

Sub Code: CS6104

Reg No: 2019503519

Sub Name: Data structures and  
Algorithms

Name: Hemanth N

## Q1.) KMP - Knuth Morris Pratt Algorithm

KMP algorithm is a linear time algorithm for string matching problems. Naive algorithm for pattern matching, where by window window we move has a time complexity  $O(m(n-m+1))$  in worst case. But KMP algorithm has  $O(n)$  in the worst case. Major disadvantage of Naive algorithm is it doesn't work if many matching characters are followed by a mismatching character.

The above disadvantage is overcome by KMP algorithm. Here, whenever we detect a mismatch after some matches, we already know some of the characters in the text of the next window, so we avoid matching characters that we know will anyway match.

④ Prefix function: It for pattern ~~text~~ - how the pattern matches against shift of itself. This is used to avoid useless shift of the pattern.  
④ KMP matcher: With string & pattern, Prefix function & as inputs, the occurrence of pattern in string and returns no of shifts in pattern after which occurrence is found.

So, the basic problem statement would be given a string  $s_1$  and  $P$ , ( $P \in S$ ), find all occurrences of  $P$  in  $s_1$ .

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Simple Pseudo code for Prefix function: Takes  $O(m)$  time

$m \leftarrow \text{length}[P]$       || P is pattern to be matched  
 $\pi[i] \leftarrow 0$   
 $k \leftarrow 0$   
For  $i \leftarrow 1$  to  $m$   
do while  $k > 0$  and  $P[k+i] \neq P[i]$   
do  $k \leftarrow \pi[k]$   
if  $P[k+1] = P[i]$   
then     $k \leftarrow k+1$   
 $\pi[i] \leftarrow k$   
Return  $\pi$

For example,

Pattern is abc d abc

Prefixes  $\rightarrow$  a, ab, abc, abcd,  
suffix  $\rightarrow$  c, bc, abc, abc

(abc - prefix & suffix  
match)

computing  $\pi$ :

say,  $P_1 = ab\underset{0}{c}\underset{0}{d}\underset{0}{a}\underset{1}{b}\underset{2}{a}\underset{2}{b}f$

$\downarrow$  (values)

Let us take a proper example,

P: a b a b a c a

0 0 1 2 3 0 1  $\rightarrow \begin{cases} \pi[3]=1 \\ \pi[4]=2 \\ \pi[5]=3 \end{cases}$  (This is precomputed KMP matching)

Example: T is b a c b a c b a b a b a c a c a  
P is a b a b a c a

P a b a b a c a  
0 0 1 2 3 0 1

Comparing using KMP matching

T: b a c b a b a b a b a c a a b } i & i+1 compare  
P: a b a b a c }

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Comparing  $i$  and  $j+1$ , if it match,

move  $i$  and  $j$

If mismatch, move  $j$  to the index of  $b$   
 $j$  only moves  
 $i$  doesn't move

T: b a c b a b a b a c a a b  
P: a b a b a c a

Backtrack on P

$P[1] \neq T[3]$

$i=4 \Rightarrow j=0$

$P[1]$  doesn't match with  $T[4]$

$A + i = 7 \Rightarrow P[2] = T[7]$

a b

, try going on,

[a b a b a c a]

matches from

$T[7]$  to  $T[13]$

$\therefore$  Total shifts is 6 shifts

Time complexity as analyzed above is linear

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Algorithms13.) Infix to Postfix conversion:

The algorithm is to use a stack to temporarily hold operators and left parenthesis. we begin by pushing a left parenthesis onto stack and adding a right parenthesis at end.

Basic Algorithm: (Infix expr x)

- ① Push "(" onto stack and add ")" at end of x.
- ② Scan x from left to right and Repeat steps 3 and 6 for each element  $\in x$  until the stack is empty.
  - ③ If an operand is encountered, add it to y.
  - ④ If a left parenthesis is encountered, add to y.
  - ⑤ If operator is encountered,
    - (a) Repeatedly pop from stack and add y to each operator (on top of stack) which has same precedence
    - (b) Add operator to stack.
  - ⑥ If right parenthesis is encountered,
    - (a) Repeatedly pop from stack and add to y each operator (on top of stack) until a left parenthesis is encountered.
    - (b) Remove the left parenthesis
- ⑦ END.

