# Social network Graph Link Prediction - Facebook Challenge

#### **Problem statement:**

Given a directed social graph, have to predict missing links to recommend users (Link Prediction in graph)

#### **Data Overview**

Taken data from facebook's recruting challenge on kaggle <a href="https://www.kaggle.com/c/FacebookRecruiting">https://www.kaggle.com/c/FacebookRecruiting</a>

data contains two columns source and destination eac edge in graph

```
Data columns (total 2 columns):source_node int64destination node int64
```

#### Mapping the problem into supervised learning problem:

- Generated training samples of good and bad links from given directed graph and for each link got some features like no of followers, is he followed back, page rank, katz score, adar index, some svd fetures of adj matrix, some weight features etc. and trained ml model based on these features to predict link.
- Some reference papers and videos :
  - https://www.cs.cornell.edu/home/kleinber/link-pred.pdf
  - https://www3.nd.edu/~dial/publications/lichtenwalter2010new.pdf

- https://kaggle2.blob.core.windows.net/forum-messageattachments/2594/supervised link prediction.pdf
- https://www.youtube.com/watch?v=2M77Hgy17cg

#### **Business objectives and constraints:**

- No low-latency requirement.
- Probability of prediction is useful to recommend ighest probability links

#### **Performance metric for supervised learning:**

- Both precision and recall is important so F1 score is good choice
- Confusion matrix

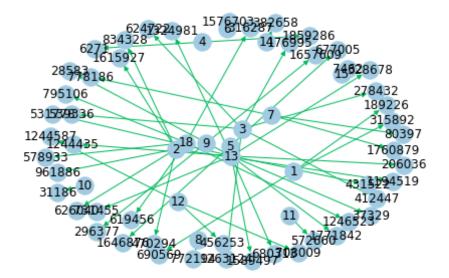
```
In [1]: #Importing Libraries
        # please do go through this python notebook:
        import warnings
        warnings.filterwarnings("ignore")
        import csv
        import pandas as pd#pandas to create small dataframes
        import datetime #Convert to unix time
        import time #Convert to unix time
        # if numpy is not installed already : pip3 install numpy
        import numpy as np#Do aritmetic operations on arrays
        # matplotlib: used to plot graphs
        import matplotlib
        import matplotlib.pylab as plt
        import seaborn as sns#Plots
        from matplotlib import rcParams#Size of plots
        from sklearn.cluster import MiniBatchKMeans, KMeans#Clustering
        import math
        import pickle
        import os
```

```
# to install xgboost: pip3 install xgboost
         import xqboost as xqb
         import warnings
         import networkx as nx
         import pdb
         import pickle
In [9]: #reading graph
         if not os.path.isfile('G:\\machine learning\\case study\\Case Study 3Fa
         cebook Friend Recommendation using Graph Mining\\assignment\\FacebookRe
         cruiting\\train woheader.csv'):
             traincsv = pd.read csv('G:\\machine learning\\case study\\Case Stud
         y 3Facebook Friend Recommendation using Graph Mining\\assignment\\Faceb
         ookRecruiting\\train.csv')
             traincsv = traincsv[0:100000]
             print(traincsv[traincsv.isna().any(1)])
             print(traincsv.info())
             print("Number of diplicate entries: ",sum(traincsv.duplicated()))
             traincsv.to csv('G:\\machine learning\\case study\\Case Study 3Face
         book Friend Recommendation using Graph Mining\\assignment\\FacebookRecr
         uiting\\train woheader.csv',header=False,index=False)
             print("saved the graph into file")
         else:
             q=nx.read edgelist('G:\\machine learning\\case study\\Case Study 3F
         acebook Friend Recommendation using Graph Mining\\assignment\\FacebookR
         ecruiting\\train woheader.csv',delimiter=',',create using=nx.DiGraph(),
         nodetype=int)
             print(nx.info(q))
         Name:
         Type: DiGraph
         Number of nodes: 105845
         Number of edges: 100000
         Average in degree:
                              0.9448
         Average out degree:
                               0.9448
In [10]: | abc = pd.read csv('G:\\machine learning\\case study\\Case Study 3Facebo
         ok Friend Recommendation using Graph Mining\\assignment\\FacebookRecrui
```

```
ting\\train woheader.csv')
In [11]: abc.shape
Out[11]: (99999, 2)
               Displaying a sub graph
In [12]: if not os.path.isfile('G:\\machine learning\\case study\\Case Study 3Fa
         cebook Friend Recommendation using Graph Mining\\assignment\\FacebookRe
         cruiting\\train woheader sample.csv'):
             pd.read csv('G:\\machine learning\\case study\\Case Study 3Facebook
          Friend Recommendation using Graph Mining\\assignment\\FacebookRecruiti
         ng\\train.csv', nrows=50).to csv('G:\\machine learning\\case study\\Cas
         e Study 3Facebook Friend Recommendation using Graph Mining\\assignment
         \\FacebookRecruiting\\train woheader sample.csv',header=False,index=Fal
         se)
         subgraph=nx.read edgelist('G:\\machine learning\\case study\\Case Study
          3Facebook Friend Recommendation using Graph Mining\\assignment\\Facebo
         okRecruiting\\train woheader sample.csv',delimiter=',',create using=nx.
         DiGraph().nodetvpe=int)
         # https://stackoverflow.com/questions/9402255/drawing-a-huge-graph-with
         -networkx-and-matplotlib
         pos=nx.spring layout(subgraph)
         nx.draw(subgraph,pos,node color='#A0CBE2',edge color='#00bb5e',width=1,
         edge cmap=plt.cm.Blues,with labels=True)
         plt.savefig("G:\\machine learning\\case study\\Case Study 3Facebook Fri
         end Recommendation using Graph Mining\\assignment\\FacebookRecruiting\\
         graph sample.pdf")
         print(nx.info(subgraph))
         Name:
         Type: DiGraph
         Number of nodes: 66
```

Number of edges: 50

Average in degree: 0.7576 Average out degree: 0.7576



```
In [13]: xyz = pd.read_csv('G:\\machine_learning\\case_study\\Case Study 3Facebo
  ok Friend Recommendation using Graph Mining\\assignment\\FacebookRecrui
  ting\\train_woheader_sample.csv')
```

```
In [14]: xyz.shape
```

Out[14]: (49, 2)

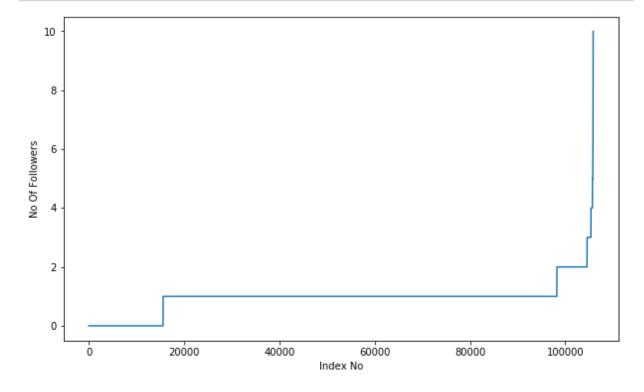
## 1. Exploratory Data Analysis

```
In [15]: # No of Unique persons
print("The number of unique persons",len(g.nodes()))
```

The number of unique persons 105845

## 1.1 No of followers for each person

```
In [16]: indegree_dist = list(dict(g.in_degree()).values())
    indegree_dist.sort()
    plt.figure(figsize=(10,6))
    plt.plot(indegree_dist)
    plt.xlabel('Index No')
    plt.ylabel('No Of Followers')
    plt.show()
```

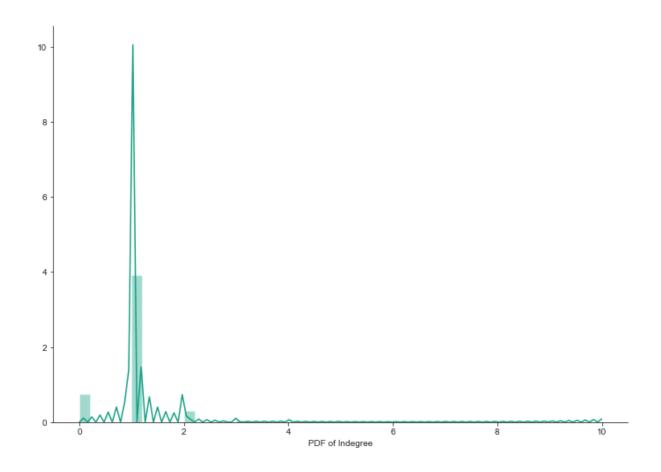


```
In [17]: indegree_dist = list(dict(g.in_degree()).values())
indegree_dist.sort()
```

