Day 4, Practical 2, Hely's solution

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Task 1: Implementing the targeting algorithm.

1.

```
sim.fun <- function(n, intervene=list()) {</pre>
    # baseline covariates
    X0.1 < - runif(n, -2, 2)
    X0.2 <- rnorm(n)</pre>
    X0.3 < - rbinom(n, 1, 0.2)
    # baseline treatment (randomized)
    if ("A0" %in% names(intervene)) {
    AO <- intervene$AO
    } else {
    A0 < - rbinom(n, 1, 0.5)
    }
    # follow-up covariates
    X1.1 \leftarrow rbinom(n, 1, plogis(-0.7 + 0.3*X0.3 + 0.8*A0))
    X1.2 \leftarrow rbinom(n, 1, plogis(0.25 - 0.55*X0.3))
    # follow-up treatment
    if ("A1" %in% names(intervene)) {
    A1 <- intervene$A1(X1.1)
    A1 <- rbinom(n, 1, prob=plogis(0.9 - 5*(1-A0) - 4.7*X1.1 - 4.8*X1.2))
    # outcome
    Y <- rbinom(n, 1, prob=plogis(-0.9 - 0.2*A0 + 1.2*X1.1 - 0.1*A1 - 0.8*A1*(X1
    .1==0)))
    if (length(names(intervene))>0) {
    return(mean(Y))
    } else {
    return(data.table(X0.1=X0.1, X0.2=X0.2, X0.3=X0.3,
              AO=AO,
              X1.1=X1.1, X1.2=X1.2,
              A1=A1,
              Y=Y))
    }
```

```
set.seed(15)
   (sim.data <- sim.fun(n=2000))
             X0.1
                         X0.2 X0.3 A0 X1.1 X1.2 A1 Y
   1: 0.40845618 -0.19620228
                                 0 1
                                          1
                                               0 0 1
  2: -1.21982429 0.59503302
                                  1 1
                                          0
                                               0 1 0
                                  0 1
                                          0
                                               0 0 0
  3: 1.86583493 -1.60888231
  4: 0.60362212 0.04123507
                                  0 1
                                               0 1 0
                                 0 0
  5: -0.53171243 -1.25139144
                                          0
                                             1 0 0
1996: -0.72294993 -0.43541869
                                          0
                                             0 0 1
                                 0 1
1997: -0.13592934 -0.80204340 0 0
                                          0
                                             0 0 0
                                 0 0
                                             1 0 0
1998: -1.67193359 -1.57095686
                                          0
1999: 0.68115948 -0.72905589
                               0 1
                                         0
                                             0 1 0
2000: 0.04187752 0.10649384
                                  0 0 0 0 0 1
  2.
   weight.truncation <- FALSE
   fit.pi0 <- glm(A0 ~ X0.1+X0.2+X0.3, family=binomial, data=sim.data)
   fit.pi1 <- glm(A1 \sim X0.1+X0.2+X0.3+A0+X1.1+X1.2, family=binomial, data=sim.data)
   sim.data[, cum.pi0:=predict(fit.pi0, type="response")]
   sim.data[, cum.pi1:=predict(fit.pi0, type="response")*predict(fit.pi1, type="response")
       )]
   if (weight.truncation) {
       sim.data[cum.pi0<0.01, cum.pi0:=0.01]
       sim.data[cum.pi1<0.01, cum.pi1:=0.01]
   sim.data[, H1:=(A0==1)/cum.pi0]
   sim.data[, H2:=(A0==1)*(A1==1)/cum.pi1]
  3.
   fit.Q2 <- glm(Y \sim A1 + X1.1 + X1.2 + A0 + X0.1 + X0.2 + X0.3,
            family=binomial, data=sim.data)
   sim.data[, pred.Q2:=predict(fit.Q2, newdata=copy(sim.data)[, A1:=1], type="response")]
  4.
   fit.tmle2 <- glm(Y \sim offset(qlogis(pred.Q2)), weights=H2,
           family=binomial, data=sim.data)
   sim.data[, pred.Q2.star:=predict(fit.tmle2, type="response")]
   ##-- check that we solve:
   sim.data[, mean(H2*(Y-pred.Q2.star))]
```

-2.22802486597902e-12

5.

