

№ 1,66

$$\int \sin\left(\frac{1}{x}\right) \cdot \frac{dx}{x^2} = -2 \int \sin\left(\frac{1}{x}\right) \left(-\frac{1}{2x^2}\right) dx =$$

$$= -2 \int \sin\left(\frac{1}{x}\right) d\left(\frac{1}{x}\right) = 2 \cos\left(\frac{1}{x}\right) + C$$

№ 1,68

$$\int \frac{dx}{x \sqrt{x^2 - 1}} = \int \frac{dx}{x^2 \sqrt{1 - \frac{1}{x^2}}} = - \int \frac{1}{\sqrt{1 - \frac{1}{x^2}}} d\left(\frac{1}{x}\right)$$

$$= - \int \frac{d\left(\frac{1}{x}\right)}{\sqrt{1 - \left(\frac{1}{x}\right)^2}} = \arcsin \frac{1}{x} + C$$

№ 1,70

$$\int \frac{dx}{\sqrt{x(x+1)}} = \int \frac{dx}{\sqrt{x^2 + x}} = \int \frac{dx}{\sqrt{x^2 + x + \left(\frac{1}{2}\right)^2 - \left(\frac{1}{2}\right)^2}}$$

$$= \int \frac{dx}{\sqrt{\left(x + \frac{1}{2}\right)^2 - \left(\frac{1}{2}\right)^2}} = \ln \left| x + \frac{1}{2} + \sqrt{x^2 + x} \right| + C.$$

№ 1,72

$$\int \frac{dx}{e^{2x} + e^{-2x}} = \int \frac{dx}{e^{2x} + \frac{1}{e^{2x}}} = \int \frac{e^{2x} dx}{e^{4x} + 1} =$$

$$= \frac{1}{2} \int \frac{de^{2x}}{(e^{2x})^2 + 1^2} = \frac{1}{2} \operatorname{arctg} e^{2x} + C$$