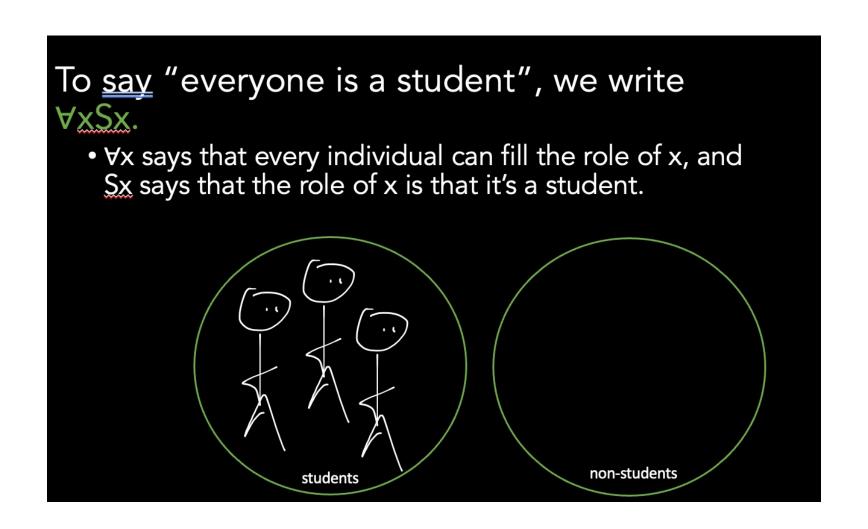
What are models?

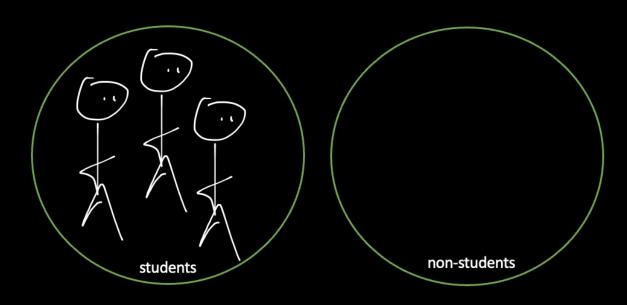
Week 6. Deeper dive.

Recall:



- A model is a representation of a particular state of affair.
 - Models are kind of like rows on a truth table.
 - Models help us reason: e.g., sometimes we can see that two formulas can't be true in the same model, or that if one is true then the other must be true in a model.

A model supplies a *domain of discourse* (or just domain): the class of objects relative to which the names and predicate letters are interpreted.



We have three objects.
Let's call them a, b, and c.
We have one predicate "Sx"
meaning "x is a student."

To collect up a bunch of objects in an ordered list, we use curly braces: {...} and separate each object with commas.

So, in this example, we write our domain of discourse as {a,b,c}

Also supplies an interpretation of any non-logical symbols occurring some wffs of QL.

Symbol

name letter

zero-place predicate letter (sentence letter)

one-place predicate letter n-place predicate letter (n > 1)

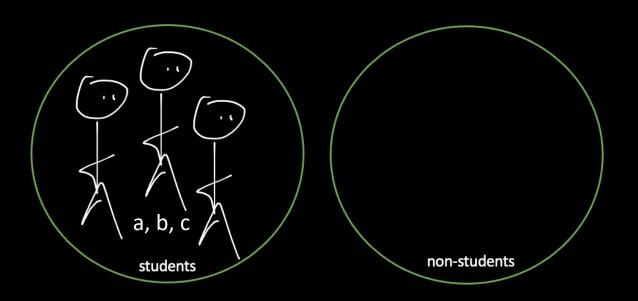
Interpretation
individual object (e.g., the Moon)
truth value (T or F)
class of objects (e.g., the class of people)
relation between n objects (e.g., the relation that holds between a pair of objects just in case the first is bigger than the second)

What does this look like?

Also supplies an interpretation of any non-logical symbols occurring some wffs of QL.

The interpretation function, which we usually write capital 'I', tells us about two different sorts of linguistic items

- For each name, it provides the object denoted by that name.
 - Ex: I(s) = Stella. This is the interpretation of 's'
- For each **predicate**, it provides its *extension*.
 - The extension of a predicate is the collection of objects that have this predicate as a property.
 - We'll use curly braces again.



We have three objects.
Let's call them a, b, and c.
We have one predicate "Sx"
meaning "x is a student."

The interpretation of our predicate is: $I(S)=\{a,b,c\}$

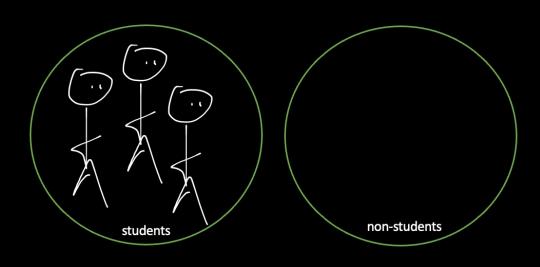
One more notational thing:

As noted, we use curly braces for a collection of unordered objects. And we use the inclusion symbol 'E' for **membership**

- e.g., $a \in \{a,b,c\}$
- e.g., Helen ∈ {Helen, Josiah, Jessica}
- **e.g.**, **d** ∉ {a,b,c}

Truth in models...

Given a property S and a name h, the proposition Sh is true in a model M if and only if: $I(h) \in I(S)$

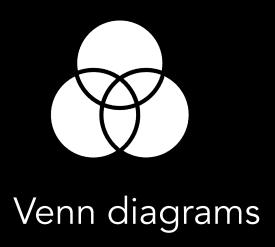


h = Helen, j = Jessica, o = Josiah I(S)={Helen, Jessica, Josiah} I(h) = Helen

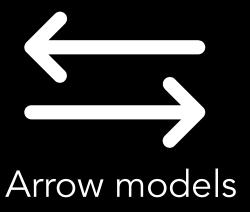
The above is saying that "Helen is a student" is true in the model iff $I(h) \in I(S)$

Is it? Yes!: $I(h) = Helen \in I(S)$ since $I(S) = \{Helen, Jessica, Josiah\}$

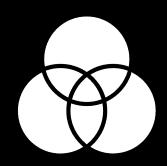
Types of models we will consider:





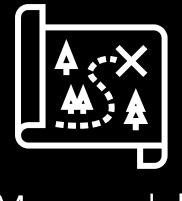


Types of models we will consider:

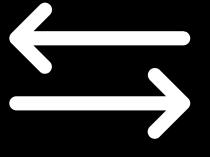


Venn diagrams

good for representing objects with properties



Map models



Arrow models

good for representing objects with properties and relations between objects

Why are we talking about models...?

Validity via models: a valid argument is an argument in which the conclusion is true *in every model* in which the premises are true.

By 'every model' we mean each model which interprets the vocabulary in the argument

wait...every model??

Validity via models: a valid argument is an argument in which the conclusion is true *in every model* in which the premises are true.

Yes...remember a model is like a row on a truth table and we have to check every row in which the premises were true when we were checking for validity!

wait...every model??

Validity via models: a valid argument is an argument in which the conclusion is true *in every model* in which the premises are true.

BUT unlike truth tables, here we'd have infinitely many models...which is impossible!

wait...every model??

Validity via models: a valid argument is an argument in which the conclusion is true in every model in which the premises are true.

Instead, we'll often use models as counterexamples! Remember an argument was invalid if we found a row on which the premises were true but the conclusion wasn't. We often want to give these kinds of counterexamples to show an argument is invalid!

To come:

