



# Optimizing single-qubit control with Floquet theory

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### **Outline**



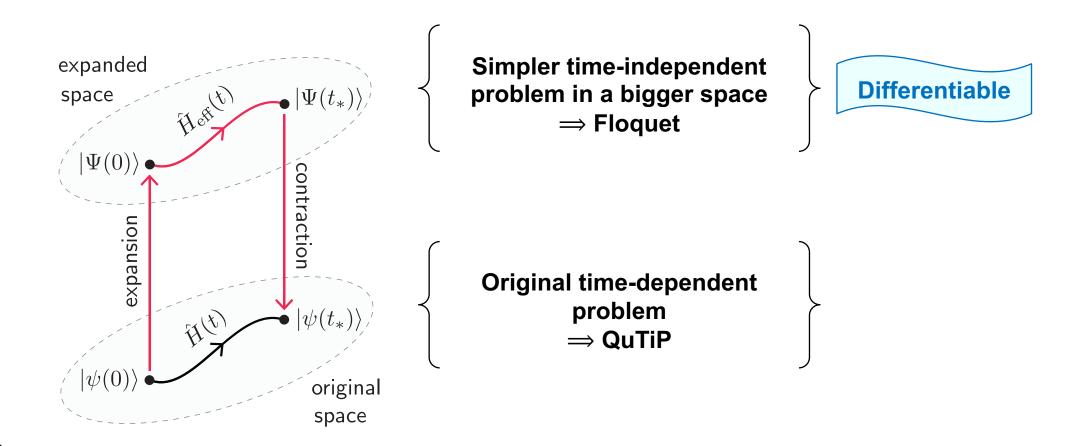
- Quantum optimal control using Floquet theory in a nutshell
- 1QB gates for the transmon qubit
  - Implementation and numerical details
  - Convergence of the Fourier Ansatz
  - Speed limit vs qubit anharmonicity
  - Spectral analysis: discovering the DRAG Ansatz
- 1QB gates for the heavy-fluxonium qubit
  - Microwave gates via charge coupling
  - Single-cycle gates via flux coupling
  - Which gate is best for your fluxonium?



## Optimal control with Floquet theory in a nutshell



- Floquet theory is an efficient way to solve the time-periodic Schrodinger equation
- We solve a simpler, time-independent Schrodinger equation in a bigger Hilbert space:

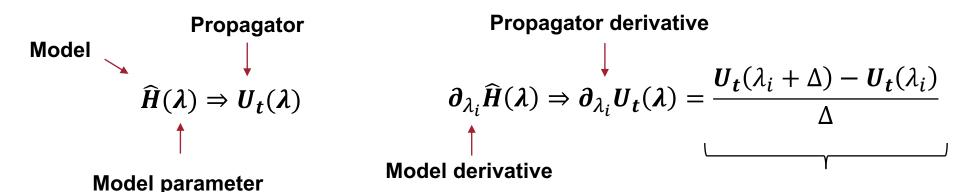




## Optimal control with Floquet theory in a nutshell

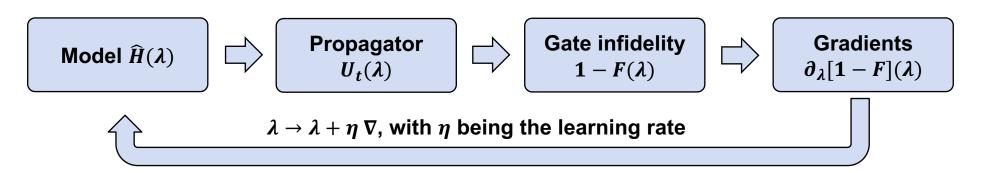


What do we mean by differentiable and why is it important?



