

Information: The final exam is open book and will be divided in the following way:

- 30%: Problems from the material of guides 1 and 2 [DPV 0, 2-6]
- 70%: Problems from the topics of this guide

Topics:

1. Huffman encoding
 - (a) Definition of the compression problem
 - (b) Huffman encoding algorithm
 - (c) Tracing of the Huffman encoding algorithm
 - (d) Analysis of Huffman encoding using a min-heap
2. Dynamic programming
 - (a) Using tables instead of recursion
 - (b) Edit distance algorithm
 - (c) Chain matrix multiplication
 - (d) All pairs shortest paths problem
 - (e) Floyd Warshall's Algorithm
3. Max Flow Problem [DPV 7.2, CLRS 26.1, 26.2]
 - (a) Definition of the problem
 - (b) Flow properties
 - (c) Ford and Fulkerson's Algorithm
 - (d) Cut properties
 - (e) Max flow - min cut
 - (f) Correctness of Ford and Fulkerson's Algorithm
 - (g) Analysis of Ford and Fulkerson's algorithm
 - (h) Edmonds Karp Algorithm
4. Maximum Bipartite Matching [DPV 7.3, CLRS 26.3]
 - (a) Definition of polynomial reductions
 - (b) Description of the problem
 - (c) Reduction to Max flow

5. P and NP [DPV 8.2, CLRS 34.1-34.2]
 - (a) Definition of Turing Machine [lecture 17, 18]
 - (b) Decision, Optimization, and Search problems
 - (c) Polynomial time reducibility (\leq_P)
 - (d) Definition of P
 - (e) Definition of NP (verification, non-deterministic)
6. NP-hard [DPV 8.2, CLRS 34.3-34.4]
 - (a) Definition of NP-hard
 - (b) Definition of NP-complete
 - (c) Relationships among the classes P, NP, NP-hard, NP-complete
7. NP-complete problems [DPV 8.3, CLRS 34.5]
 - (a) Reduction from Turing Machines to CNF-SAT
 - (b) $\text{CNFSAT} \leq_P \text{3SAT}$
 - (c) $\text{3SAT} \leq_P \text{Clique}$
 - (d) $\text{Clique} \leq_P \text{Vertex Cover}$
 - (e) $\text{3SAT} \leq_P \text{Subset sum}$
8. Coping with NP-completeness [DPV 9.1, 9.2, CLRS 35.1]
 - (a) Pseudopolynomial time algorithm for Subset Sum
 - (b) Backtracking; Branch and Bound
 - (c) Approximation Algorithms
 - (d) Vertex Cover approximation algorithm
 - (e) Concepts of APX, PTAS, PTAS reducibility