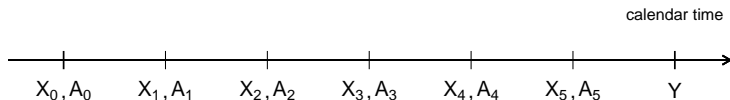


1. More complex treatment interventions.
  2. More subtleties in confounding bias.
  3. Right-censoring and competing risks.
- ⋮

# Longitudinal data structure

This data structure matches quite well the data collected in a **randomized clinical trial** with follow-up visits:

- ▶  $X_0$  are baseline covariates (age, sex, disease/medical history, ...)
- ▶  $A_0$  tells us the randomization arm (treatment/placebo)
- ▶  $\vdots$
- ▶  $X_k$  are covariates measured at the  $k$ th follow-up visit
- ▶  $A_k$  is the treatment decision made at the  $k$ th follow-up visit (adherence to randomization arm)
- ▶  $\vdots$
- ▶ Final outcome  $Y$

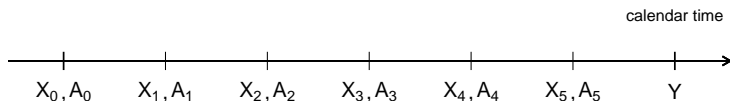




# Longitudinal data structure (sidenote #1)

When data is not randomized (i.e., **observational**).

- ▶ the time-grid data structure may be a bit artificial;<sup>2</sup>
- ▶ but otherwise the difference mostly consists in the randomized treatment decision at baseline.



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<sup>2</sup>There may be more data modeling choices to make it fit nice structure.

## Longitudinal data structure (sidenote #2)

Over the course of time of a study, we may not be able to observe the outcome of interest due to:

**Loss to follow-up (right-censoring)** For some individuals the event of interest is not known.

**Presence of competing risk events** No one cannot get experience the outcome event of interest if they already died.

How we handle these complications is reflected in our

- ▶ formulation of causal parameter;
- ▶ formulation of ideal interventions.

## Longitudinal data structure (sidenote #2)

**Example:** Trial comparing treatment versus placebo on survival chances.

Causal question *What is the effect of the treatment?*

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**Causal question** *What is the effect of the treatment?*

- ▶ Patients experiencing deteriorating health conditions are more prone to drop out.
- ▶ Patients randomized to placebo experience worse health conditions.



**Causal question** *What is the effect of the treatment **had there been no loss to follow-up?***

- ▶ Intervention strategy: Treatment + **prevent loss to follow-up.**
- ▶ Control strategy: Placebo + **prevent loss to follow-up.**

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**Causal question** *What is the effect of the treatment?*

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A hypothetical world where subjects cannot die is a weird world.



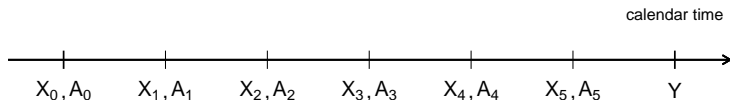
## Longitudinal data structure (sidenote #2)

- ▶ Whenever the outcome of interest is not all-cause mortality, there can be competing risks.
- ▶ A competing risk event is not a right-censoring event.
- ▶ We are not (rarely?) interested in reporting the treatment effect *if subjects could not die*.

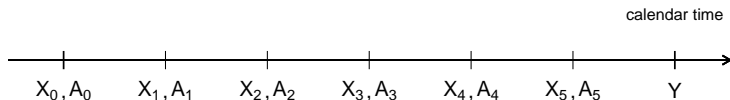
# Longitudinal data structure

We consider (for now) the case that  $Y$  is fully observed:

- ▶ no right-censoring.
- ▶ no competing risks.



