



Module (B) Final Examination 2022-2023 Discrete Mathematics BSD- 103 Module (B)

قبل الشروع في الحل تأكد أن الإمتحان يقع في ثلاث ورقات مرقمة من 1 إلى 6

Choose the correct answer for the following statements:

- [1] If a matrix of a relation is $M_R = \begin{bmatrix} 1 & 0 & 1 \\ 0 & 1 & 1 \\ 0 & 0 & 1 \end{bmatrix}$, then $\overline{M_R}$ is..
(a) $\begin{bmatrix} 0 & 1 & 0 \\ 1 & 0 & 0 \\ 1 & 1 & 0 \end{bmatrix}$; (b) $\begin{bmatrix} 0 & 1 & 0 \\ 1 & 0 & 0 \\ 1 & 1 & 0 \end{bmatrix}$; (c) $\begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 1 & 1 & 1 \end{bmatrix}$; (d) $\begin{bmatrix} 1 & 0 & 1 \\ 0 & 1 & 1 \\ 0 & 0 & 1 \end{bmatrix}$
- [2] The set of solution of the equation:
 $\left[\frac{1}{2}\right]x^2 + \left[-\frac{1}{2}\right]x - (-26 \bmod 7) = 0$ is...
(a) $\{-1, 2\}$; (b) $\{1, -2\}$
(c) $\{1, 2\}$; (d) $\{-1, -2\}$
- [3] $P \rightarrow Q \equiv \dots$
(a) $Q \rightarrow P$; (b) $\overline{Q} \rightarrow P$; (c) $P \rightarrow \overline{Q}$; (d) $\overline{Q} \rightarrow \overline{P}$
- [4] The relation R is called *reflexive* closure if $R_1 = \dots$
(a) $R \cup \Delta$; (b) R^∞ ; (c) $R \cup R^{-1}$
- [5] For any two non-empty sets A and B , if $B \subset A$, then $B \equiv \dots$
(a) \overline{A} ; (b) A
(c) $A \cap B$; (d) $A \cup B$
- [6] $(P \vee Q) \wedge \overline{P} \equiv \dots$
(a) $\overline{P} \wedge Q$; (b) $\overline{Q} \wedge \overline{P}$; (c) $P \vee \overline{Q}$; (d) $\overline{Q} \vee \overline{P}$
- [7] If n is odd, then we have $\left[\frac{n^2}{4}\right] = \dots$
(a) $\frac{n^2+3}{2}$; (b) $\frac{n^2-3}{4}$; (c) $\frac{n^2+4}{3}$; (d) $\frac{n^2+3}{4}$
- [8] $\neg[\forall x, \overline{P}(x)] \equiv \dots$
(a) $\exists x, \overline{P}(x)$; (b) $\exists x, P(x)$; (c) $\forall x, P(x)$
- [9] $(p \vee q) \wedge \overline{p} \equiv \dots$
(a) $p \vee \overline{q}$; (b) $\overline{p} \wedge q$; (c) F ; (d) T
- [10] If $R_1 = \{(1, x), (2, x), (1, y), (2, y), (3, x)\}$, $R_2 = \{(x, a), (x, b), (y, a), (y, c)\}$, then
 $R_2 \circ R_1 =$
(a) $\begin{bmatrix} 1 & 1 & 1 \\ 1 & 1 & 1 \\ 1 & 1 & 1 \end{bmatrix}$; (b) $\begin{bmatrix} 0 & 1 & 0 \\ 1 & 0 & 0 \\ 1 & 1 & 0 \end{bmatrix}$; (c) $\begin{bmatrix} 1 & 1 & 1 \\ 1 & 1 & 1 \\ 1 & 1 & 0 \end{bmatrix}$; (d) $\begin{bmatrix} 1 & 1 & 1 \\ 1 & 0 & 1 \\ 1 & 0 & 1 \end{bmatrix}$
- [11] If P is false and Q is true propositions, then $P \rightarrow Q \equiv \dots$
(a) T ; (b) F ; (c) P ; (d) Q
- [12] $[x] - [x] = 0$ if $x \in \dots$
(a) \mathbb{C} ; (b) \mathbb{R} ; (c) \mathbb{Q} ; (d) \mathbb{Z}
- [13] $(T \wedge q) \vee (T \wedge r) \equiv \dots$
(a) T ; (b) F ; (c) $q \vee r$; (d) $q \wedge r$
- [14] For $X = \{2, 3, 4\}$, $Y = \{3, 4, 5, 6\}$, the relation
 $R: X \rightarrow Y$ defined by $x + y \leq 2$ is
(a) $\{(4, 5)\}$; (b) Y ; (c) X ; (d) \emptyset
- [15] If $(x, y) \in R$, then $(y, x) \in \dots$
(a) R ; (b) \overline{R} ; (c) D_R ; (d) R^{-1}
- [16] The length of the path: a-b-a-c equals:
(a) 4; (b) 6; (c) 3; (d) 5
- [17] $(p \wedge q) \vee (p \wedge \overline{q}) \vee (\overline{p} \wedge \overline{q}) \equiv \dots$
(a) $\overline{p} \vee q$; (b) P ; (c) $p \vee \overline{q}$; (d) q

