

Q11.

$$P_1 = \frac{1}{3}, P_2 = \frac{2}{5}, P_3 = \frac{2}{3}$$

$$q_1 = 1 - \frac{1}{3} \quad q_2 = 1 - \frac{2}{5} \quad q_3 = 1 - \frac{2}{3}$$

$$q_1 = \frac{2}{3} \quad q_2 = \frac{3}{5} \quad q_3 = \frac{1}{3}$$

prob. at least one success = $1 - q_1 q_2 q_3$

$$= 1 - \frac{2}{3} \times \frac{3}{5} \times \frac{1}{3}$$

$$= \frac{13}{15}$$

Q12. (i)

4 W
3 R
2 B

four balls are drawn without replacement their pro. (all are white)

(ii) balls are drawn with replacement then

$$P(\text{all white}) = \frac{4}{9} \times \frac{4}{9} \times \frac{4}{9} \times \frac{4}{9} = \left(\frac{4}{9}\right)^4$$

Q13. (i) without replacement $P(\text{no ball is white})$

$$= \frac{5C_4}{9C_9} = \frac{5}{126}$$

(ii) with replacement $P(\text{no ball is white})$

$$= \frac{5}{9} \times \frac{5}{9} \times \frac{5}{9} \times \frac{5}{9}$$

Q14. (i)

2 R
3 B

Three ball are drawn at random

$$\begin{aligned} \text{Req. prob} &= P(2R \neq 1B) + P(1R 2B) \\ &= \frac{2C_2 \times 3C_1}{5C_3} + \frac{^2C_1 \times 3C_2}{5C_3} = \frac{3+6}{10} = \frac{9}{10} \end{aligned}$$

Q15.

5W
7R
4B

four ball drawn one by one with replacement

$$P(\text{No white}) = \frac{11}{16} \times \frac{11}{16} \times \frac{11}{16} \times \frac{11}{16} = \left(\frac{11}{16}\right)^4$$

16.

1W
5R
4B

Three ball are drawn one by one without replacement

$$\text{Req. Prob.} = P(WRR)$$

$$= \frac{1}{10} \times \frac{5C_2}{9C_2} = \frac{10}{10} \times \frac{1}{36}$$

$$= \frac{1}{36}$$

18.(iii) 4R

7B

Two ball are drawn with replacement

$$P(\text{one red one black})$$

$$= P(RB) + P(BR)$$

$$= \frac{4}{11} \times \frac{7}{11} + \frac{7}{11} \times \frac{4}{11}$$

$$= \frac{56}{121}$$

Dt.

Pg.

Q1

3W
3R
3B

Three ball are drawn without replacement

$$P(\text{atleast one Red ball}) = \frac{{}^3C_1 \times {}^6C_2 + {}^3C_2 \times {}^6C_1 + {}^3C_3}{{}^9C_3}$$

$$= \frac{45 + 18 + 1}{84} = \frac{64}{84} = \frac{16}{21}$$

$$Q2 \quad P(G) = \frac{30}{100}$$

$$P(\bar{G}) = \frac{70}{100}$$

In three days prob. of getting green signal in two consecutive day

$$= P(G G \bar{G}) + P(\bar{G} G G)$$

$$= \frac{30}{100} \times \frac{30}{100} \times \frac{70}{100} + \frac{70}{100} \times \frac{30}{100} \times \frac{30}{100}$$

$$= \frac{126}{1000}$$

$$= \frac{63}{500}$$

22. (ii)

3W
7R
15B

I

10W
6R
9B

II

one ball is drawn from each bag

$$\begin{aligned}
 P(\text{same color}) &= P(WW) + P(RR) + P(BB) \\
 &= \frac{3}{25} \times \frac{10}{25} + \frac{7}{25} \times \frac{6}{25} + \frac{15}{25} \times \frac{9}{25} \\
 &= \frac{30}{625} + \frac{42}{625} + \frac{135}{625} = \frac{207}{625}
 \end{aligned}$$

24.

3 Boys
3 Girls

members in a group = 4

$$\text{Req. prob} = P(3B\ 1G) + P(3G\ 1B)$$

$$\frac{3C_3 \times 3C_1}{6C_4} + \frac{3C_3 \times 3C_1}{6C_4}$$

$$= \frac{6}{15} = \frac{2}{5}$$

Q5. Four cards are drawn from pack of 52 cards

$$(i) P(\text{all are same suit}) = 4 \times \frac{13C_4}{52C_4} = \frac{44}{4365}$$

$$(ii) P(\text{all are of same no.}) = \frac{13 \times 4C_4}{52C_4} = \frac{1}{20825}$$

(iii) Three cards are drawn

$$P(\text{one King, one Queen, one Jack}) = \frac{4C_1 \times 4C_1 \times 4C_1}{52C_3}$$

$$= \frac{64}{22100} - \frac{16}{5525}$$

Q6.