(drive amplitude, coupling
strength, etc.)
How much does the propagator
change when we change the
system or <u>drive parameters</u>

Optimal-control loop (i.e., gradient descent):





### Unique properties of our optimal control method







Exact 1st and higher-order derivatives	Dimensionality / memory
Handles nonlinear controls (e.g., fast-flux)	Runtime scales with K
Avoids approximations such as RWA (well-suited for driven problems)	Implementation
<ul><li>Uses a physical basis:</li><li>Easier to integrate with experiment</li><li>Convergence is exponential with K</li></ul>	
Parallelizable	
<ul><li>Handles dissipation:</li><li>Deterministic (Liouvillian)</li><li>Stochastic (non-Hermitian Hamiltonian)</li></ul>	

### **Other benefits of our implementation:**

- Full average-gate-fidelity metric as cost-function w/ 1QB-phase corrections
- Custom optimizer w/ adaptive learning rate → the cost never increases

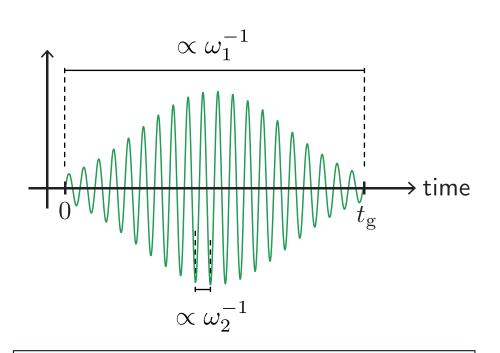


# Single-qubit microwave pulses

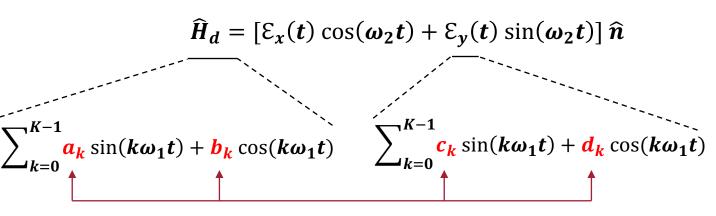


### Typical microwave pulse as a two-tone problem

### **Two-quadrature driving Hamiltonian**



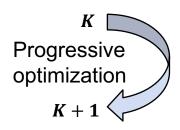
 $a_k-d_k$  determine the spectral weight of the pulse at frequencies  $\omega_2\pm k\omega_1$ 



Parameters + (Z correction, drive frequency  $\omega_2$ , QB params)

Gradient descent

- 0. Initial condition
- 1. Make operator



$$\begin{cases} \theta_1(t) = \omega_1 t \to \widehat{\theta}_1 \ (2 M_1 + 1 \dim) \\ \theta_2(t) = \omega_2 t \to \widehat{\theta}_2 \ (2 M_2 + 1 \dim) \end{cases}$$