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Example :

$A + (B * C - (D / E \uparrow F) * G) * H$  to Postfix

Symbol scanned

Symbol scanned	Stack	Expression Y
A	(	A
+	(+	A
(	( +	A
B	( + C	A B
*	( + C (	A B C
C	( + C ( *	A B C *
-	( + C ( *	A B C *
(	( + C ( -	A B C *
D	( + C ( - (	A B C *
/	( + C ( - ( /	A B C *
E	( + C ( - ( / E	A B C *
\uparrow	( + C ( - ( / E \uparrow	A B C *
F	( + C ( - ( / E \uparrow F	A B C *
)	( + C ( - ( / F )	A B C *
*	( + C ( - ( / F ) *	A B C *
G	( + C ( - ( / F ) * G	A B C *
)	( + C ( - ( / F ) * G )	A B C *
*	( + C ( - ( / F ) * G ) *	A B C *
H	( + C ( - ( / F ) * G ) * H	A B C *
)	( + C ( - ( / F ) * G ) * H )	A B C *

Answer : ABC \* DEF ↑ / G \* - H \* +

Postfix

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12.) Algorithm to insert a node X after Y (given), In DLL having  
pointer p to first node .

```
struct Node {  
    int data;  
    struct Node * prev;  
    struct Node * next;  
}
```

Pointer p pointing  
to first node  
(head)

Node \* head = p;

Inserting New-data after  $\Rightarrow$  Y .

```
Void ins_node_after_y (struct Node * Y, int new_data)
```

Algorithm :

- ① Start
- ② Check whether Node Y is null (i.e) ( $Y == \text{NULL}$ )
- ③ If yes, Print the given node can't be null as error message and exit.
- ④ Node is created for insertion
- ⑤ Put the data in New Node

New-node  $\rightarrow$  data = new-data;

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⑥ Make next of new-node as next of Y

new-node → next = Y → next

⑦ Make next of Y as new-node

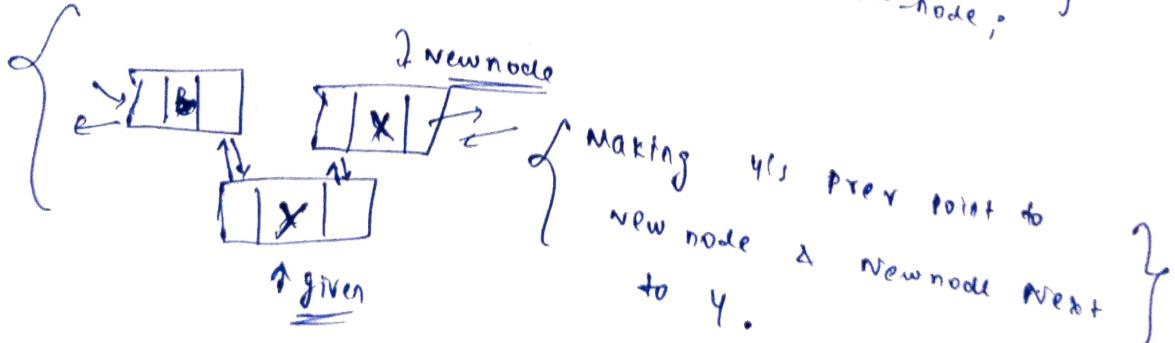
Y → next = new-node

⑧ Make Y as previous of new-node

new-node → prev = Y,

⑨ Previous of new-node's next node as newnode.  
} If (new-node → next != NULL)  
new-node → next → prev = new-node;

⑩ END.



