

# **Prática de Física dos Dispositivos Eletrônicos**

## **FGA0100**

### **Laboratório-2**

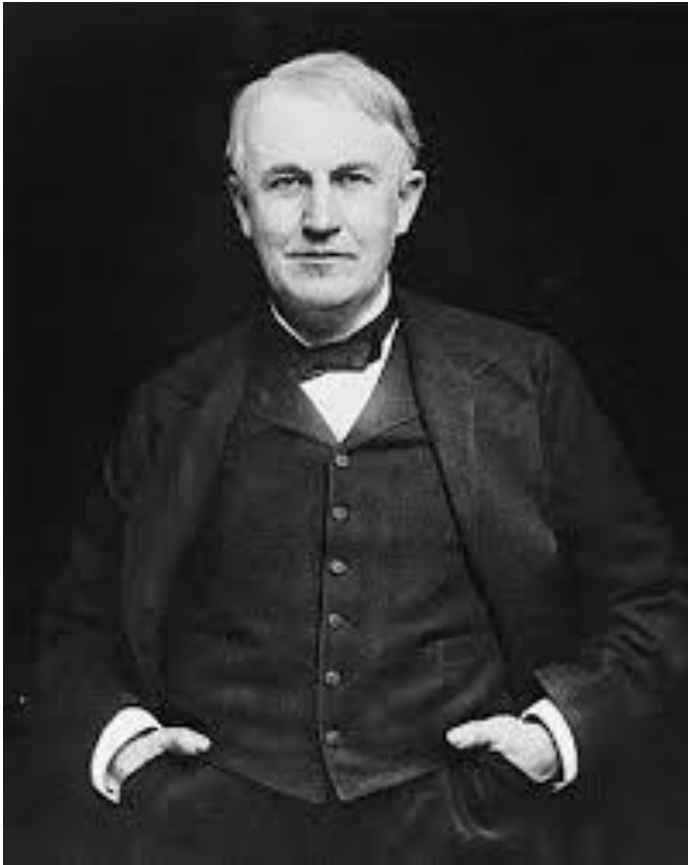
## **Lâmpada Elétrica de Filamento**

### **02/2020**

**FGA**

**Universidade de Brasília**





Thomas A. Edison  
1847-1931



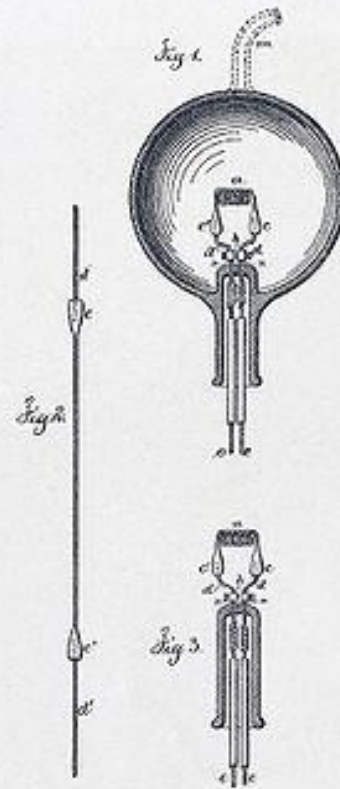
22 Outubro de 1879  
(Menlo Park - NJ)



T. A. EDISON.  
Electric-Lamp.

No. 223,898.

Patented Jan. 27, 1880.

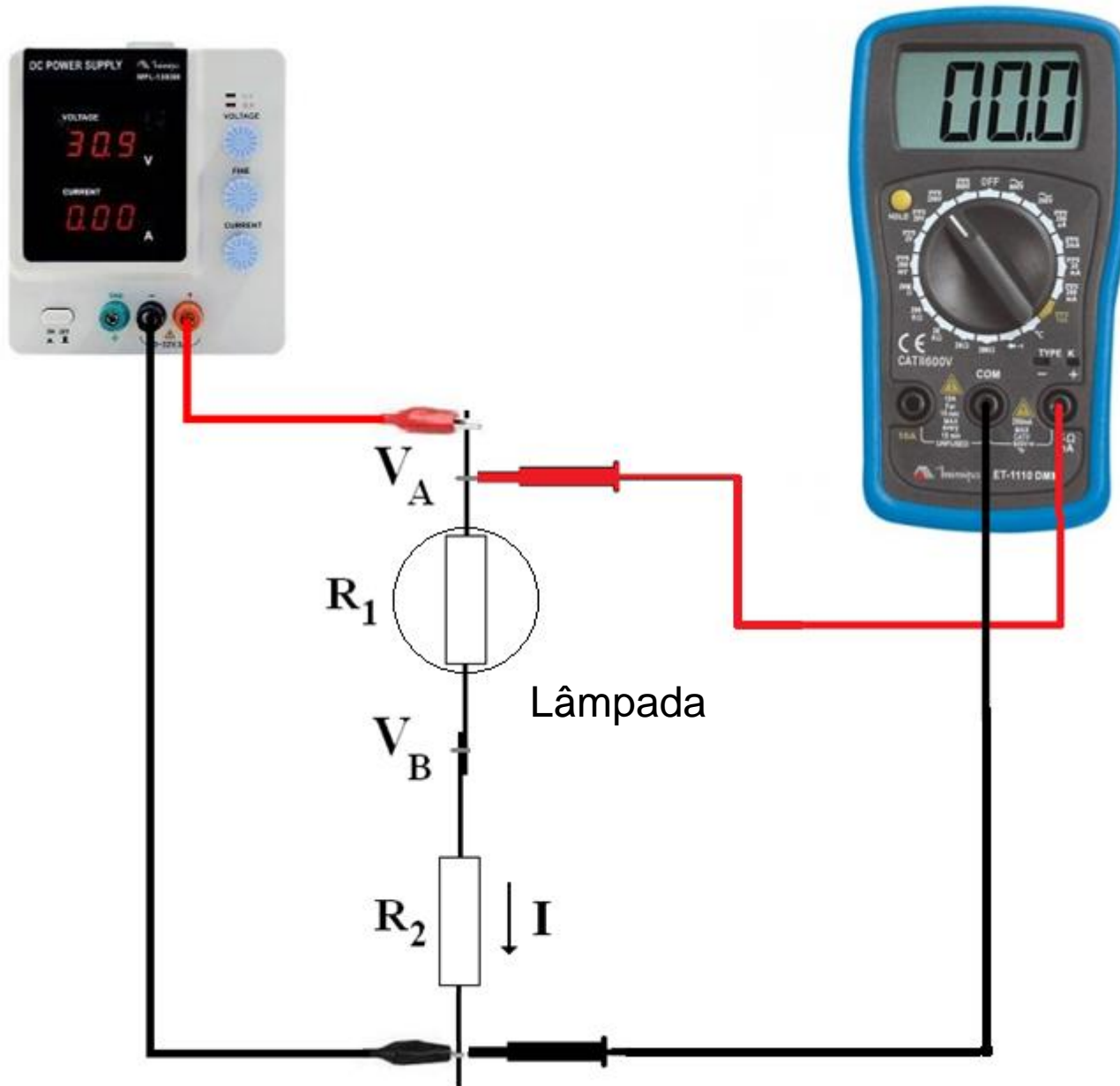


Witnesses  
Chas. H. Smith  
Geo. D. Pinckney

Inventor  
Thomas A. Edison  
f. Lemuel W. Furrell  
att'y

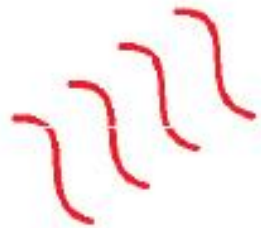


# Circuito de Medidas



# Lâmpada Elétrica

Convecção



Argônio  
ou criptônio

Filamento

Suporte  
de vidro

Bulbo

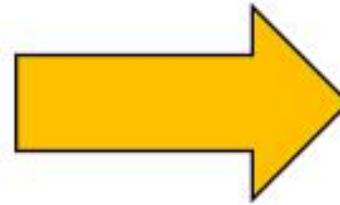
Condução



Contato

Contato

Radiação



Equilíbrio Térmico  
(alto-aquecimento)

