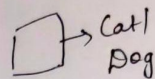
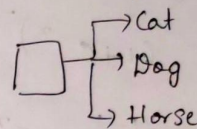
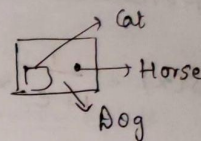


12/10

Binary class

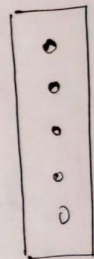
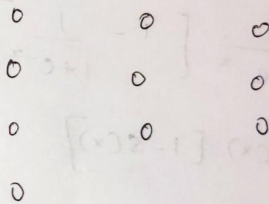
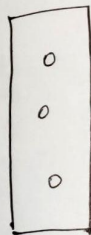
2 variables

Multi-classMulti-labelSingle image,
identifying different
labels

$$\begin{bmatrix} 1 \\ 0 \\ 1 \end{bmatrix}$$

Multi-task learningMulti-label classification

Instead of training separate neural networks for cat, Dog and Horse, we use a single Neural Network to learn all the labels for generalized representation



Input Image

$i = 1 - m$ - no. of Images
 $i = 1 - n$ - no. of labels

$$\begin{aligned} \text{Loss} &= \frac{1}{m} \sum_{i=1}^m \sum_{j=1}^n L(\hat{y}_i - y_i) \\ &= -y_i \log \hat{y}_i - (1 - y_i) \log (1 - \hat{y}_i) \end{aligned}$$

Differentiation of Sigmoid Activation function

$$\begin{aligned}
 S(x) &= \frac{1}{1+e^{-x}} = (1+e^{-x})^{-1} \\
 &= -1 (1+e^{-x})^{-1-1} \cdot e^{-x} \cdot -1 \\
 &= \frac{e^{-x}}{(1+e^{-x})^2} = \frac{1-1+e^{-x}}{(1+e^{-x})^2} \\
 &= \frac{1+e^{-x}}{(1+e^{-x})^2} - \frac{1}{(1+e^{-x})^2} \\
 &= \frac{1}{1+e^{-x}} - \frac{1}{(1+e^{-x})^2} \\
 &= \frac{1}{1+e^{-x}} \left[1 - \frac{1}{1+e^{-x}} \right] \\
 &= S(x) [1 - S(x)]
 \end{aligned}$$

Classify the network factor using Hebbian learning

13/10/24 RNN - Recurrent Neural Network

ANN VS RNN
↳ RNN

Structure of RNN
unrolled / unrolled RNN
Rolled RNN

(BPTT)

Applications of RNN

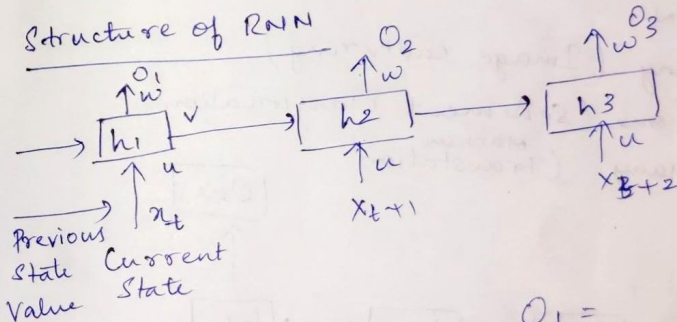
Types of RNN

Drawbacks of RNN

RNN

Time series Application
Sequence of Data

Structure of RNN



$O_1 =$
h - hidden state

u - weight of x_t / weight to the i/p value

v - weight of i/p to h_2

RNN

Autocomplete

↳ Ordering of words is important

↳ Different Varying length

Ex: Stock Market Prediction

Predict tomorrow stock value →

Sequential data i/p from 1 to 12/10

Notation of RNN

$$u x_t + v h_{t-1} + \text{bias}$$

↑
weights

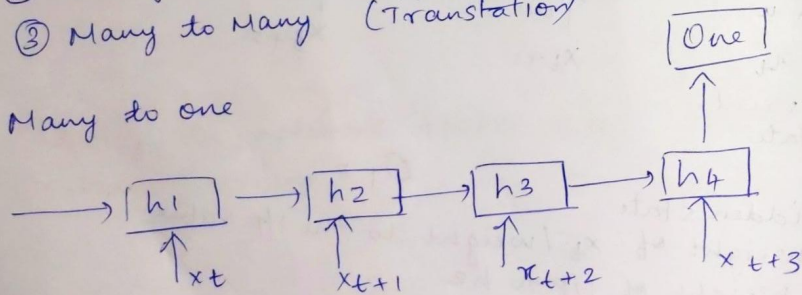
Applications of RNN

- i) Speech Recognition
- ii) Music translation
- iii) Image captioning
- iv) Sentiment classification
- v) Machine translation
- vi) DNA Sequencing
- vii) Stock market prediction

