

SUBSTITUTION . TECH

TRANSPOSITION . TECH

① CAESER CIPHER (P) ① RAIL FENCE (P)

② MONO ALPHABETIC CIPHER (P) ② ROW COLUMN (P)

③ POLYALPHABETIC CIPHER

(i) VERNAM

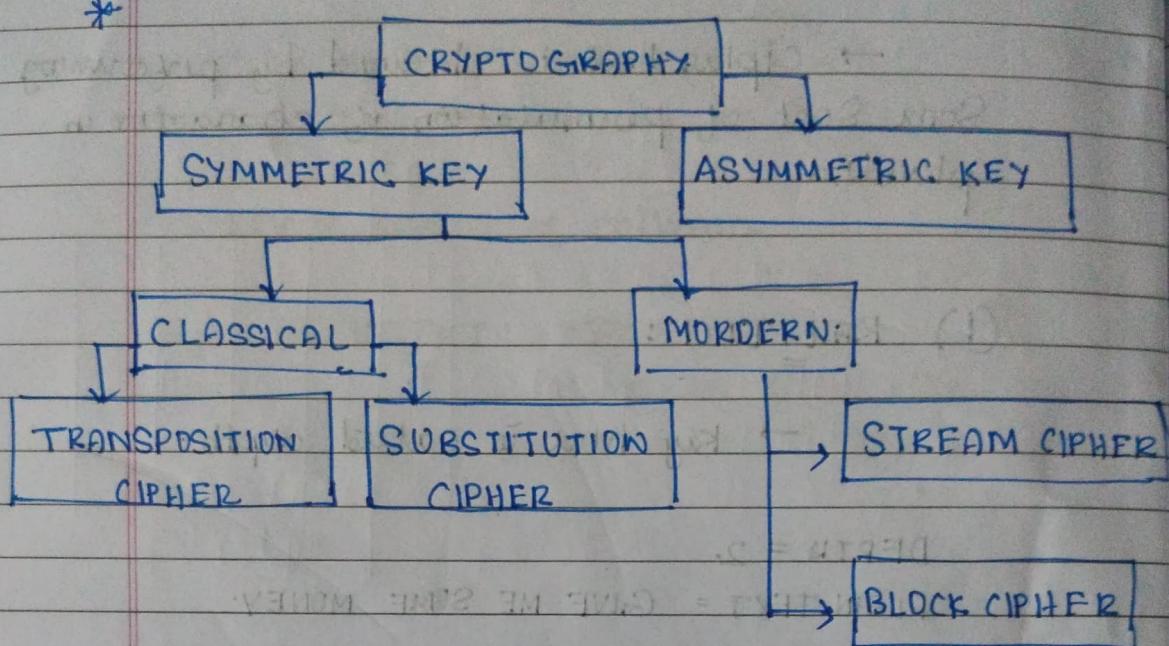
(ii) VIGENÉR (P)

Normal and Auto Key

④ PLAYFAIR CIPHER (P)

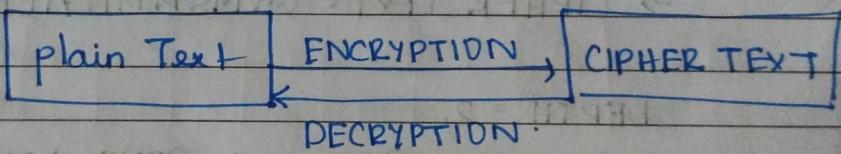
* ⑤ HILL CIPHER (P)

