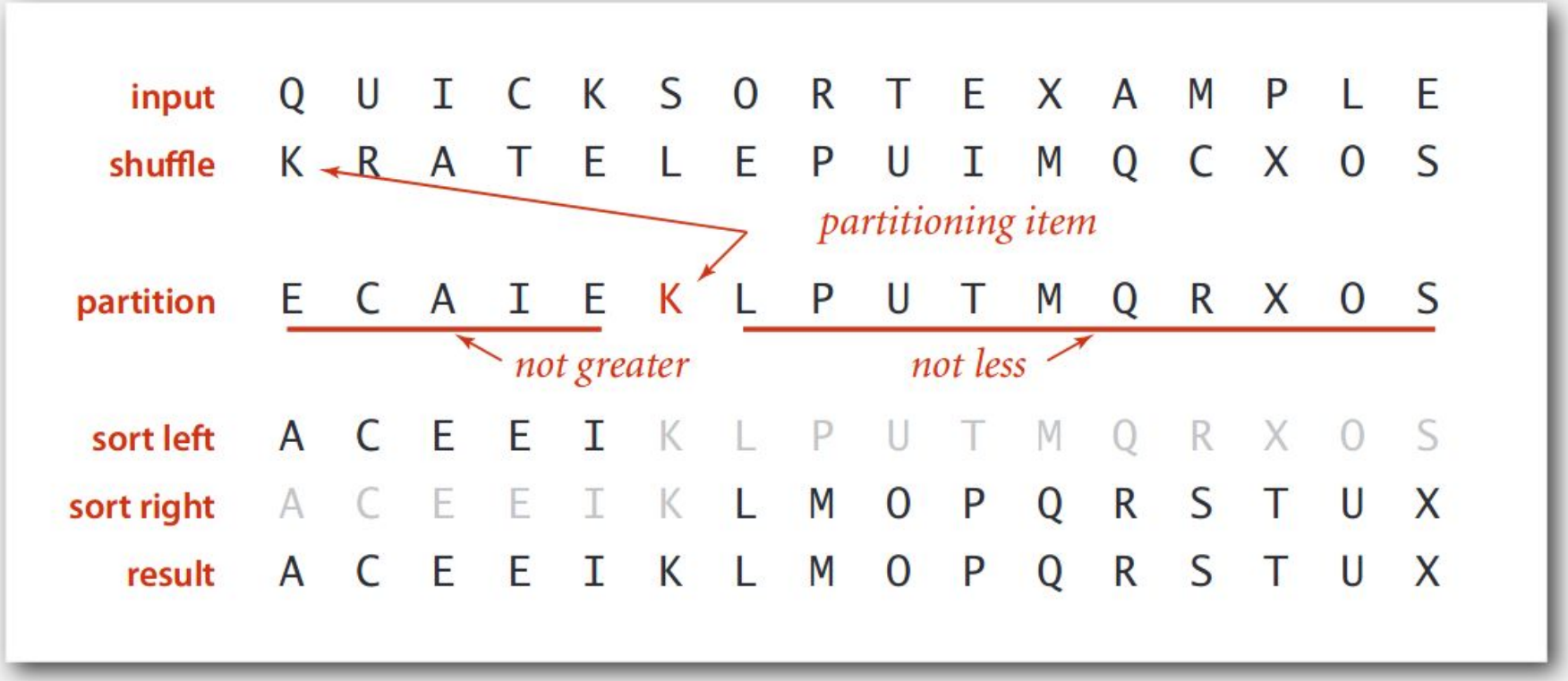
Quick Sort

Motivation. Merge sort uses auxiliary array.
Can we do O(n log(n)) sort in-place?

Quick sort. Idea

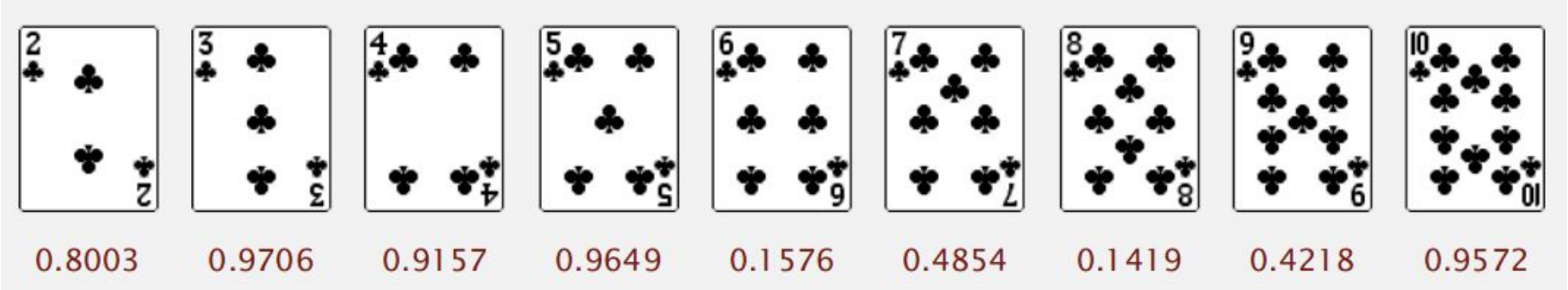
- Shuffle the array
- Partition so that, for some `j`:
  - Entry `a[j]` is in place
  - No larger entry to the left of `j`
  - No smaller entry to the right of `j`
- Sort each piece recursively

Quick sort. Idea



How to shuffle array?