6.

```
[1] -1.271552e-17
```

7.

```
(est.own.tmle <- sim.data[, mean(pred.Q1.star)])</pre>
```

[1] 0.2759537

8. Compute the standard error by evaluating the efficient influence function, i.e.,

[1] 0.1107792

Task 2: Using ltmle software.

1.

```
Qform not specified, using defaults:
formula for X1.1:
Q.kplus1 ~ X0.1 + X0.2 + X0.3 + A0
formula for Y:
Q.kplus1 ~ X0.1 + X0.2 + X0.3 + A0 + X1.1 + X1.2 + A1
```

```
gform not specified, using defaults:
formula for AO:
A0 \sim X0.1 + X0.2 + X0.3
formula for A1:
A1 \sim X0.1 + X0.2 + X0.3 + A0 + X1.1 + X1.2
Estimate of time to completion: < 1 minute
Warning message:
In CheckForVarianceWarning(inputs, g.ratio) :
  Variance estimate is based on influence curve only, which may be significantly anticonservative b
Estimator: tmle
Call:
ltmle(data = sim.data, Anodes = paste0("A", 0:1), Lnodes = c(paste0("X0.",
    1:3), paste0("X1.", 1:2)), Ynodes = "Y", abar = c(1, 1),
    variance.method = "ic")
   Parameter Estimate: 0.15695
    Estimated Std Err: 0.051843
               p-value: 0.0024662
    95% Conf Interval: (0.055343, 0.25856)
  2. Go back and change argument weight.truncation to TRUE.
  3.
   summary(fit.ltmle, estimator="iptw")$treatment$estimate
     iptw
0.1460717
  4.
   library(ltmle)
   set.seed(15)
   sim.data <- sim.fun(n=2000)</pre>
   fit.g <- ltmle(sim.data,</pre>
              Anodes=paste0("A",0:1),
              Lnodes=c(paste0("X0.", 1:3), paste0("X1.", 1:2)),
              Ynodes="Y",
              gcomp=TRUE,
              abar=c(1,1), variance.method="ic")
   summary(fit.g)
Qform not specified, using defaults:
formula for X1.1:
Q.kplus1 \sim X0.1 + X0.2 + X0.3 + A0
formula for Y:
Q.kplus1 \sim X0.1 + X0.2 + X0.3 + A0 + X1.1 + X1.2 + A1
gform not specified, using defaults:
```

```
formula for AO:
A0 \sim X0.1 + X0.2 + X0.3
formula for A1:
A1 \sim X0.1 + X0.2 + X0.3 + A0 + X1.1 + X1.2
Estimate of time to completion: < 1 minute
Warning message:
In CheckForVarianceWarning(inputs, g.ratio) :
  Variance estimate is based on influence curve only, which may be significantly anticonservative b
Estimator: gcomp
Warning: inference for gcomp is not accurate! It is based on TMLE influence curves.
Call:
ltmle(data = sim.data, Anodes = paste0("A", 0:1), Lnodes = c(paste0("X0.",
    1:3), paste0("X1.", 1:2)), Ynodes = "Y", abar = c(1, 1),
    gcomp = TRUE, variance.method = "ic")
   Parameter Estimate: 0.22819
    Estimated Std Err: 0.055393
              p-value: 0.000037983
    95% Conf Interval: (0.11962, 0.33676)
```

True values of parameters:

