

Convolved Convolutional Neural Networks

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What is a convolutional neural network?

Overview [\[edit \]](#)

Convolutional neural networks model animal visual perception, and can be applied to visual recognition tasks.

Image recognition [\[edit \]](#)

Convolutional neural networks (CNNs) consist of multiple layers of **receptive fields**. These are small^[clarification needed] neuron collections which process portions of the input image. The outputs of these collections are then tiled^[how?] so that their input regions overlap, to obtain a better^[how?] representation of the original image; this is repeated for every such layer. Tiling allows CNNs to tolerate **translation** of the input image.^[8]

Convolutional networks may include local or global pooling layers^[clarification needed], which combine the outputs of neuron clusters.^{[9][10]} They also consist of various combinations of **convolutional** and fully connected layers, with pointwise nonlinearity applied at the end of or after each layer.^[11] A convolution operation on small regions of input is introduced^[how?] to reduce the number of free parameters and improve generalization^[how?]. One major advantage of convolutional networks is the use of shared weight in convolutional layers, which means that the same filter (weights bank) is used for each pixel in the layer; this both reduces memory footprint and improves performance^[how?].^[3]

Caffe: Image Processing

Caffe Demos

The [Caffe](#) neural network library makes implementing state-of-the-art computer vision systems easy.

Classification

[Click for a Quick Example](#)



Maximally accurate

Maximally specific

bag

1.19015

mailbag

0.90366

container

0.53076

backpack

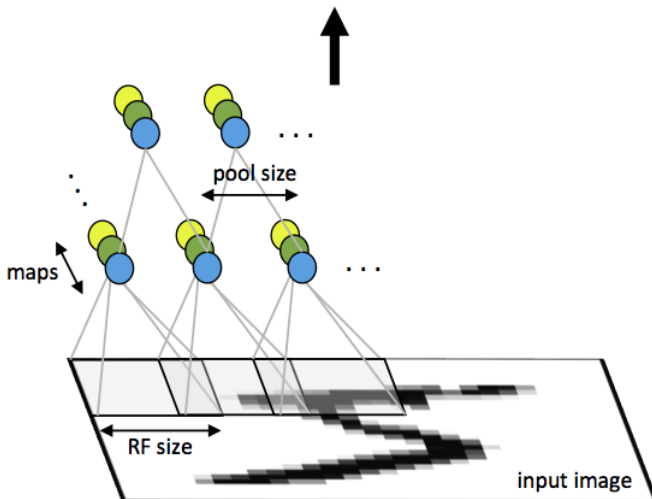
0.43018

covering

0.40157

CNN took 0.071 seconds.

Convolutional Neural Network



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 3. m filters

Convolutional Layers

```
for w in 1..W
  for h in 1..H
    for x in 1..K
      for y in 1..K
        for m in 1..M
          for d in 1..D
            output(w, h, m) += input(w+x, h+y, d) * filter(m, x, y, d)
          end
        end
      end
    end
  end
end
```

Mathematical Convolution



$$w \times h \times d \times k \times k \times m$$

$$\therefore$$

6D

Mathematical Convolution



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6D

- ▶ Convolution: a function derived from two given functions by integration that expresses how the shape of one is modified by the other.

Mathematical Convolution

- ▶ The convolution $f * g$ of two functions $f(t)$ and $g(t)$ is the function defined by

$$(f * g)(t) = \int_0^t f(t - u)g(u)du.$$

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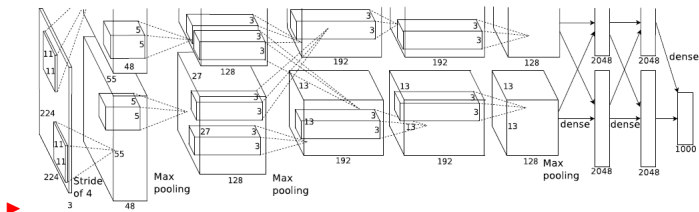
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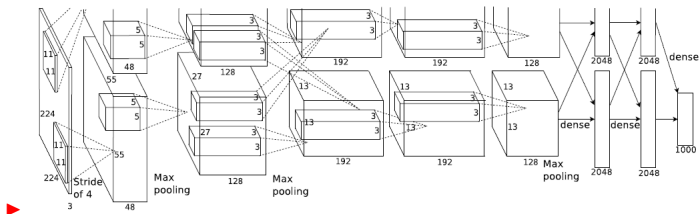
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Mathematical Convolution

- The convolution $f * m$ of two functions image $f(D)$ and filters $m(D)$ is the function defined by

$$(f * m)(D) = \int_0^D f(D - u)m(D) dD.$$



Unrolling Convolutional Layers

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3. The output of the two matrices can be rolled back into 2D matrices equivalent to the original 2D layout.

Matrix Multiplication Methods

We have a large matrix-matrix product.

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 - ▶ ability to access memory in a 2D manner
 - ▶ independent arithmetic logic units (ALUs)

Sources

- Jia, Yangqing. "Convolution in Caffe: A Memo." GitHub. BERKELEY VISION AND LEARNING CENTER, 19 June 2015. Web. 15 Nov. 2016.
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