2. Solve w/ Floquet



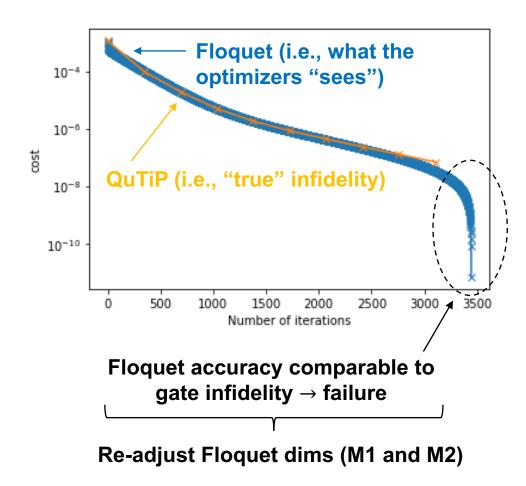
3. Compute fidelity



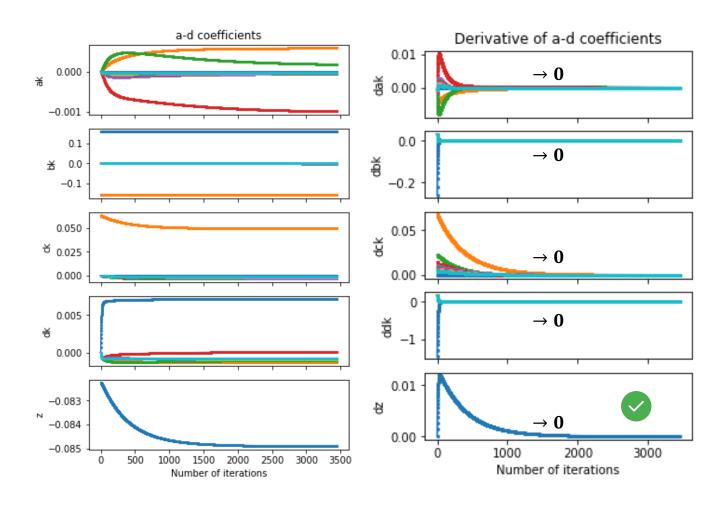
## Typical runs and consistency checks



### **Cost function minimization**



### Do parameters converge w/ iteration number?



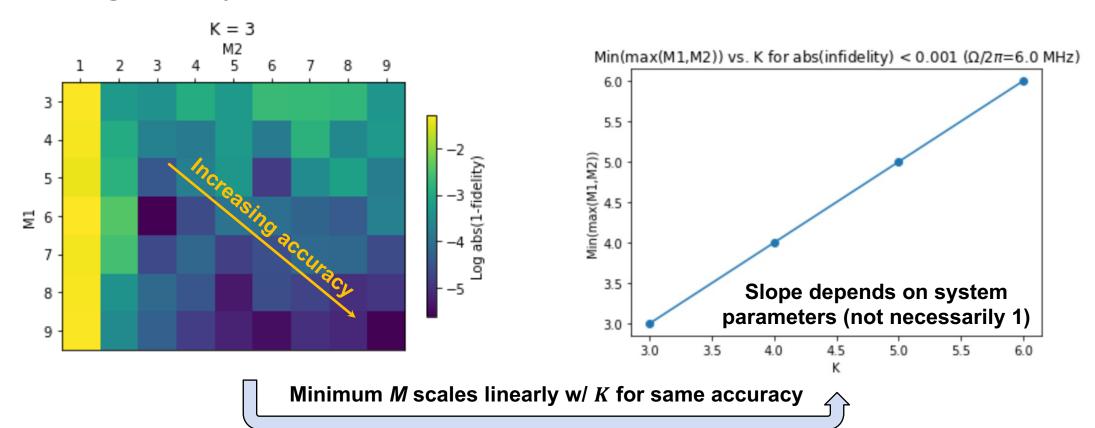


### Adjusting the accuracy of the Floquet solver



### Plot $F(U_{\text{Floquet}}, U_{\text{QuTiP}})$ averaged over randomly sampled drive parameters $a_k - d_k$

Log abs(1-fidelity) for  $\Omega/2\pi=10.0$  MHz

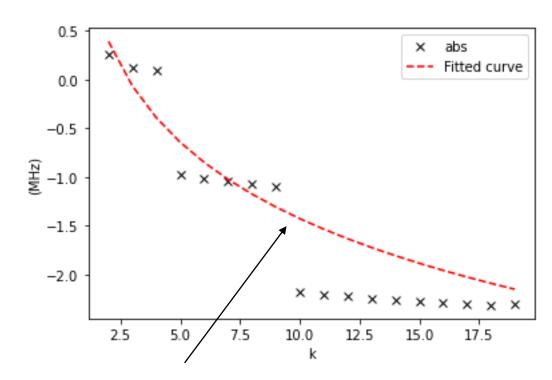




### How do we select M1 and M2?



- To benchmark, we create random pulses and compares the Floquet solver's propagator for that pulse against QuTiP's propagator.
- We increment M1 & M2 until we find (M1, M2) that produces an infidelity lower than a given target infidelity (e.g., 1.e-4)



We fit the typical "decay" of pulse coefficients with *k* to a power law, and this information to generate realistic random pulses

