

# Induction-variable Optimizations in GCC

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# Outline

- Background
- Implementation of GCC
- Learned points
- Shortcomings
- Improvements
- Question & Answer
- References

## Background – Induction variable

- Induction variable
  - Variables whose successive values form an arithmetic progression over some part of program, usually a loop.

```
int  a[100], i;  
for (i = 0; i < 100; i++) {  
    a[i] = 202 - 2 * i  
}
```

```
/*Induction variables:  
    i, &a[i], 2*i, 202-2*i  
*/
```

## Background – Identify induction variables

- Basic/Fundamental induction variable
  - Variables explicitly modified by a same constant amount during each iteration of a loop.
- Derived/General induction variable
  - Variables modified in more complex ways

```
int  a[100], i;  
for (i = 0; i < 100; i++) {  
    a[i] = 202 - 2 * i  
}
```

```
/*Induction variables:  
    i, &a(i), 2*i, 202-2*i  
*/
```

# Background – Induction-variable optimizations

## ■ Strength reduction

```
int  a[100], i;  
for (i = 0; i < 100; i++) {  
    a[i] = 202 - 2 * i  
}
```

```
//&a[i]  $\leftrightarrow$  a + 4 * i  
//202 - 2 * i
```

```
int  a[100], i;  
int *iv1 = a, iv2 = 202;  
  
for (i = 0; i < 100; i++) {  
    *iv1 = iv2;  
    iv1 += 4;  
    iv2 -= 2;  
}
```

# Background – Induction-variable optimizations

## ■ Linear function test replacement

```
int  a[100], i;
int *iv1 = a, iv2 = 202;

for (i = 0; i < 100; i++) {
    *iv1 = iv2;
    iv1 += 4;
    iv2 -= 2;
}

int  a[100], i;
int *iv1 = a, iv2 = 202;

for (i = 0; iv2 != 2; i++) {
    *iv1 = iv2;
    iv1 += 4;
    iv2 -= 2;
}
```

# Background – Induction-variable optimizations

## ■ Removal of induction variables

```
int  a[100], i;  
int *iv1 = a, iv2 = 202;  
  
for (i = 0; iv2 != 2; i++) {  
    *iv1 = iv2;  
    iv1 += 4;  
    iv2 -= 2;  
}
```

```
int  a[100];  
int *iv1 = a, iv2 = 202;  
  
for (; iv2 != 2;) {  
    *iv1 = iv2;  
    iv1 += 4;  
    iv2 -= 2;  
}
```

# Background – Induction-variable optimizations

- Unnecessary bounds checking elimination
  - refers to determine whether the value of a variable is within specified bounds in all of its uses in a program

```
var b: array[1..100,1..10] of integer;  
  i, j, s: integer;  
s := 0;  
for i = 1 to 50 do  
  for j = 1 to 10 do  
    s := s + b[i,j]
```



```
  i ← init  
L1: . . .  
  if i < lo trap 6  
  if i > hi trap 6  
  use of i that must  
    satisfy  $lo \leq i \leq hi$   
  . . .  
  i ← i + 1  
  if i <= fin goto L1
```



```
  if lo > init trap 6  
  t1 ← fin min hi  
  i ← init  
L1: . . .
```

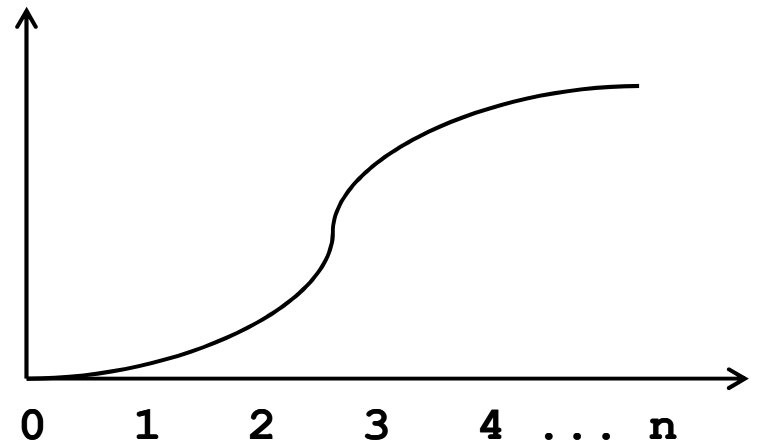
```
  use of i that must  
    satisfy  $lo \leq i \leq hi$   
  . . .  
  i ← i + 1  
  if i <= t1 goto L1  
  if i <= fin trap 6
```