Void Insert after Y (node \*n, int d)

{ node \*temp;

temp = new node();

temp → data = d; temp → prev = n;

temp → next = n → next; n → next = temp;

If (newnode == NULL) cout << "Error";

Pseudo code

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#### Inorder and Preorder of Binary Trees:

##### Inorder:

- ① Traverse the left subtree
- ② Visit the root
- ③ Traverse the right subtree
- ④ Repeat until all nodes are visited

Void Inorder ( struct Node \* node )  
{

    if (node == NULL)  
        return;

    Inorder (node->left); // recur on left child

    cout << node->data << " "; // print data on node

    Inorder (node->right); // recur on right child nodes

##### Preorder:

- ① Visit the root
  - ② Traverse Left subtree
  - ③ Traverse Right subtree
- & repeat till nodes are visited.

Void Preorder ( struct Node \* node )  
{

    if (node == NULL)  
        return;

    cout << node->data << " "; // print data in node

    Preorder (node->left); // recur on left child

    Preorder (node->right); // recur on right child

```
struct Node {  
    int data;  
    struct Node *left,  
                *right;  
};  
Node (int data)  
{  
    left = data = right = NULL;  
}
```

g,

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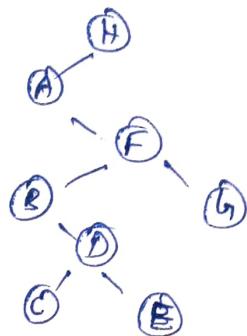
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Preorder of the tree is

[H A F B D C G E]



The node H is first visited,  
Then left subtree & then the Right subtree

Inorder of the tree is

[A B C D E F G H]

|| The left child nodes are first visited, then node,  
and then the right node is visited.

17) Longest common subsequence is basically the longest  
subsequence common to the strings given. It must  
strictly be a increasing sequence.

A B A C D

A B A , A A C , A A D are subsequences

but A C A is not a subsequence.

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LCS using Dynamic Programming is a

Bottom up approach.

A: a c d b c e

B: a b c b f e

Basic Pseudo code is

If ( $A[i] = B[j]$ )

$LCS[i, j] = 1 + LCS[i-1, j-1]$   
else

$LCS[i, j] = \max(LCS[i-1, j], LCS[i, j-1])$

	0	a	b	c	b	f	e
0	0	0	0	0	0	0	0
a	0	1	1	1	1	1	1
b	0	1	2	2	2	2	2
c	0	1	2	2	3	3	3
d	0	1	2	2	3	3	3
b	0	1	2	2	3	3	3
e	0	1	2	2	3	3	4

Follow the arrows  
if diagonal  $\Rightarrow$  include  
in sequence

Length of LCS is 4

a b c e

Following the arrows, we get LCS as a b c e

## (b) Greedy Method : Knapsack Problem

Basically we must,

$$\begin{array}{l} \text{maximize } \sum_{i \in S(n)} p_i x_i \\ \text{subject to } \sum_{i \in S(n)} w_i x_i \leq M \\ \text{and } 0 \leq x_i \leq 1, i \in S(n) \end{array}$$

Given problem,

Knapsack capacity = 50

Item      Profit      Weight

	Profit	Weight	Profit per weight
1	100	20	
2	80	30	5 ( $100/20$ )
3	110	10	2.67 ( $80/30$ )
4	95	40	11 ( $110/10$ )
			2.38 ( $95/40$ )

(i) Add item 3 (weight=10)       $\underline{\underline{\text{max profit per weight}}}$

$$\text{Rem: } 50 - 10 = 40$$

(ii) Add item 1 (20)

$$\text{Remaining is } 40 - 20 = 20$$

(iii) Add  $\underline{\underline{\text{item 2}}}$ . Part of it,  $20 - \frac{2}{3}(20) = 0$

$$(1, 2(3, 1, 0))$$

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Solution obtained is  $(1, 2, 3, 1, 0)$

$$\text{Total Profit} = \sum p_i x_i$$

$$= (x_{100} + \frac{2}{3}x_{80} + 1x_{110} + 0x_{95})$$

$$= 100 + 53.83 + 110 + 0 = 263.33$$

Total Profit = 263.33

$$\text{Total weight filled} = \sum w_i x_i$$

$$= 20(1) + 30(2) + 10(1) + 40(0)$$

50

*(exact capacity &  
exceed filled)*

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### (9.) Heap sort:

- ① Build a max heap.

with last item of heap followed by reducing the size of heap by 1. Heapify the root of tree

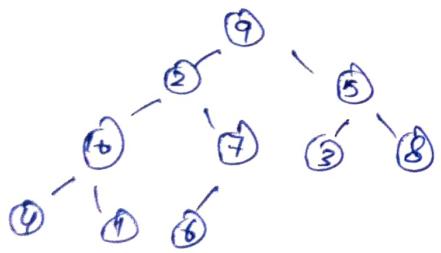
- ② Repeat ① until size of heap is > 1.

Heapification is performed in Bottom up Order.

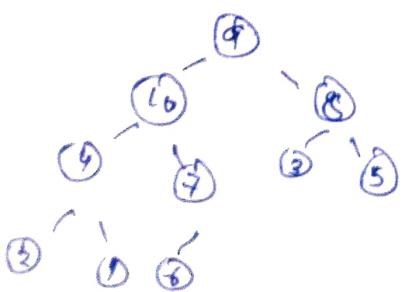
Time complexity of heap sort is

$$\Theta(n \log n)$$

9, 2, 5, 10, 7, 3, 8, 4, 1, 6



(Building Max)



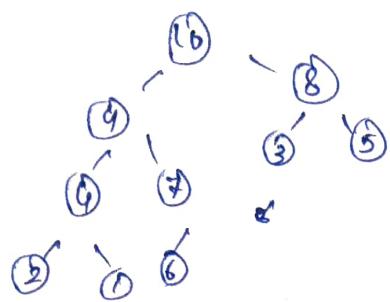
10 is larger than 2 & 4  
∴ (the following heap)

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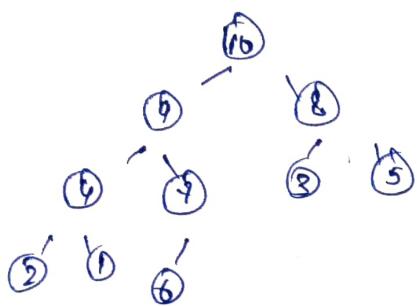
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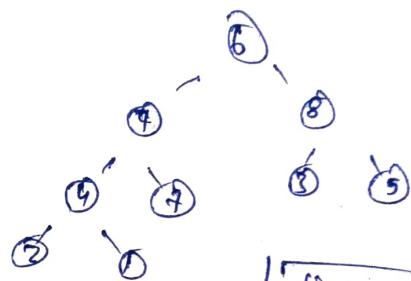


$10 > 9$

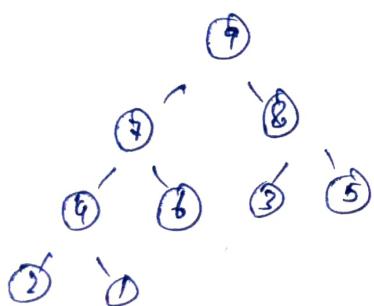
( $\therefore$  Step 1:  
This is the  
heap at  
this step)



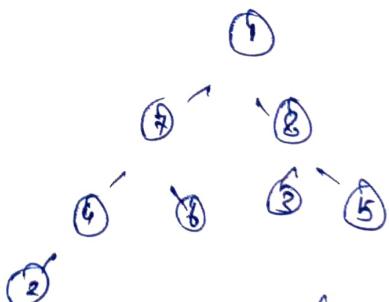
→



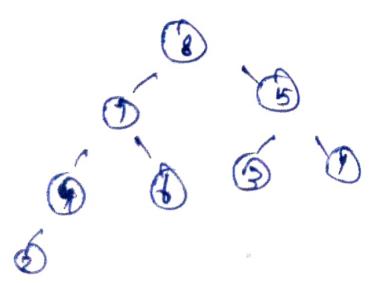
Step 2 heap  
reduced by 1



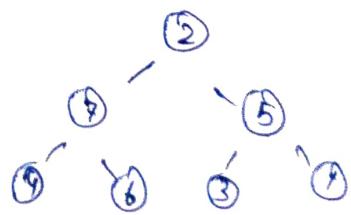
→



(The  
element  
is 1)



