

$$\Rightarrow (\nabla f(x) - \nabla f(y))^T (x-y) - \mu \|x-y\|_2^2 \geq \frac{1}{L-\mu} \left\{ \|\nabla f(x) - \nabla f(y)\|_2^2 + \mu^2 \|x-y\|_2^2 - 2\mu (\nabla f(x) - \nabla f(y))^T (x-y) \right\}$$

$$\Rightarrow (\nabla f(x) - \nabla f(y))^T (x-y) + \frac{2\mu}{L-\mu} (\nabla f(x) - \nabla f(y))^T (x-y) \geq \frac{1}{L-\mu} \|\nabla f(x) - \nabla f(y)\|_2^2 + \frac{\mu^2}{L-\mu} \|x-y\|_2^2 + \mu \|x-y\|_2^2$$

$$\left(\frac{L+\mu}{L-\mu}\right) (\nabla f(x) - \nabla f(y))^T (x-y) \geq \frac{1}{L-\mu} \|\nabla f(x) - \nabla f(y)\|_2^2 + \frac{\mu^2}{L-\mu} \|x-y\|_2^2 + \mu \|x-y\|_2^2$$

$$\Rightarrow \left(\frac{L+\mu}{L-\mu}\right) (\nabla f(x) - \nabla f(y))^T (x-y) \geq \frac{1}{L-\mu} \|\nabla f(x) - \nabla f(y)\|_2^2 + \frac{\mu L}{L-\mu} \|x-y\|_2^2$$

$$\Rightarrow (\nabla f(x) - \nabla f(y))^T (x-y) \geq \frac{1}{L+\mu} \|\nabla f(x) - \nabla f(y)\|_2^2 + \frac{\mu L}{L+\mu} \|x-y\|_2^2$$