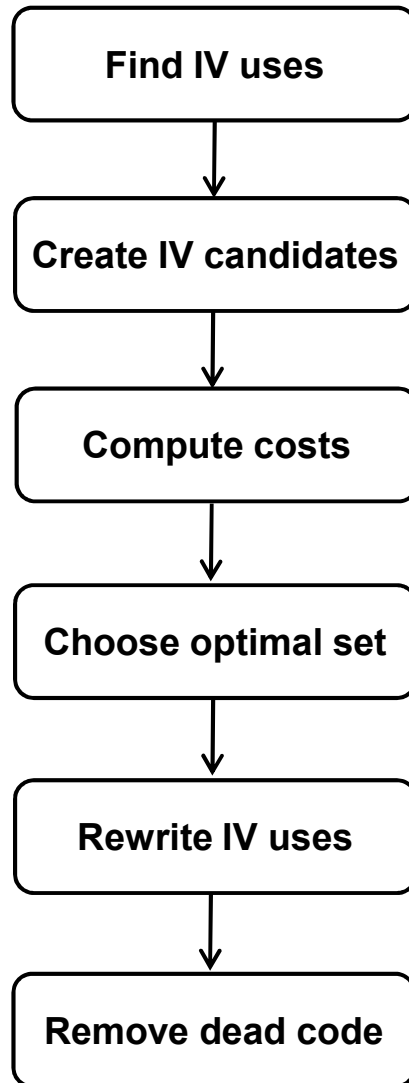
# Implementation of GCC

- Identify induction variable
  - SSA form
  - Scalar evolution
    - implemented in tree-scalar-evolution.[ch]
    - analyzes the evolution of scalar variables in loop
  - Chain of recurrence
    - is a canonical representation of polynomials functions
    - can evaluate polynomials function at a number of points in an interval effectively
    - models induction variable analysis

$$f(x) = x^a + x^{(a-1)} + c$$
$$f(0), f(1), f(2), \dots, f(n)$$



# Implementation of GCC - Unified algorithm



```
int  a[100], i;  
for (i = 0; i < 100; i++) {  
    a[i] = 202 - 2 * i  
}
```

use 0: 202-2\*i      cand 0: <0, 1>  
use 1: &a[i]      cand 1: <202, -2>  
use 2: i < 100      cand 2: <a, 4>  
cand 3: <a-4, 4>

The diagram shows four uses on the left and four candidates on the right. Red arrows indicate the mapping: use 0 maps to cand 1 and cand 2; use 1 maps to cand 0 and cand 2; use 2 maps to cand 1 and cand 3.

```
int  a[100];  
int *iv1 = a, iv2 = 202;  
  
for (; iv2 != 2;) {  
    *iv1 = iv2;  
    iv1 += 4;  
    iv2 -= 2;  
}
```

# Implementation of GCC – Example

- IR before IVOPT

```
<bb 3>:  
# i_14 = PHI <i_11(4), 0(2)>  
i_0_4 = (unsigned int) i_14;  
_5 = i_0_4 * 4;  
_7 = a_6(D) + _5;  
_8 = 101 - i_14;  
_9 = _8 * 2;  
* _7 = _9;  
i_11 = i_14 + 1;  
if (i_11 != 100)  
    goto <bb 3>;  
else  
    goto <bb 5>;
```

- IV uses

```
use 0: <202, -2, _9>  
use 1: <a, 4, _7>  
use 2: <0, 1, i_11>
```

- IV candidates

```
cand 0: <0, 1, normal>  
cand 1: <202, -2, normal>  
cand 2: <a, 4, normal>  
cand 3: <a-4, 4, before>  
cand 4: <a, 4, after>
```

# Implementation of GCC – Example

## ■ Representation

	use 0	use 1	use 2
cand 0	$202 - 2 * iv\_cand$	$a + 4 * iv\_cand$	$iv\_cand \neq 100$
cand 1	$iv\_cand$	$a + 2 * (202 - iv\_cand)$	$iv\_cand \neq 2$
cand 2	NA	$MEM[iv\_cand]$	$iv\_cand \neq a + 400$
cand 3	NA	$MEM[iv\_cand]$	$iv\_cand \neq a + 400$
cand 4	NA	$MEM[iv\_cand]$	$iv\_cand \neq a + 400$

