

Assignment_9

Hemal Agarwal

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1 Data

```
#setwd("C:/Users/Adroit/Desktop/CourseProject")
Project.Data <- read.csv("PCA_ExampleData.csv",header=TRUE,sep=",")
Project.Data[1:10,]
```

##	V1	V2	V3	V4	V5	V6
## 1	-10.00000	-8.00000	-6.00000	-4.00000	-2.00000	0.00000
## 2	335.26043	167.30996	36.42212	-57.023949	-112.88559	-131.66066
## 3	106.04431	61.94413	22.68583	-4.491896	-16.86543	-23.94030
## 4	-138.25926	-69.13931	-14.48162	24.403158	47.02190	55.09567
## 5	139.51863	66.76133	11.15244	-28.738979	-53.45132	-61.10555
## 6	416.99904	207.59255	45.27888	-70.756695	-140.82071	-163.84332
## 7	-190.35076	-104.67105	-34.61287	14.833058	41.78893	52.80835
## 8	331.03604	177.06454	52.22067	-36.066936	-85.00319	-104.34305
## 9	18.52366	16.95822	13.74827	11.802604	12.21568	11.16780
## 10	-375.72268	-182.05494	-34.09990	72.048443	137.85975	158.20484

##	V7	V8	V9	V10	V11
## 1	2.00000	4.00000	6.00000	8.00000	10.00000
## 2	-113.07746	-56.864257	36.48108	167.10119	335.37523
## 3	-20.52873	-1.442949	23.81151	57.95828	108.23602
## 4	47.68518	23.851115	-14.68544	-68.41763	-138.65609
## 5	-52.72716	-29.341695	10.92991	67.54925	139.08538
## 6	-140.40840	-71.099858	45.15218	208.04116	416.75236
## 7	44.31460	12.730956	-35.38898	-101.92300	-191.86184
## 8	-88.76262	-32.937981	53.37590	172.97410	333.28527
## 9	10.74362	13.027791	14.20061	15.35655	19.40438
## 10	135.88303	73.693656	-33.49248	-184.20571	-374.54004

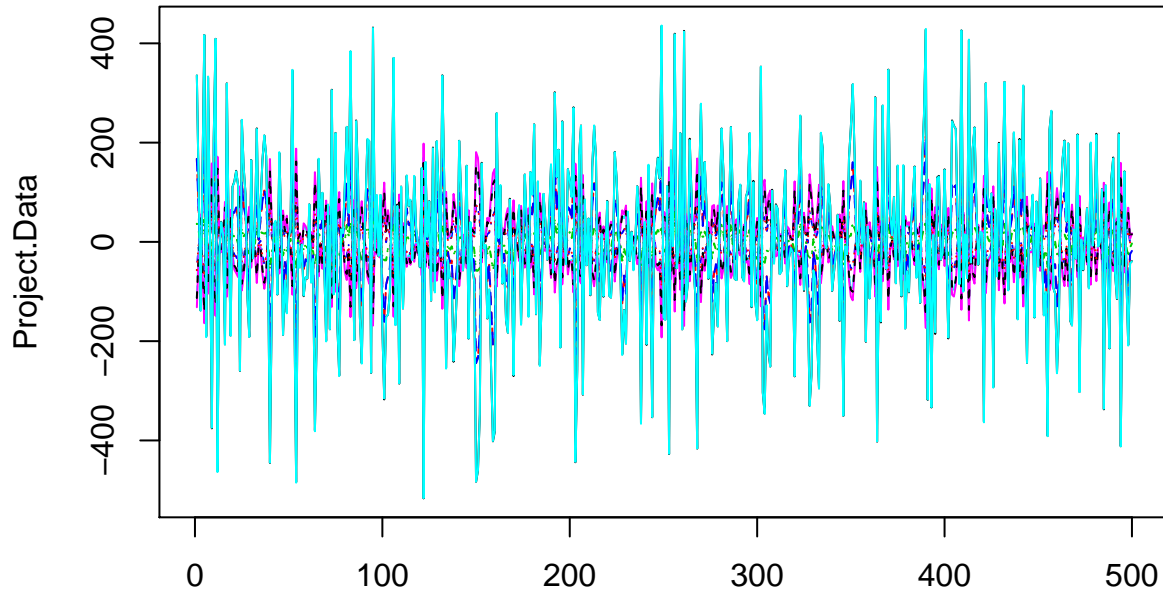
```
Data.Levels<-as.numeric(Project.Data[1,])
Project.Data<-Project.Data[-1,]
head(Project.Data)
```