* ⑥ ONE TIME PAD

CRYPTOLOGY

* Plain Text \Rightarrow Original message

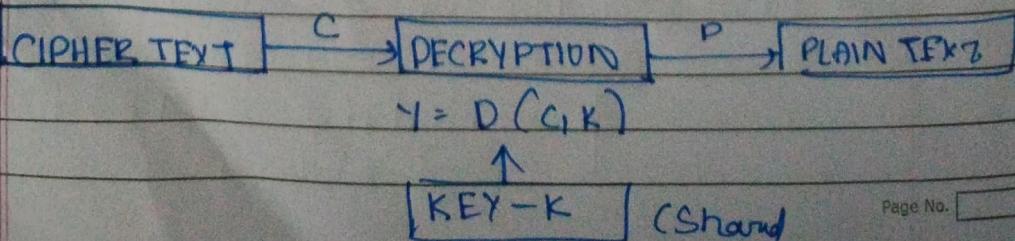
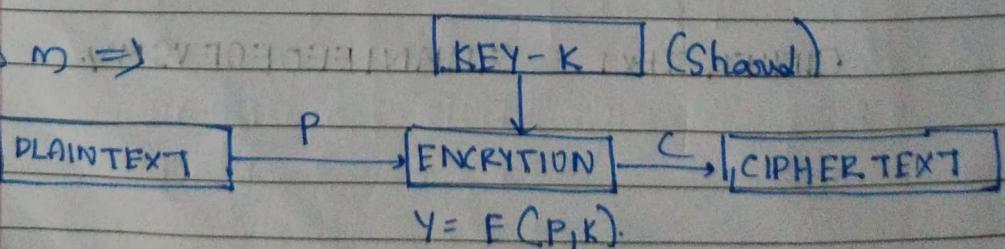
* cipher Text \Rightarrow coded / modified / encrypted message



\Rightarrow SYMMETRIC CIPHER MODEL / SYMMETRIC CRYPTOGRAPHY

\rightarrow Both Sender and Recipient Share a Secret Key.

Mechanism \Rightarrow



* TRANPOSITION TECHNIQUE:

→ Cipher text is obtained by performing some sort of permutation of characters in plaintext.

(i) RAIL FENCE:

→ Key here is called depth.

DEPTH = 2.

PLAIN TEXT = GIVE ME SOME MONEY.

G	V	M	.	S	M	M	N	Y
I	E	E	O	E	O	E		

⇒ CIPHER TEXT = GIVMSMMNYIEEDEOE.

DEPTH = 2.

PLAIN TEXT = GIVE ME SOME MONEY.

G	M	M	N
I	E	E	O
V	S	M	Y

CIPHER TEXT = GMMNIEEEOFEOEVSMY.

(ii) ROW-COLUMN:

- plain text written row by row
- Read column by column.

KEY ⇒ order of columns

Eg: PLAINTEXT: ~~WANT YOU~~

GIVE ME SOME MONEY AS

SOON AS POSSIBLE

1	2	3	4	5
G	I	V	E	M
E	S	O	M	E
M	O	N	E	Y
A	S	S	O	O
N	A	S	P	D
S	S	I	B	L
F	A	B	C	D

KEY: 4 3 1 2 5

⇒ CIPHER TEXT: EMEOPBCVONSISBGEMONSE
ISOSASAMEYDOLD.

→ This cipher text can again be feeded into the above matrix and can be encrypted again ⇒ increase complexity

Main types of Symmetric Encryption are

- ① Substitution Cipher 2 Classic Methods
- ② Transposition Cipher.

* SUBSTITUTION TECHNIQUE:

→ Letters of plaintext are replaced by some other letters.

\downarrow
Substituted by cipher text value

(i) CAESER CIPHER:

→ Shift characters in a plaintext by K characters.

i.e.	A	B	C	D	E	F	G	H	I	J	K	L
	0	1	2	3	4	5	6	7	8	9	10	11

M	N	O	P	Q	R	S	T	U	V	W	X
12	13	14	15	16	17	18	19	20	21	22	23

Y	Z
24	25

Eg : AFTER $K=3 \Rightarrow DIWHU$
 $K=1 \Rightarrow BGUFS$

\Rightarrow Encryption Function = ~~$CD=CBQR, CR=(PQ+K) \bmod 26$~~

$$C = E(P, K) = (P + K) \bmod 26$$

→ Shifting back by K characters will give the plaintext

$$P = D(C, K) = (C - K) \bmod 26$$

→ only 25 possible key values ($1 \div 25$)
i.e. Key Space is very small So easy to Brute Force.

(ii) MONO ALPHABETIC CIPHER:

→ increases the Key Space dramatically when compared to Caesar cipher (25 to $26!$).

→ achieved by using permutation of characters (A-Z)

\downarrow
N! permutations for N chars

→ A B C D E F G H I J K L M N O P Q R S T
→ D E F G H I J K L M O N P Q R S T U V X

→ V W X Y Z

W Y Z C B A

Eg: AFTER \Rightarrow DIXHV

→ can be cracked by analysing the frequency of characters in cipher text (by comparing to Standard character frequency).