ITT: -0.00931700000000002

static: -0.063294 dynamic: -0.050709

Task 3: Estimating the static effect.

```
summary(fit.ltmle.static)$effect.measures$ATE
   message("----")
   message("ipw output:")
   message("---")
   summary(fit.ltmle.static, estimator="iptw")$effect.measures$ATE
Qform not specified, using defaults:
formula for X1.1:
Q.kplus1 \sim X0.1 + X0.2 + X0.3 + A0
formula for Y:
Q.kplus1 \sim X0.1 + X0.2 + X0.3 + A0 + X1.1 + X1.2 + A1
gform not specified, using defaults:
formula for AO:
A0 \sim X0.1 + X0.2 + X0.3
formula for A1:
A1 \sim X0.1 + X0.2 + X0.3 + A0 + X1.1 + X1.2
Estimate of time to completion: < 1 minute
Warning message:
In CheckForVarianceWarning(inputs, g.ratio) :
  Variance estimate is based on influence curve only, which may be significantly anticonservative b
tmle output:
$long.name
[1] "Additive Treatment Effect"
$estimate
[1] -0.215463
$std.dev
[1] 0.05409723
$pvalue
[1] 0.00006808408
$CI
           2.5%
                     97.5%
[1,] -0.3214916 -0.1094343
$log.std.err
[1] FALSE
ipw output:
$long.name
[1] "Additive Treatment Effect"
```

message("---")

\$estimate

```
[1] -0.2263073
$std.dev
[1] 0.04865195
$pvalue
[1] 0.000003294405
$CI
            2.5%
                      97.5%
[1,] -0.3216633 -0.1309512
$log.std.err
[1] FALSE
Task 4: Estimating the static effect with g-formula estimation.
   set.seed(15)
   sim.data <- sim.fun(n=2000)</pre>
   fit.g.static <- ltmle(sim.data,</pre>
                 Anodes=paste0("A",0:1),
                 Lnodes=c(paste0("X0.", 1:3), paste0("X1.", 1:2)),
                 Ynodes="Y",
                 abar=list(treatment=c(1,1), control=c(0,0)),
                 gcomp=TRUE,
                 variance.method="ic")
   message("----")
   message("g-formula output:")
   message("---")
   summary(fit.g.static)$effect.measures$ATE
Qform not specified, using defaults:
formula for X1.1:
Q.kplus1 \sim X0.1 + X0.2 + X0.3 + A0
formula for Y:
Q.kplus1 \sim X0.1 + X0.2 + X0.3 + A0 + X1.1 + X1.2 + A1
```

```
[1] "Additive Treatment Effect"
$estimate
[1] -0.1435938
$std.dev
[1] 0.05750552
$pvalue
[1] 0.01252333
$CI
          2.5%
                     97.5%
[1,] -0.2563026 -0.03088509
$log.std.err
[1] FALSE
Task 5.
   message("----")
   message("tmle output:")
   message("---")
   summary(fit.ltmle.static)$effect.measures$ATE[c("estimate")]
   message("----")
   message("ipw output:")
   message("---")
   summary(fit.ltmle.static, estimator="iptw")$effect.measures$ATE[c("estimate")]
   message("----")
   message("g-formula output:")
   message("---")
   summary(fit.g.static)$effect.measures$ATE[c("estimate")]
-----
tmle output:
$estimate
[1] -0.215463
_____
ipw output:
---
$estimate
[1] -0.2263073
_____
g-formula output:
---
$estimate
[1] -0.1435938
```

Task 6: Estimating the ITT effect.

```
Qform not specified, using defaults:
formula for X1.1:
Q.kplus1 \sim X0.1 + X0.2 + X0.3 + A0
gform not specified, using defaults:
formula for AO:
A0 \sim X0.1 + X0.2 + X0.3
Estimate of time to completion: < 1 minute
$long.name
[1] "Additive Treatment Effect"
$estimate
[1] 0.03664088
$std.dev
[1] 0.02179757
$pvalue
[1] 0.09277035
$CI
             2.5%
                        97.5%
[1,] -0.006081571 0.07936332
$log.std.err
[1] FALSE
```