##	V1	V2	V3	V4	V5	V6
## 2	335.2604	167.30996	36.42212	-57.023949	-112.88559	-131.66066
## 3	106.0443	61.94413	22.68583	-4.491896	-16.86543	-23.94030
## 4	-138.2593	-69.13931	-14.48162	24.403158	47.02190	55.09567
## 5	139.5186	66.76133	11.15244	-28.738979	-53.45132	-61.10555
## 6	416.9990	207.59255	45.27888	-70.756695	-140.82071	-163.84332
## 7	-190.3508	-104.67105	-34.61287	14.833058	41.78893	52.80835

##	V7	V8	V9	V10	V11
## 2	-113.07746	-56.864257	36.48108	167.10119	335.3752
## 3	-20.52873	-1.442949	23.81151	57.95828	108.2360
## 4	47.68518	23.851115	-14.68544	-68.41763	-138.6561

```
## 5 -52.72716 -29.341695 10.92991 67.54925 139.0854
## 6 -140.40840 -71.099858 45.15218 208.04116 416.7524
## 7 44.31460 12.730956 -35.38898 -101.92300 -191.8618
```

```
matplot(Project.Data,type="l")
```



```
# 2 PCA
```

```
Project.Data.PCA <- princomp(Project.Data)
names(Project.Data.PCA)
```

```
## [1] "sdev"      "loadings" "center"   "scale"    "n.obs"    "scores"
## [7] "call"
```

```
Project.Data.PCA$loadings
```

```
##
## Loadings:
##      Comp.1 Comp.2 Comp.3 Comp.4 Comp.5 Comp.6 Comp.7 Comp.8 Comp.9 Comp.10
## V1  -0.584 -0.108  0.232  0.725                -0.261
## V2  -0.295 -0.217 -0.420        -0.450 -0.103        -0.198  0.402  0.229
## V3         -0.294  0.121          0.293  0.635  0.329 -0.397 -0.147  0.133
## V4         -0.351  0.325 -0.102  0.188 -0.562  0.545          0.286
## V5   0.186 -0.391 -0.385        -0.168          0.160 -0.477 -0.576
## V6   0.218 -0.400          0.157 -0.470  0.207  0.213 -0.120  0.152  0.116
```

```

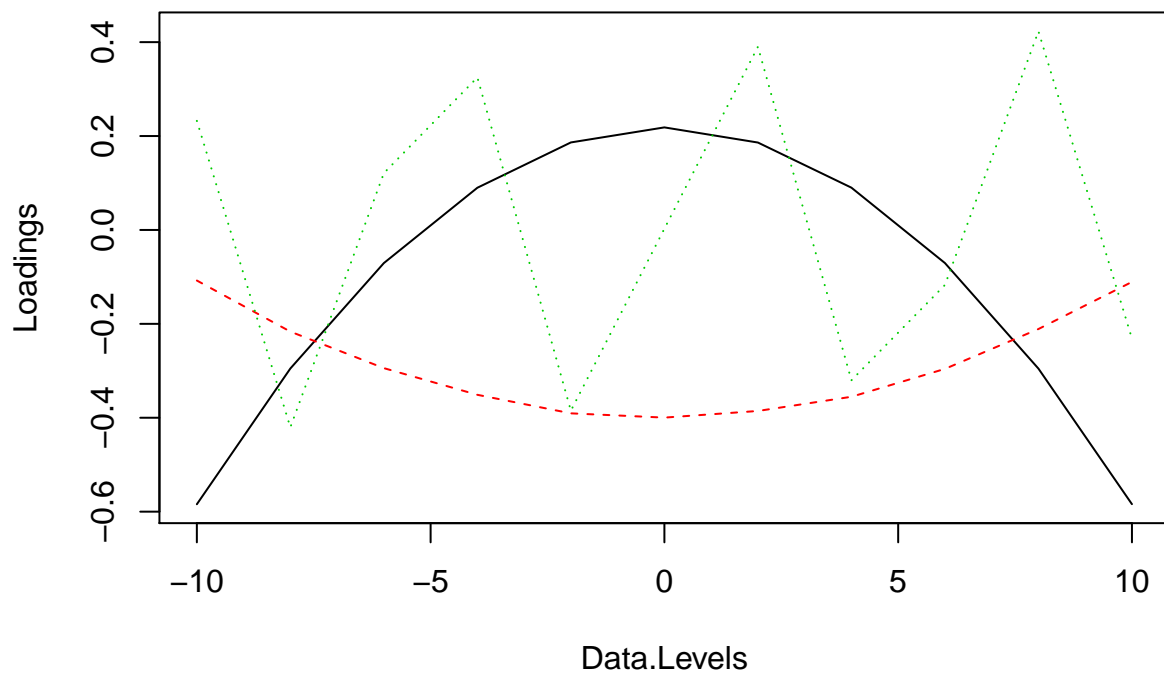
## V7  0.186 -0.386  0.390  0.134 -0.126 -0.167 -0.429          -0.392  0.462
## V8          -0.355 -0.320          0.565 -0.176 -0.423 -0.360  0.178
## V9          -0.296 -0.117          0.238  0.330          0.785  0.305  0.120
## V10 -0.295 -0.211  0.423 -0.558 -0.164          -0.359          0.129 -0.425
## V11 -0.584 -0.111 -0.231 -0.298          -0.218  0.189          -0.436  0.319
##      Comp.11
## V1
## V2  0.460
## V3  0.302
## V4  0.139
## V5  0.202
## V6 -0.639
## V7  0.210
## V8 -0.241
## V9
## V10 -0.106
## V11 -0.340
##
##              Comp.1 Comp.2 Comp.3 Comp.4 Comp.5 Comp.6 Comp.7 Comp.8
## SS loadings    1.000  1.000  1.000  1.000  1.000  1.000  1.000  1.000
## Proportion Var 0.091  0.091  0.091  0.091  0.091  0.091  0.091  0.091
## Cumulative Var 0.091  0.182  0.273  0.364  0.455  0.545  0.636  0.727
##              Comp.9 Comp.10 Comp.11
## SS loadings    1.000  1.000  1.000
## Proportion Var 0.091  0.091  0.091
## Cumulative Var 0.818  0.909  1.000