# Time-dependent treatment interventions



*What effect are we targeting?*

Counterfactual outcomes

$$Y^{A_0=a_0^*, A_1=a_1^*, \dots, A_K=a_K^*}, \quad \text{for,} \quad a_0^*, \dots, a_K^* \in \{0, 1\}$$

= defined by a sequence of treatment decision rules that we choose.

also called:

- ▶ hypothetical treatment **interventions**
- ▶ hypothetical treatment **strategies**
- ▶ hypothetical treatment **regimes**

# Time-dependent treatment interventions

## Continued treatment and never treated:

- ▶  $Y^{A_0=1, A_1=1, \dots, A_K=1}$  = outcome if treated throughout follow-up
- ▶  $Y^{A_0=0, A_0=0, \dots, A_K=0}$  = outcome if untreated throughout follow-up

The risk difference

$$\mathbb{E}[Y^{A_0=1, A_1=1, \dots, A_K=1}] - \mathbb{E}[Y^{A_0=0, A_0=0, \dots, A_K=0}]$$

is the effect of being treated versus untreated throughout follow-up.

# Time-dependent treatment interventions

## Intention-to-treat (ITT):

- ▶  $Y^{A_0=1}$  = outcome if assigned to treatment arm
- ▶  $Y^{A_0=0}$  = outcome if assigned to placebo arm

The risk difference

$$\mathbb{E}[Y^{A_0=1}] - \mathbb{E}[Y^{A_0=0}]$$

is the effect of being assigned to the treatment versus the placebo arm

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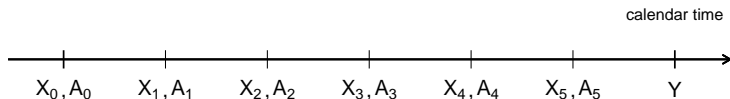
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The current user strategy is an attempt to estimate the effect of treatment *usage* (contrary to initiation)?

- ▶ Most appropriate summary measure would be the adherence-adjusted effect (comparing 'always treated' to 'never treated')?

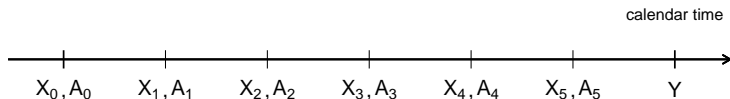
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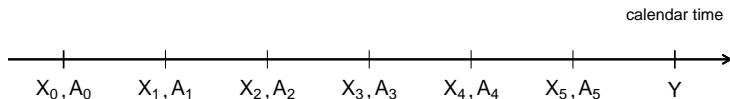
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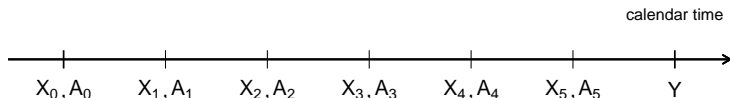
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- ▶ ITT treatment strategies:
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- ▶ ITT treatment strategies:
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  2. Control strategy  $A_0 = 0$
- ▶ Enforcing continued exposure (adherence-adjusted):
  1. Intervention strategy  $A_0 = 1, A_1 = 1, A_2 = 1, \dots$
  2. Control strategy  $A_0 = 0, A_1 = 0, A_2 = 0, \dots$

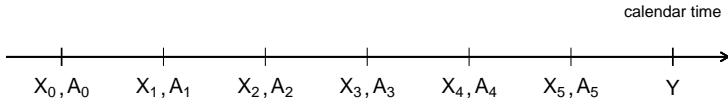
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2. When imitating the analysis of the randomized trial, targeting the ITT effect, the result that the treatment has a **harmful** effect was reproduced.
3. A **larger harmful** effect was found when targeting the effect of 'continued exposure', i.e., the adherence-adjusted effect.

# Identification of effects of time-dependent treatment interventions





# Time-dependent treatment interventions

Identification of  $\mathbb{E}[Y^{A_0=a_0^*, A_1=a_1^*, \dots, A_K=a_K^*}]$ .

1. Consistency:  $Y^{A_0=a_0^*, A_1=a_1^*, \dots, A_K=a_K^*} = Y$

if  $A_k = a_k^*$  for  $k = 0, 1, \dots, K$

2. Exchangeability:  $Y^{A_0=a_0^*, A_1=a_1^*, \dots, A_K=a_K^*} \perp\!\!\!\perp A_k \mid \bar{X}_k, \bar{A}_{k-1}$

for  $k = 0, 1, \dots, K$

3. Positivity: 
$$\prod_{k=0}^K \frac{1\{A_k = a_k^*\}}{P(A_k = a_k^* \mid \bar{X}_k, \bar{A}_{k-1})} < \infty$$

for  $k = 0, 1, \dots, K$

Notation for histories of variables:  $\bar{X}_k = (X_0, X_1, \dots, X_k)$ ,  $\bar{A}_k = (A_0, A_1, \dots, A_k)$ .