$$P_E \cong P_R$$

Coeficiente Térmico

$$\alpha_T = \frac{1}{R(T)} \left. \frac{dR}{dT} \right|_T$$

$$P_E = IV = \frac{V^2}{R(T)} = I^2 R(T)$$



## Radiação de Corpo Negro

$$\begin{aligned} B(\nu, T) &= \frac{2h\nu^3}{c^2} \frac{1}{e^{\frac{h\nu}{kT}} - 1} \left[ \frac{W.sr^{-1}.m^{-2}}{Hz} \right] \\ B(\lambda, T) &= \frac{2hc^2}{\lambda^5} \frac{1}{e^{\frac{hc}{\lambda kT}} - 1} \left[ \frac{W.sr^{-1}.m^{-2}}{m} \right] \end{aligned} \quad \left. \vphantom{\begin{aligned} B(\nu, T) \\ B(\lambda, T) \end{aligned}} \right\} \text{Lei de Planck}$$

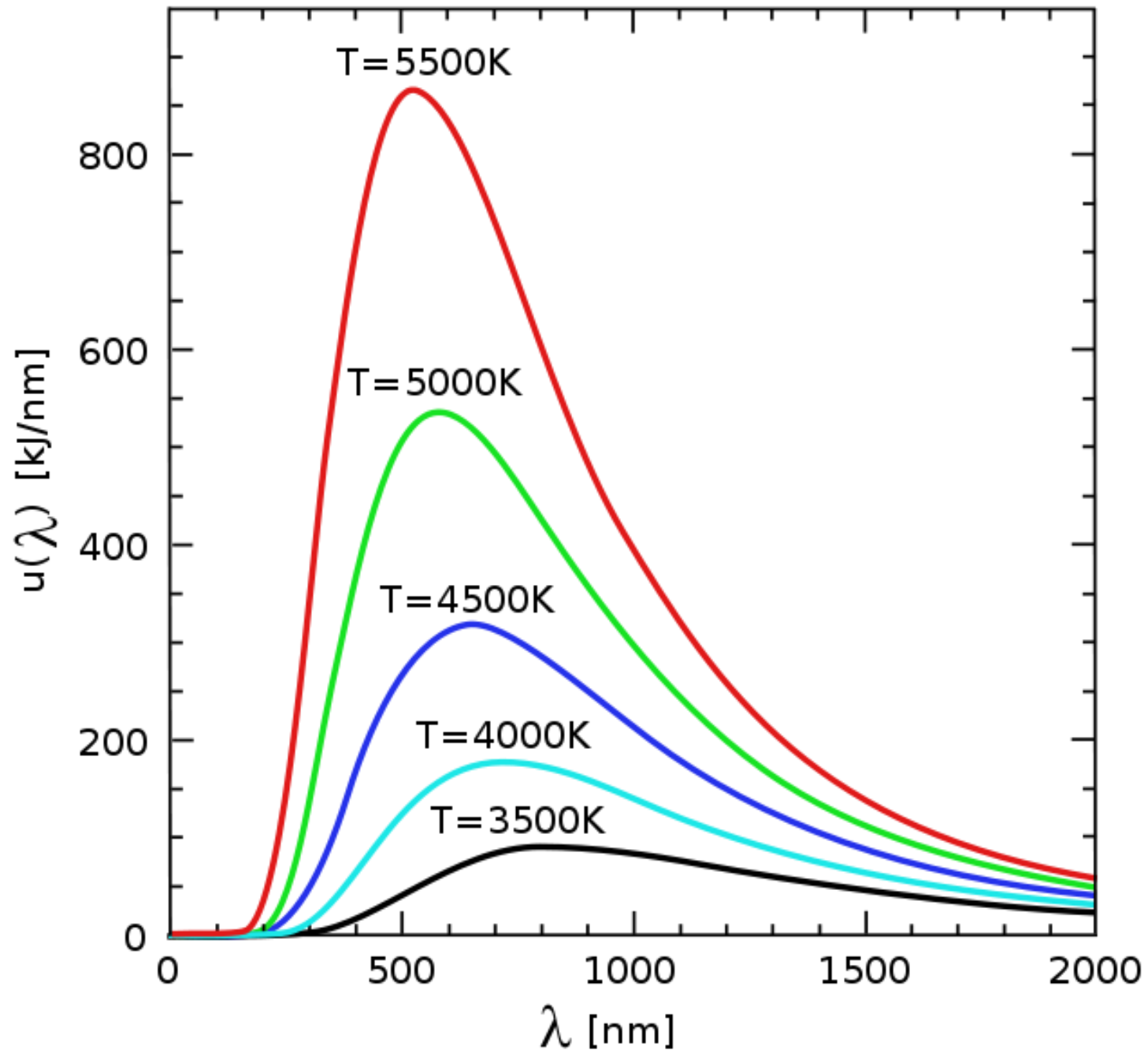
$$P_R = A\varepsilon\sigma T^4 \quad [W] \quad \text{Lei de Stefan-Boltzmann}$$

$$\sigma = 5.67 \times 10^{-8} \quad [W \, m^{-2} \, K^{-4}]$$

$$\varepsilon \approx 1 \quad \text{Emissividade}$$



# Radiação de Corpo Negro



## Radiação de Filamento

Ponto de Máximo:  $\frac{dB(\lambda, T)}{d\lambda} = 0$

$$\lambda_{\max} T = 2897,756 \text{ } [\mu\text{m.K}]$$

Temperatura Ideal (Centro da Banda Visível):