(iii) PLAYFAIR CIPHER:

- multi-letter encryption cipher
- uses a 5×5 matrix of letters constructed using a Keyword

KEY = "MONARCHY"

→ Int Fill Key, Repeat
 When should we
 Skipped, then fill
 remaining with A-Z
 again repeats should be skipped.

M	D	N	A	R
C	H	Y	B	D
E	F	G	I/J	K
L	P	Q	S	T
U	V	W	X	Z

Encryption Steps: (group letters as pair)

- ① if repeating letters in plaintext
 Separate them with 'x' \Rightarrow i.e. both same in pair

Eg: BALLOON \Rightarrow BA LLO OON X
 BA LX LD OON

- ② if Both letters in a pair are in same row, each letter will be replaced by next character in cyclic manner

Eg: OR \Rightarrow NM , MN \Rightarrow OA (Same row)

OF \Rightarrow HP , GW \Rightarrow QN (Same col)

- ③ otherwise replace by same row and column of other letter.

Eg: EW \Rightarrow GV , FX \Rightarrow JV / JV

Date _____ / _____ / _____

→ The pair of letters in the plain text
is called digrams

→ Used during World War I and II

Eg: KEY = "TONYSTARK"

PLAINTEXT = "ENCRYPTION"

T	O	N	Y	S
A	R	K	B	C
D	E	F	G	H
I/J	L	M	P	Q
U	V	W	X	Z

EN CR YP TI DN

FD AK BX AV NY

⇒ CIPHER TEXT = "FDAK BX AVNY"

(iv) HILL CIPHER:

→ Also a multi-letter cipher.

→ Key used here will be a Square matrix of size $M \times M$.

Eg: ATTACK = plaintext, $K = \begin{bmatrix} 17 & 17 & 5 \\ 91 & 18 & 21 \\ 2 & 2 & 19 \end{bmatrix}$

⇒ Take 'M' characters
from plain text.

$$ATT = [0, 19, 19]$$

$$\Rightarrow \begin{bmatrix} 0 & 19 & 19 \end{bmatrix} \begin{bmatrix} 17 & 17 & 5 \\ 21 & 18 & 21 \\ 2 & 2 & 19 \end{bmatrix} = \boxed{[] \bmod 26}$$

$$\Rightarrow \begin{bmatrix} 0 \times 17 + 19 \times 21 + 19 \times 2, 0 \times 17 + 19 \times 18 + 19 \times 2, 0 \times 5 + 19 \times 21 + 19 \times 19 \end{bmatrix} \bmod 26$$

$$= \begin{bmatrix} 437 & 380 & 760 \end{bmatrix} \bmod 26$$

$$= \begin{bmatrix} 21 & 16 & 6 \end{bmatrix} \Rightarrow \boxed{ATT = VQG}$$

$$ACK = [0 \ 2 \ 10]$$

$$\Rightarrow \begin{bmatrix} 0 & 2 & 10 \end{bmatrix} \begin{bmatrix} 17 & 17 & 5 \\ 21 & 18 & 21 \\ 2 & 2 & 19 \end{bmatrix} \bmod 26$$

$$= \begin{bmatrix} 0 \times 17 + 2 \times 21 + 10 \times 2, 0 \times 17 + 2 \times 18 + 10 \times 2, 0 \times 5 + 2 \times 21 + 10 \times 19 \end{bmatrix} \bmod 26$$

$$= \begin{bmatrix} 62 & 56 & 232 \end{bmatrix} \bmod 26$$

$$= \begin{bmatrix} 10 & 4 & 24 \end{bmatrix} \Rightarrow \boxed{ACK = KEY}$$

$$\Rightarrow \boxed{CIPHER\ TEXT = VQGKEY}$$

\Rightarrow Decryption is done by computing inverse of K

[LEARN THIS]



Date _____ / _____ / _____

→ If key matrix is $N \times N$, then we can encrypt N characters at a time.

$$\begin{bmatrix} C_1 & C_2 & C_3 \end{bmatrix} = \begin{bmatrix} P_1 & P_2 & P_3 \end{bmatrix} \begin{bmatrix} K_{11} & K_{12} & K_{13} \\ K_{21} & K_{22} & K_{23} \\ K_{31} & K_{32} & K_{33} \end{bmatrix} \mod 26$$

$$\Rightarrow C = PK \mod 26$$

→ Can we fill characters 'x' if ends went out of size?