```

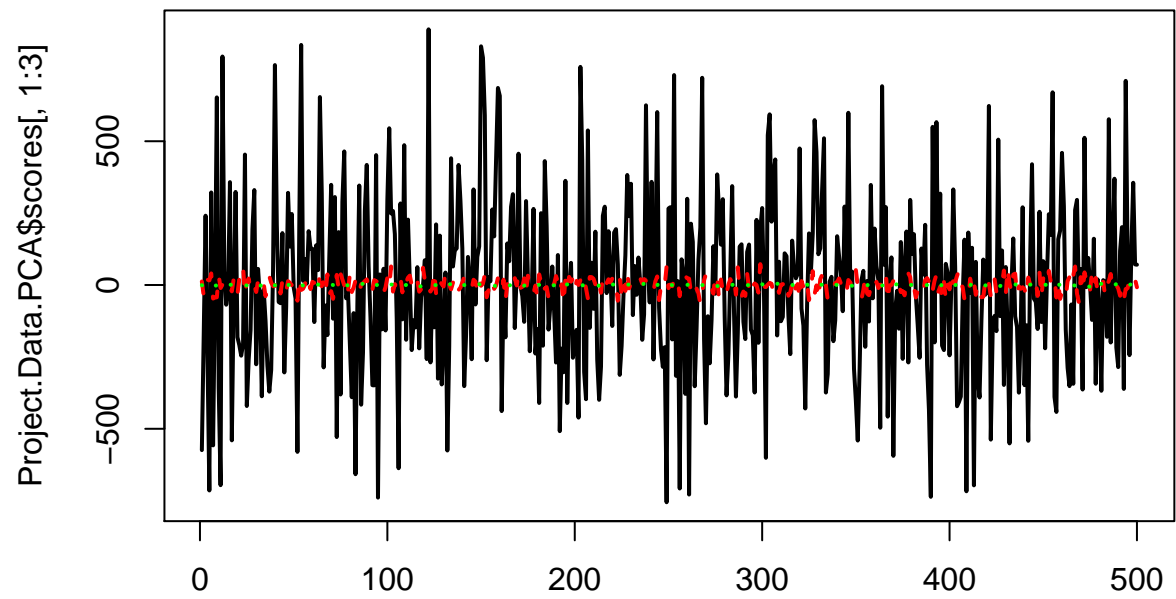
```

matplot(Data.Levels,Project.Data.PCA$loadings[,1:3],type = "l",ylab = "Loadings")

```

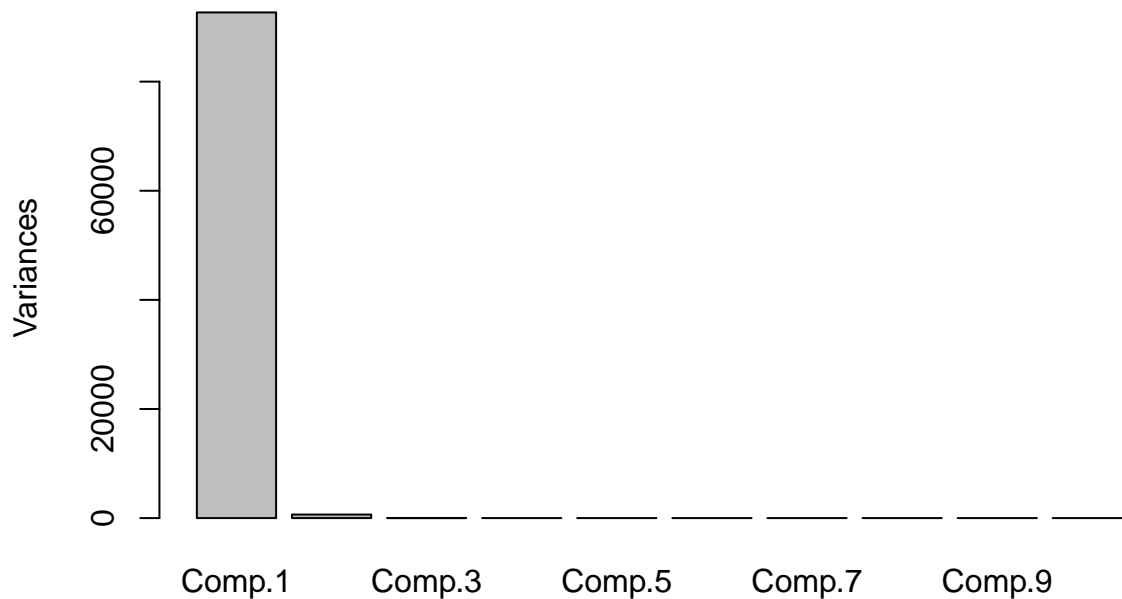


```
matplot(Project.Data.PCA$scores[,1:3],type="l",lty=c(1,2,3),lwd=2,col=c("black","red","green"))
```



```
plot(Project.Data.PCA)
```