→



(Step 6 heap reduced by 1)

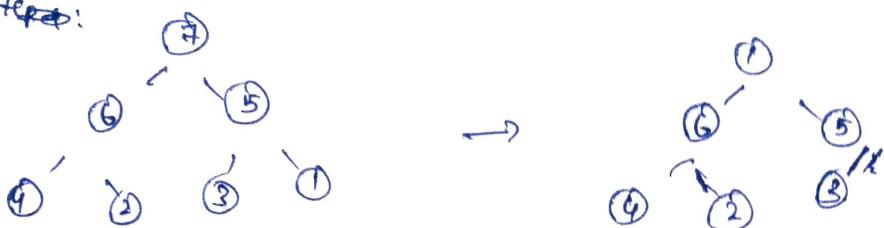
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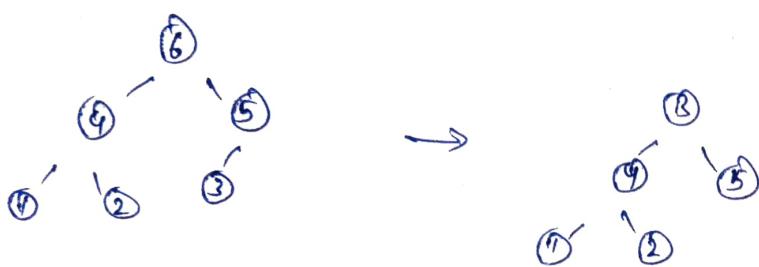
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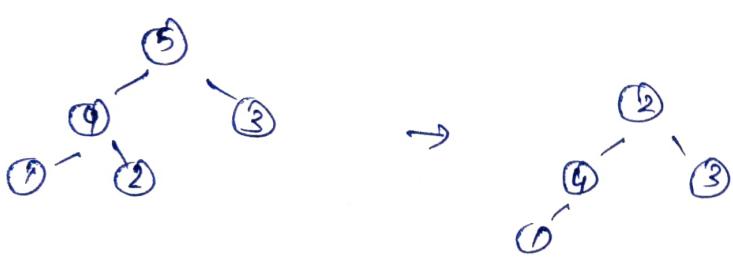
Step 1:



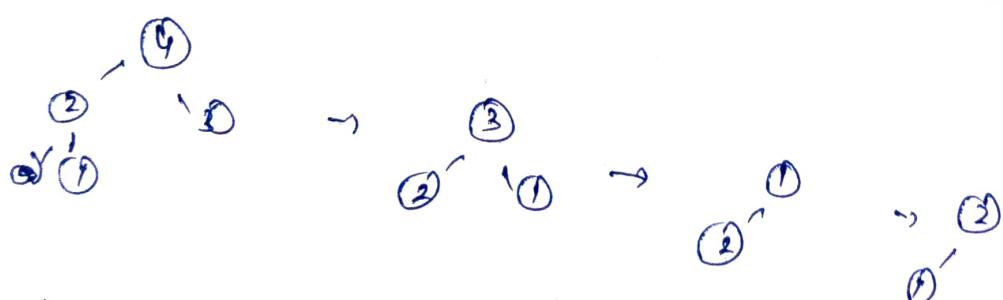
(Heap at each step is being shown)



(According to step 2,  
the size is reduced)



(Size of heap  
reduced)



Last step, 1 will remain,

∴ The sorted Order is (increasing) out of heap sort

1	2	3	4	5	6	7	8	9	10
---	---	---	---	---	---	---	---	---	----

Heap at each step each to show property

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Qn.) When there are more number of elements, say  $n$ ,  
collision occurs in hash function when it produces  
the same value for more than one element.

If there is more than one element then no. of cells,  
there might be high probability that 2 values might be  
placed in same cell of hash table.

There are many methods to reduce collision.

Open addressing → Linear Probing

Quadratic Probing, etc.,

Collision can be reduced in

$$\lambda = N/r$$

$N$  = no. of elements,  $r$  = table size

$\lambda$  = load factor.