5W	7W
4B	• 9B

One ball is drawn from I bag & two from other bag

$$P(\text{one w two Black}) = P(W(BB)) + P(B(WB)) \\ = \frac{5}{9} \times \frac{9C_2}{10C_2} + \frac{4}{9} \times \frac{7C_1 \times 9C_1}{10C_2}$$

$$= \frac{180}{1080} + \frac{252}{1080} \Rightarrow \frac{2}{5}$$

Q27 Two dice are rolled

i) $P(\text{both dice have diff. no.}) = \frac{6 \times 5}{6 \times 6} = \frac{5}{6}$

(ii) $P(\text{Total is at least } 4) = 1 - P(\text{sum is less than } 4)$

sum is less than 4 = $\{(1,1), (1,2), (2,1)\}$

Req. event Required prob. = $1 - \frac{3}{36} = \frac{11}{12}$

$$= \frac{11}{12}$$

(iii) $P(\text{product is odd}) = \frac{3}{6} \times \frac{3}{6} = \frac{9}{36} = \frac{1}{4}$

Q28 Three dice are rolled

(i) $P(\text{same on three dice})$

$$= \frac{6}{6} \times \frac{1}{6} \times \frac{1}{6}$$

$$= \frac{1}{36}$$

(ii) $E = \text{Total is } 5$

$$= \{(1, 1, 3), (1, 3, 1), (3, 1, 1), \\ (2, 2, 2), (2, 1, 2), (2, 2, 1)\}$$

$$P(E) = \frac{6}{216} = \frac{1}{36}$$

(iii) $E = \text{Total is atmost } 5$

$$= \{(1, 1, 1), (1, 1, 2), (1, 2, 1), (2, 1, 1), \\ (1, 1, 3), (1, 3, 1), (3, 1, 1), (1, 2, 2), \\ (2, 1, 2), (2, 2, 1)\}$$

$$P(E) = \frac{10}{216} = \frac{5}{108}$$

(iv) $P(\text{at least } 5)$

$$= 1 - P(\text{at most } 5) + P(5)$$

$$= 1 - \frac{5}{108} + \frac{1}{36}$$

$$= \frac{108 - 5 + 3}{108}$$

$$= \frac{106}{108} = \frac{53}{54}$$

$$= \frac{53}{54}$$

Q30.

Horse A

$$P(A) = \frac{1}{5}$$

$$P(\bar{A}) = \frac{4}{5}$$

Horse B

$$P(B) = \frac{2}{3}$$

$$P(\bar{B}) = \frac{1}{3}$$

$$(i) P(\text{both are selected}) = P(A) \cdot P(B) = \frac{1}{5} \times \frac{2}{3} = \frac{2}{15}$$

$$P(\text{only one will select}) = P(A) \cdot P(\bar{B}) + P(B) \cdot P(\bar{A}) \\ = \frac{1}{5} \times \frac{1}{3} + \frac{4}{5} \times \frac{2}{3} = \frac{8}{15}$$

$$P(\text{none of them will select}) = P(\bar{A}) \cdot P(\bar{B}) = \frac{4}{5} \times \frac{1}{3} \\ = \frac{4}{15}$$

$$P(\text{at least one of them will select}) = 1 - P(\text{none of them}) \\ = 1 - \frac{4}{15} = \frac{11}{15}$$

D1.

P0.

$$\text{Q32. (iii)} \quad P(A) = \frac{1}{2} \quad P(B) = \frac{1}{3}$$

$$P(\bar{A}) = 1 - \frac{1}{2} = \frac{1}{2}$$

$$P(\bar{B}) = 1 - \frac{1}{3} = \frac{2}{3}$$

$$P(C) = \frac{1}{4} \quad P(\bar{C}) = \frac{3}{4}$$

$$P(\text{only one will solve}) = P(A) \cdot P(\bar{B}) \cdot P(\bar{C}) + \\ P(B) \cdot P(\bar{A}) \cdot P(\bar{C}) + P(C) \cdot P(\bar{A}) \cdot P(\bar{B})$$

$$= \frac{1}{2} \times \frac{2}{3} \times \frac{3}{4} + \frac{1}{3} \times \frac{1}{2} \times \frac{3}{4} + \frac{1}{4} \times \frac{1}{2} \times \frac{2}{3}$$

$$= \frac{6+3+2}{24} = \frac{11}{24}$$

$$P(\text{exactly two will solve}) = P(A) \cdot P(B) \cdot P(\bar{C}) + P(B) \cdot P(C) \cdot P(\bar{A}) + P(C) \cdot P(A) \cdot P(\bar{B})$$

$$= \frac{1}{2} \times \frac{1}{3} \times \frac{3}{4} + \frac{1}{3} \times \frac{1}{4} \times \frac{1}{2} + \frac{1}{4} \times \frac{1}{2} \times \frac{2}{3}$$