Project.Data.PCA



```
(Project.Data.PCA$sdev)^2
```

```
##      Comp.1      Comp.2      Comp.3      Comp.4      Comp.5
## 9.268609e+04 6.489602e+02 5.576366e+00 3.053585e-11 3.062401e-12
##      Comp.6      Comp.7      Comp.8      Comp.9      Comp.10
## 1.785265e-12 1.371684e-12 0.000000e+00 0.000000e+00 0.000000e+00
##      Comp.11
## 0.000000e+00
```

Estimate PCA using manual calculation with `eigen()`. For this recall the steps on slide 16 of the lecture notes.

```
setwd("C:/Users/Adroit/Desktop/CourseProject")
Project.Data <- read.csv("PCA_ExampleData.csv",header=TRUE,sep=",")
Project.Data<-Project.Data[-1,]
mean_vector <- as.vector(apply(as.matrix(Project.Data),2, mean))
mean_matrix <- matrix(mean_vector, length(Project.Data$V1),length(mean_vector), byrow= TRUE)
centered_matrix <- as.matrix(Project.Data) - as.matrix(mean_matrix)
head(centered_matrix)
```

```
##      V1      V2      V3      V4      V5      V6
## 2  333.9805 166.99331 36.83981 -56.079121 -111.61265 -130.28723
## 3  104.7643  61.62748 23.10352 -3.547069 -15.59249 -22.56687
## 4 -139.5392 -69.45596 -14.06393 25.347986  48.29483  56.46910
```

```
## 5 138.2387 66.44468 11.57013 -27.794151 -52.17839 -59.73211
## 6 415.7191 207.27590 45.69657 -69.811867 -139.54778 -162.46989
## 7 -191.6307 -104.98770 -34.19517 15.777886 43.06186 54.18178
##      V7      V8      V9      V10      V11
## 2 -111.81554 -55.910258 36.90216 166.77256 334.1018
## 3 -19.26681 -0.488951 24.23260 57.62964 106.9626
## 4 48.94710 24.805113 -14.26436 -68.74627 -139.9295
## 5 -51.46524 -28.387697 11.35099 67.22061 137.8120
## 6 -139.14649 -70.145860 45.57326 207.71253 415.4790
## 7 45.57652 13.684954 -34.96789 -102.25163 -193.1352
```

```
covariance_matrix <-cov(centered_matrix)
eigen_values<-eigen(covariance_matrix)
eigen_values$vectors
```