$$\lambda_{\max} = \frac{0,7 + 0,4}{2} = 0,55 \text{ } [\mu\text{m}]$$

$$T = \frac{2897,756}{0,55} = 5268,6473 \text{ } [\text{K}]$$

**Ponto de fusão do tungstênio = 3695 K**

**Ponto de Sublimação do Carbono = 3915 K**





# Olho Humano

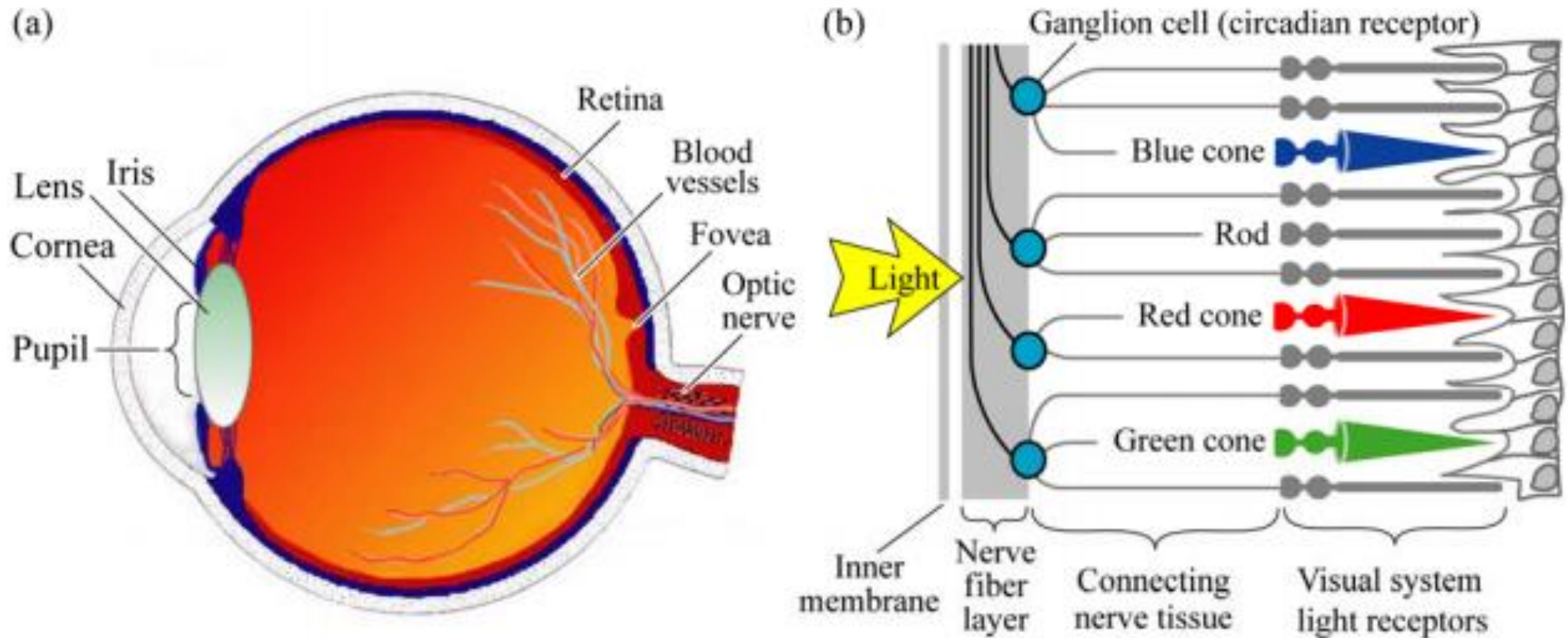
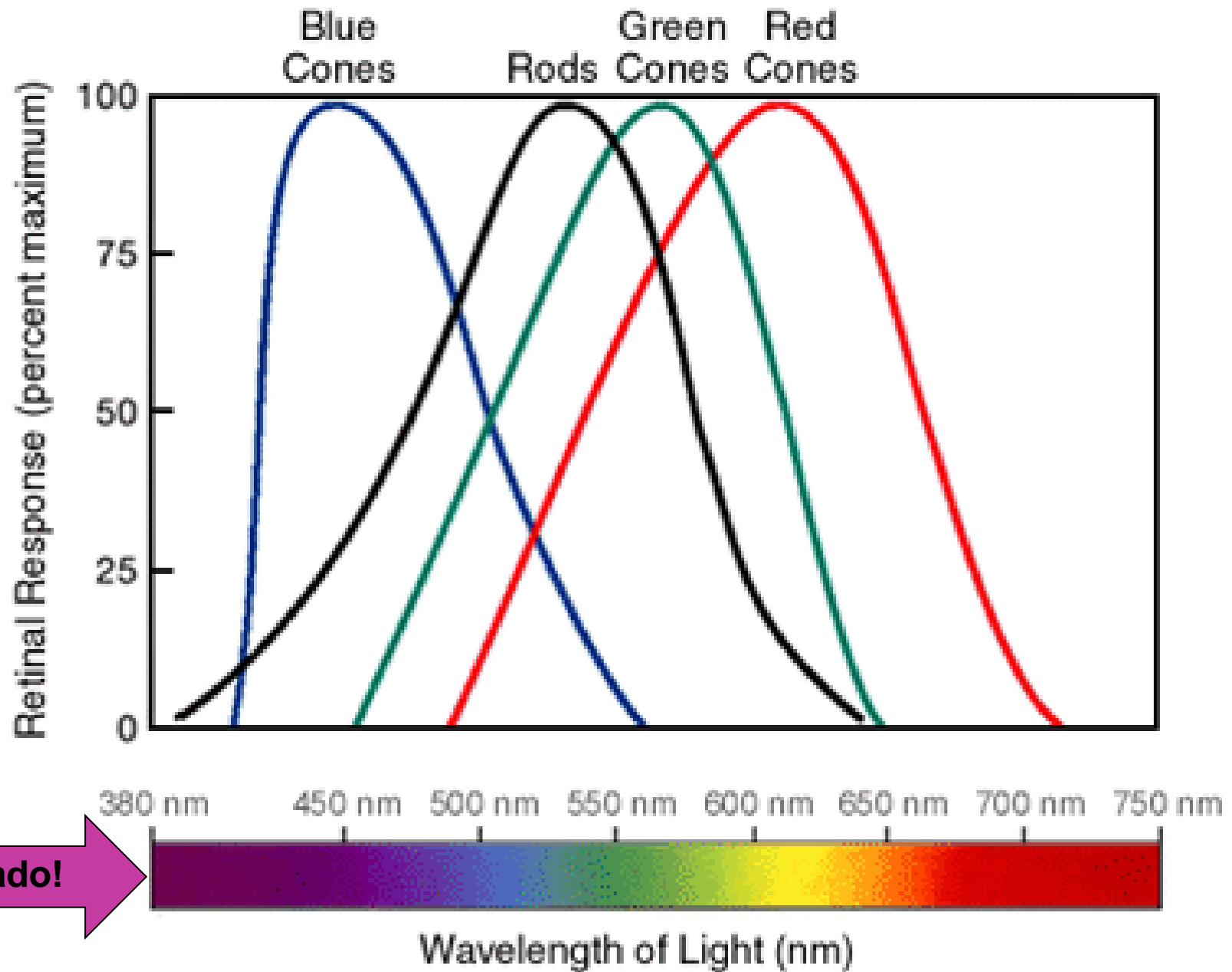


Fig. 16.1. (a) Cross section through a human eye. (b) Schematic view of the retina including rod and cone light receptors (adapted from Encyclopedia Britannica, 1994).