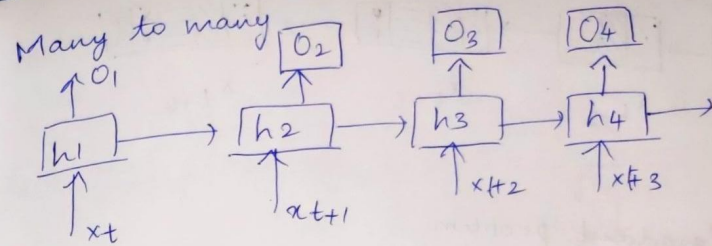
Types of RNN

- ① One to many (Image capturing)
- ② Many to one (Sentiment classification)
- ③ Many to Many (Machine Translation)

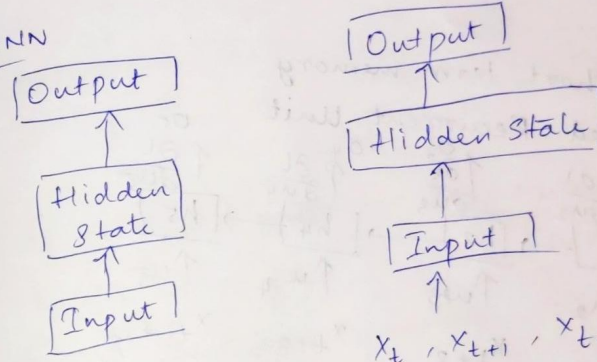
Many to one



Ordering
is important

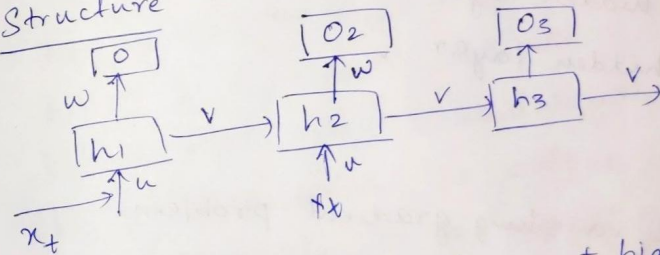


ANN



$x_t, x_{t+1}, x_{t+2}, x_{t+3}, x_{t+4}$

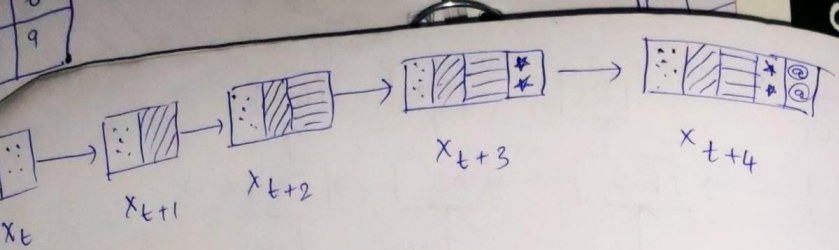
Structure



$$h_t = u x_t + v h_{t-1} + \text{bias}$$

$$o_t = \text{sigmoid}(w h_t + \text{bias})$$



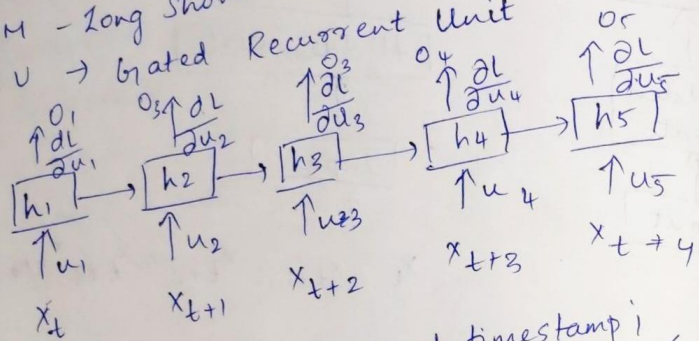


Drawback

Vanishing gradient problem

→ Information flow is very minimal

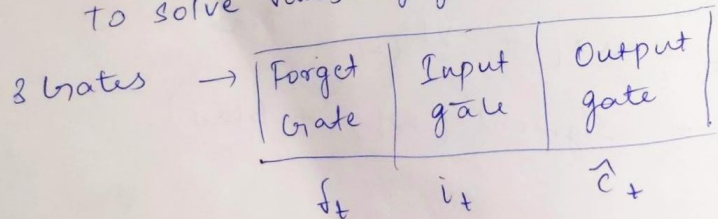
LSTM - Long Short term memory
GRU → Gated Recurrent Unit



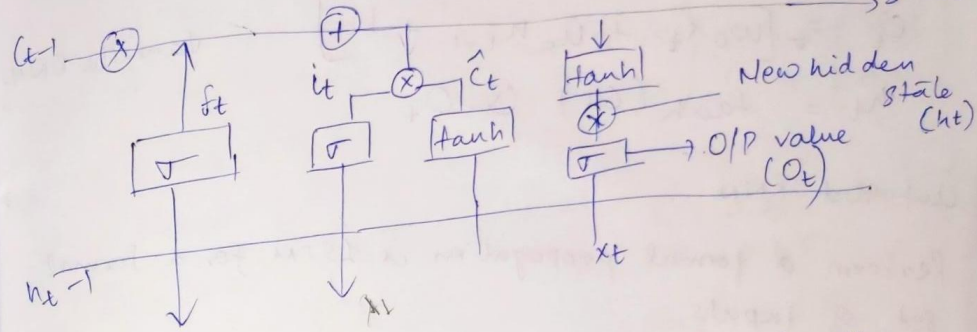
h_1, h_2, \dots hidden layers at timestamp i ,
only one hidden layer.