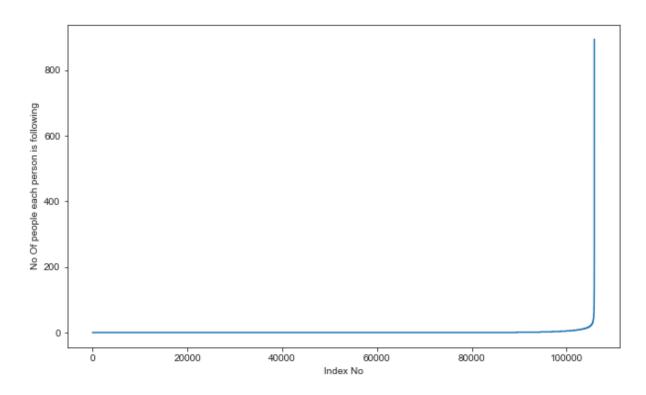
```
plt.figure(figsize=(10,6))
            plt.plot(indegree_dist[0:1000000])
            plt.xlabel('Index No')
            plt.ylabel('No Of Followers')
            plt.show()
               10
            No Of Followers
                2
                                  20000
                                                                                           100000
                                                40000
                                                               60000
                                                                             80000
                                                         Index No
In [18]: plt.boxplot(indegree_dist)
    plt.ylabel('No Of Followers')
            plt.show()
```

```
In [19]: ### 90-100 percentile
         for i in range(0,11):
              print(90+i, 'percentile value is', np.percentile(indegree dist, 90+i))
         90 percentile value is 1.0
         91 percentile value is 1.0
         92 percentile value is 1.0
         93 percentile value is 2.0
         94 percentile value is 2.0
         95 percentile value is 2.0
         96 percentile value is 2.0
         97 percentile value is 2.0
         98 percentile value is 2.0
         99 percentile value is 3.0
         100 percentile value is 10.0
         99% of data having followers of 40 only.
In [20]: ### 99-100 percentile
         for i in range(10,110,10):
              print(99+(i/100), 'percentile value is', np.percentile(indegree dist,
         99+(i/100)))
```

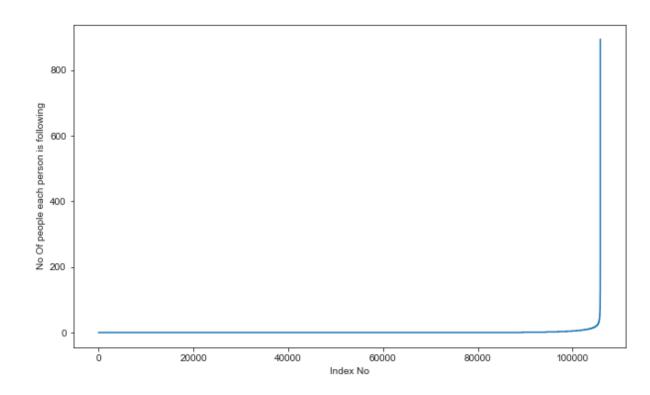
```
99.1 percentile value is 3.0
         99.2 percentile value is 3.0
         99.3 percentile value is 3.0
         99.4 percentile value is 3.0
         99.5 percentile value is 3.0
         99.6 percentile value is 4.0
         99.7 percentile value is 4.0
         99.8 percentile value is 4.0
         99.9 percentile value is 5.0
         100.0 percentile value is 10.0
In [21]: %matplotlib inline
         sns.set style('ticks')
         fig, ax = plt.subplots()
         fig.set size inches(11.7, 8.27)
         sns.distplot(indegree dist, color='#16A085')
         plt.xlabel('PDF of Indegree')
         sns.despine()
         #plt.show()
```



## 1.2 No of people each person is following



```
In [23]: indegree_dist = list(dict(g.in_degree()).values())
    indegree_dist.sort()
    plt.figure(figsize=(10,6))
    plt.plot(outdegree_dist[0:1500000])
    plt.xlabel('Index No')
    plt.ylabel('No Of people each person is following')
    plt.show()
```

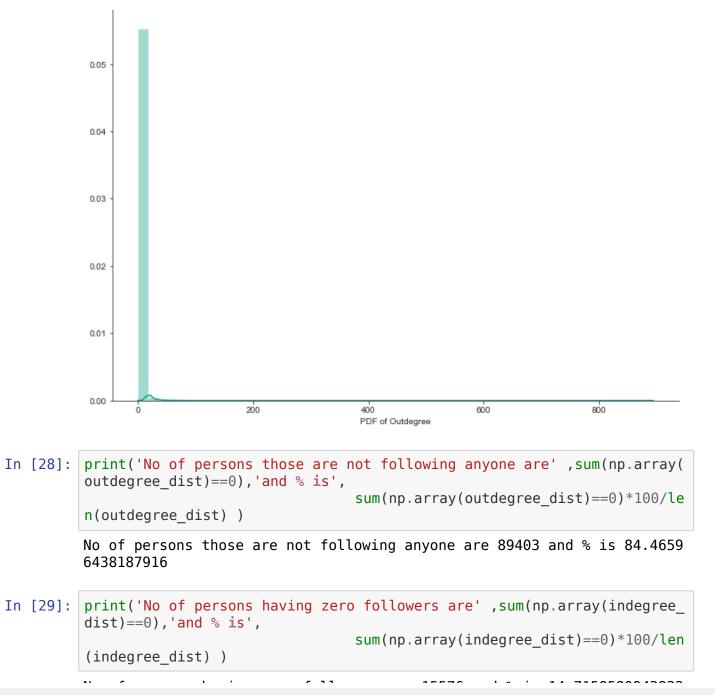


```
In [24]: plt.boxplot(indegree_dist)
   plt.ylabel('No Of people each person is following')
   plt.show()
```

```
10
                                    0
                                    0
           No Of people each person is following
                                    0
In [25]: ### 90-100 percentile
          for i in range(0,11):
              print(90+i, 'percentile value is', np.percentile(outdegree dist, 90+i
          90 percentile value is 2.0
          91 percentile value is 2.0
          92 percentile value is 3.0
          93 percentile value is 3.0
          94 percentile value is 4.0
          95 percentile value is 5.0
          96 percentile value is 7.0
          97 percentile value is 9.0
          98 percentile value is 12.0
          99 percentile value is 18.0
          100 percentile value is 895.0
In [26]: ### 99-100 percentile
          for i in range(10,110,10):
              print(99+(i/100), 'percentile value is', np.percentile(outdegree dist
          ,99+(i/100)))
          99.1 percentile value is 19.0
```

99.2 percentile value is 20.0

```
99.3 percentile value is 21.0
99.4 percentile value is 23.0
99.5 percentile value is 25.0
99.6 percentile value is 28.0
99.7 percentile value is 31.46799999999348
99.8 percentile value is 39.0
99.9 percentile value is 56.15600000001723
100.0 percentile value is 895.0
In [27]:
sns.set_style('ticks')
fig, ax = plt.subplots()
fig.set_size_inches(11.7, 8.27)
sns.distplot(outdegree_dist, color='#16A085')
plt.xlabel('PDF of Outdegree')
sns.despine()
```