[18]	$\sum_{k=1}^n k = \dots$	$\{(a) \frac{n}{2}; (b) \frac{n^2}{2}; (c) n^2 + n; (d) \frac{n^2+n}{2}\}$
[19]	A binary tree with 9 -vertices has exactly ... edges	$\{(a) 7; (b) 8; (c) 5; (d) 6\}$
[20]	The series $(0.3 + 0.03 + 0.003 + 0.0003 + \dots)$ is	$\{(a) \text{Convergent}; (b) \text{divergent}\}$
[21]	$\sum_{k=1}^{2n} \left(\frac{1}{2}\right) = \dots$	$\{(a) 2n; (b) 4n; (c) \frac{n}{2}; (d) n\}$
[22]	A relation R is <i>transitive</i> if	$\{(a) \forall xRy, yRz \rightarrow xRz; (b) xRx; (c) \forall xRy \rightarrow yRx\}$
[23]	If p is true proposition, and q is false, then $p \oplus q$ is ...	$\{(a) F (b) T (c) q\}$
[24]	A number being divisible by 2, then it should be even. This represents condition.	$\{(a) \text{sufficient}; (b) \text{necessary}\}$
[25]	$(p \wedge \bar{p}) \rightarrow T \equiv \dots$	$\{(a) \bar{p}; (b) p; (c) F; (d) T\}$
[26]	If $x \bmod y = r$, then y divides....	$\{(a) r; (b) y - r (c) -r + x; (d) x\}$
[27]	The relation which is defined by: " is divisible by" is ... on z^* .	$\{(a) \text{Reflexive} (b) \text{transitive} (c) \text{Symmetric}; (d) \text{Reflexive and transitive}\}$
[28]	The quantity $h(137) + (-12 \bmod 5) - [-1]$ equals	$\{(a) 8; (b) 6; (c) 7 (d) 9\}$
[29]	In case of 4 input of a given gate, then the number of possible input combination.	$\{(a) 16; (b) 4; (c) 64; (d) 8\}$
[30]	The relation is said to be equivalence if it is	$\{(a) \text{Reflexive} (b) \text{transitive} (c) \text{Symmetric}; (d) \text{All of them}\}$
[31]	If a, b, c are lengths of a triangle such that $p: a^2 + b^2 = c^2$ and $q: \text{the triangle is right, then....}$	$\{(a) \text{only } p \rightarrow q; (b) \text{only } q \rightarrow p; (c) p \leftrightarrow q\}$
[32]	A relation R is <i>symmetric</i> if $\forall (x, y) \in R$, then	$\{(a) \forall xRy, yRz \rightarrow xRz; (b) xRx; (c) \forall xRy \rightarrow yRx\}$
[33]	$A \cup B = \dots$	$\{(a) \{x: (x \in A) \vee (x \in B)\}; (b) \{x: (x \in A) \wedge (x \in B)\}; (c) \{x: (x \notin A) \vee (x \notin B)\}\}$
[34]	If $S_n = \{5k \mid k = 1, 2\}$, then $\bigcup_{n=2}^{10} S_n = \dots$	$\{(a) \{5, 20\}; (b) \{5, 10, 25\}; (c) \{5, 10\}\}$
[35]	The general term of the sequence: 5, 0.5, 0.05, ... is, $n \geq 0$	$\{(a) \left(\frac{0.5}{10^n}\right); (b) \left(\frac{5}{10^{n-1}}\right); (c) \left(\frac{5}{10^n}\right); (d) \left(\frac{5}{10^{n+1}}\right)\}$
[36]	If $f(x) = x + 1$, then $\lim_{n \rightarrow 1} \sum_{k=1}^n f(n)$ equals	$\{(a) 1/2; (b) 3/2; (c) 2\}$
[37]	$j! = \dots, j \in \mathbb{Z}^+$	$\{(a) \prod_{k=1}^j k; (b) \sum_{k=1}^j k; (c) \sum_{k=0}^j k; (d) \prod_{k=0}^j k\}$
[38]	The relation "less than" on a set $\{1, 2, 3, 4\}$	$\{(a) \text{Reflexive}; (b) \text{transitive} (c) \text{Symmetric}; (d) \text{All of them}\}$