## ■ Costs

	use 0	use 1	use 2
cand 0	8	8	0
cand 1	0	26	0
cand 2	NA	6	0
cand 3	NA	2	0
cand 4	NA	2	0

# Implementation of GCC – Example

- Choose optimal iv set

```
use:0  → cand:0  → cand:1  → cand:1
use:1  → cand:0  → cand:0  → cand:4
use:2  → cand:0  → cand:0  → cand:1
```

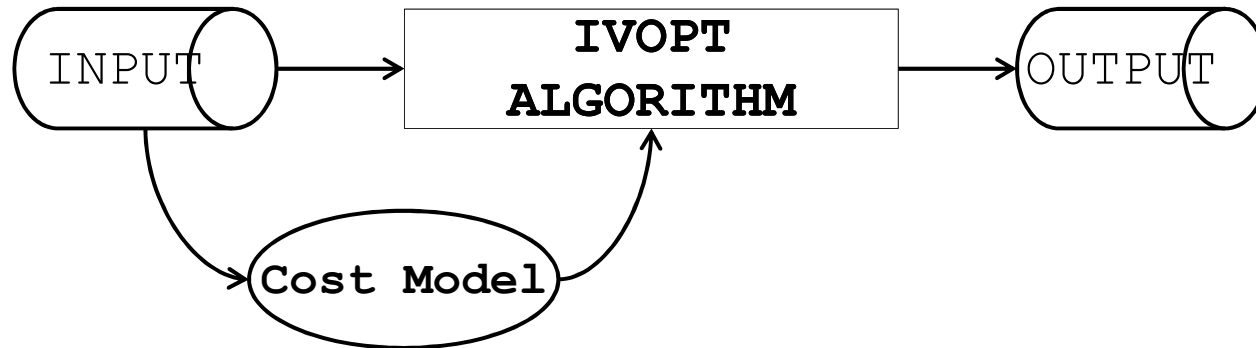
- Rewrite iv uses and remove dead code

```
<bb 3>:
# i_14 = PHI <i_11(4), 0(2)>
i_0_4 = (unsigned int) i_14;
_5 = i_14 * 4;
_7 = a_6(D) + _5;
_8 = 101 - i_14;
_9 = _8 * 2;
*_7 = _9;
i_11 = i_14 + 1;
if (i_11 != 100)
    goto <bb 3>;
else
    goto <bb 5>;
```

```
<bb 2>:
iv.9_2 = (unsigned int) a_6(D);
<bb 3>:
# i_14 = PHI <i_11(4), 0(2)>
# iv.6_3 = PHI <iv.6_2(4), 202(2)>
# iv.9_1 = PHI <iv.9_3(4), iv.9_2(2)>
_5 = i_14 * 4;
_7 = a_6(D) + _5;
_8 = 101 - i_14;
_9 = (int) iv.6_3;
_16 = (void *) iv.9_1;
MEM[base: _16, offset: 0B] = _9;
iv.9_3 = iv.9_1 + 4;
iv.6_2 = iv.6_3 - 2;
i_11 = i_14 + 1;
if (iv.6_2 != 2)
    goto <bb 3>;
else
    goto <bb 5>;
```

# Implementation of GCC – Learned points

- Infrastructure



- Unified algorithm
- Cost Model
  - rtx cost, like “+,-,\*,/,%,<<,...”
  - address cost
- Context information
  - Loop invariant
  - Register pressure
- Interact with other optimizations

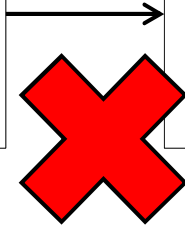
addressing mode
[reg]
[reg + reg]
[reg + reg<<const]
[reg + const]!
[reg], #const

# Shortcomings - implementation

- fine tuned only for x86/x86\_64
  - scaled addressing mode not supported for ARM, etc.
  - support of auto-increment addressing mode is weak for ARM

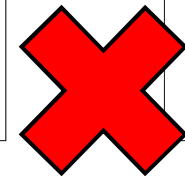
addressing mode
[reg]
[reg + reg]
[reg + reg<<const]
[reg + const]!
[reg], #const

```
int  a[100], i;
for (i = 0; i < 100; i++){
    tmp = a + i*4
    MEM[tmp] = 202 - 2*i
}
```



```
int  a[100], i;
for (i = 0; i < 100; i++){
    MEM[a+i<<2] = 202 - 2*i
}
```