Method: Linear Probing → open addressing method,

If a cell is filled or then value will be stored in  
next empty cell.

(This is also called Closed Hashing)

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Example,

Consider a hash function,  $h(x) = x \mod 10$  then 10, 20 occupy same place, after this as

$$h_i(x) = (\text{Hash}(x) + b_i) \mod 10$$

$b_i$  is index of Hash table array

Load factor must be below 5.

Assume series

19, 28, 39, 24, 48, 9  
19 is inserted at 9th index.

28 is inserted at 8th index  $\Rightarrow$  [   |   |   |   |   |   |   |   | ]  
0 .. 9

39  $\mod 10 \neq 9$ , already filled

$$h(39) = (9+1) \mod 10 \Rightarrow 0$$

$\Rightarrow$  [   |   |   |   |   |   |   |   | ]  
0 .. 8 9  
39 | 28 | 19

Take 48, again 8th index is filled

$$8+1 = 9$$

$\Rightarrow$  also filled

$$8+2 = 10 \mod 10 = 0 \Rightarrow \text{also filled}$$

$$8+3 = 11 \mod 10 = 1 \Rightarrow \text{not filled}$$

$\Rightarrow$  [   |   |   |   |   |   |   |   | ]  
0 .. 8 9  
39 | 48 | ... | 28 | 19

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Again take q,

Now, 111y, q, 0, are filled,

$\therefore (q+3) + 10 = 2$  is where q will be filled.

$\therefore$  ~~48~~

39	48	9	1	1	1	1	28	19
0	1	2	3	...	8	9		

$\therefore$  Total Probe  $\Rightarrow$  39  $\rightarrow$  1,  
48  $\rightarrow$  4      9  $\rightarrow$  4

~~totaly 9 probes~~

Hence, this way, collision is avoided.

Linear probing method, with a example is  
explained properly.

Other Methods, like

Open Hashing, Quadratic Probing, Double Hashing etc. also  
reduce the collision in Hash Tables.

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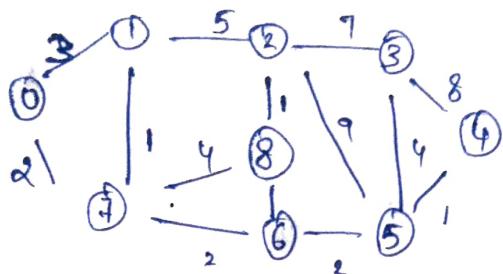
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Q4)

### PART-C

Kruskal Method:



First step is to sort them in decreasing order of weight

A	$\rightarrow$	B	Weight
1		7	1
2		8	1
4		5	1
0		7	2
7		6	2
6		5	2
0		1	3
7		8	4
3		5	4
1		2	5
8		6	6
2		3	7
3		4	8
2		5	9

Basically, a MST  
will have (no of vertices - 1)  
edges.

$\therefore$  8 edges in our  
final MST

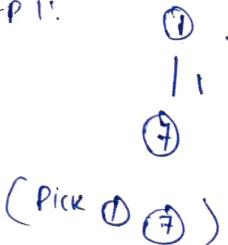
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Sub name : Data structures and  
AlgorithmsKruskal Algorithm:

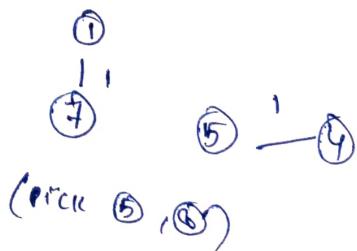
- ① Sort all the edges in non-decreasing order of their weight.
- ② Pick the smallest edge. Check if cycle is formed.
- ③ In case, no cycle is formed, include that edge in graph.
- ④ If cycle is formed, discard that edge.
- ⑤ Repeat the above 2 steps until  $(V-1)$  edges are in spanning tree.

Solving the question,

Step 1:



x:



Step 3:



The edges are picked and included, since it doesn't form a cycle.