[39] If $f(x) = 2[x]$, then $7 \bmod 5 - 0.5 f(-0.5)$ equals $\{(a)2; (b)1.5; (c)3; (d)2.5\}$

[40] If the inverse of the function $f(x) = 2^x$ form a relation R on the set $\{1, 2, 4, 8\}$, then R equals.. $\{(a) \{(1,2), (2,4), (4,16), (8,256)\}; (b) \{(1,0), (2,1), (4,2), (8,3)\}; (c) \{(1,1), (2,2), (4,4), (8,8)\}\}$

[41] The standard form of the odd integer is $\{(a) n; (b) n^2; (c) 2n + 1; (d) n + 1\}$

[42] $\forall x, y, z \in \mathbb{Z}^+$, if $P(x, y, z): x + zy + 2yz$, then $p(x^2, x, x) \equiv \{(a) x^3; (b) 4x^2; (c)x; (d) 3x^2\}$

[43] If $[1 + x] = [2.5x]$, then $x = \dots \{(a) 1; (b) 0; (c) 3/4; (d) 1/2\}$

[44] If $a_n = 2^n$, then $\sum_{n=2}^4 a_n = \dots \{(a) 28; (b) 6; (c) 60; (d) 12\}$

[45] $\sum_{k=1}^{k=n} a_k a_{k+n-1} = \dots \{(a) \sum_{k=0}^{n-1} a_{k-1} a_{n+k}; (b) \sum_{k=0}^{n-1} a_{k-1} a_{n-k}; (c) \sum_{k=0}^{n-1} a_{k+1} a_{k+n}\}$

[46] $\bigcap_{n=1}^N A_n = \dots \left\{ \begin{array}{l} (a) \{x | \exists n, x \notin A_n\} \\ (b) \{x | \exists n, x \in A_n\} \\ (c) \{x | \forall n, x \in A_n\} \\ (d) \{x | \forall n, x \notin A_n\} \end{array} \right\}$

[47] If $f(x) = [x + 1]$, then $12 \bmod 4 - 0.5 f(-1.5) = \{(a) -1; (b) -1/2; (c) 3; (d) 0\}$

[48] The sequence $\left\{\frac{1}{2}, \frac{5}{8}, \frac{3}{4}, \dots\right\}$ is.... $\{(a) \text{increasing}; (b) \text{decreasing}\}$

[49] $(12 \bmod 5) + h(15) - 3[-4.7] + 2[0.3] = \dots \{(a) 20; (b) 21; (c) 23; (d) 32\}$

[50] If $f(x) = x^2$, then $\lim_{n \rightarrow \infty} \sum_{k=1}^n f\left(\frac{k}{n}\right) = \dots \{(a) 1; (b) 2; (c) k; (d) n\}$

* In terms of unit step function, $f(t) = \begin{cases} t^2 + 7 & 0 \leq t < 1 \\ t^2 & 1 \leq t < 3 \\ 7 & t \geq 3 \end{cases}$ is equivalent to

[51] (a) $f(t) = t^3 u(t) + 7 u(t) - 7 u(t-1) - t^2 u(t-3) + 7 u(t-3)$
 (b) $f(t) = -t^2 u(t) - 7 u(t) - 7 u(t-1) - t^2 u(t-3) - 7 u(t-3)$
 (c) $f(t) = t^2 u(t) + 7 u(t) - 7 u(t-1) - t^2 u(t-3) + 7 u(t-3)$

* In terms of unit step function, $f(t) = \begin{cases} 3 & 0 < t \leq 2 \\ t & 2 < t \leq 3 \\ -t & 3 < t \leq 5 \end{cases}$ is equivalent to

[52] (a) $f(t) = (3 + t)u(t-2) + 2tu(t-3) + u(t-5) + 3$
 (b) $f(t) = (-3 + t)u(t-2) - 2tu(t-3) + u(t-5) + 3$
 (c) $f(t) = (-3 + t)u(t-2) - 2tu(t-3) - u(t-5) + 3$

[53] $[-1.5] = 4 + \dots \{(a) [-1.5]; (b) [-3.2]; (c) [-5.2]; (d) [-5.2]\}$

Taylor series expansion for the function $\sin x$ is...

