

Question #1: Binary Numbers

Please convert the following number to/from binary to decimal and complete the missing values in the chart below. Be sure to show your work (you may take pictures/scan your written work or provide typed responses).

Binary	Signedness	Decimal
1101	Unsigned	13
100110	One's Complement	-25
1011010110	Two's Complement	-298
0111011001110	One's Complement	3790
110000110010	Two's Complement	-974

$$\textcircled{1} \quad 1101_2 = 2^0 + 0 + 2^2 + 2^3 = 13_{10}$$

$$\textcircled{2} \quad -25 = 2^4 + 2^3 + 2^0 = 011001_2 \Rightarrow 1\text{'s comp. } 100110_2.$$

$$\textcircled{3} \quad 298 = 256 + 32 + 8 + 2 = 2^8 + 2^5 + 2^3 + 2^1 = 100101010$$

$$\Rightarrow 1\text{'s comp. } 01101010 \Rightarrow 2\text{'s comp. } \begin{array}{r} 01101010 \\ + 10110101 \\ \hline 1011010110_2 = -298 \end{array}$$

1 at the most left means negative

$$\textcircled{4} \quad 0111011001110 = 2^1 + 2^2 + 2^3 + 2^6 + 2^7 + 2^{10} + 2^{11} = 3790.$$

Zero at the most left means the result is positive, so we don't flip 1 & 0.

$$\textcircled{5} \quad 110000110010$$

One at the most left means negative, so.

$$\Rightarrow 1\text{'s comp. } 001111001101$$

$$\Rightarrow 2\text{'s comp. } \begin{array}{r} 001111001101 \\ + 001111001110 \\ \hline 001111001110_2. \end{array}$$

$$\Rightarrow -(2^1 + 2^2 + 2^3 + 2^6 + 2^7 + 2^8 + 2^9) = (-974)$$

Question #2: Hexadecimal Numbers

Please convert the following number to/from hexadecimal to decimal/binary and complete the missing values in the chart below. Be sure to show your work (you may take pictures/scan your written work or provide typed responses).

Hex	Signedness	Decimal	Binary
B2C	Unsigned	2860	1011 0010 1100
E6	One's Complement	-25	1110 0110
AC	Two's Complement	-84	1010 1100
3AFD	One's Complement	15301	0011 1010 1111 1101
BEE	Two's Complement	-1042	1011 1110 1100

- ① $\begin{array}{cccc} 1 & 1 & 2 & 12 \end{array} \Rightarrow \text{Binary format } = 1011 \ 0010 \ 1100_2 \\ = (2^1 + 2^9 + 2^8 + 2^5 + 2^3 + 2^2)_{10} = 2860_{10} \end{math}$
- ② $\begin{array}{ccccc} 1 & 4 & 6 & 1 & 4 \\ E & 6 & _{16} & \Rightarrow & 1110 \ 0110_2 \end{array} \Rightarrow 1\text{'s comp. } 0001 \ 1001_2$
 leftmost is 1 so result is negative $\Rightarrow (2^0 + 2^3 + 2^4)_{10} = (1+8+16)_{10} = -25_{10}$
- ③ $\begin{array}{c} -84 = (2^2 + 2^4 + 2^6)_{10} = 0101 \ 0100_2 \Rightarrow 1\text{'s comp. } 1010 \ 1011_2 \\ -84 = + \frac{1010 \ 1011_2}{1010 \ 1100_2} \quad \frac{1010 \ 1100_2}{2^3 + 2^1} = AC_{16} \end{array}$
- ④ $\begin{array}{c} 0011 \ 1010 \ 1111 \ 1101_2 \text{ leftmost is zero so result is positive,} \\ \text{we don't flip 1 and 0.} \end{array}$
 $\text{Decimal Value} = (2^0 + 2^2 + 2^3 + 2^4 + 2^5 + 2^6 + 2^7 + 2^9 + 2^{11} + 2^{12} + 2^{13})_{10} = 15301_{10}$
- ⑤ $\begin{array}{c} 0011 \ 1010 \ 1111 \ 1101_2 \Rightarrow \text{Hex.} = 3AFD_{16} \\ 2^0 + 2^1 \ 2^2 + 2^3 \ 2^4 + 2^5 + 2^6 \ 2^7 + 2^8 + 2^9 + 2^{10} \end{array}$
 $\begin{array}{c} 11 \ 15 \ 15 \\ BEE_{16} = 1011 \ 1110 \ 1100_2 \text{ leftmost is 1 so result is negative} \\ \Rightarrow 1\text{'s comp. } 0100 \ 0001 \ 0001_2 \\ \Rightarrow 2\text{'s Comp. } 0100 \ 0001 \ 0010_2 \end{array}$
 $\text{decimal value} = -(2^1 + 2^4 + 2^{10})_{10} = -1042_{10}$

Question #3: Octal Numbers

Please convert the following number to/from octal to decimal/binary/hex and complete the missing values in the chart below. Be sure to show your work (you may take pictures/scan your written work or provide typed responses).