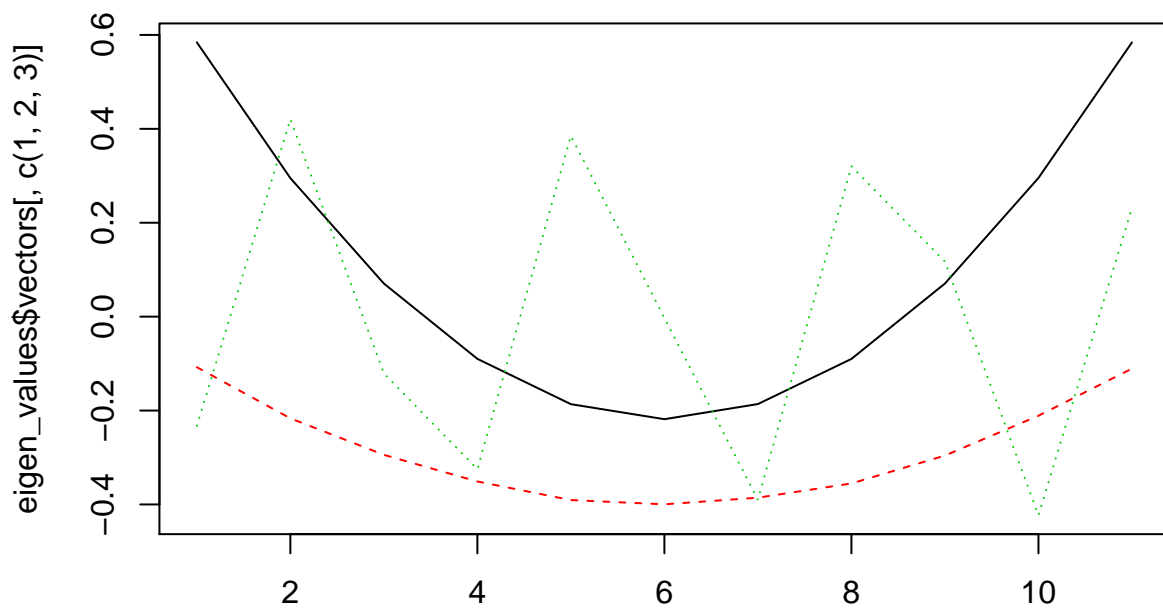
```
##      [,1]      [,2]      [,3]      [,4]      [,5]
## [1,] 0.58420418 -0.1077103 -0.232409041 0.704088457 0.00000000
## [2,] 0.29510562 -0.2165408 0.420358898 -0.445851077 -0.04958303
## [3,] 0.07055080 -0.2943480 -0.120991690 -0.101718860 0.39148860
## [4,] -0.08989770 -0.3511162 -0.324880404 -0.119855757 -0.22566137
## [5,] -0.18640449 -0.3906019 0.384963011 0.263811539 0.45870310
## [6,] -0.21839512 -0.3996945 -0.002667934 0.100673838 -0.40721865
## [7,] -0.18618311 -0.3855492 -0.390129058 -0.105466307 0.15420914
## [8,] -0.09008195 -0.3553215 0.320223821 0.221787141 -0.50799816
## [9,] 0.07048278 -0.2959006 0.117184214 0.001162004 0.34780785
## [10,] 0.29534648 -0.2110431 -0.422977624 -0.315124579 -0.05611926
## [11,] 0.58407174 -0.1107333 0.231318707 -0.203506399 -0.10562822
##      [,6]      [,7]      [,8]      [,9]      [,10]
## [1,] 0.00000000 0.00000000 0.00000000 0.00000000 0.00000000
## [2,] -0.02976470 0.02421440 0.02556953 0.009529595 0.08423477
## [3,] -0.03071383 0.09868706 -0.76589307 0.266898146 0.22963443
## [4,] 0.70711677 0.38064516 0.01132780 -0.042577037 -0.21269880
## [5,] -0.15010781 0.49940024 0.29068194 -0.089986835 -0.10509697
## [6,] -0.36508083 -0.14412998 -0.04445893 0.521624807 -0.43209635
## [7,] -0.27458962 -0.33382232 -0.02329083 -0.633460487 -0.11996743
## [8,] 0.06242348 -0.08920801 -0.11772099 -0.253343219 0.56506975
## [9,] 0.41412266 -0.63922546 0.30828191 0.269378476 0.05220206
## [10,] -0.30080502 0.21554266 0.44666628 0.207805404 0.39296306
## [11,] -0.03260110 -0.01210376 -0.13116364 -0.255868849 -0.45424453
##      [,11]
## [1,] -0.31200873
## [2,] -0.69193000
## [3,] 0.09429502
## [4,] -0.07558668
## [5,] 0.09439269
## [6,] -0.04177062
## [7,] -0.16291027
## [8,] 0.21595673
## [9,] 0.14945530
## [10,] 0.22980901
## [11,] 0.50029755
```

