


Merge-sort (S):

if $|S| \leq 1$, then return S

divide S into two subsets S_1, S_2 , of equal size

$A = \text{merge-sort}(S_1)$

$B = \text{merge-sort}(S_2)$

function (A, B)

└

(A, B)

$C = \text{merge-sort}(A+B);$ ★

return C ;

Binary Search Tree (BST)

Quick Sort:

2 6 5 3 8 7 1 0
 ↑
 pivot

2 6 5 0 8 7 1 3
 ↑ ↑ ↓
 ←

⇒ 2 item. 1st: from left which is the first item that is larger than pivot.

2nd: item from right which the first item is smaller than pivot

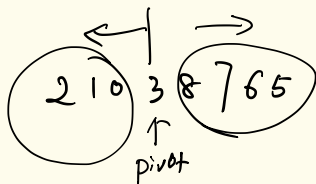
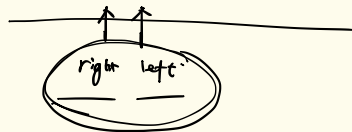
2 6 5 0 8 7 1 3 ⇒ 2 1 5 0 8 7 6 3
 ↑ ↑

2 | 5 0 8 7 6 3



\Rightarrow

2 1 0 5 8 7 6 3



Worst $O(n^2)$

Average $O(n \log n)$

Guess & Verify

$$T(n) = 2T\left(\frac{n}{2}\right) + \frac{n}{\log n} = O(n)$$

$$T(n) \leq C\left(n - \frac{n}{\log n}\right)$$

$$\Rightarrow T\left(\frac{n}{2}\right) \leq C\left(\frac{n}{2} - \frac{n/2}{\log n/2}\right)$$

$$\Rightarrow 2C\left(\frac{n}{2} - \frac{n/2}{\log n/2}\right) + \frac{n}{\log n} \leq Cn - C\frac{n}{\log n}$$

$$Cn - \frac{Cn}{\log n/2} + \frac{n}{\log n} \leq Cn - \frac{Cn}{\log n} \quad (C)$$

$$\Rightarrow Cn - \frac{Cn}{\log n - 1} + \frac{n}{\log n} \leq Cn - \frac{Cn}{\log n} \quad \star$$

$$\Rightarrow \star \frac{1}{\log n} \leq \frac{c}{\log n - 1} - \frac{c}{\log n} \quad c$$

$$\frac{c}{\log n - 1} \geq \frac{c+1}{\log n}$$

$$\frac{c}{c+1} \geq \frac{\log n - 1}{\log n} \in (0, 1)$$

$$1 \geq$$

(C)

Concept

$$T(n) = a T\left(\frac{n}{b}\right) + f(n)$$

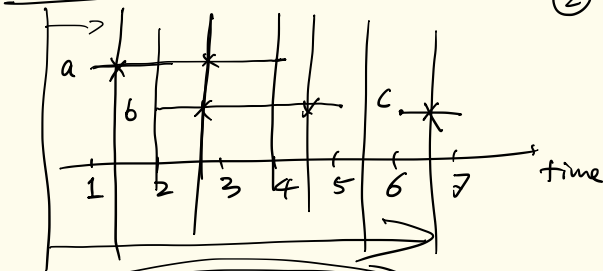
$$\rightarrow \text{Guess } \frac{O(n)}{O(n^2)} \quad \begin{aligned} &\leq C(n - f(n)) \\ &\leq C(n^2 - f(n)) \end{aligned}$$

$$\left\{ \begin{aligned} T(n) &\leq Cn = O(n) \\ aT\left(\frac{n}{b}\right) &\leq \underline{dn} = O(n) \end{aligned} \right. \leftarrow$$

Sweep Line.

Leetcode: ① Number of Airplane in the sky

② Building Outline.



$$a = [1, 4]$$

$$b = [2, 5]$$

$$c = [6, 7] \quad (2)$$

What's max number of
Airplane at one time

$$(1, 1) \quad (4, 0)$$

↑ ↓

$$[1, T] \quad [4, F]$$

$$[2, T] \quad [5, F]$$

$$[6, T] \quad [7, F]$$

for loop for all intervals:

List.add [(i.start, 1)]

List.add [(i.end, 0)]

Sort (List)

for point in List:

if p.fly == 1, count++

else:

count--

ans = Math.max(ans, count)

return ans

$O(n \log n)$

(count)

1 1 2 2 3 2 2 1

1 1 2 2 3 3 3 3

(ans)