Octal	Signedness	Decimal	Binary	Hex
1051	Unsigned	553	0010 0010 1001	229
-167	One's Complement	-199	110001000 - 001110111	-77
246	Two's Complement	166	10100110	
176544	One's Complement	64868	1111110101100100	FD64
-143	Two's Complement	-99	0011101 = 1100011	-63

$$\textcircled{1} \quad 1051 = 001 \underline{000} \underline{101} \underline{001}_2$$

$$= (2^0 + 2^3 + 2^5 + 2^9)_{10} = 553_{10}$$

$$= \underline{2^1} + \underline{2^1} + \underline{2^0 + 2^3} = 229_{16}.$$

$$\textcircled{2} \quad -167_8 = -001 \underline{110} \underline{111}_2 = -(2^0 + 2^1 + 2^2 + 2^4 + 2^5 + 2^6)_{10} = -199_{10}.$$

$$\Rightarrow \textcircled{-167} \quad \textcircled{442+7} \Rightarrow \text{Hex. Value} = -77_{16}.$$

$$\textcircled{3} \quad \text{Hex} \rightarrow \text{octal, binary}$$

$$00A6_{16} = 0000 \underline{0000} \underline{1010} \underline{0110}_2 = 246_8. \quad \begin{matrix} \text{leftmost bit is 0, simply} \\ \text{convert Binary} \Rightarrow \text{decimal} \end{matrix}$$

$$\text{decimal} \rightarrow \text{octal, binary}$$

$$166_{10} = (2^7 + 2^5 + 2^3 + 2^1)_0 = 0000 0000 \underline{10100110}_2 = 246_8.$$

$$\textcircled{4} \quad 1111 \underline{1101} \underline{0110} \underline{0100}_2 = (2^2 + 2^5 + 2^6 + 2^8 + 2^{10} + 2^{11} + 2^{12} + 2^{13} + 2^{14} + 2^{15})_{10}$$

$$= 64868_{10}.$$

$$\Rightarrow \textcircled{FD64}_{16}.$$

$$\Rightarrow \underline{001} \underline{111} \underline{110} \underline{011} \underline{010} \underline{000}_2 = 176544_8.$$

$$\textcircled{5} \quad \text{decimal} \rightarrow \text{binary}$$

$$99 = 64 + 32 + 2 + 1 = 2^6 + 2^5 + 2^2 + 2^0 = 1100011_2 \Rightarrow \begin{matrix} \text{1's Comp.} + \\ \text{1} \end{matrix}$$

$$\begin{matrix} 0011100 \\ 1 \end{matrix}$$

$$\text{binary} \rightarrow \text{octal, Hex}$$

$$-(1100011) = -143_8$$

$$-(0110 \underline{0011}) = \underline{(4+2)} \underline{2+1} = -63_{16}.$$

Question #4: Arithmetic and Overflow

Complete the following arithmetic operations and tell whether or not there is overflow and provide a brief justification. Please be sure to show your work (you may take pictures/scan your written work or provide typed responses).

Unsigned, 5-bit binary addition			5-bit Binary Sum	5-bit Decimal Sum	Overflow?
01010	+	01011	10101	21	Not overflow

Justification: We can represent the 5-bit decimal with 5-bit Binary sum.

$$\begin{aligned}
 01010_2 &= 2^4 + 2^3 = 10_{10} \\
 + 01011_2 &= 2^4 + 2^3 + 2^2 = 11_{10} \\
 \hline
 10101 &= 2^4 + 2^3 + 2^2 = 21_{10}
 \end{aligned}$$

Unsigned, 8-bit binary addition			8-bit Binary Sum	8-bit Decimal Sum	Overflow?
11011001	+	10100110	(1)01111111	383	Overflow

Justification: we can't represent the result in 8-bit because it requires 9 bits

$$\begin{aligned}
 11011001_2 &= 2^8 + 2^7 + 2^6 + 2^5 + 2^4 + 2^3 + 2^2 + 2^1 = 217_{10} \\
 + 10100110_2 &= 2^8 + 2^7 + 2^6 + 2^5 + 2^4 + 2^3 + 2^2 + 2^1 = 166_{10} \\
 \hline
 10111111_2 &= 2^8 + 2^7 + 2^6 + 2^5 + 2^4 + 2^3 + 2^2 + 2^1 = 383_{10}
 \end{aligned}$$

Here, I can't be disregarded, otherwise the decimal value will be 127, which is less than 383