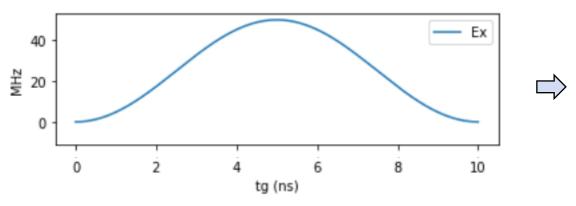


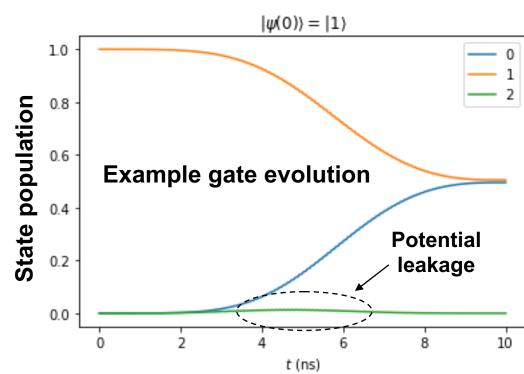
### Single-qubit gates for the transmon qubit



- Optimize gate fidelity of  $\frac{\pi}{2}$ -pulse as a function of:
  - Number of pulse parameters  $\propto K$
  - Maximum drive amplitude ( $|\Omega|/2\pi$ ).  $\mathcal{E}_x(t)=\mathrm{Re}[\Omega(t)]$ ,  $\mathcal{E}_y(t)=\mathrm{Im}[\Omega(t)]$ ,
  - Qubit anharmonicity  $(\alpha/2\pi)$