Task 7: Estimating the dynamic effect.

```
Qform not specified, using defaults:
formula for X1.1:
Q.kplus1 \sim X0.1 + X0.2 + X0.3 + A0
formula for Y:
Q.kplus1 \sim X0.1 + X0.2 + X0.3 + A0 + X1.1 + X1.2 + A1
gform not specified, using defaults:
formula for AO:
A0 \sim X0.1 + X0.2 + X0.3
formula for A1:
A1 \sim X0.1 + X0.2 + X0.3 + A0 + X1.1 + X1.2
Estimate of time to completion: < 1 minute
Warning message:
In CheckForVarianceWarning(inputs, g.ratio) :
  Variance estimate is based on influence curve only, which may be significantly anticonservative b
$long.name
[1] "Additive Treatment Effect"
$estimate
[1] 0.04175735
$std.dev
[1] 0.04672911
$pvalue
[1] 0.3715335
$CI
            2.5%
                     97.5%
[1,] -0.04983003 0.1333447
$log.std.err
[1] FALSE
Task 8.
   message("----")
   message("tmle for static effect:")
   message("---")
   summary(fit.ltmle.static)$effect.measures$ATE[c("estimate", "std.dev")]
   message("----")
   message("tmle for dynamic effect:")
   message("---")
   summary(fit.ltmle.dynamic)$effect.measures$ATE[c("estimate", "std.dev")]
```

message("---")

message("----")
message("tmle for itt effect:")

summary(fit.ltmle.itt)\$effect.measures\$ATE[c("estimate", "std.dev")]

```
tmle for static effect:
$estimate
[1] -0.215463
$std.dev
[1] 0.05409723
tmle for dynamic effect:
$estimate
[1] 0.04175735
$std.dev
[1] 0.04672911
______
tmle for itt effect:
$estimate
[1] 0.03664088
$std.dev
[1] 0.02179757
```

Task 9: Simulation study targeting the static effect.

```
library(ltmle)
ate.ltmle.static <- list()</pre>
ate.ipw.static <- list()</pre>
ate.g.static <- list()</pre>
ate.g2.static <- list()</pre>
for (m in 1:500) {
   set.seed(15+m)
   sim.data <- sim.fun(n=2000)</pre>
   ##- 1.
   fit.ltmle <- ltmle(sim.data,</pre>
              Anodes=paste0("A",0:1),
              Lnodes=c(paste0("X0.", 1:3),
               paste0("X1.", 1:2)),
              Ynodes="Y",
              abar=list(treatment=c(1,1), control=c(0,0)))
   ate.ipw.static[[m]] <- summary(fit.ltmle, estimator="iptw")$effect.measures$ATE$
    estimate
   fit.g <- ltmle(sim.data, Anodes=paste0("A",0:1), Lnodes=c(paste0("X0.", 1:3),</pre>
   paste0("X1.", 1:2)), Ynodes="Y",
          abar=list(treatment=c(1,1), control=c(0,0)), gcomp=TRUE)
   ate.g.static[[m]] <- summary(fit.g)$effect.measures$ATE$estimate</pre>
   ##- 3.
```

Task 10. See Figure 1.