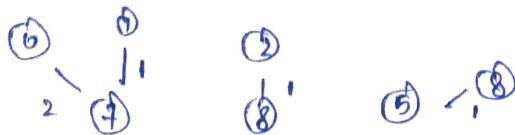
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Step 4:



PICK

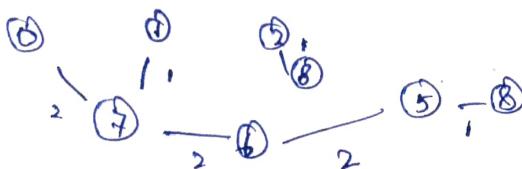
( $6 \rightarrow 2$ )

Step 5:



(These edges  
are all included  
since it doesn't  
form a cycle)

Step 6:

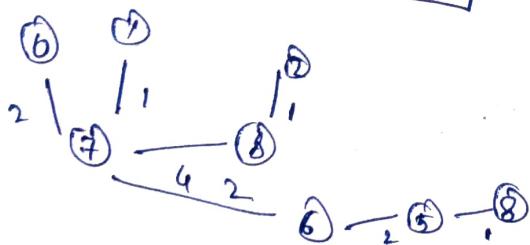


PICK ( $6 \rightarrow 5$ )

[including 0-1 will form a cycle]

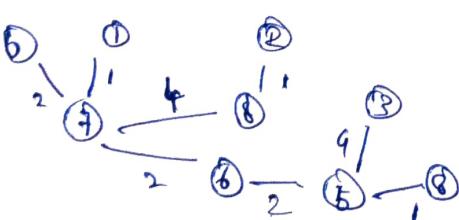
thus discarded

7:



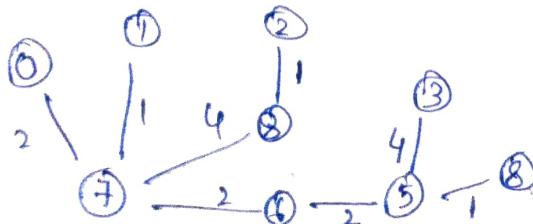
Picking ( $7 \rightarrow 8$ )  
(not form cycle)

8:



Picking ( $5 \rightarrow 3$ )  
(not form cycle)

Thus, the final MST has 8 edges



→ [MST using Kruskal algorithm]

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Q3.)

$$T(n) = 4T(n/2) + n \quad ; \quad n > 1, T(n) = 1, n = 1$$

Substitution Method:

$$T(n) = 4T(n/2) + n \rightarrow ①$$

when  $n = n/2$  condition,

$$\Rightarrow T(n/2) = 4T(n/4) + n/2 \rightarrow ②$$

$$T(n) = 4(4T(n/4) + n/2) + n \rightarrow ③$$

$$= 16T(n/4) + 3n \quad (\text{Sub } ② \text{ in } ①)$$

$$n = n/4 \quad \rightarrow ④$$

$$T(n/4) = 4T(n/8) + n/4 \rightarrow ⑤$$

Sub ④ in ⑤

$$\begin{aligned} T(n) &= 4(16(4T(n/8) + n/4) + n) + 3n \\ &= 64T(n/8) + 4n + 3n \\ &= 64T(n/8) + 7n \end{aligned}$$

$$T(n) = 64T(n/8) + n + 2n + 4n$$

We observe a series,

$$\{4^3 T(n/2^3) + n + 2n + 4n \dots\}$$

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$\therefore T(n) \in \Theta(4^k)$

$$\begin{aligned}T(n) &= 4^k (1 + n(1+2+4+\dots+k)) \\&= 2^{2k} + n(1+2+4+\dots+k) \quad \text{--- (5)}\end{aligned}$$

$$2^k = n \quad \therefore$$

$$k = \log_2 n \quad \text{--- (6)}$$

Sub (6) in (5)

$$\begin{aligned}T(n) &= n^2 + n(1+2+4+\dots+k) \\&= O(n^2)\end{aligned}$$

$$\begin{aligned}T(n) &= n \left( 2^{\frac{\log_2 n}{2} - 1} + 4^{\log_2 n} \right) \\&= O(n^2)\end{aligned}$$