### Initial condition: cosine pulse (single quad.)

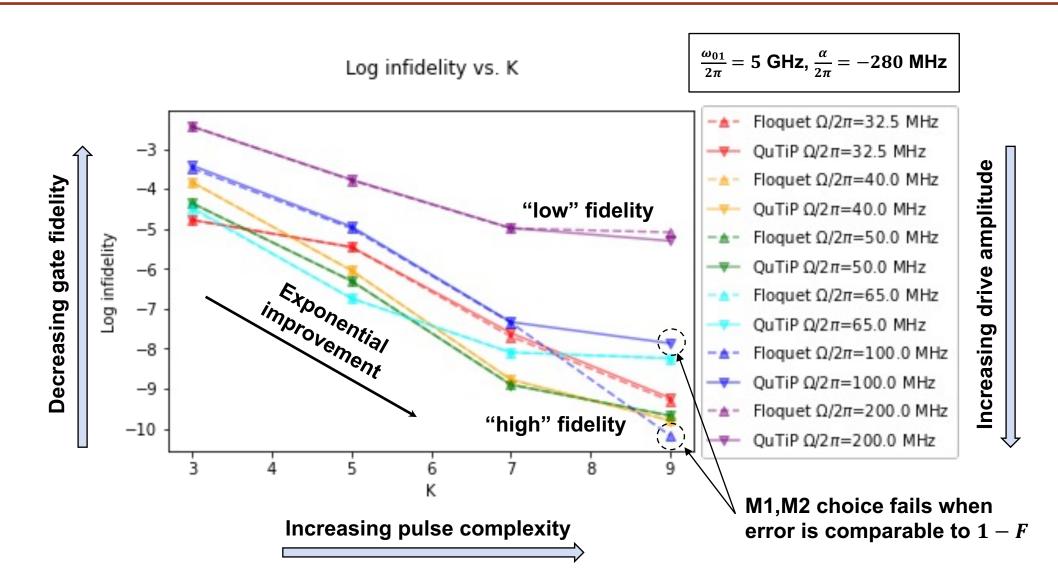






# 1QB gates for transmons: $1 - F \propto e^{-\beta K}$



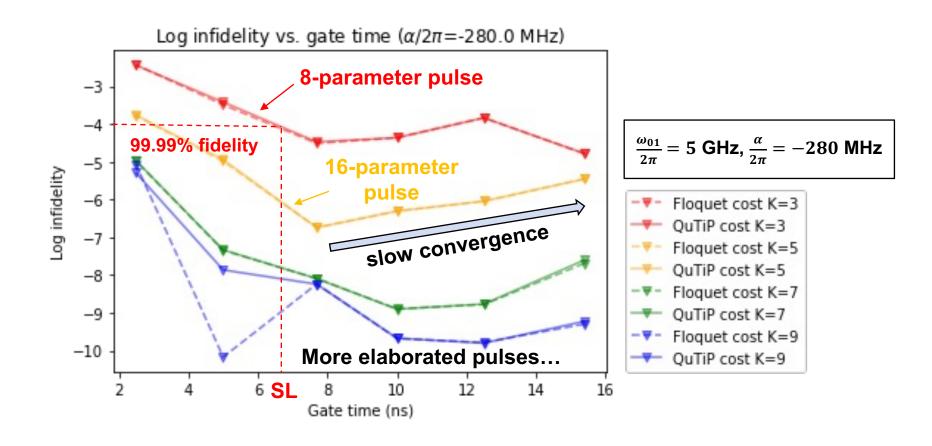




# Driving a typical transmon: speed limit (SL)



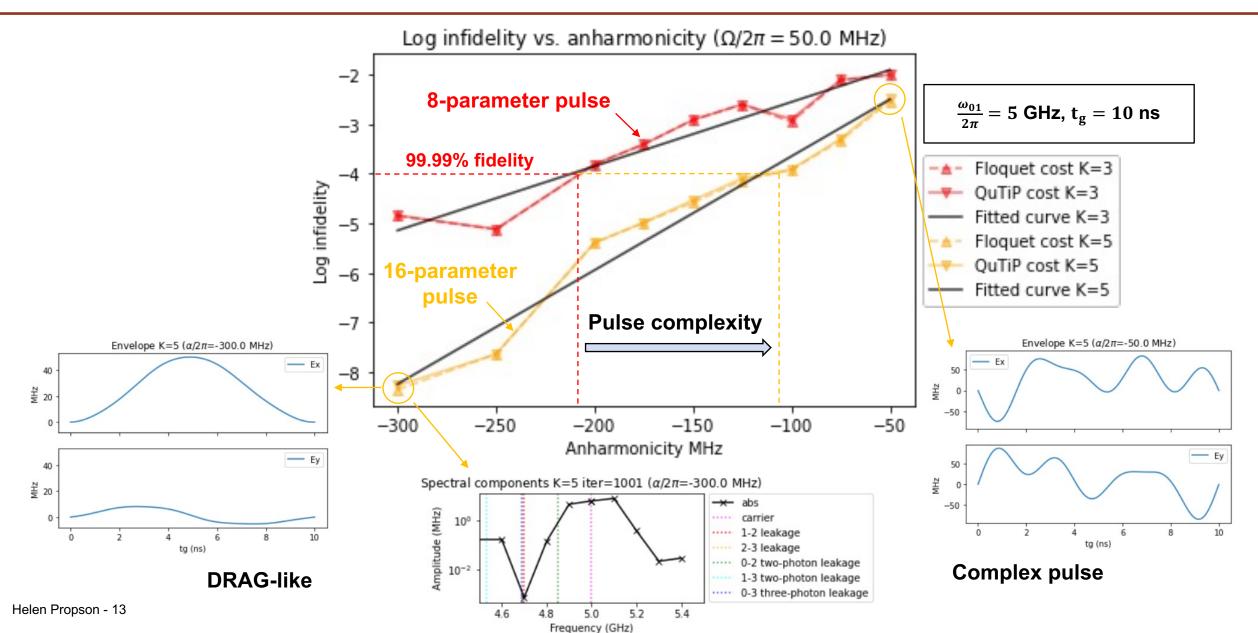
• Speed limit: how fast can we drive a  $\pi/2$  rotation? ~ 6 ns for a "nice" pulse