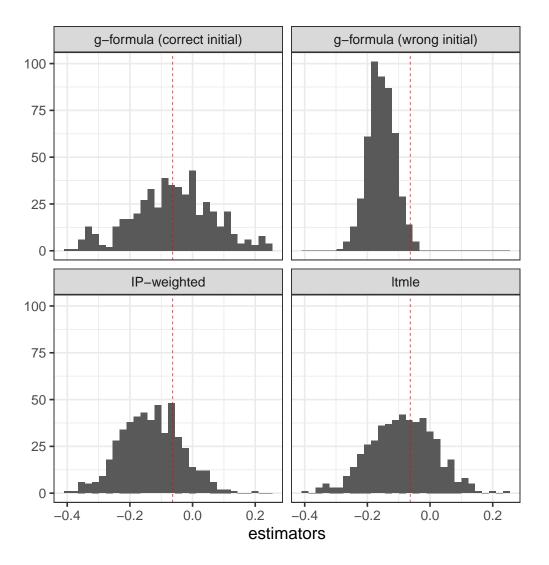


Figure 1

Task 11: Continuing the simulation study with TMLE targeting the dynamic effect and the ITT effect.

```
library(ltmle)
ate.ltmle.static <- list()</pre>
ate.se.ltmle.static <- list()</pre>
ate.ltmle.itt <- list()</pre>
ate.se.ltmle.itt <- list()</pre>
ate.ltmle.dynamic <- list()</pre>
ate.se.ltmle.dynamic <- list()</pre>
for (m in 1:500) {
    set.seed(15+m)
    sim.data <- sim.fun(n=2000)
    ##- 1.
    fit.ltmle <- ltmle(sim.data,</pre>
               Anodes=paste0("A",0:1),
               Lnodes=c(paste0("X0.", 1:3), paste0("X1.", 1:2)),
               Ynodes="Y",
                abar=list(treatment=c(1,1), control=c(0,0)),
                Qform=c(X1.1="Q.kplus1\sim X0.1+X0.2+X0.3+A0",
                    Y="Q.kplus1\sim X0.1+X0.2+X0.3+A0+X1.1+X1.2+A1*X1.1"),
               variance.method="ic")
    ate.ltmle.static[[m]] <- summary(fit.ltmle)$effect.measures$ATE$estimate
    ate.se.ltmle.static[[m]] <- summary(fit.ltmle)$effect.measures$ATE$std.dev</pre>
    fit.ltmle.itt <- ltmle(sim.data,</pre>
               Anodes=paste0("A",0),
               Lnodes=c(paste0("X0.", 1:3), paste0("X1.", 1:2), "A1"),
                {\tt Qform=c\,(X1.1="Q.kplus1}{\sim}{\tt X0.1+X0.2+X0.3+A0"}\,,
                    Y="Q.kplus1\sim X0.1+X0.2+X0.3+A0+X1.1+X1.2+A1*X1.1"),
                abar=list(treatment=c(1), control=c(0)),
                variance.method="ic")
    ate.ltmle.itt[[m]] <- summary(fit.ltmle.itt)$effect.measures$ATE$estimate
    ate.se.ltmle.itt[[m]] <- summary(fit.ltmle.itt)$effect.measures$ATE$std.dev
    fit.ltmle.dynamic <- ltmle(sim.data,</pre>
                    Anodes=paste0("A",0:1),
                    Lnodes=c(paste0("X0.", 1:3), paste0("X1.", 1:2)),
                    Ynodes="Y".
                    Qform=c(X1.1="Q.kplus1~X0.1+X0.2+X0.3+A0",
                        Y="Q.kplus1\sim X0.1+X0.2+X0.3+A0+X1.1+X1.2+A1*X1.1"),
                    rule=list(treatment=function(row) c(1, ifelse(row["X1.1"]==1, 0, 1)
    ),
                      control=function(row) c(0,0)),
                    variance.method="ic")
    ate.ltmle.dynamic[[m]] <- summary(fit.ltmle.dynamic)$effect.measures$ATE$estimate
    ate.se.ltmle.dynamic[[m]] <- summary(fit.ltmle.dynamic)$effect.measures$ATE$std.
    dev
}
```

Task 12. See Figure 2.

coverage: tmle for static effect:
--[1] 0.568
----coverage: tmle for itt effect:
--[1] 0.938
----coverage: tmle for dynamic effect:

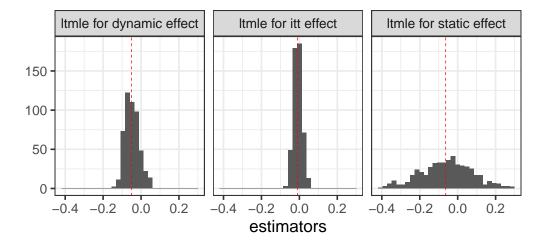


Figure 2

Task 13: Using super learning.

1.