## Time-dependent treatment interventions

Imposing a static regime, like 'always treat',

$$A_0 = 1, A_1 = 1, \dots, A_K = 1$$

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**Example (Robins 1986)** Effects of exposure of chemicals on employees: Static regimes cannot be identified since subjects can only be exposed when at work.

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may not always be realistic (or even feasible).

**Example (Robins 1986)** Effects of exposure of chemicals on employees: Static regimes cannot be identified since subjects can only be exposed when at work.

**Another example** Development of adverse effects or contraindications (e.g., pregnancy) can force a subject to stop an assigned treatment.

## Time-dependent treatment interventions

But the positivity assumption dictates that the treatment level imposed by the intervention cannot in the observed data be deterministically assigned at any time point based on a subject's observed past.

3. Positivity:

$$\prod_{k=0}^K \frac{1\{A_k = a_k^*\}}{P(A_k = a_k^* \mid \bar{X}_k, \bar{A}_{k-1})} < \infty$$

for  $k = 0, 1, \dots, K$

# Time-dependent treatment interventions

What we can do  $\Rightarrow$  change the question/intervention.

- ▶ 'Expose when at work'
- ▶ 'Treat until adverse event or contraindication happen'
- ▶ 'Initiate antidiabetic treatment when HbA1c level increases beyond some level'

# Time-dependent treatment interventions

## Dynamic treatment regimes

- ▶ A prespecified set of rules which assign treatment over time by responding to a patient's time-varying conditions.

# Time-dependent treatment interventions

## Dynamic treatment regimes

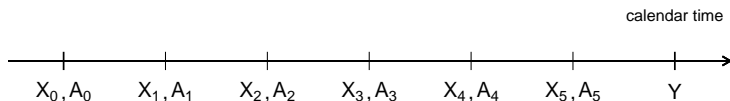
- ▶ A prespecified set of rules which assign treatment over time by responding to a patient's time-varying conditions.
- ▶ Mathematically, defined as function  $\mathcal{S}_k(\bar{X}_k, \bar{A}_{k-1})$  that maps (a subset of) previous covariate/treatment values  $\bar{X}_k, \bar{A}_{k-1}$  to a binary treatment assignment, e.g.,

$$\mathcal{S}_k(\bar{X}_k, \bar{A}_{k-1}) = \begin{cases} 1 & \text{if } X_k > \theta, \\ 0 & \text{if } X_k \leq \theta. \end{cases}$$



# Time-dependent treatment interventions

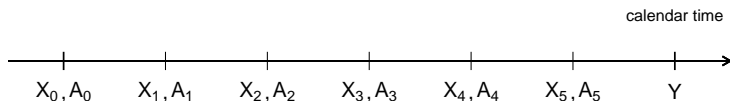
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for  $k = 0, 1, \dots, K$



- ▶  $X_k$  may be affected by earlier treatment decisions  $A_{k-1}, \dots, A_1, A_0$ .
- ▶  $X_k$  may be a confounder for the effect of  $A_k, A_{k+1}, \dots, A_K$  on  $Y$ .

# Time-dependent treatment interventions

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} time-dependent  
confounding

# Time-dependent treatment interventions

In presence of time-dependent confounding, "standard methods" may cause bias

- ▶ Multiple regression
- ▶ Random effects models
- ▶ Time-dependent Cox regression

The problem is that:

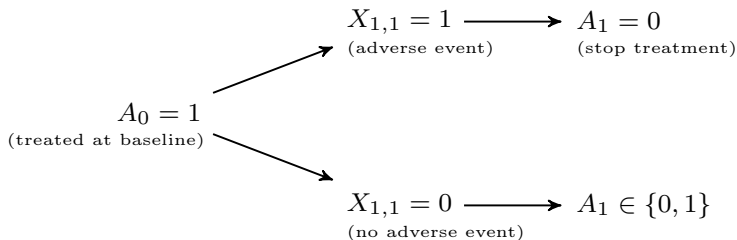
- ▶ If we control for  $X_k$  in our model, we will not capture the effect from earlier treatment decisions  $A_{k-1}, \dots, A_1, A_0$  through  $X_k$ .
- ▶ But we have to control for  $X_k$  to assess the effect of  $A_k, A_{k+1}, \dots, A_K$  on  $Y$ .

