

Nature Chemistry

## Towards Quantum Chemistry on a Quantum Computer

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Problem to solve

Experiment

Influence

### Outline

- Problem to solve
- Experiment
- Influence

Problem to solve

Experiment

Influence

### The problem

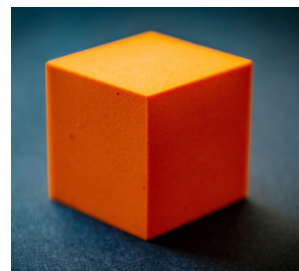
“**Exact first-principles calculations** of molecular properties are currently **intractable** because their **computational cost** grows exponentially with both the number of atoms and basis set size.”

Problem to solve

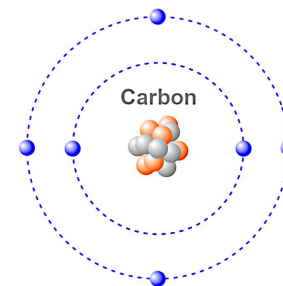
Experiment

Influence

### First Principles Calculations



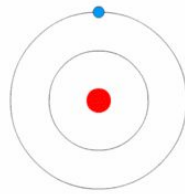
Condensed Matter



Atoms and Molecules

## First Principles Calculations

“For the most part, the way this is done is to pick a particular macroscopic phenomenon, which has been well studied experimentally, and to build empirical, or semi-empirical, models to describe the experimentally observed results.”



The Niels Bohr model of Hydrogen atom.

## First Principles Calculations

**The first principles approach** to condensed matter theory is entirely different from this. It starts from what we know about all condensed matter systems - that they are made of **atoms**, which in turn are made of **a positively charged nucleus**, and **a number of negatively charged electrons**. The interactions between atoms, such as chemical and molecular bonding, are determined by the **interactions of their constituent electrons and nuclei**.

**All of the physics of condensed matter systems arises ultimately from these basic interactions.**

If we can model these interactions accurately, then all of the complex physical phenomena that arise from them should emerge naturally in our calculations.

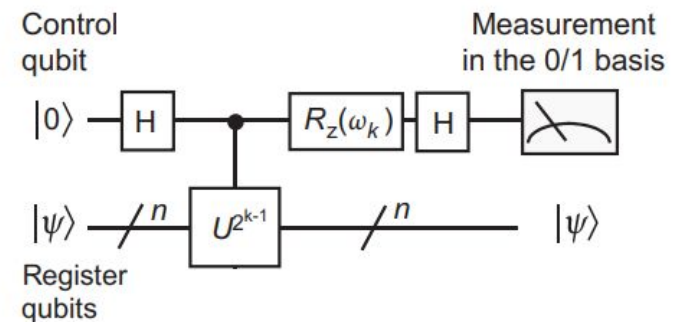
## First Principles Calculations

The Many-Electron Schrödinger Equation

$$\hat{T}\Psi_{\text{MB}} + \hat{V}\Psi_{\text{MB}} = -i\frac{d\Psi_{\text{MB}}}{dt},$$

**Intractable Computational Problem even for Supercomputers**

## Linear Optic Quantum Computer(2 qubits)



## Methodology

1. Encoding a molecular wave function into qubits;
2. Simulating its time evolution using quantum logic gates;
3. Extracting the approximate energy using the phase estimation algorithm.

## Encoding Wave Function into Qubits

### Basis Set

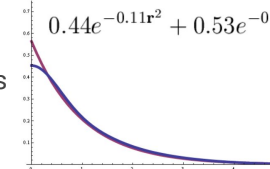
A set of functions (called basis functions) that is used to **represent the electronic wave function** in the Hartree–Fock method or density-functional theory in order to turn the partial differential equations of the model into algebraic equations **suitable for efficient implementation on a computer.**

### Minimal Basis Sets

**STO-3G**, 3 Gaussian primitive functions comprising a single basis function.

STO-3G functions for the 1s orbital of a hydrogen atom

$$0.44e^{-0.11r^2} + 0.53e^{-0.41r^2} + 0.15e^{-2.23r^2}$$



## Encoding Wave Function into Qubits

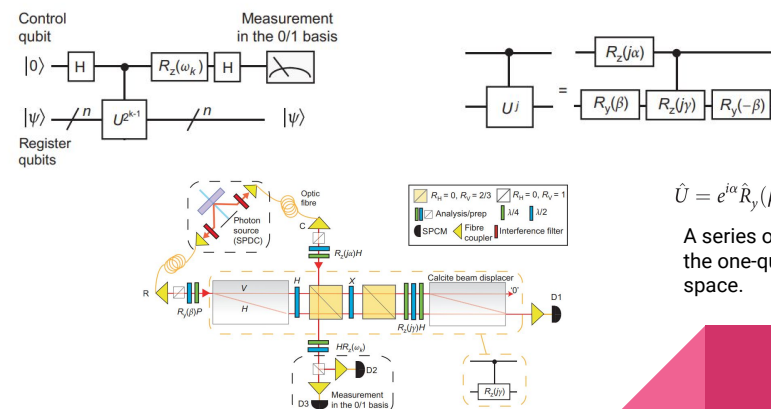
Six two-electron configurations

$$\{\Phi_i\}_{i=1}^6 \rightarrow \{\Phi_1, \Phi_6\} \quad \{\Phi_2\} \quad \{\Phi_3, \Phi_4\} \quad \{\Phi_5\}$$

Finding the **eigenvalues** of the two  $2 \times 2$  submatrices in the Hamiltonian,  $H^{(1,6)}$  and  $H^{(3,4)}$ , is what we need.

Estimating the eigenvalues of  $2 \times 2$  matrices is the simplest problem for the IPEA.

