## Proof strategies

Week 4. Deep dive.

## ABCS

- Assumptions (write them down)
- Break down the assumptions
  - $E \wedge_{i} E \rightarrow_{i} E \leftrightarrow$
  - Sometimes E v (though this can be tricky to identify)
- Conclusion (what's the main connective?)
  - $|\sim, |\rightarrow, |\vee, |\wedge$
- Stuff in the middle (trial and error)
  - Start with non-hypothetical rules
  - Then try out hypothetical rules

**Table 4-1 Proof Strategies** 

| If the conclusion is $a(n)$ : | Then do this:   |
|-------------------------------|---|
| Atomic formula                | If no other strategy is immediately apparent, hypothesize the negation of the conclusion for ~I. If this is successful, then the conclusion can be obtained after the ~I by ~E.   |
| Negated formula               | Hypothesize the conclusion without its negation sign for $\sim$ I. If a contradiction follows, the conclusion can be obtained by $\sim$ I.  |
| Conjunction                   | Prove each of the conjuncts separately and then conjoin them with &I.   |
| Disjunction                   | Sometimes (though not often) a disjunctive conclusion can be proved directly simply by proving one of its disjuncts and applying $\bigvee I$ . Otherwise, hypothesize the negation of the conclusion and try $\sim I$ . |
| Conditional Biconditional     | Hypothesize its antecedent and derive its consequent by $\rightarrow$ I. Use $\rightarrow$ I twice to prove the two conditionals needed to obtain the conclusion by $\leftrightarrow$ I.                                |

## How for all x puts it:

Working backward from what you want.

• What does working backwards from each connective involve? Which connective is easiest to work backwards from? Hardest?

Work forward from what you have.

• What does working forward from each connective involve? Which connective is easiest to work forward from? Hardest?

My tip: There are no magical unicorn people who "just get proofs"! It's a matter of practicing and recognizing patterns.

Remember, there aren't that many rules anyway.