### **Driving weakly anharmonic transmons?**



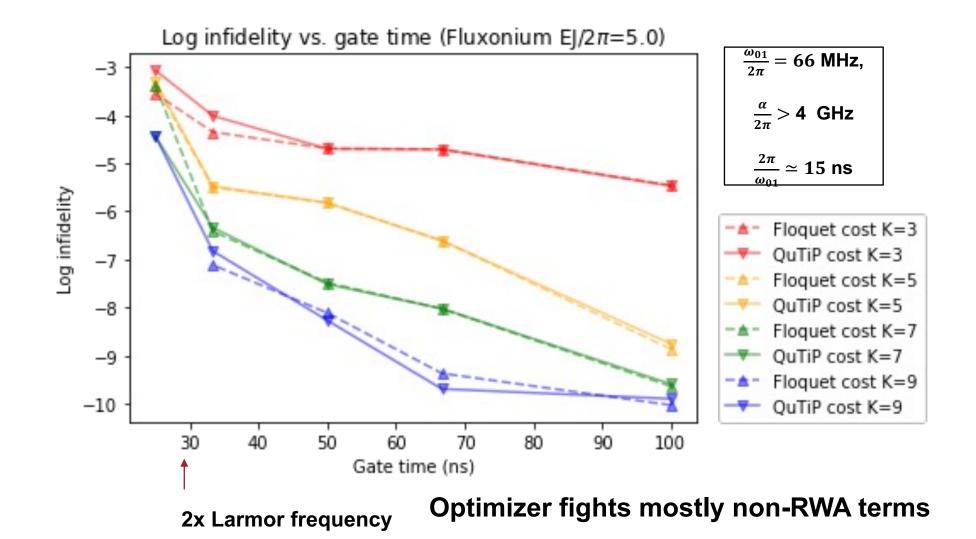




# Single-qubit gates for the fluxonium qubit



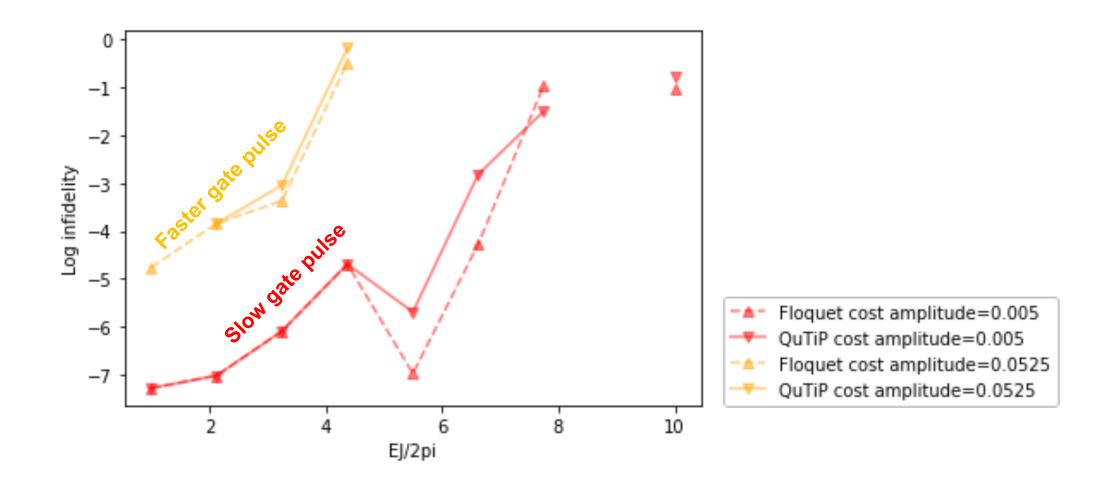
### Gates via strong capacitive driving





## Microwave driving is harder at