[54] (a) $1 + \frac{x}{1!} + \frac{x^2}{2!} + \frac{x^3}{3!} + \dots$ (b) $1 - \frac{x^2}{2!} + \frac{x^4}{4!} - \dots$
 (c) $x - \frac{x^3}{3!} + \frac{x^5}{5!} - \dots$ (d) $x^2 - \frac{x^4}{4!} + \frac{x^6}{6!} - \dots$

[55] If n is an even positive integer, then $n^2 + 2(3n + 1)$ is {(a) odd ; (b) not even not odd ; (c) even }

[56] If $a_n = n^2$, then $\prod_{n=3}^5 a_n$ {(a) 50 ; (b) 3600 ; (c) 3600 ; (d) 60}

[57] The solution of the recurrence relation $a_n = a_{n-1} + 1$ with the initial condition $a_0 = 2$ is.... {(a) $n - 2$; (b) n ; (c) $n + 2$; (d) $2n$ }

[58] The quantity $h(137) + 12 \bmod 5 - [-1] + [-0.5]$ equals {(a) 6 ; (b) 8 ; (c) 7 (d) 4}

[59] $\sum_{k=2}^n a_{n+k} = \dots$ {(a) $\sum_{k=0}^{n-2} a_{n+k+2}$; (b) $\sum_{k=0}^n a_{n+k+2}$; (c) $\sum_{k=0}^{n-1} a_{n+k+2}$ }

[60] A tree with 3 -edges has exactly vertices. {(a) 3 ; (b) 1 ; (c) 3 ; (d) 4}

[61] If the matrix of a relation R is :	$\begin{matrix} & 1 & 2 & 3 & 4 \\ \begin{matrix} 1 \\ 2 \end{matrix} & \begin{bmatrix} 1 & 0 & 1 & 0 \\ 0 & 1 & 1 & 1 \end{bmatrix} \end{matrix}$	then R^{-1} is....	(a)	(b)
	$\begin{matrix} & 1 & 2 & 3 & 4 \\ \begin{matrix} 1 \\ 2 \end{matrix} & \begin{bmatrix} 0 & 1 & 0 & 1 \\ 1 & 0 & 0 & 0 \end{bmatrix} \end{matrix}$		$\begin{matrix} & 1 & 2 \\ \begin{matrix} 1 \\ 2 \\ 3 \\ 4 \end{matrix} & \begin{bmatrix} 1 & 0 \\ 0 & 1 \\ 1 & 1 \\ 0 & 1 \end{bmatrix} \end{matrix}$	

[62] $2 \times [1.2] = \dots$ {(a) [2] ; (b) [4] ; (c) [2.4] ; (d) [1] }

[63] If $[2x + 1] = [2x + 1]$, then $2x + 1$ should be ... {(a) rational (b) integer (c) irrational }

[64] If $R_1 = R \cup R^{-1}$, then $R_1 \dots \dots$ closure. {(a) symmetric; (b) transitive; (c) reflexive}

The digit number of the following bar code is.....

[65]  {(a) 4 ; (b) 5 ; (c) 7 ; (d) 6 }

[66] The symmetric closure of $A = \begin{bmatrix} 1 & 0 & 0 \\ 0 & 0 & 1 \\ 1 & 0 & 1 \end{bmatrix}$ is

(a) $\begin{bmatrix} 1 & 0 & 1 \\ 0 & 0 & 1 \\ 1 & 1 & 1 \end{bmatrix}$; (b) $\begin{bmatrix} 0 & 1 & 0 \\ 1 & 1 & 0 \\ 0 & 0 & 0 \end{bmatrix}$; (c) $\begin{bmatrix} 0 & 1 & 1 \\ 1 & 1 & 0 \\ 0 & 1 & 0 \end{bmatrix}$; (d) $\begin{bmatrix} 1 & 0 & 0 \\ 0 & 0 & 1 \\ 1 & 0 & 1 \end{bmatrix}$