## Sensibilidade da Visão



# Espectro de Sensibilidade do Olho Humano

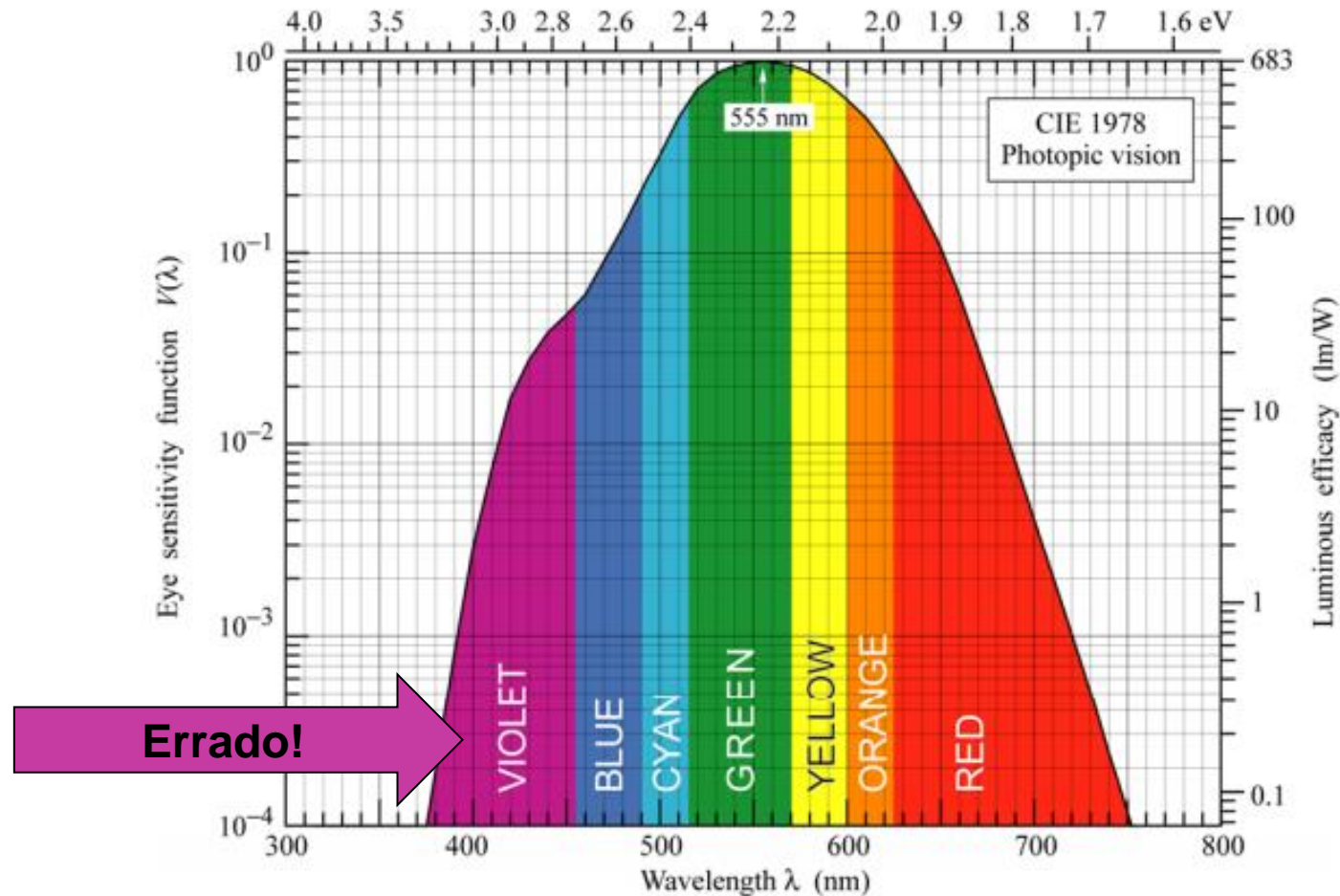
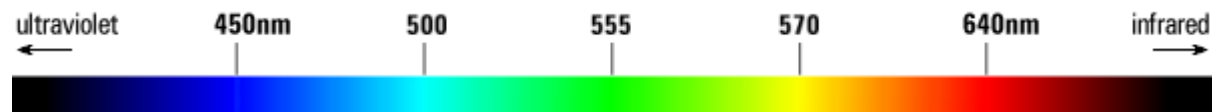


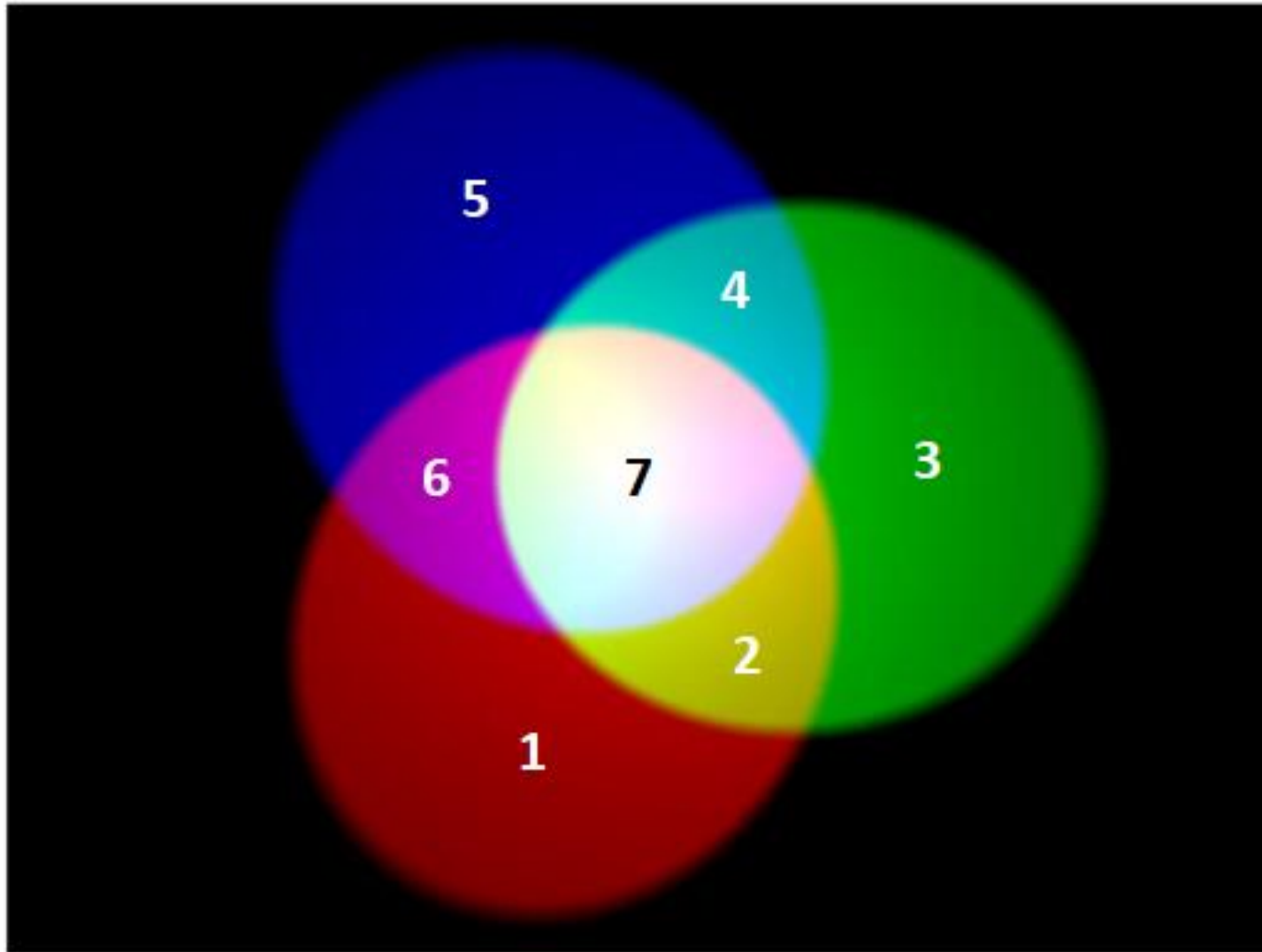
Fig. 16.7. Eye sensitivity function,  $V(\lambda)$ , (left-hand ordinate) and luminous efficacy, measured in lumens per watt of optical power (right-hand ordinate).  $V(\lambda)$  is maximum at 555 nm (after 1978 CIE data).