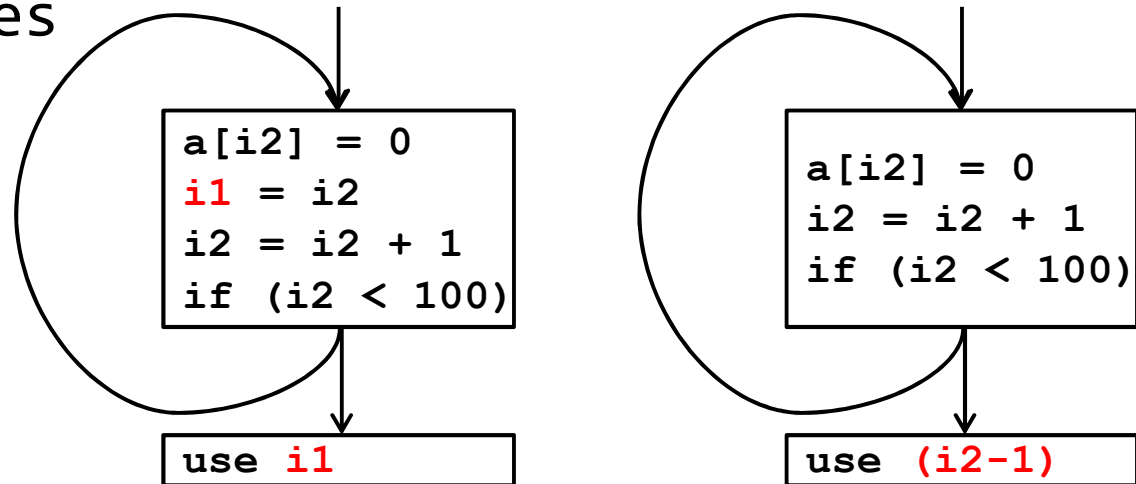
```
int  a[100];
int *iv1 = a, iv2 = 202;
for (; iv2 != 2;) {
    *iv1 = iv2;
    iv1 += 4;
    iv2 -= 2;
}
```



```
int  a[100];
int *iv1 = a, iv2 = 202;
for (; iv2 != 2;) {
    MEM([iv1], #4) = iv2;
    iv2 -= 2;
}
```

## Shortcomings - implementation

- iv uses outside of loop are not handled along loop exit edges



- induction variables in both branches of IF-statement are not recognized

```
int  a[100], i = 0;
while (i < 100) {
    if (i % 2 == 0)
        a[i] = 0;  i++;
    else
        a[i] = 1;  i++;
}
```



# Shortcomings – implementation

- complex address expression

- hard to process
- inaccurate cost

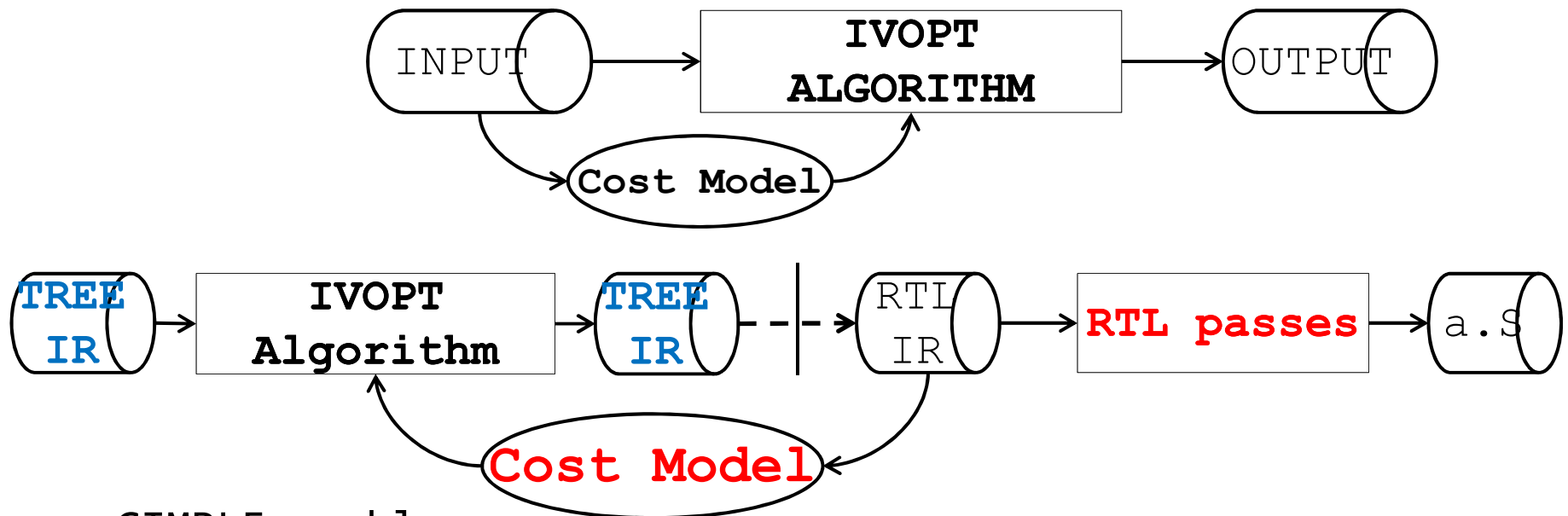
```
&MEM[ptr+offset]
&arr[index].y
&MEM[ptr+offset] +/- step
&arr[index].y      +/- step
```

```
ptr + offset
arr + index*obj_size + y_offset
ptr + offset                               +/- step
arr + index*obj_size + y_offset           +/- step
```

```
ptr + const_1
arr + const_2
```