# Time-dependent treatment interventions

## A simulation setting

- ▶  $X_{0,1}, X_{0,2}, X_{0,3}$  are baseline covariates.
- ▶  $A_0 \in \{0, 1\}$  is a randomized treatment indicator.
- ▶  $X_{1,1}, X_{1,2}$  are follow-up covariates.
- ▶  $A_1 \in \{0, 1\}$  is a follow-up treatment decision.
- ▶  $Y \in \{0, 1\}$  is the final outcome.

# Time-dependent treatment interventions



- ▶ The variable  $X_{1,1}$  is an indicator of an adverse event from the baseline treatment, an adverse event that causes treated subjects to switch from 'treatment' ( $A_0 = 1$ ) to 'no treatment' ( $A_1 = 0$ ).
- ▶ The variable  $X_{1,2}$  is a marker of being likely to forget to take the medicine (or thinking it is too bothersome) which increases the probability of switching treatment as well.

# Time-dependent treatment interventions

Say we are interested in the effects of different types of interventions:

1. The intention-to-treat (ITT) effect which only sets treatment at baseline and contrasts the two scenarios of being treated at baseline ( $A_0 = 1$ ) and not being treated at baseline ( $A_0 = 0$ ).
2. A static effect of being 'always treated' ( $A_0 = A_1 = 1$ ) and 'never treated' ( $A_0 = A_1 = 0$ ).
3. A dynamic effect of being treated at baseline ( $A_0 = 1$ ) and only treated at follow-up if the adverse event has not happened, i.e.,  $X_{1,1} = 0$  — contrasted to being 'never treated' ( $A_0 = A_1 = 0$ ).

## Time-dependent treatment interventions

The true ITT average treatment effect:

ITT: -0.93%

The true static average treatment effect:

static: -6.33%

The true dynamic average treatment effect:

dynamic: -5.07%

## Time-dependent treatment interventions

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## Time-dependent treatment interventions

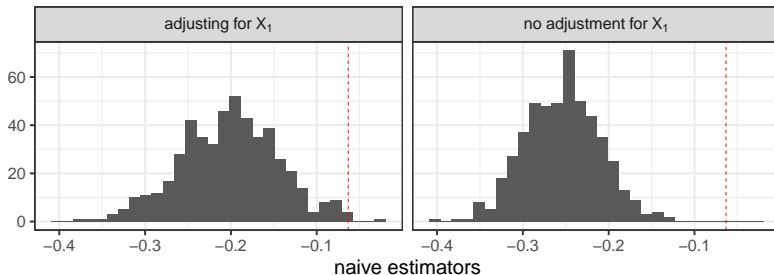
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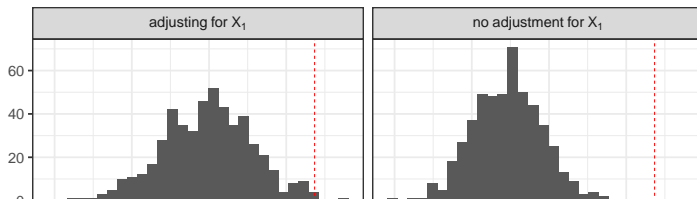
1. Logistic regression of the outcome regressed on all treatment variables and covariates: Contrast means of the predictions under  $A_0 = A_1 = 1$  to the mean of the predictions under  $A_0 = A_1 = 0$ .
2. Logistic regression of the outcome regressed on baseline covariates and both treatment variables (leaving out follow-up covariates): Contrast means of the predictions under  $A_0 = A_1 = 1$  to the mean of the predictions under  $A_0 = A_1 = 0$ .

# Time-dependent treatment interventions

In a simulation study with  $M = 500$  repetitions:



Both naive approaches give biased results — due to time-dependent confounding.



# Practical:

Kreif et al. (2017) as an example

- ▶ Data structure, static and dynamic intervention, time-dependent treatment interventions.
- ▶ IP-weighting, g-formula, TMLE.

Questions for the paper that you should go over can be found in: **day3\_practical1.pdf**.