[1] 0.928

```
fit.ltmle.sl <- ltmle(sim.data, Anodes=paste0("A",0:1),</pre>
                 Lnodes=c(paste0("X0.", 1:3), paste0("X1.", 1:2)),
                 Ynodes="Y",
                 SL.library=list(Q=c("SL.glm", "SL.mean", "SL.glm.interaction",
                         "SL.glmnet", "SL.gam"),
                         g=c("SL.glm", "SL.mean", "SL.glmnet",
                         "SL.gam")),
                 rule=list(treatment=function(row) c(1, ifelse(row["X1.1"]==1, 0, 1)),
                   control=function(row) c(0,0)), variance.method="ic")
  2.
   fit.ltmle.sl$fit$Q[[1]]
   fit.ltmle.sl\fit\g
$X1.1
                               Risk
                                           Coef
SL.glm_All
                         0.02662852 0.00000000
SL.mean_All
                         0.02792894 0.04233679
SL.glm.interaction_All 0.02660383 0.50686160
SL.glmnet_All
                                 NA 0.0000000
SL.gam_All
                         0.02660866 0.45080161
$Y
                                          Coef
                              Risk
                         0.2166817 0.00000000
                         0.2385468 0.00000000
                         0.2158281 0.90147281
                         0.2167009 0.00000000
```

SL.glm_All SL.mean_All SL.glm.interaction_All 0.2186063 0.09852719 SL.glmnet_All SL.gam_All [[1]]

[[1]]\$AO

Risk Coef SL.glm_All 0.2501241 SL.mean_All 0.2497703 1 SL.glmnet_All 0.2497703 0 SL.gam_All 0.2502473 0

[[1]]\$A1

Risk Coef SL.glm_All 0.02687716 0.0000000 SL.mean_All 0.06689833 0.0000000 SL.glmnet_All 0.02684041 0.6521786 SL.gam_All 0.02688544 0.3478214

[[2]] [[2]]\$AO

Risk Coef

```
SL.glm_All
             0.2501241
SL.mean_All
             0.2497703
                           1
SL.glmnet_All 0.2497703
                           0
SL.gam_All
              0.2502473
                           0
[[2]]$A1
                    Risk
                              Coef
SL.glm_All
              0.02687716 0.0000000
SL.mean_All
              0.06689833 0.0000000
SL.glmnet_All 0.02684041 0.6521786
SL.gam_All
              0.02688544 0.3478214
```

1 ltmle with right-censored data

Task 14.

```
set.seed(100)
head(sim.data2 <- sim.fun2())</pre>
```

Task 15.

```
(risk.switch <- sim.fun2(n=1e6, intervene=list(A0=0, A1=1)))
(risk.not.switch <- sim.fun2(n=1e6, intervene=list(A0=0, A1=0)))</pre>
```

[1] 0.732033

[1] 0.732059

Task 16.

```
sim.data2[, (paste0("C", 1)):=BinaryToCensoring(is.censored=get(paste0("C", 1)))]
```

Task 17.

```
summary(ltmle.fit2)
```

Treatment Estimate:

Parameter Estimate: 0.66787 Estimated Std Err: 0.020457

```
p-value: <2e-16
    95% Conf Interval: (0.62778, 0.70797)
Control Estimate:
   Parameter Estimate: 0.72594
    Estimated Std Err: 0.049985
              p-value: <2e-16
    95% Conf Interval: (0.62797, 0.82391)
Additive Treatment Effect:
   Parameter Estimate: -0.058066
    Estimated Std Err: 0.051609
              p-value: 0.26054
    95% Conf Interval: (-0.15922, 0.043085)
Relative Risk:
   Parameter Estimate: 0.92001
  Est Std Err log(RR): 0.071808
              p-value: 0.24564
    95% Conf Interval: (0.79923, 1.059)
Odds Ratio:
   Parameter Estimate: 0.75917
  Est Std Err log(OR): 0.25668
              p-value: 0.28306
    95% Conf Interval: (0.45904, 1.2555)
Task 18.
   sim.data2[, X0.squared:=X0^2]
   setcolorder(sim.data2, c(names(sim.data2)[1],
               "X0.squared",
               names(sim.data2)[-c(1,ncol(sim.data2))]))
   ltmle.fit2 <- ltmle(sim.data2,</pre>
              Anodes=paste0("A", 0:1),
              Lnodes=paste0("X", 0:1),
              Cnodes="C1",
              Ynodes=paste0("D", 1:2),
              abar=list(treatment=c(0,1), control=c(0,0)),
              survivalOutcome=TRUE)
   summary(ltmle.fit2)
Estimator: tmle
Call:
ltmle(data = sim.data2, Anodes = paste0("A", 0:1), Cnodes = "C1",
    Lnodes = paste0("X", 0:1), Ynodes = paste0("D", 1:2), survivalOutcome = TRUE,
    abar = list(treatment = c(0, 1), control = c(0, 0)))
Treatment Estimate:
```