<https://www.ecse.rpi.edu/~schubert/Light-Emitting-Diodes-dot-org/Sample-Chapter.pdf>

Correto

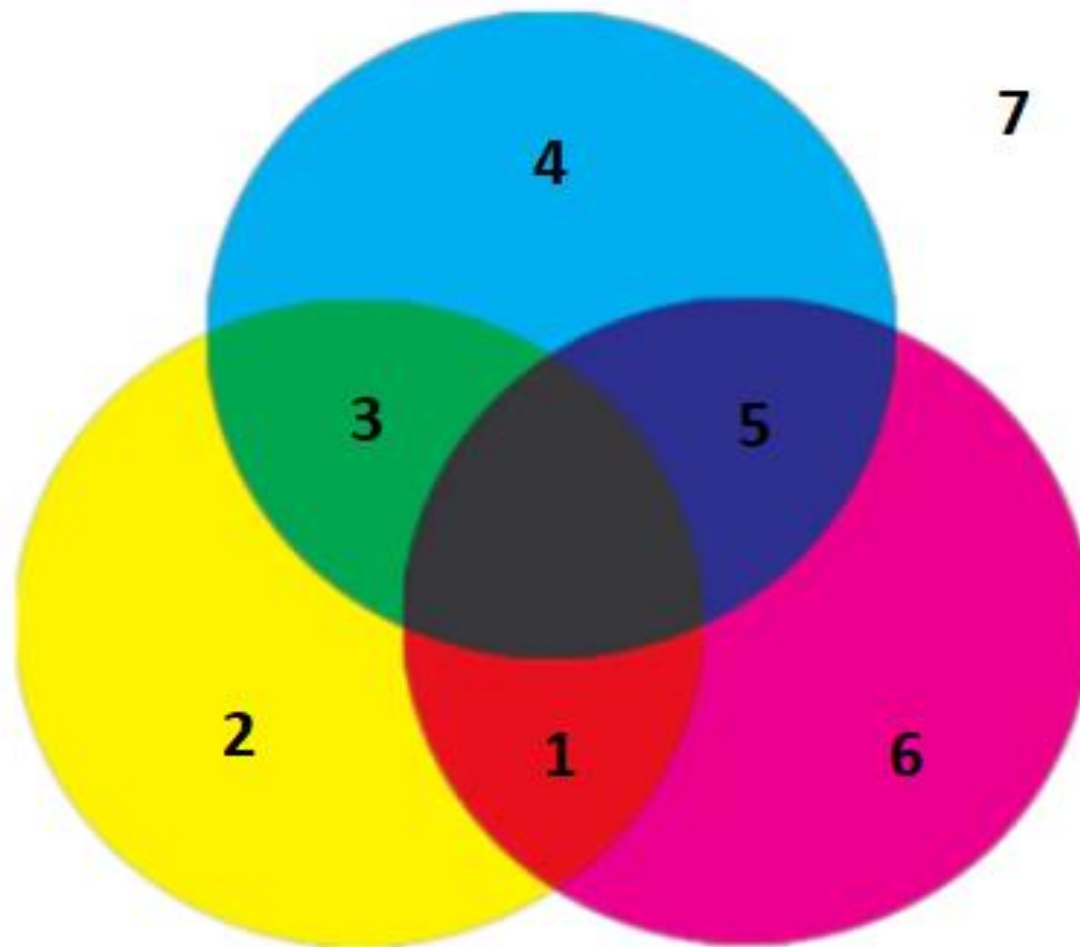


# Processo Aditivo



*Additive color mixing. If you (like me) have a hard time wrapping your head around how red and green mix together to make yellow, watch [this YouTube video](#).*

# Processo Subtrativo



*Subtractive color mixing is pretty close to the paint mixing we did in grade school. This video does a great job visualizing the “subtractive” part of it.*

# 7 Cores + Preto (Nenhuma Cor) ou Branco (Todas as Cores)

**N = 3 => R,G,B (Retina, 1 bit por cor)**

Ligado/Desligado

$$2^3 = 8$$

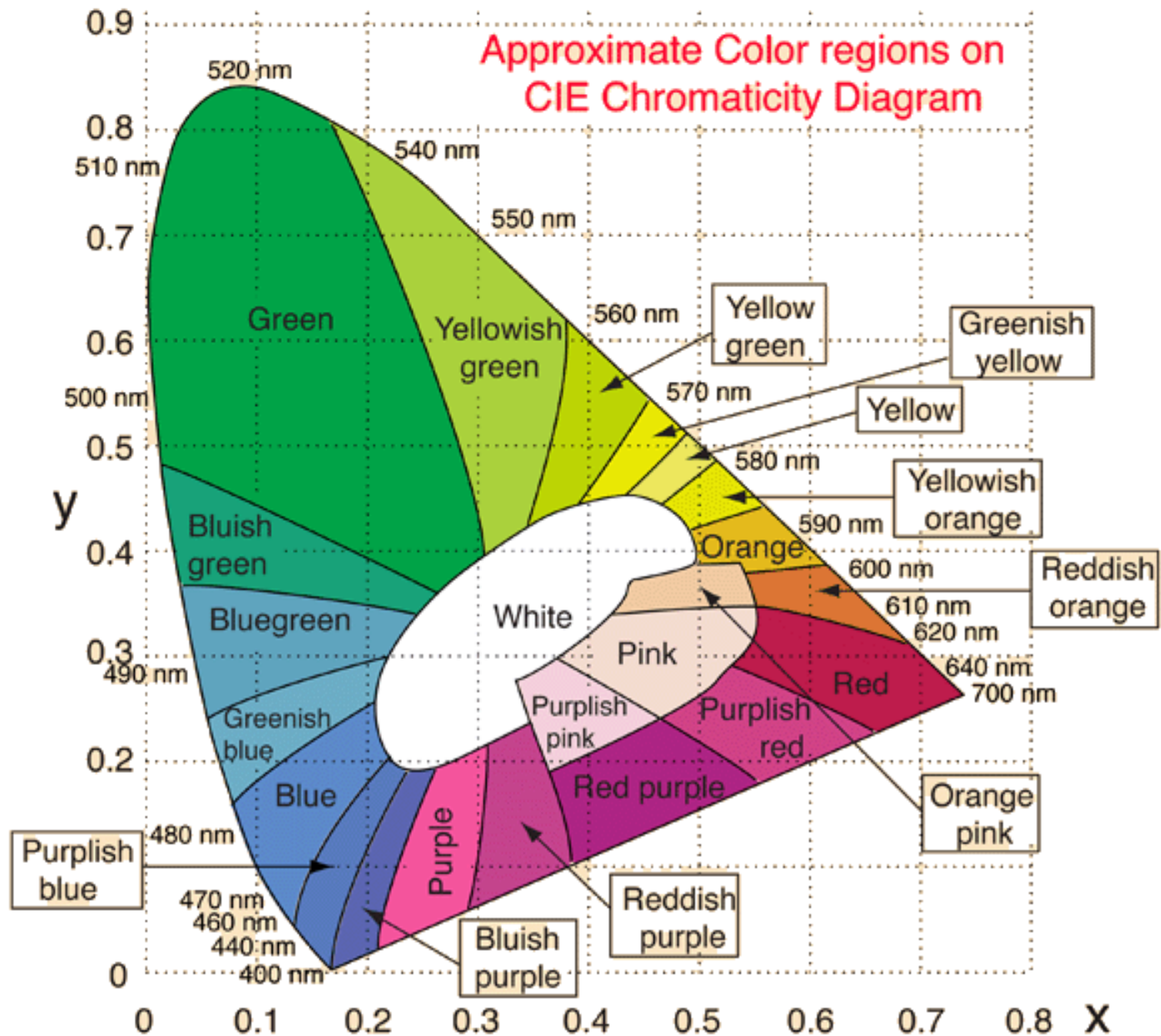
Processo Aditivo:

(2 níveis - 0 ou 1)

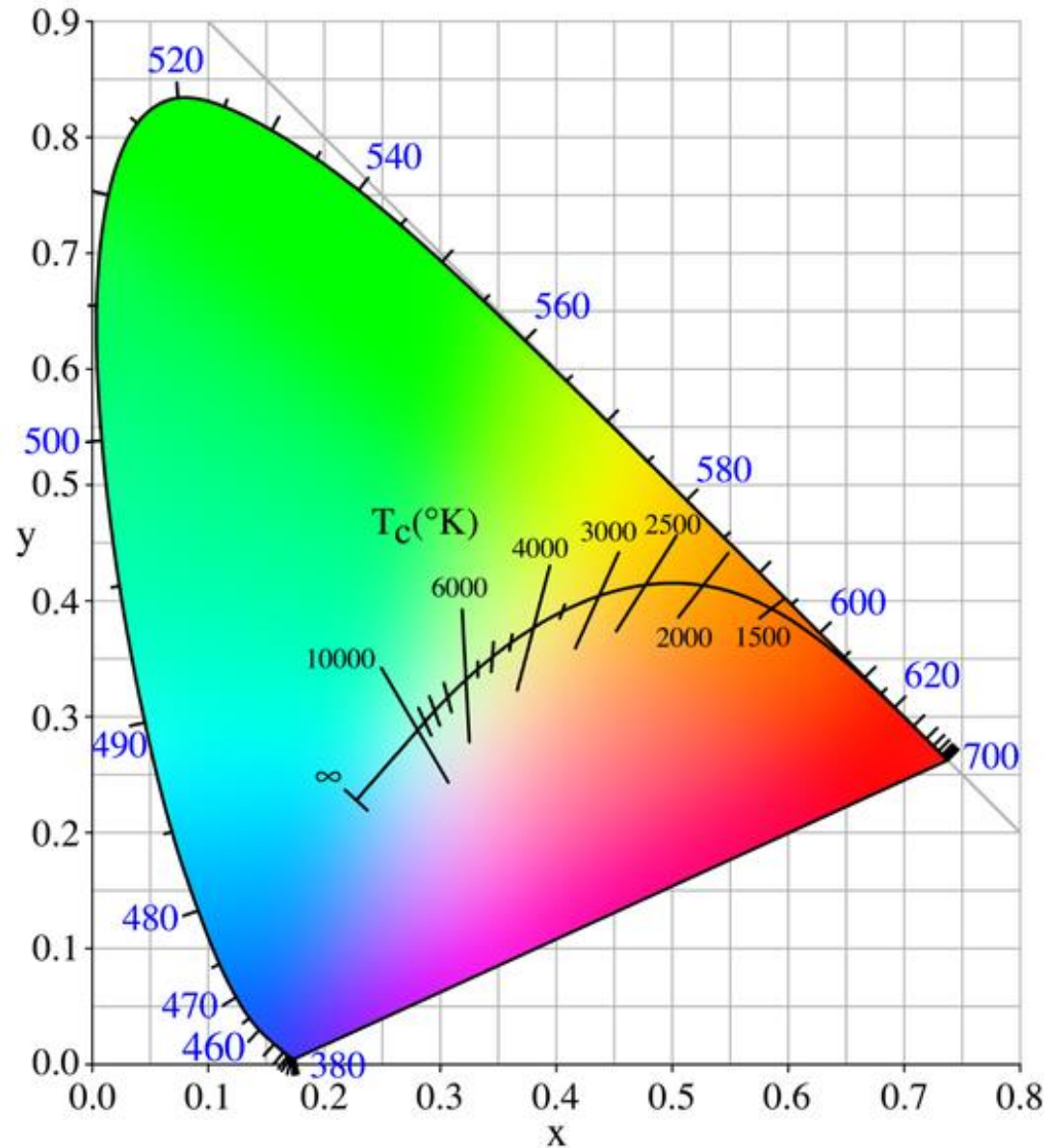
R	G	B		#
0	0	0	Preto	0
1	0	0	Vermelho	1
1	1	0	Amarelo	2
0	1	0	Verde	3
0	1	1	Ciano	4
0	0	1	Azul	5
1	0	1	Violeta	6
1	1	1	Branco	7

Não existe na  
sequência do  
espectro!





# Radiação de Corpo Negro



CIE 1931 color space chromaticity diagram

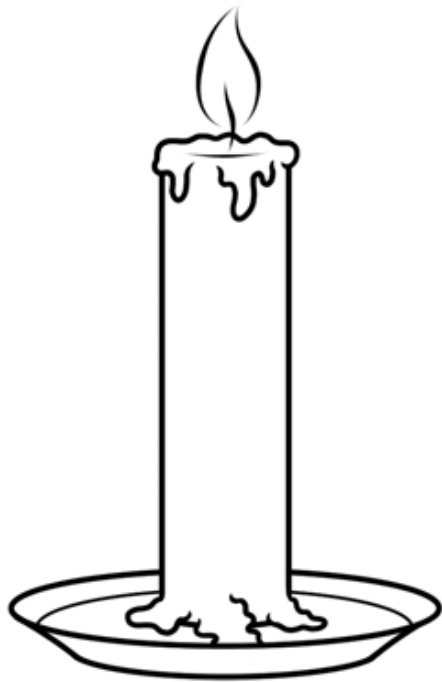
Ponto de fusão do tungstênio = 3695 K

Ponto de Sublimação do Carbono = 3915 K

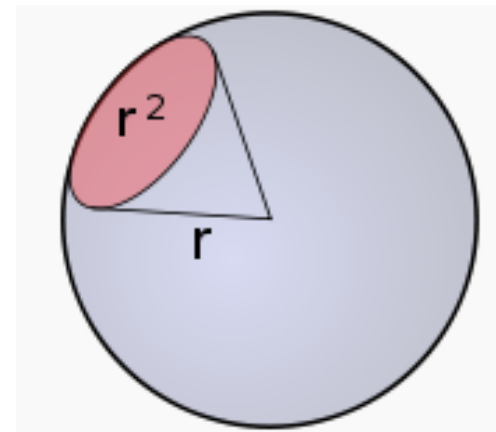


## Candela e Lúmen

A candela é a intensidade luminosa, numa dada direção, de uma fonte que emite uma radiação monocromática de frequência  $540 \times 10^{12}$  hertz e que tem uma intensidade radiante nessa direção de  $\frac{1}{683}$  watt por esferorradiano (sr).