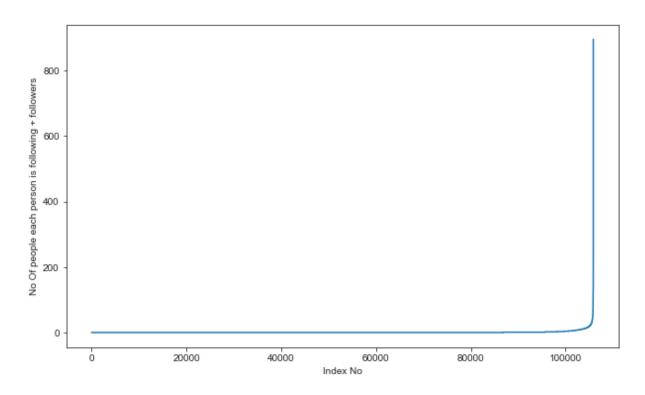
No of persons having zero followers are 15576 and % is 14.7158580943832

No of persons those are not not following anyone and also not having an y followers are  $\boldsymbol{\theta}$ 

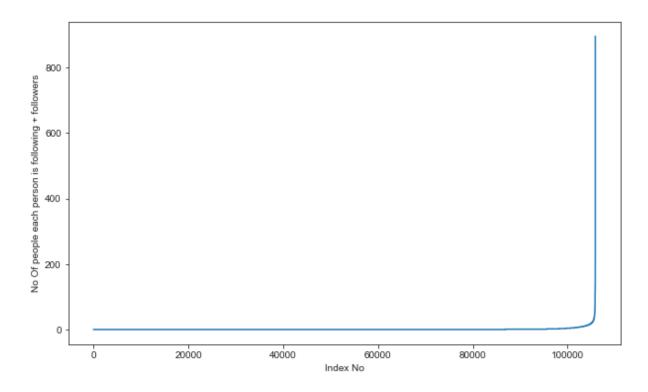
### 1.3 both followers + following

```
In [31]: from collections import Counter
dict_in = dict(g.in_degree())
dict_out = dict(g.out_degree())
d = Counter(dict_in) + Counter(dict_out)
in_out_degree = np.array(list(d.values()))
```

```
In [32]: in_out_degree_sort = sorted(in_out_degree)
    plt.figure(figsize=(10,6))
    plt.plot(in_out_degree_sort)
    plt.xlabel('Index No')
    plt.ylabel('No Of people each person is following + followers')
    plt.show()
```



```
In [33]: in_out_degree_sort = sorted(in_out_degree)
    plt.figure(figsize=(10,6))
    plt.plot(in_out_degree_sort[0:1500000])
    plt.xlabel('Index No')
    plt.ylabel('No Of people each person is following + followers')
    plt.show()
```



```
In [34]: ### 90-100 percentile
for i in range(0,11):
     print(90+i, 'percentile value is',np.percentile(in_out_degree_sort,9
0+i))

90 percentile value is 2.0
91 percentile value is 3.0
92 percentile value is 3.0
93 percentile value is 4.0
94 percentile value is 4.0
95 percentile value is 5.0
96 percentile value is 7.0
97 percentile value is 7.0
98 percentile value is 12.0
99 percentile value is 18.0
100 percentile value is 895.0
```

```
In [35]: ### 99-100 percentile
         for i in range(10,110,10):
             print(99+(i/100), 'percentile value is', np.percentile(in out degree
         sort,99+(i/100))
         99.1 percentile value is 19.0
         99.2 percentile value is 20.0
         99.3 percentile value is 22.0
         99.4 percentile value is 23.0
         99.5 percentile value is 26.0
         99.6 percentile value is 28.0
         99.7 percentile value is 32.0
         99.8 percentile value is 39.312000000005355
         99.9 percentile value is 57.0
         100.0 percentile value is 895.0
In [36]: print('Min of no of followers + following is',in out degree.min())
         print(np.sum(in out degree==in out degree.min()),' persons having minim
         um no of followers + following')
         Min of no of followers + following is 1
         86847 persons having minimum no of followers + following
In [37]: print('Max of no of followers + following is',in out degree.max())
         print(np.sum(in out degree==in out degree.max()), ' persons having maxim
         um no of followers + following')
         Max of no of followers + following is 895
         1 persons having maximum no of followers + following
In [38]: print('No of persons having followers + following less than 10 are',np.
         sum(in out degree<10))</pre>
         No of persons having followers + following less than 10 are 102945
         print('No of weakly connected components',len(list(nx.weakly connected
In [39]:
         components(g))))
         count=0
```

```
for i in list(nx.weakly_connected_components(g)):
    if len(i)==2:
        count+=1
print('weakly connected components wit 2 nodes',count)
```