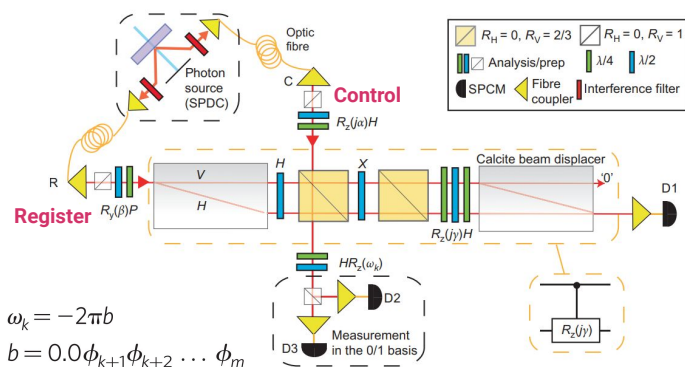
## Experiment Design



$$\hat{U} = e^{i\alpha} \hat{R}_y(\beta) \hat{R}_z(\gamma) \hat{R}_y(-\beta)$$

A series of rotations of the one-qubit Hilbert space.

## Experiment Design



To produce an m-bit approximation to the phase of the eigenstate, we need to repeat this algorithm m times.

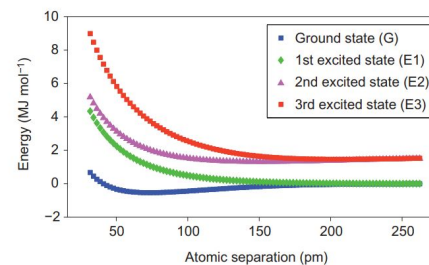
IF control horizontally polarized:  
Nothing is changed  
IF control vertically polarized:  
 $\hat{U}^{2^{k-1}}$  is implemented on the register

$$\omega_k = -2\pi b$$

$$b = 0.0\phi_{k+1}\phi_{k+2} \dots \phi_m$$

starting from the least significant ( $\phi_m$ )

## Result



$$E = 2\pi\phi E_h + \left(\frac{e^2}{4\pi\epsilon R}\right) - E_\infty$$

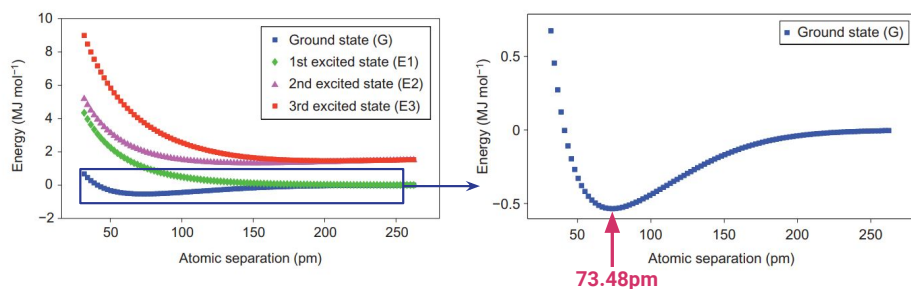
Proton-proton  
Coulomb energy  
at atomic  
separation R

Each point was calculated with a 20-bin iterative phase estimation algorithm, using n=31 samples per bit.

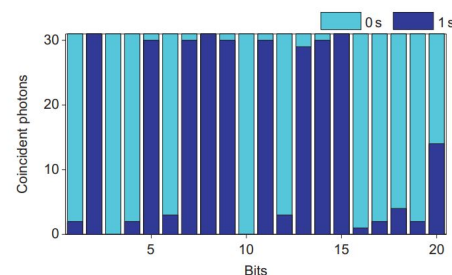
- Ground state (G) – Low Eigenvalue of  $H^{(1,6)}$
- 1st excited state (E1) – Low Eigenvalue of  $H^{(3,4)}$
- 2nd excited state (E2) – High Eigenvalue of  $H^{(3,4)}$
- 3rd excited state (E3) – High Eigenvalue of  $H^{(1,6)}$

Ground state energy of  
two hydrogen atoms  
at infinite separation

## Result



## Result



0.01001011101011100000

Equal to the exact value  
of minimal basis, to a  
precision of  $\pm 2^{-20}E_h$

## Impact

### Previous Idea:

- [1] Feynman, R.P. Simulating physics with computers. Int J Theor Phys 21, 467–488 (1982).  
<https://doi.org/10.1007/BF02650179>
- [2] Lloyd, Seth. "Universal quantum simulators." Science (1996): 1073-1078.
- [3] Abrams, Daniel S., and Seth Lloyd. "Simulation of many-body Fermi systems on a universal quantum computer." Physical Review Letters 79.13 (1997): 2586.

### Previous Algorithm:

- [1] Brown, Kenneth R., Robert J. Clark, and Isaac L. Chuang. "Limitations of quantum simulation examined by simulating a pairing Hamiltonian using nuclear magnetic resonance." Physical review letters 97.5 (2006): 050504.
- [2] Somaroo, S., et al. "Quantum simulations on a quantum computer." Physical review letters 82.26 (1999): 5381.
- [3] Yang, Xiaodong, et al. "Experimental simulation of a pairing Hamiltonian on an NMR quantum computer." Chemical physics letters 422.1-3 (2006): 20-24.
- [4] Friedenauer, Axel, et al. "Simulating a quantum magnet with trapped ions." Nature Physics 4.10 (2008): 757-761.
- [5] Gerritsma, Rene, et al. "Quantum simulation of the Dirac equation." Nature 463.7277 (2010): 68-71.

Experimentally proved the feasibility of quantum computer simulating particles.

## Is it believable?

Yes.

Nature Chemistry

582 citations in 10 years.

## Limitations

- 2-qubits quantum computer
- STO-3G H<sub>2</sub> model
- Non-scalable implementation of IPEA

## Questions?