# Shortcomings - infrastructure

- GCC's two IRs: GIMPLE(IVOPT) & RTL
  - Inaccurate rtx cost
  - “WRONG” address cost model for ARM
  - Conflict with RTL optimizations, like loop unrolling



- GIMPLE problems
  - Conflict with GIMPLE optimizations, like DOM
  - Association of loop invariant in IVOPT

$x=a+b+c \rightarrow t=a+b; x=t+c$   
or  
 $\rightarrow t=a+c; x=t+b$

# Improvements – Work & patches

- Support scaled addressing mode for architectures other than x86/x86\_64.
  - <http://gcc.gnu.org/ml/gcc-patches/2013-08/msg01642.html>
  - <http://gcc.gnu.org/ml/gcc-patches/2013-09/msg01927.html>
- Simplify address expressions for IVOPT
  - <http://gcc.gnu.org/ml/gcc-patches/2013-11/msg00537.html>
  - <http://gcc.gnu.org/ml/gcc-patches/2013-11/msg01075.html>
- Fix wrong address cost for auto-increment addressing mode
  - <http://gcc.gnu.org/ml/gcc-patches/2013-11/msg00156.html>
- Expedite the use of auto-increment addressing mode
  - <http://gcc.gnu.org/ml/gcc-patches/2013-09/msg00034.html>
  - more patches coming...
- Compute outside loop iv uses along exit edges
  - <http://gcc.gnu.org/ml/gcc-patches/2013-11/msg00535.html>
- Improve the optimal iv set choosing algorithm
  - patches coming...
- Miscellaneous fixes for IVOPT
  - ...

# Improvements – Work & patches

- Following work
  - Fix address cost mode and RTL passes, e.g. fwprop\_addr

```
arm_arm_address_cost (rtx x)
{
  enum rtx_code c = GET_CODE (x);

  if (c == PRE_INC || c == PRE_DEC || c == POST_INC || c == POST_DEC)
    return 0;
  if (c == MEM || c == LABEL_REF || c == SYMBOL_REF)
    return 10;

  if (c == PLUS)
  {
    if (GET_CODE (XEXP (x, 1)) == CONST_INT)
      return 2;

    if (ARITHMETIC_P (XEXP (x, 0)) || ARITHMETIC_P (XEXP (x, 1)))
      return 3;

    return 4;
  }
  return 6;
}
```

addr mode	[reg]	[reg+reg]	[reg+reg<<i]	[reg+offset]	[reg], #off
cost	6	4	3	2	0

# Improvements – Benchmark data

- Performance
  - Coremark
  - EEMBC\_v1
    - automotive, office, consumer, telecom
  - Spec2000
- Code size
  - CSIBE

**Question and Answer**

**Thank You!**

# References

- source code & internal & mailing list
  - `gcc.gnu.org`
- Advanced compiler design and implementation
- Symbolic Evaluation of Chains of Recurrences for Loop Optimization, etc.