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CS-225: Discrete Structures in CS  
Homework 7, Part 2

### Exercise Set 9.4: Problem 6

A. By the pigeon hole principle if seven integers are divided by 6 then a minimum of two must have the same remainder as at most there can be 6 (0,1,2,3,4 & 5) ANS: Yes

B. Take the set 0,1,2,3,4,5,6. None have the same remainder when divided by 8. ANS: No

### Exercise Set 9.4: Problem 8

$$T = \{1, 2, 3, 4, 5, 6, 7, 8, 9\}$$

ANS: No

If we take (1,9) (2,8) (3,7) (4,6) each adds to 10 but if we take 5,  $\{1,2,3,4,5\}$  no two integers will add up to 10 and the biggest sum 4+5 is 1 short.

### Exercise Set 9.4: Problem 16

ANS: 81

We know there are 20 integers between 1-100 that are divisible by 5 so in order to pick 1 that is divisible by 5 we would need the 80 (100-20) that are not divisible by 5 and 1 that is,  $80+1=81$

### Exercise Set 9.4: Problem 28

$$n = 500 \quad k = 17 \quad \text{ANS: Yes}$$

$$\frac{n}{k} = \frac{500}{17} = 29.42 \approx 30$$

By the pigeon hole rule there is at least one day.