Parameter Estimate: 0.72423

Estimated Std Err: 0.022258

p-value: <2e-16

95% Conf Interval: (0.68061, 0.76786)

Control Estimate:

Parameter Estimate: 0.71872 Estimated Std Err: 0.05146

p-value: <2e-16

95% Conf Interval: (0.61786, 0.81958)

Additive Treatment Effect:

Parameter Estimate: 0.0055139 Estimated Std Err: 0.053037 p-value: 0.9172

95% Conf Interval: (-0.098436, 0.10946)

Relative Risk:

Parameter Estimate: 1.0077 Est Std Err log(RR): 0.073737

p-value: 0.91745

95% Conf Interval: (0.87208, 1.1644)

Odds Ratio:

Parameter Estimate: 1.0278
Est Std Err log(OR): 0.26267

p-value: 0.9168

95% Conf Interval: (0.61423, 1.7199)

ltmle.fit2\$fit\$Q[[1]]

\$D1

Estimate Std. Error t value Pr(>|t|)
(Intercept) 1.56596540 0.06922717 22.620677 4.787834e-101
X0 -0.08085172 0.02985490 -2.708156 6.823564e-03
X0.squared -0.42284781 0.02997600 -14.106214 3.823172e-43
A0 -0.67167523 0.07179688 -9.355215 2.164993e-20

\$X1

Estimate Std. Error t value Pr(>|t|)
(Intercept) 0.4849548188 0.003442044 140.89153226 1.250570e-305
X0 -0.3660083765 0.002033794 -179.96337273 0.000000e+00
X0.squared -1.1552932320 0.002111787 -547.06905922 0.000000e+00
A0 -0.0001867727 0.004182044 -0.04466063 9.644038e-01

\$D2

Estimate Std. Error t value Pr(>|t|)
(Intercept) 0.6512907 0.4119586 1.5809615 0.114813911874227001
X0 -0.3734311 0.1645689 -2.2691480 0.023883589133921471
X0.squared -1.1560105 0.1562277 -7.3995218 0.00000000001073994
A0 0.3850730 0.3195341 1.2051075 0.228997450239672690

```
X1 0.1034213 0.4280875 0.2415892 0.809243706916227379
A1 -0.1715239 0.4212253 -0.4072024 0.684114853083405361
```

```
ltmle.fit2$fit$g[[1]]
```

\$A0

Estimate Std. Error t value Pr(>|t|)
(Intercept) -0.09470835 0.06663170 -1.421371 0.1553652
X0 -0.03949804 0.03927721 -1.005623 0.3147190
X0.squared 0.03702366 0.03792029 0.976355 0.3290068

\$C1

Estimate Std. Error t value Pr(>|t|)
(Intercept) -1.1960037 0.1324855 -9.0274285 8.300060e-19
X0 0.0334300 0.0597762 0.5592526 5.761095e-01
X0.squared 0.7983833 0.0644685 12.3840838 5.850710e-33
A0 -1.2015567 0.1534715 -7.8291862 1.202877e-14

\$A1

Estimate Std. Error t value Pr(>|t|)
(Intercept) 1.2032820 0.2539590 4.738095 0.000003168252174
X0 -1.3645602 0.2240725 -6.089815 0.00000003039204
X0.squared 0.3558945 0.1492711 2.384216 0.017660315374184
A0 0.4106480 0.2809646 1.461565 0.144778651394808
X1 -0.4976473 0.3091209 -1.609879 0.108346808036168