Two's Complement, 16-bit hex addition			16-bit Binary Sum	16-bit Decimal Sum	Overflow?
FACE	+	6EEF	(1)011010011011101	27069	Overflow

Justification: FACE = 1111 1010 1100 1110 \Rightarrow 1's = 0000 0101 0011 0011 \Rightarrow 2's = 1111 0100 0110 0000 \Rightarrow 23 \Rightarrow 0000 0101 0011 0010 \Rightarrow 28339. \Rightarrow -(2¹⁶ + 2¹⁵ + 2¹⁴ + 2¹³) = -1536.

$$\begin{aligned}
 \text{Binary Sum} &= 1011010011011101_2 = -1536. \\
 \text{If 1 carry bit is disregarded, the result is } &\text{so only when the 1 (carry-out is regarded)} \\
 &\text{binary sum} = 27069 = 28339 + (-1536).
 \end{aligned}$$

Two's Complement, 8-bit hex subtraction			8-bit Binary Sum	8-bit Decimal Sum	Overflow?
0x88	-	0x0A	(1)01111110	126	Not overflow

Justification:

$$88_{16} = 10001000_2 = (2^7 + 2^3)_{10} = 136_{10}$$

$$0A_{16} = 00001010_2 = (2^4 + 2^3)_{10} = 10_{10}. \quad \text{Decimal Sum} = 136 - 10 = 126_{10}.$$

$$\Rightarrow 1's = 11110101$$

$$\Rightarrow 2's = \frac{1}{11110101}$$

$$\begin{array}{r}
 10001000 \\
 + 00001010 \\
 \hline
 10111110
 \end{array}$$

1 carry-out is disregarded and result is

$$2^7 + 2^6 + 2^5 + 2^4 + 2^3 + 2^2 = 126_{10}$$

When 1 carry value is disregarded,

8-bit decimal sum can be represented by 8-bit binary sum. Hence, Not overflow.

Question #5: IEEE 754 Floating-point Number

Please convert the following number to its binary and hexadecimal IEEE 754-formatted equivalent:

-8765.125

Sign bit will be 1 as the number is negative

$$8765_{10} = 8192 + 512 + 32 + 16 + 8 + 4 + 1$$

$$= (2^13 + 2^9 + 2^5 + 2^4 + 2^3 + 2^2 + 2^0)_{10}$$

$$\text{binary format} = 1000100011101.$$

$$0.125 \times 2 = 0.25 \rightarrow 0$$

$$0.25 \times 2 = 0.5 \rightarrow 0 \quad \text{so} \quad 0.125_{10} = (0.01)_2$$

$$0.5 \times 2 = 1.0 \rightarrow 1.$$

$$\begin{aligned} \text{Combine together, } 8765.125 &= 1000100011101_2 \cdot 001 \\ &= 1.000100011101001_2 \times 2^{13} \end{aligned}$$

Exponent $E = 13 + 127$ to account bias, we get

$$\begin{aligned} E &= 140_{10} = 128 + 8 + 4 = 2^7 + 2^3 + 2^2 \\ &= 10001100_2 \end{aligned}$$

Then we Convert fraction, $f = 16 \text{ bits} + 7 \text{ zeros}$

$$= 00010001110100100000000$$

Combine together, -8765.125_{10} in binary is

$$\begin{array}{cccccccccc} 1 & 1 & 0 & 0 & 0 & 1 & 0 & 0 & 0 & 0 \\ \hline 12 & = & C & & 6 & & 0 & & 8 & 15 = F \\ & & & & & & & & & 4 \\ & & & & & & & & & 8 \\ & & & & & & & & & 0 \end{array}$$

In hexadecimal,

$$-8765.125_{10} = C608F48D_{16}.$$

Question #6: Converting Bytes to Binary and ASCII Text

Please convert the following string of bytes to:

1. Binary
2. ASCII text

0x43 0x6F 0x6D 0x70 0x75 0x74 0x65 0x72 0x20 0x4F 0x72 0x67 0x21

convert Hexadecimal to binary

$$43_{16} = \underline{4}(\underline{2+1}) = 0100\ 0011$$

$$6F_{16} = \underline{6}(\underline{2+4+2+1}) = 0110\ 1111$$

$$6D_{16} = 0110\ 1101$$

$$70_{16} = 0111\ 0000$$

$$75_{16} = 0111\ 0101$$

$$74_{16} = 0111\ 0100$$

$$65_{16} = 0110\ 0110$$

$$72_{16} = 0111\ 0010$$

$$20_{16} = 0100\ 0000$$

$$4F_{16} = 0100\ 1111$$

$$72_{16} = 0111\ 0010$$

$$67_{16} = 0110\ 0111$$

$$21_{16} = 0010\ 0001$$

251.2073

ASCII /UTF-8

Computer Org!