Vela: ~1 candela



$$1 \text{ cd} \cdot 1 \text{ sr} = 1 \text{ lm}$$

$$\text{Isotrópica: } 1 \text{ candela} = 4\pi \text{ lúmens}$$

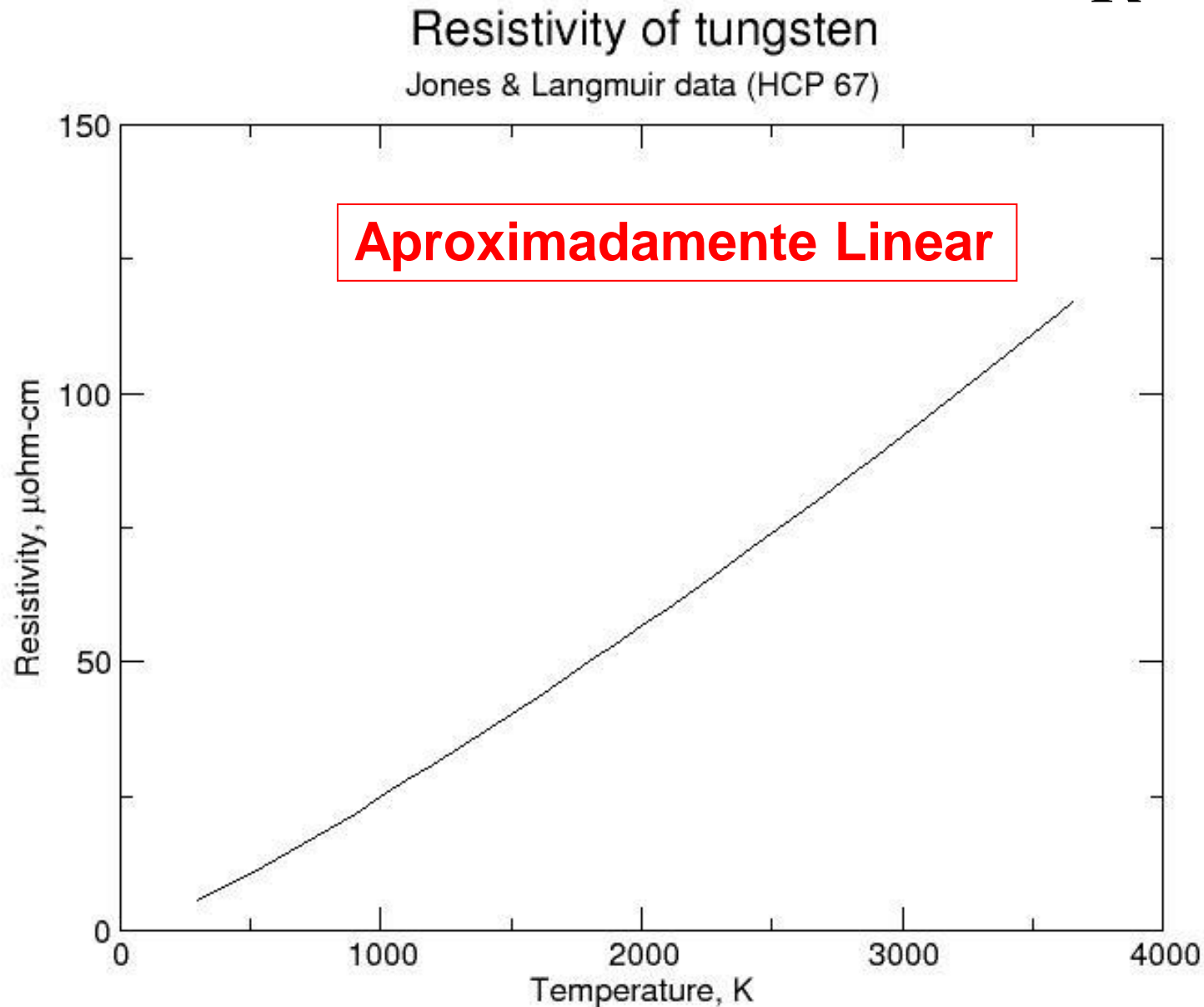
$$\text{Esfera: } A = 4\pi r^2$$

## Eficiência e Eficácia

Type	Overall luminous efficiency	Overall luminous efficacy (lm/W)
40 W tungsten incandescent	1.9%	12.6 <sup>[1]</sup>
60 W tungsten incandescent	2.1%	14.5 <sup>[1]</sup>
100 W tungsten incandescent	2.6%	17.5 <sup>[1]</sup>
glass halogen	2.3%	16
quartz halogen	3.5%	24
photographic and projection lamps with very high filament temperatures and short lifetimes	5.1%	35 <sup>[53]</sup>
ideal black-body radiator at 4000 K (or a class K star like Arcturus)	7.0%	47.5
ideal black-body radiator at 7000 K (or a class F star like Procyon)	14%	95
ideal monochromatic 555 nm (green) source	100%	683 <sup>[54]</sup>

## Resistividade do Tungstênio

$$R = \rho \frac{L}{A}$$



## Modelo para a Lâmpada Elétrica

$$V = RI \quad R(T) = \rho(T) \frac{L}{A} \quad \rho(T) \cong K_T T$$

**Aprox. Linear**

$$R(T) = K_T T \frac{L}{A} = K'_T T$$

$$P_E = IV = \frac{V^2}{R(T)} = I^2 R(T) = \frac{V^2}{K'_T T} = I^2 K'_T T$$

$$P_E \cong P_R$$

$$P_R = A \varepsilon \sigma T^4$$

$$I^2 K'_T T \cong A \varepsilon \sigma T^4$$

$$\frac{V^2}{K'_T T} \cong A \varepsilon \sigma T^4$$



$$I^2 \cong \frac{A\varepsilon\sigma}{K'_T} T^3$$

$$V^2 \cong K'_T A\varepsilon\sigma T^5$$

$$I \cong \sqrt{\frac{A\varepsilon\sigma}{K'_T}} T^{\frac{3}{2}}$$

$$V \cong \sqrt{K'_T A\varepsilon\sigma} T^{\frac{5}{2}}$$

$$I \cong K_I T^{\frac{3}{2}}$$

$$V \cong K_V T^{\frac{5}{2}}$$

**Verificando:**  $R(T) = \frac{V}{I} \cong \frac{K_V T^{\frac{5}{2}}}{K_I T^{\frac{3}{2}}} = K'_T T$  **Aprox. Linear**

$$I \cong K_I T^{\frac{3}{2}}$$

$$V \cong K_V T^{\frac{5}{2}}$$

$$V^{\frac{2}{5}} \cong (K_V)^{\frac{2}{5}} T$$

$$T = \frac{V^{\frac{2}{5}}}{(K_V)^{\frac{2}{5}}}$$

$$I \cong K_I \left( \frac{V^{\frac{2}{5}}}{(K_V)^{\frac{2}{5}}} \right)^{\frac{3}{2}} \quad \rightarrow \quad I \cong \left( \frac{K_I}{(K_V)^{\frac{3}{5}}} \right) V^{\frac{3}{5}}$$