No of weakly connected components 12030 weakly connected components wit 2 nodes 4526

## 2. Posing a problem as classification problem

## 2.1 Generating some edges which are not present in graph for supervised learning

Generated Bad links from graph which are not in graph and whose shortest path is greater than 2.

```
In [40]: |%time
         ###generating bad edges from given graph
         import random
         if not os.path.isfile('G:\\machine learning\\case study\\Case Study 3Fa
         cebook Friend Recommendation using Graph Mining\\assignment\\FacebookRe
         cruiting\\missing edges final.p'):
             #getting all set of edges
             r = csv.reader(open('G:\\machine learning\\case study\\Case Study 3
         Facebook Friend Recommendation using Graph Mining\\assignment\\Facebook
         Recruiting\\train woheader.csv','r'))
             edges = dict()
             for edge in r:
                 edges[(edge[0], edge[1])] = 1
             missing edges = set([])
             while (len(missing edges)<100000):</pre>
                 a=random.randint(1, 100000)
```

```
b=random.randint(1, 100000)
                 tmp = edges.get((a,b),-1)
                 if tmp == -1 and a!=b:
                      try:
                          if nx.shortest path length(q,source=a,target=b) > 2:
                              missing edges.add((a,b))
                          else:
                              continue
                      except:
                              missing edges.add((a,b))
                 else:
                      continue
              pickle.dump(missing edges,open('G:\\machine learning\\case study\\C
         ase Study 3Facebook Friend Recommendation using Graph Mining\\assignmen
         t\\FacebookRecruiting\\missing edges final.p','wb'))
         else:
             missing edges = pickle.load(open('G:\\machine learning\\case study
         \\Case Study 3Facebook Friend Recommendation using Graph Mining\\assign
         ment\\FacebookRecruiting\\missing edges final.p','rb'))
         Wall time: 1.33 s
In [41]: missing edges = pickle.load(open('G:\\machine learning\\case study\\Case
         e Study 3Facebook Friend Recommendation using Graph Mining\\assignment
         \\FacebookRecruiting\\missing edges final.p','rb'))
         len(missing edges)
Out[41]: 100000
         2.2 Training and Test data split:
         Removed edges from Graph and used as test data and after removing used that graph for
         creating features for Train and test data
In [42]: from sklearn.model selection import train test split
         if (not os.path.isfile('G:\\machine learning\\case study\\Case Study 3F
```

```
acebook Friend Recommendation using Graph Mining\\assignment\\FacebookR
ecruiting\\train pos after eda.csv')) and (not os.path.isfile('G:\\mach
ine learning\\case study\\Case Study 3Facebook Friend Recommendation us
ing Graph Mining\\assignment\\FacebookRecruiting\\test_pos_after_eda.cs
v')):
    #reading total data df
    df pos = pd.read csv('G:\\machine learning\\case study\\Case Study
3Facebook Friend Recommendation using Graph Mining\\assignment\\Facebo
okRecruiting\\train.csv')
    df pos = df pos[0:100000]
    df neg = pd.DataFrame(list(missing edges), columns=['source node',
'destination node'])
    print("Number of nodes in the graph with edges", df pos.shape[0])
    print("Number of nodes in the graph without edges", df neg.shape[0
1)
    #Trian test split
    #Spiltted data into 80-20
    #positive links and negative links seperatly because we need positi
ve training data only for creating graph
    #and for feature generation
   X train pos, X test pos, y train pos, y test pos = train test spli
t(df pos,np.ones(len(df pos)),test size=0.2, random_state=9)
    X train neg, X test neg, y train neg, y test neg = train test spli
t(df neg,np.zeros(len(df neg)),test size=0.2, random state=9)
    print('='*60)
    print("Number of nodes in the train data graph with edges", X train
pos.shape[0], "=", y train pos.shape[0])
    print("Number of nodes in the train data graph without edges", X tr