```
Project.Data.PCA$loadings
```

```
##
## Loadings:
##      Comp.1 Comp.2 Comp.3 Comp.4 Comp.5 Comp.6 Comp.7 Comp.8 Comp.9 Comp.10
## V1 -0.584 -0.108  0.232  0.725                -0.261
## V2 -0.295 -0.217 -0.420        -0.450 -0.103        -0.198  0.402  0.229
## V3         -0.294  0.121        0.293  0.635  0.329 -0.397 -0.147  0.133
## V4         -0.351  0.325 -0.102  0.188 -0.562  0.545        0.286
## V5  0.186 -0.391 -0.385        -0.168        0.160 -0.477 -0.576
## V6  0.218 -0.400        0.157 -0.470  0.207  0.213 -0.120  0.152  0.116
## V7  0.186 -0.386  0.390  0.134 -0.126 -0.167 -0.429        -0.392  0.462
## V8         -0.355 -0.320        0.565 -0.176 -0.423 -0.360  0.178
## V9         -0.296 -0.117        0.238  0.330        0.785  0.305  0.120
## V10 -0.295 -0.211  0.423 -0.558 -0.164        -0.359        0.129 -0.425
## V11 -0.584 -0.111 -0.231 -0.298        -0.218  0.189        -0.436  0.319
##      Comp.11
## V1
## V2  0.460
## V3  0.302
## V4  0.139
## V5  0.202
## V6 -0.639
## V7  0.210
## V8 -0.241
## V9
## V10 -0.106
## V11 -0.340
##
##      Comp.1 Comp.2 Comp.3 Comp.4 Comp.5 Comp.6 Comp.7 Comp.8
## SS loadings  1.000  1.000  1.000  1.000  1.000  1.000  1.000  1.000
## Proportion Var 0.091  0.091  0.091  0.091  0.091  0.091  0.091  0.091
## Cumulative Var 0.091  0.182  0.273  0.364  0.455  0.545  0.636  0.727
##      Comp.9 Comp.10 Comp.11
## SS loadings  1.000  1.000  1.000
## Proportion Var 0.091  0.091  0.091
## Cumulative Var 0.818  0.909  1.000
```