**Modelo:**

$$I \cong KV^{\frac{3}{5}}$$

**Não-linear**

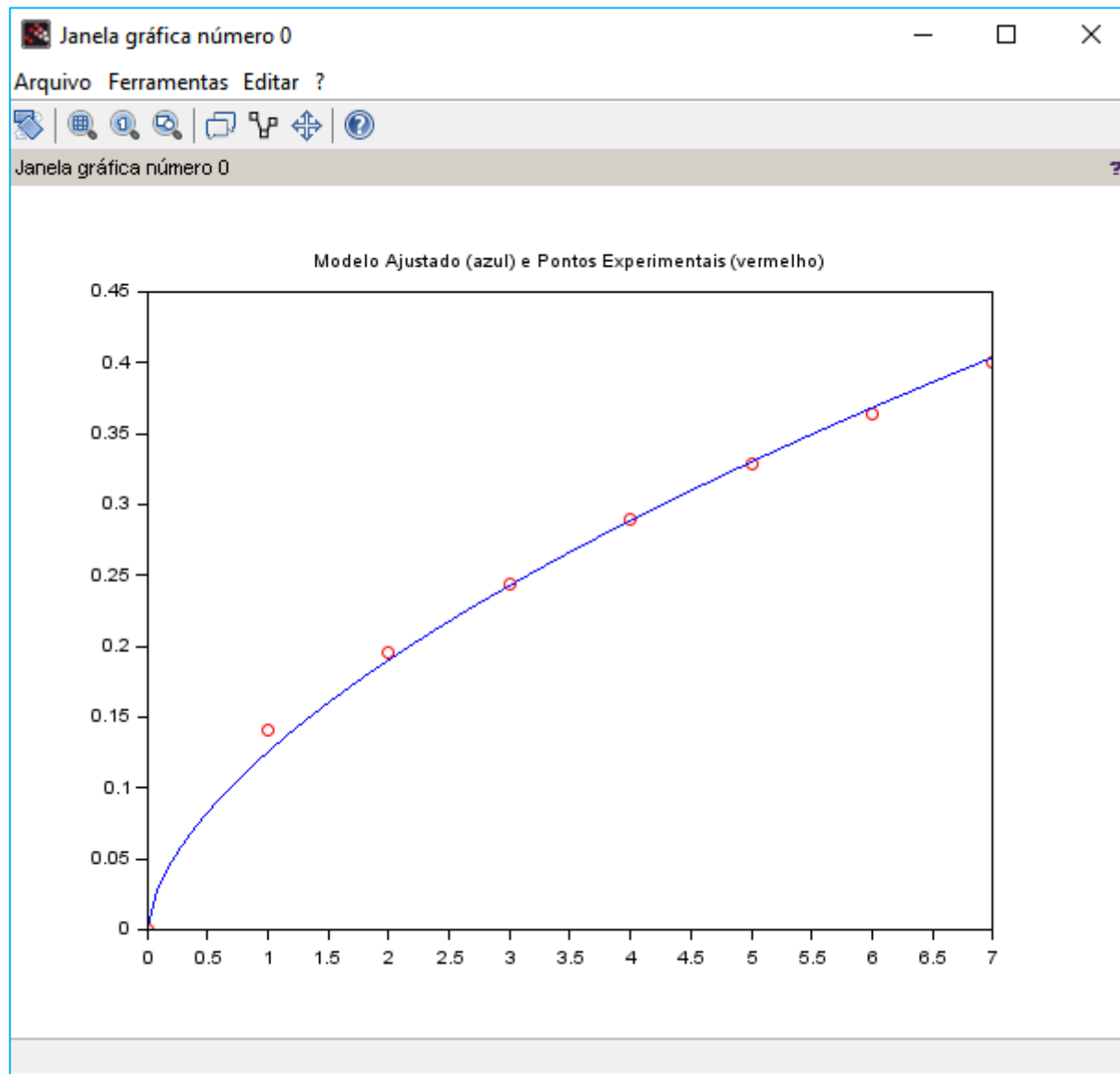
# Scilab: Ajuste de Modelo para a Lâmpada Elétrica (Método dos Mínimos Quadrados)

```
MQ_Lâmpada.sce (C:\Users\Marcus\Desktop\FGA\FGA_1_2020\FDE\Novos_Laboratórios\Lab_2\MQ_Lâmpada.sce) - SciNotes
Arquivo  Editar  Formatar  Opções  Janela  Executar ?

MQ_Lâmpada.sce (C:\Users\Marcus\Desktop\FGA\FGA_1_2020\FDE\Novos_Laboratórios\Lab_2\MQ_Lâmpada.sce) - SciNotes
MQ_Lâmpada.sce

1  //Exemplo: Ajuste de Modelo da Lâmpada por Mínimos Quadrados
2  //%Programa:MQ_Lâmpada.sce
3  clear;
4
5  //Pontos Experimentais
6  N = 8; //Número de pontos experimentais
7  yp = [-0.0.1406.0.1951.0.244.0.290.0.329.0.364.0.400]; //Corrente [A]
8  xp = [-0.1.001.2.00.3.00.4.00.5.00.6.00.6.99]; //Tensão [V]
9  plot(xp, yp, 'or');
10
11 //Modelo Adotado:  $y = k \cdot (x^p)$ 
12 p = 3/5; //Expoente Fracionário (Modelo)
13 g = xp.^p; //Função Base
14 k = sum(yp.*g)/sum(g.*g); //Ajuste da Constante do Modelo
15
16 xc = linspace(min(xp), max(xp), 100); //Base de Plotagem do Modelo Ajustado
17 yc = k*(xc.^p); //Modelo Ajustado
18 plot(xc, yc, 'b');
19 title('Modelo Ajustado (azul) e Pontos Experimentais (vermelho)');
20
21 //Erro Quadrático Médio
22 ym = k*(xp.^p); //Valores da corrente a partir do modelo ajustado
23 EQM = (1/N)*sum((ym-yp).^2);
24 disp(EQM);
```

# Modelo Ajustado da Lâmpada



## Erro Quadrático Médio

Scilab 6.1.0 Console

0.0000346

## Constante do Modelo

Scilab 6.1.0 Console

--> k

k =

0.1256746