ain neg.shape[0],"=", y train neg.shape[0])
    print('='*60)
    print("Number of nodes in the test data graph with edges", X test p
os.shape[0], "=", y test pos.shape[0])
    print("Number of nodes in the test data graph without edges", X tes
t neg.shape[0], "=", y test neg.shape[0])
    #removing header and saving
```

```
X train pos.to csv('G:\\machine learning\\case study\\Case Study 3F
        acebook Friend Recommendation using Graph Mining\\assignment\\FacebookR
         ecruiting\\train pos after eda.csv',header=False, index=False)
            X test pos.to csv('G:\\machine learning\\case study\\Case Study 3Fa
         cebook Friend Recommendation using Graph Mining\\assignment\\FacebookRe
         cruiting\\test pos after eda.csv',header=False, index=False)
            X train neg.to csv('G:\\machine learning\\case study\\Case Study 3F
         acebook Friend Recommendation using Graph Mining\\assignment\\FacebookR
         ecruiting\\train neg after eda.csv',header=False, index=False)
            X test neg.to csv('G:\\machine learning\\case study\\Case Study 3Fa
         cebook Friend Recommendation using Graph Mining\\assignment\\FacebookRe
         cruiting\\test neg after eda.csv',header=False, index=False)
         else:
            #Graph from Traing data only
            del missing edges
        Number of nodes in the graph with edges 100000
        Number of nodes in the graph without edges 100000
         ______
        Number of nodes in the train data graph with edges 80000 = 80000
        Number of nodes in the train data graph without edges 80000 = 80000
         _____
        Number of nodes in the test data graph with edges 20000 = 20000
        Number of nodes in the test data graph without edges 20000 = 20000
In [43]: if (os.path.isfile('G:\\machine learning\\case study\\Case Study 3Faceb
         ook Friend Recommendation using Graph Mining\\assignment\\FacebookRecru
        iting\\train pos after eda.csv')) and (os.path.isfile('G:\\machine lear
         ning\\case study\\Case Study 3Facebook Friend Recommendation using Grap
         h Mining\\assignment\\FacebookRecruiting\\test pos after eda.csv')):
            train graph=nx.read edgelist('G:\\machine learning\\case study\\Cas
         e Study 3Facebook Friend Recommendation using Graph Mining\\assignment
         \\FacebookRecruiting\\train pos after eda.csv',delimiter=',',create usi
         ng=nx.DiGraph(),nodetype=int)
            test graph=nx.read edgelist('G:\\machine learning\\case study\\Case
         Study 3Facebook Friend Recommendation using Graph Mining\\assignment\\
         FacebookRecruiting\\test pos after eda.csv',delimiter=',',create using=
         nx.DiGraph(),nodetype=int)
```

```
print(nx.info(train graph))
    print(nx.info(test graph))
    # finding the unique nodes in the both train and test graphs
    train nodes pos = set(train graph.nodes())
    test nodes pos = set(test graph.nodes())
    trY teY = len(train nodes pos.intersection(test nodes pos))
    trY teN = len(train nodes pos - test nodes pos)
    teY trN = len(test nodes pos - train nodes pos)
    print('no of people common in train and test -- ',trY teY)
    print('no of people present in train but not present in test -- ',t
rY teN)
    print('no of people present in test but not present in train -- ',t
eY trN)
    print(' % of people not there in Train but exist in Test in total T
est data are {} %'.format(teY trN/len(test nodes pos)*100))
Name:
Type: DiGraph
Number of nodes: 88074
Number of edges: 80000
Average in degree:
                     0.9083
Average out degree: 0.9083
Name:
Type: DiGraph
Number of nodes: 27902
Number of edges: 20000
Average in degree:
                     0.7168
Average out degree: 0.7168
no of people common in train and test -- 10131
no of people present in train but not present in test -- 77943
no of people present in test but not present in train -- 17771
 % of people not there in Train but exist in Test in total Test data ar
e 63.69077485484912 %
```

```
In [44]: #final train and test data sets
         if (not os.path.isfile('G:\\machine learning\\case study\\Case Study 3F
