## MCMD model. Grand reaction ensemble

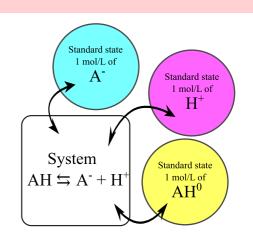
## System free energy

$$\Omega = E - TS + \sum_{i} (\mu_i - \mu_i^{\ominus}) N_i$$

## Reactions

$$HA \stackrel{\mathcal{K}}{\hookrightarrow} A^{-} + H^{+} \qquad \qquad \emptyset \hookrightarrow Na^{+} + Cl^{-}$$

$$\mathcal{K} = \mu_{H^{+}}^{\ominus} + \mu_{A^{-}}^{\ominus} - \mu_{HA}^{\ominus} \qquad \mathcal{K} = \mu_{Na^{+}} + \mu_{Cl^{-}}$$



The change of system free energy during a reaction step

$$\Delta\Omega = k_B T \ln \left( \prod_i V^{\nu_i \xi} \frac{N_i!}{(N_i + \nu_i \xi)!} \right) + \xi \left( \sum_i \nu_i \mu_i - \sum_i \nu_i \mu_i^{\ominus} \right) + \Delta E$$

$$\Delta\Omega = k_B T \ln \left( \mathcal{K}^{\xi} \prod_i V^{
u_i \xi} rac{N_i!}{(N_i + 
u_i \xi)!} 
ight) + \Delta E$$

accept if  $\mathcal{R}^{\xi} < e^{\Delta\Omega/k_BT}$