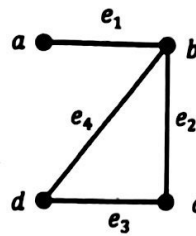
[67] The reflexive closure of $A = \begin{bmatrix} 1 & 0 & 0 \\ 0 & 0 & 1 \\ 1 & 0 & 1 \end{bmatrix}$ is

(a) $\begin{bmatrix} 1 & 1 & 1 \\ 1 & 1 & 1 \\ 1 & 0 & 1 \end{bmatrix}$; (b) $\begin{bmatrix} 1 & 0 & 0 \\ 0 & 0 & 1 \\ 1 & 0 & 1 \end{bmatrix}$; (c) $\begin{bmatrix} 0 & 1 & 1 \\ 1 & 1 & 0 \\ 0 & 1 & 0 \end{bmatrix}$; (d) $\begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 1 \\ 1 & 0 & 1 \end{bmatrix}$

[68] If a matrix of a relation is $M_R = \begin{bmatrix} 1 & 0 & 1 \\ 0 & 1 & 1 \\ 0 & 0 & 1 \end{bmatrix}$, then $\overline{M_R}$ is..

(a) $\begin{bmatrix} 1 & 1 & 1 \\ 1 & 1 & 1 \\ 1 & 1 & 1 \end{bmatrix}$; (b) $\begin{bmatrix} 0 & 1 & 0 \\ 1 & 0 & 0 \\ 1 & 1 & 0 \end{bmatrix}$; (c) $\begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 1 & 1 & 1 \end{bmatrix}$; (d) $\begin{bmatrix} 1 & 0 & 1 \\ 0 & 1 & 1 \\ 0 & 0 & 1 \end{bmatrix}$

* For the diagram



[69] The adjacency matrix is:

(a)

$$\begin{matrix} & \begin{matrix} a & b & c & d \end{matrix} \\ \begin{matrix} a \\ b \\ c \\ d \end{matrix} & \begin{bmatrix} 0 & 1 & 1 & 0 \\ 1 & 0 & 1 & 1 \\ 0 & 1 & 0 & 1 \\ 0 & 1 & 1 & 0 \end{bmatrix} \end{matrix}$$

(b)

$$\begin{matrix} & \begin{matrix} a & b & c & d \end{matrix} \\ \begin{matrix} a \\ b \\ c \\ d \end{matrix} & \begin{bmatrix} 0 & 1 & 1 & 0 \\ 1 & 1 & 1 & 1 \\ 1 & 1 & 1 & 1 \\ 0 & 1 & 1 & 0 \end{bmatrix} \end{matrix}$$

(c)

$$\begin{matrix} & \begin{matrix} a & b & c & d \end{matrix} \\ \begin{matrix} a \\ b \\ c \\ d \end{matrix} & \begin{bmatrix} 0 & 1 & 0 & 0 \\ 1 & 0 & 1 & 1 \\ 0 & 1 & 0 & 1 \\ 0 & 1 & 1 & 0 \end{bmatrix} \end{matrix}$$

[70] The incident matrix is:

(a)

$$\begin{matrix} & \begin{matrix} e_1 & e_2 & e_3 & e_4 \end{matrix} \\ \begin{matrix} a \\ b \\ c \\ d \end{matrix} & \begin{bmatrix} 1 & 0 & 0 & 0 \\ 1 & 1 & 0 & 1 \\ 0 & 1 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix} \end{matrix}$$

(b)

$$\begin{matrix} & \begin{matrix} e_1 & e_2 & e_3 & e_4 \end{matrix} \\ \begin{matrix} a \\ b \\ c \\ d \end{matrix} & \begin{bmatrix} 1 & 0 & 0 & 0 \\ 1 & 1 & 0 & 1 \\ 0 & 1 & 1 & 1 \\ 0 & 0 & 1 & 1 \end{bmatrix} \end{matrix}$$

(c)

$$\begin{matrix} & \begin{matrix} e_1 & e_2 & e_3 & e_4 \end{matrix} \\ \begin{matrix} a \\ b \\ c \\ d \end{matrix} & \begin{bmatrix} 1 & 0 & 0 & 0 \\ 1 & 1 & 0 & 1 \\ 0 & 1 & 1 & 0 \\ 0 & 0 & 1 & 1 \end{bmatrix} \end{matrix}$$

[71] The Laplacian matrix is:

(a)

$$\begin{matrix} & \begin{matrix} a & b & c & d \end{matrix} \\ \begin{matrix} a \\ b \\ c \\ d \end{matrix} & \begin{bmatrix} 1 & -1 & -1 & 0 \\ -1 & 3 & -1 & -1 \\ -1 & -1 & 2 & -1 \\ 0 & -1 & -1 & 3 \end{bmatrix} \end{matrix}$$

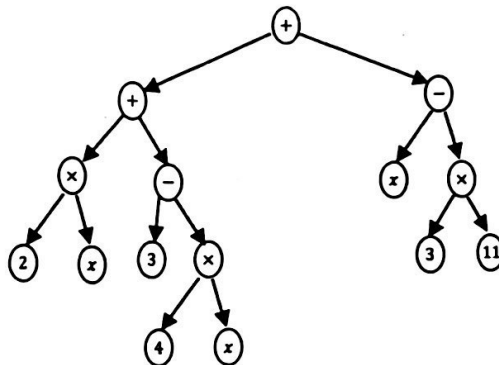
(b)

$$\begin{matrix} & \begin{matrix} a & b & c & d \end{matrix} \\ \begin{matrix} a \\ b \\ c \\ d \end{matrix} & \begin{bmatrix} 1 & -1 & 0 & 0 \\ -1 & 3 & -1 & -1 \\ -1 & -1 & 2 & -1 \\ 0 & -1 & -1 & 2 \end{bmatrix} \end{matrix}$$

(c)

$$\begin{matrix} & \begin{matrix} a & b & c & d \end{matrix} \\ \begin{matrix} a \\ b \\ c \\ d \end{matrix} & \begin{bmatrix} 1 & -1 & 0 & 0 \\ -1 & 3 & -1 & -1 \\ 0 & -1 & 2 & -1 \\ 0 & -1 & -1 & 2 \end{bmatrix} \end{matrix}$$

* The mathematical expression representing the following tree is



(a) $((2 \times x) + (3 - (4 \times x))) + (x - (3 \times 11))$

[72] (b) $((2 \times x) + (3 - (4 \times x))) - (x - (3 \times 11))$

(c) $((2 \times x) \times (3 - (4 \times x))) + (x - (3 \times 11))$

[73] The height of the previous tree equals ...

{(a) 2; (b) 5; (c) 3; (d) 4 }

[74] The number of edges in the previous tree equals...

{(a) 12; (b) 15; (c) 13; (d) 14 }

* If $A = \{a, b, c, d\}$, $R: A \rightarrow A$ and $R = \{(a, b), (b, c), (a, c), (c, d)\}$,	
[75] The reflexive closure of R is	(a) $\{(a, b), (b, a), (b, c), (c, b), (a, c), (c, a), (c, d), (d, c)\}$ (b) R^∞ (c) $\{(a, b), (a, a), (b, c), (b, b), (a, c), (c, c), (c, d), (d, d)\}$ (d) $A \times A$
[76] The symmetric closure of R is	(a) $\{(a, b), (b, a), (b, c), (c, b), (a, c), (c, a), (c, d), (d, c)\}$ (b) R^∞ (c) $\{(a, b), (a, a), (b, c), (b, b), (a, c), (c, c), (c, d), (d, d)\}$ (d) $A \times A$
[77] The transitive closure of R is	(a) $\{(a, b), (b, a), (b, c), (c, b), (a, c), (c, a), (c, d), (d, c)\}$ (b) R^∞ (c) $\{(a, b), (a, a), (b, c), (b, b), (a, c), (c, c), (c, d), (d, d)\}$ (d) $A \times A$
[78] $\overline{A \cap B} = \dots$	$\{(a) \{x x \in \overline{A \cap B}\}; (b) \{x x \in \overline{A} \cup \overline{B}\}; (c) \{x x \in A \cap B\}\}$
[79] If $d = \max(d_1, d_2)$, then	$\{(a) (d_1 < d) \wedge (d_2 < d);$ $(b) (d_1 < d) \vee (d_2 < d);$ $(c) (d_1 > d) \wedge (d_2 > d);$
[80] $3 \lceil 1.8 \rceil + 2 \lfloor -1.1 \rfloor = \dots$	$\{(a) 2; (b) 10; (c) 1/2; (d) 1\}$

With our best wishes

Ass. Prof. Y.M.Hamada

Dr/ M.G. Brika