low frequency

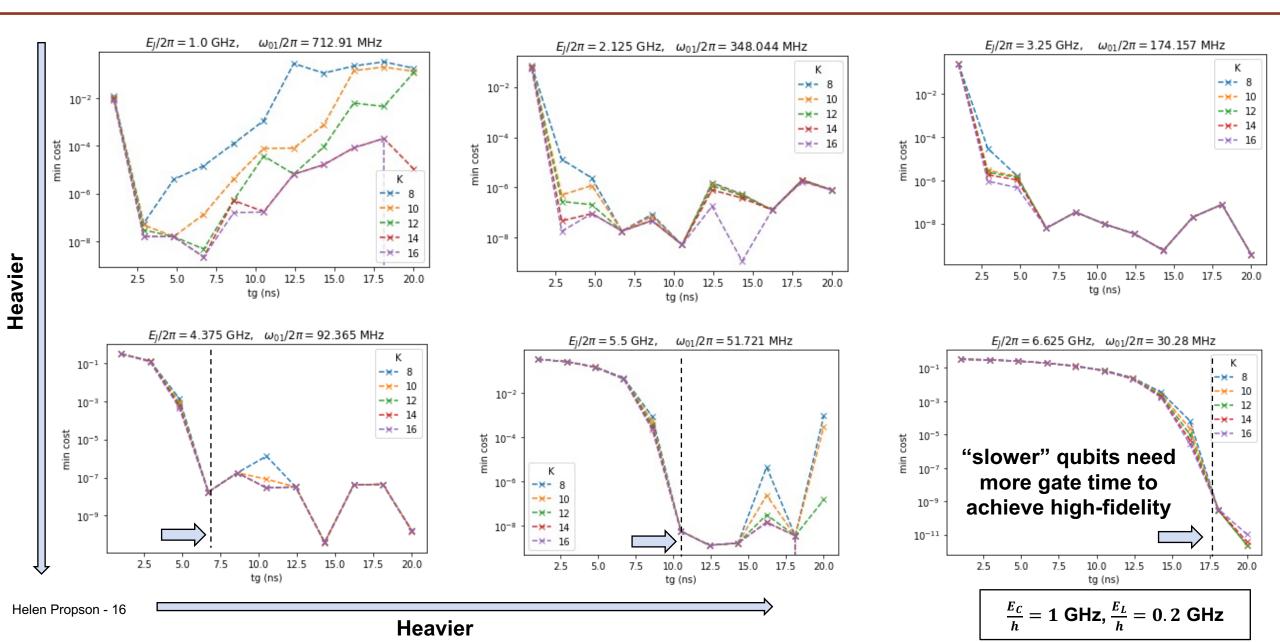






# Single-cycle 1QB fluxonium gates (fast-flux)

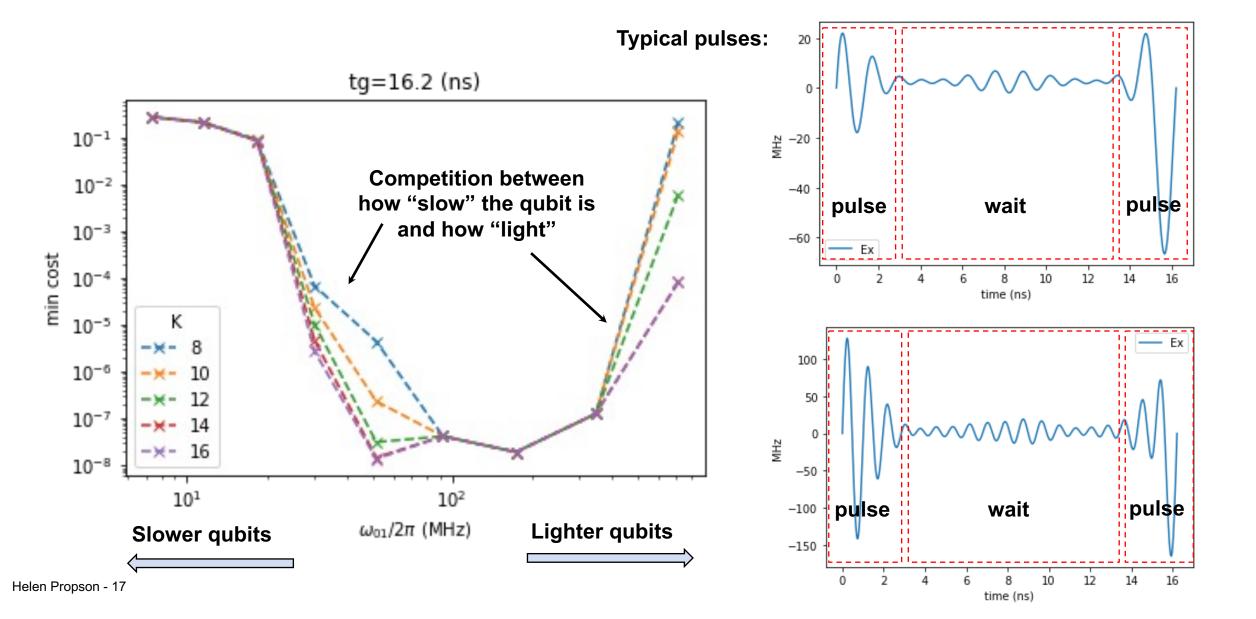






# Which kind of pulses are we "discovering"?







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