

$$2.6 \quad \int_{-1}^3 \sqrt[3]{x} dx = \int_{-1}^3 x^{\frac{1}{3}} dx = \frac{\sqrt[3]{3^4}}{\frac{4}{3}} - \frac{\sqrt[3]{(-1)^4}}{\frac{4}{3}}$$

$$= \frac{9\sqrt[3]{3}}{4} - \frac{3}{4}$$

$$\text{№ 2,7} \quad \int_{\frac{1}{\sqrt{3}}}^{\sqrt{3}} \frac{dx}{1+x^2} = \operatorname{arctg} x \Big|_{\frac{1}{\sqrt{3}}}^{\sqrt{3}} =$$

$$= \operatorname{arctg} \sqrt{3} - \operatorname{arctg} \frac{1}{\sqrt{3}} = \frac{\pi}{6} - \frac{1}{\sqrt{3}}$$

$$\text{№ 2,35} \quad \int_0^{\pi} x \sin x dx = \begin{cases} y=x \\ du=dx \end{cases} \quad \begin{aligned} dv &= \sin x \\ v &= \int \sin x = -\cos x \end{aligned}$$

$$= -x \cos x \Big|_0^{\pi} + \int_0^{\pi} -\cos x dx = (-\pi \cos \pi - 0).$$

$$= (-\sin x \Big|_0^{\pi}) = (-\pi \cos \pi) - (\sin \pi - \sin 0)$$

№ 2,15

$$\int_0^1 x^{15} \sqrt{1+3x^8} dx =$$

$$\left[\begin{array}{l} 1+3x^8 = t; \quad 24x^7 dx = 2 dt = \frac{dt}{12} \\ \begin{array}{c|c|c} x & 0 & 1 \\ \hline t & 1 & 2 \end{array} \quad \begin{array}{l} 3x^8 = t^2 - 1 \\ x^8 = \frac{t^2 - 1}{3} \end{array} \end{array} \right] =$$

$$= \int_1^2 \frac{t^2 - 1}{3} \cdot t \cdot \frac{dt}{12} = \frac{1}{36} \int_1^2 (t^3 - t) dt =$$

$$= \frac{1}{36} \left(\frac{32}{5} - \frac{8}{3} - \frac{1}{5} + \frac{1}{3} \right) = \frac{1}{36} \left(\frac{31}{5} - \frac{7}{3} \right) = \frac{29}{270}$$