DESCRIPTION $\Rightarrow C \times K^{-1} \mod 26$.

$$K^{-1} = \frac{1}{|K|} \text{ Adj } K. \quad |K| \quad (\text{matrix inverse})$$

$$\Rightarrow \begin{bmatrix} 17 & 17 & 5 \\ 21 & 18 & 21 \\ 2 & 2 & 19 \end{bmatrix}$$

$$= 17(18 \times 19 - 2 \times 21) - 17(21 \times 19 - 2 \times 21) + 5(21 \times 2 - 2 \times 18)$$

$$= 5100 - 6069 + 30$$

$$= -939 \implies -939 \mod 26$$

$$= -3 \mod 26 \Rightarrow 23$$

$$|K| = 23$$

① Find determinant of K.

$$|K| = |K| \text{ mod. } 26.$$

mod 26 for
both steps

if $|K| < 0 \Rightarrow$ divide $|K|$ by 26
(and ≥ 26) and write - remainder
↳ then just add

② Find adjoint.

$$K = \begin{bmatrix} 17 & 17 & 5 \\ 21 & 18 & 21 \\ 2 & 2 & 19 \end{bmatrix} \Rightarrow \begin{bmatrix} 17 & 17 & 5 & 17 & 17 \\ 21 & 18 & 21 & 21 & 18 \\ 2 & 2 & 19 & 2 & 2 \\ 7 & 17 & 5 & 17 & 17 \\ 21 & 18 & 21 & 21 & 18 \end{bmatrix}$$

$$18 \times 19 - 2 \times 21 \quad 2 \times 5 - 17 \times 19 \quad 17 \times 21 - 18 \times 5$$

$$21 \times 2 - 19 \times 21 \quad 19 \times 17 - 5 \times 2 \quad 5 \times 21 - 21 \times 17$$

$$21 \times 2 - 2 \times 18 \quad 2 \times 17 - 17 \times 2 \quad 17 \times 18 - 21 \times 17$$

$$\begin{bmatrix} 300 & -313 & 267 \\ -357 & 313 & -252 \\ 6 & 0 & -51 \end{bmatrix} \xrightarrow{\text{mod 26}} \begin{bmatrix} 300 & -313 & 267 \\ -357 & 313 & -252 \\ 6 & 0 & -51 \end{bmatrix}$$

$$\text{Adj } K = \begin{bmatrix} 14 & 25 & 7 \\ 19 & 1 & 8 \\ 6 & 0 & 1 \end{bmatrix}$$

Date _____ / _____ / _____

$$\Rightarrow |K| = 23 \quad \text{ADJ}(K) = \begin{bmatrix} 14 & 25 & 7 \\ 7 & 1 & 8 \\ 6 & 0 & 1 \end{bmatrix}$$

~~for more details~~

\Rightarrow NUMBER THEORY NEEDED
BADLY : (.)

(v). POLYALPHABETIC CIPHER (VIGENIER CIPHER):

- Single letter cipher.
- uses Caesar cipher principle

Eg:

KEY = "ATTACK"

PLAIN TEXT = "GIVE MONEY"

P.T	G I V E M O N E Y
K	A T T A C K A T T
AT	

Enc	P.T	6	8	21	4	12	14	13	4	24
	KEY	0	19	19	0	2	10	0	19	19
	C.T	6	1	14	4	14	24	13	22	17

\Rightarrow CIPHER TEXT = GIBOE ■ OYNWR.

Dec.	C.T	6	1	14	4	14	24	13	22	17
	K	0	19	19	0	2	10	0	19	19
	P.T	6	8	21	4	12	14	13	4	24

→ Auto Key Systems : Having the same key repeated can be vulnerable.
So after 1st occurrence of key concat plain text & key.

i.e.) KEY = ATTACK → ATTACK GIV

PLAINTEXT = GIVE MONEY

(vi) POLYALPHABETIC CIPHER (VERNAME CIPHER).

- works using binary Bits
- Key as long as plain text (Very long but repeating after some point)

$$C_i = P_i \oplus K_i$$

(XOR)

$$P_i = C_i \oplus K_i$$

(vii) ONE-TIME PAD CIPHER:

P	E	S	M	S	A	R	S	I	F	N	L
S	E	S	O	G	S	O	N	S	I	S	S
E	S	S	N	S	N	N	I	A	S	S	S

INITIAL STATE = WAIT, FINISH

DATA PLAIN TEXT