$$= \frac{6}{24} = \frac{1}{4}$$

(iii) (at least two will solve)

$$= P(\text{exactly two solve}) + P(\text{all solve})$$

$$= \frac{1}{4} + P(A) \cdot P(B) \cdot P(C) = \frac{1}{4} + \frac{1}{2} \times \frac{1}{2} \times \frac{1}{3} \times \frac{1}{4}$$

$$= \frac{7}{24}$$

- Q34. p_1 = prob. of I component fail = 0.14
 p_2 = " II component " = 0.10
 p_3 = " III component " = 0.05

machine will work if all the three components work

$$\begin{aligned} P(\text{machine will not work}) &= 1 - (1-p_1)(1-p_2)(1-p_3) \\ &= 1 - (1-0.14)(1-0.10)(1-0.05) \\ &= 1 - 0.86 \times 0.90 \times 0.95 \\ &= 0.2647 \end{aligned}$$

- Q35. $P(A) = \text{prob. A speaks truth} = \frac{60}{100}$

- $P(B) = \text{prob. B speaks truth} = \frac{90}{100}$

$$P(\text{contradict each other}) = P(A) \cdot P(\bar{B}) + P(B) \cdot P(\bar{A})$$

$$= \frac{60}{100} \left(1 - \frac{40}{100} \right) + \frac{40}{100} \left(1 - \frac{60}{100} \right)$$

$$= \frac{3600}{10000} + \frac{1600}{10000} = \frac{52}{100} = 52\%$$

$$P(\text{Agree to each other}) = P(A) \cdot P(B) + P(\bar{A}) \cdot P(\bar{B})$$

$$= \frac{60}{100} \times \frac{40}{100} + \frac{60}{100} \times \frac{40}{100}$$

$$= \frac{4800}{10000} = 48\%$$

Q36. Ticket = {1, 2, 3, ..., 10}

Two tickets are drawn with replacement

$P(\text{one is multiple of 4 \& one is multiple of 5})$

$$= \frac{2}{10} \times \frac{2}{10} + \frac{2}{10} \times \frac{2}{10}$$

$$= \frac{8}{100} = \frac{2}{25}$$

without replacement then req. prob

$$= \frac{2C_1 \times 2C_1}{10C_2}$$

$$= \frac{4}{45}$$

Q38.

3B
5W

four balls are drawn without replacement

$$\text{Req. prob.} = P(WBW\bar{B}) + P(BWB\bar{W})$$

$$= \frac{5}{8} \times \frac{3}{7} \times \frac{4}{6} \times \frac{2}{5} + \frac{3}{8} \times \frac{5}{7} \times \frac{2}{6} \times \frac{4}{5}$$

$$= \frac{240}{8 \times 7 \times 5 \times 6} = \frac{1}{7}$$

four balls are drawn with replacement

$$\text{Req. prob.} = P(WBW\bar{B}) + P(BWB\bar{W})$$

$$= \frac{5}{8} \times \frac{3}{8} \times \frac{5}{8} \times \frac{3}{8} + \frac{3}{8} \times \frac{5}{8} \times \frac{3}{8} \times \frac{5}{8}$$

$$= \frac{450}{8 \times 8 \times 8 \times 8} = \frac{225}{2048}$$

Q39.

1 White
2 Black

one ball is drawn and keep it out of it white & put it back if it is black

i) $P(\text{first draw is a white ball}) = \frac{2}{3}$

(ii) $P(\text{second draw is white})$

$$\begin{aligned}
 &= P(BW) + P(ww) \\
 &= \frac{1}{3} \times \frac{2}{3} + \frac{2}{3} \times \frac{1}{2} \\
 &= \frac{4+6}{18} = \frac{10}{18} = \frac{5}{9}
 \end{aligned}$$

(iii) $P(\text{third draw is white})$

$$P(BBW) + P(WBW) + P(BWW)$$

$$\begin{aligned}
 &= \frac{1}{3} \times \frac{1}{3} \times \frac{2}{3} + \frac{2}{3} \times \frac{1}{2} \times \frac{1}{2} + \frac{1}{3} \times \frac{2}{3} \times \frac{1}{2} \\
 &= \frac{2}{27} + \frac{1}{6} - \frac{1}{9}
 \end{aligned}$$

$$= \frac{4+9+6}{54} = \frac{19}{54}$$

Q42.

2B

4W

3R

All the balls are drawn one by one by keeping aside

$$P(2B \ 4W \ 3R) = \frac{2}{9} \times \frac{1}{8} \times \frac{4}{7} \times \frac{3}{6} \times \frac{2}{5} \times \frac{1}{4} \times \frac{3}{3}$$

$$= \frac{1}{9 \times 4 \times 7 \times 5}$$

$$= \frac{1}{1260}$$

$$(1+1+1)(1+1+1)(1+1+1)$$