- Shuffle sort
  - Generate a random real number for each array entry
  - Sort the array



How to shuffle array?

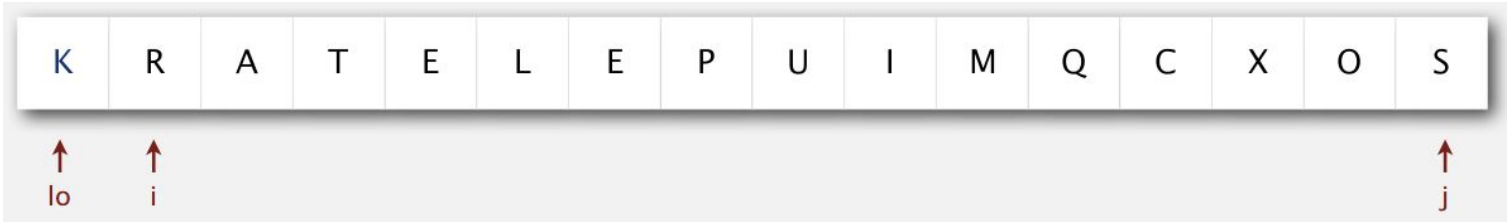
- Knuth shuffle:
  - In iteration `i`, pick integer `r` between `0` and `i` uniformly at random
  - Swap `a[i]` and `a[r]`

```
import random

def shuffle(arr):
    for i in range(len(arr)):
        r = random.randint(0, i)
        arr[r], arr[i] = arr[i], arr[r]
```

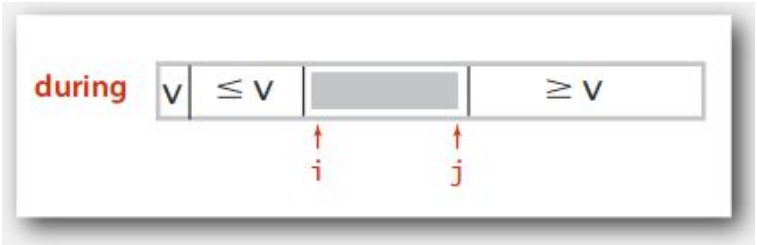
Quick sort partitioning

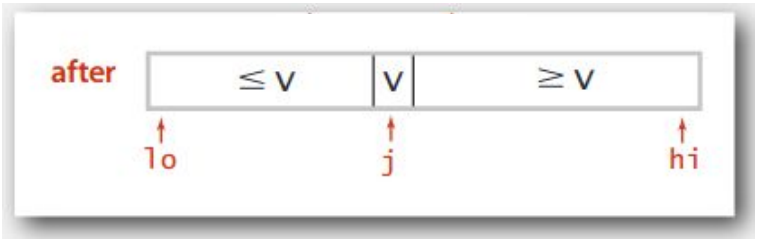
- Repeat until `i` and `j` pointers cross:
  - Scan `i` from left to right so long as `(a[i] < a[lo])`
  - Scan `j` from right to left so long as `(a[j] > a[lo])`
  - Exchange `a[i]` with `a[j]`
- When pointers cross:
  - Exchange `a[lo]` with `a[j]`



Quick sort partition() implementation

```
def partition(arr, lo, hi):
    i = lo + 1
    j = hi
    pivot = arr[lo]
    while True:
        while arr[i] <= pivot:
            if i == hi:
                break
            i += 1
        while arr[j] >= pivot:
            if j == lo:
                break
            j -= 1
        if i >= j:
            break
        arr[i], arr[j] = arr[j], arr[i]
    arr[lo], arr[j] = arr[j], arr[lo]
    return j
```





Quick sort implementation

```
def sort_req(arr, lo, hi):
    if hi <= lo:
        return
    j = partition(arr, lo, hi)
    sort_req(arr, lo, j - 1)
    sort_req(arr, j + 1, hi)


def quick_sort(arr):
    shuffle(arr)
    sort_req(arr, 0, len(arr) - 1)
```

Quick sort. Performance

- Worst-case: $O(n^2)$
- Best-case: O(n log(n))
- On average: O(n log(n))

Quick sort. Important characteristics

- One of the biggest advantage over merge sort is that quick sort doesn't take extra space. The sort is done in-place
- Number of comparisons is greater than in merge sort, but quick sort is faster in practice because of less data movements
- Probabilistic guarantee against worst case
- Quick sort is not stable

Quick sort implementation improvements

- Use insertion sort for small subarrays:
  - Quick sort has too much overhead for tiny subarrays
  - Cutoff to insertion sort for ~10 items
- Use median of sample:
  - Best choice of pivot item = median
  - Estimate true median by taking median of sample
  - Median of 3 random items