         acebook Friend Recommendation using Graph Mining\\assignment\\FacebookR
         ecruiting\\train after eda.csv')) and \
         (not os.path.isfile('G:\\machine learning\\case study\\Case Study 3Face
         book Friend Recommendation using Graph Mining\\assignment\\FacebookRecr
         uiting\\test after eda.csv')) and \
         (not os.path.isfile('G:\\machine learning\\case study\\Case Study 3Face
         book Friend Recommendation using Graph Mining\\assignment\\FacebookRecr
         uiting\\train y.csv')) and \
         (not os.path.isfile('G:\\machine learning\\case study\\Case Study 3Face
         book Friend Recommendation using Graph Mining\\assignment\\FacebookRecr
         uiting\\test v.csv')) and \
         (os.path.isfile('G:\\machine learning\\case study\\Case Study 3Facebook
          Friend Recommendation using Graph Mining\\assignment\\FacebookRecruiti
         ng\\train pos after eda.csv')) and \
         (os.path.isfile('G:\\machine learning\\case study\\Case Study 3Facebook
          Friend Recommendation using Graph Mining\\assignment\\FacebookRecruiti
         ng\\test pos after eda.csv')) and \
         (os.path.isfile('G:\\machine learning\\case study\\Case Study 3Facebook
          Friend Recommendation using Graph Mining\\assignment\\FacebookRecruiti
         ng\\train neg after eda.csv')) and \
         (os.path.isfile('G:\\machine learning\\case study\\Case Study 3Facebook
          Friend Recommendation using Graph Mining\\assignment\\FacebookRecruiti
         ng\\test neg after eda.csv')):
             X train pos = pd.read csv('G:\\machine learning\\case study\\Case S
         tudy 3Facebook Friend Recommendation using Graph Mining\\assignment\\Fa
         cebookRecruiting\\train pos after eda.csv', names=['source node', 'dest
         ination node'])
             X test pos = pd.read csv('G:\\machine learning\\case study\\Case St
         udy 3Facebook Friend Recommendation using Graph Mining\\assignment\\Fac
         ebookRecruiting\\test pos after eda.csv', names=['source node', 'destin
         ation node'])
             X train neg = pd.read csv('G:\\machine learning\\case study\\Case S
```

```
tudy 3Facebook Friend Recommendation using Graph Mining\\assignment\\Fa
cebookRecruiting\\train neg after eda.csv', names=['source node', 'dest
ination node'l)
    X test neg = pd.read csv('G:\\machine learning\\case study\\Case St
udy 3Facebook Friend Recommendation using Graph Mining\\assignment\\Fac
ebookRecruiting\\test neg after eda.csv', names=['source node', 'destin
ation node'])
    print('='*60)
    print("Number of nodes in the train data graph with edges", X train
pos.shape[0])
    print("Number of nodes in the train data graph without edges", X tr
ain neg.shape[0])
    print('='*60)
    print("Number of nodes in the test data graph with edges", X test p
os.shape[0])
    print("Number of nodes in the test data graph without edges", X tes
t neg.shape[0])
    X train = X train_pos.append(X_train_neg,ignore_index=True)
    y train = np.concatenate((y train pos,y train neg))
    X test = X test pos.append(X test neg,ignore index=True)
    y test = np.concatenate((y test pos,y test neg))
    X train.to csv('G:\\machine learning\\case study\\Case Study 3Faceb
ook Friend Recommendation using Graph Mining\\assignment\\FacebookRecru
iting\\train after eda.csv',header=False,index=False)
    X test.to csv('G:\\machine learning\\case study\\Case Study 3Facebo
ok Friend Recommendation using Graph Mining\\assignment\\FacebookRecrui
ting\\test after eda.csv',header=False,index=False)
    pd.DataFrame(y train.astype(int)).to csv('G:\\machine learning\\cas
e study\\Case Study 3Facebook Friend Recommendation using Graph Mining
\\assignment\\FacebookRecruiting\\train y.csv',header=False,index=False
    pd.DataFrame(y test.astype(int)).to csv('G:\\machine learning\\case
study\\Case Study 3Facebook Friend Recommendation using Graph Mining\\
assignment\\FacebookRecruiting\\test v.csv',header=False,index=False)
```

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Number of nodes in the train data graph with edges 80000