Calculate 3 factor loadings using PCA and using manual method based on eigen-decomposition. Combine them in one matrix `Project.Data.PCA.by.eigen.Loadings` and compare

```
matplot(eigen_values$eigenvectors[,c(1,2,3)],type = "l")
```

```
Project.Data.PCA.Eigen.Loadings= cbind(L1.eigen = eigen_values$vector[,1],L2.eigen = eigen_values$vector[,2],L3.eigen = eigen_values$vector[,3])
Project.Data.PCA.Eigen.Loadings
```

```
##      L1.eigen  L2.eigen  L3.eigen  L1.PCA  L2.PCA
## V1  0.58420418 -0.1077103 -0.232409041 -0.58420418 -0.1077103
## V2  0.29510562 -0.2165408  0.420358898 -0.29510562 -0.2165408
## V3  0.07055080 -0.2943480 -0.120991690 -0.07055080 -0.2943480
## V4 -0.08989770 -0.3511162 -0.324880404  0.08989770 -0.3511162
## V5 -0.18640449 -0.3906019  0.384963011  0.18640449 -0.3906019
## V6 -0.21839512 -0.3996945 -0.002667934  0.21839512 -0.3996945
## V7 -0.18618311 -0.3855492 -0.390129058  0.18618311 -0.3855492
## V8 -0.09008195 -0.3553215  0.320223821  0.09008195 -0.3553215
## V9  0.07048278 -0.2959006  0.117184214 -0.07048278 -0.2959006
## V10 0.29534648 -0.2110431 -0.422977624 -0.29534648 -0.2110431
## V11 0.58407174 -0.1107333  0.231318707 -0.58407174 -0.1107333
##      L3.PCA
## V1  0.232409041
## V2 -0.420358898
## V3  0.120991690
## V4  0.324880404
## V5 -0.384963011
## V6  0.002667934
## V7  0.390129058
## V8 -0.320223821
## V9 -0.117184214
```

```
## V10 0.422977624  
## V11 -0.231318707
```