LSTM

To solve vanishing gradient problem.



Previous cell state C_{t-1}



u_i = weights for the hidden state
[input gate]
 w_i ⇒ weights for the input gate
 o_t ⇒ output gate
 w_o ⇒ weights for the output gate
 u_o ⇒ weights for the hidden state [forget gate]
 f_t ⇒ forget gate
 i_t ⇒ input gate
 \hat{C}_t ⇒ candidate function
 b_f ⇒ bias value forget gate
 b_i ⇒ bias value input gate
 b_c ⇒ bias value candidate gate
 b_o ⇒ bias value for output gate
 w_f ⇒ weights for the forget gate
 u_f ⇒ weights for the hidden state

$$f_t = \sigma [w_f x_t + u_f h_{t-1} + b_f]$$

$$i_t = \sigma [w_i x_t + u_i h_{t-1} + b_i]$$

$$\hat{c}_t \Rightarrow \tanh(w_c x_t + u_c h_{t-1} + b_c)$$

$$f_t = (c_{t-1} \otimes f_t) \oplus i_t \otimes \hat{c}_t$$

$$O_t = \sigma[w_o x_t + u_o h_{t-1} + b_o]$$

$$h_t = \tanh(c_t) \otimes O_t$$

Unfolded RNN

Perform a formal propagation is LSTM for a formal set of inputs

weight for forget gate $[0.7 \ 0.45]$

weight for i/p gate $[0.95 \ 8]$

weight for o/p $[0.6 \ 0.4]$

4 candidate for $[0.45 \ 0.25]$

bias forget gate $[0.15]$

" Input gate $[0.2]$

" Candidate gate $[0.65]$

" Output gate $[0.1]$

weight for hidden forget $[0.25]$

" I/P $[0.8]$

candidate $[0.15]$

Vanilla RNN

| | x_1 | x_2 | Class Label |
|-------|-------|-------|-------------|
| t_0 | 1 | 2 | 0 |
| t_1 | 0.5 | 3 | 1 |

Input $V_i = 0.8$

Output $V_o = 0.25$

Forget $V_f = 0.1$

Candidate $V_c = 0.15$

$w_f = [0.7 \ 0.45]$ $w_i = [0.95 \ 8]$

$w_c = [0.45 \ 0.25]$ $w_o = [0.6 \ 0.4]$

Bias: $\hat{c} = 0.2$ $h_{t-1} = 0$

I/P = 0.65

Forget = 0.15

$$f_t = \sigma \left[\begin{bmatrix} 0.7 \\ 0.45 \end{bmatrix} \begin{bmatrix} 1 \\ 2 \end{bmatrix} + [0.1 \times 0] + 0.15 \right] \quad 0 = 1$$

$$= \sigma [0.7 + 0.9 + 0.15]$$

$$= \sigma [1.75] = 0.852$$

$\frac{0.16}{0.31}$

$$\text{input} = \sigma [0.95 \ 8] \begin{bmatrix} 1 \\ 2 \end{bmatrix} + [0.8 \times 0] + 0.65$$

$$= \sigma [16.95 + 0.65]$$

$$= \sigma [17.60] \quad 0.96$$

Candidate $\hat{c}_t \Rightarrow \tanh [[0.45 \ 0.25] \begin{bmatrix} 1 \\ 2 \end{bmatrix} + [0.15 \times 0] + 0.2]$

$$= [0.95 + 0.2] = 0.15$$

0.818

8 | 9 | 7

$$\text{Output gate} = \sigma [0.6 \cdot 0.4] \begin{bmatrix} 1 \\ 2 \end{bmatrix} + [0.25 \times 0] + 0.1$$

$$C_t = f_t \otimes C_{t-1} \oplus i_t \otimes \hat{C}_t = 0.817$$

$$= \sigma [1.5]$$

$$C_t = 0.786$$

$$h_t = \tanh(C_t \times \text{Output gate})$$

$$= 0.537$$

II: Input = $\sigma \left[\begin{bmatrix} 0.95 & 8 \end{bmatrix} \begin{bmatrix} 0.5 \\ 3 \end{bmatrix} + \begin{bmatrix} 0.8 \times 0.537 \end{bmatrix} + 0.65 \right]$

$$= \sigma [25.55] = 1$$

$$f =$$