$\therefore$  By substitution method,  $T(n) = O(n^2)$

Master Method:

$$f(n) = n$$

$$a = 4, b = 2$$

$$n^{\log_b a - \epsilon}$$

$$n^{\log_2 4} = n^2 \log_2 2 = \underline{n^2}$$

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$$\underline{f(n) > n^2}$$

This is case (ii)

$$\therefore \text{So, } T(n) = O(n^{\log_6 9})$$

$$= O(n^{\log_2 4})$$

$$= O(n^2)$$

$\therefore$  [By Master's Method,  $T(n) = O(n^2)$ ]

We observe that time complexity during both division  
& Master's method is same, i.e.,  $O(n^2)$ .

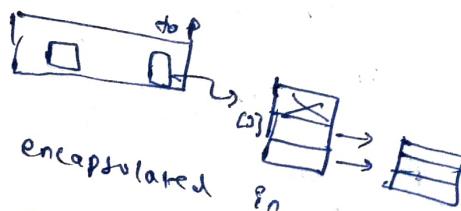
PART-A

1.)

Data abstraction basically means providing only the essential and relevant information ~~through~~ to the end user. It separates the specification of a datatype from its implementation.

For example, take Stack as a Abstract data type. Instead of data being stored in each node, the pointer to Data is stored.

Head node & data nodes are encapsulated in ADT. So, the user only needs to know what a datatype is and it can do, need not know how it is implemented.



d.) Queue is a linear data structure since elements ~~for~~ are linked in a sequential manner. It is a first In first Out data structure.

There can be only one descendant at any node, unlike Trees (more nodes connected to given node) which are non-linear. Since only one node is connected (and forms a sequence), queues are Linear data structures.

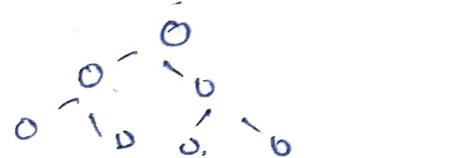
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3.) Min & Max no. of nodes in a Bin Tree of height k

$$\boxed{\begin{aligned} \text{Minimum} &= k+1 \\ \text{Maximum} &= 2^{k+1} - 1 \end{aligned}}$$



$$\text{Max is } 2^{k+1} - 1$$

$$2^{3+1} - 1 = \underline{\underline{15}}$$

$\rightarrow$  (Left skew tree is maximum)

$$k+1$$

4.) Time complexity of Naive string Matching

Given text  $\rightarrow (0, \dots, n-1)$

Given Pattern  $\rightarrow (0, \dots, m-1)$

$$n \times m$$

$$\boxed{\text{Worst case is } O(m \times (n-m+1))}$$

Avg Time Complexity of Naive Algo  $\rightarrow O(m \times n)$

(m is size of pattern)  
(n is size of string)

5.) No. of different spanning

tree with complete graph of n nodes

$$5 \text{ nodes} \Rightarrow 5^{5-2} = 5^3 = n^{n-2}$$

$$5^3 = 125 \text{ Different spanning trees}$$

4.) Divide and Conquer can't be applied to given problem.

- (i) Cannot be divided into subproblems
- (ii) cannot be recursively solved using subproblems
- (iii) Is not a combination of subproblem questions.

e.g.) Linear search cannot be solved using Divide & Conquer strategy since it involves traversal of the whole array.

Bubble sort is also not solved using Divide & Conquer since it involves traversing the whole array and bubbling the largest to stop.

- 6.)
- Divide & conquer is a top down approach while dynamic programming is bottom up approach.
  - Divide & conquer focuses more on sub-problems hence more time consumption, DP solves the sub problems only once, hence less time consumption.
  - Divide & conquer → subproblems are independent  
DP → subproblems → Interdependent

Divide & conquer → Merge Sort, Quicksort

DP → Matrix Chain Multiplication

7.) Bounding function is needed to kill the nodes without expanding. So for optimization, bounding function creates upper bound or lower bound on functions to tackle minimization or maximization problems.

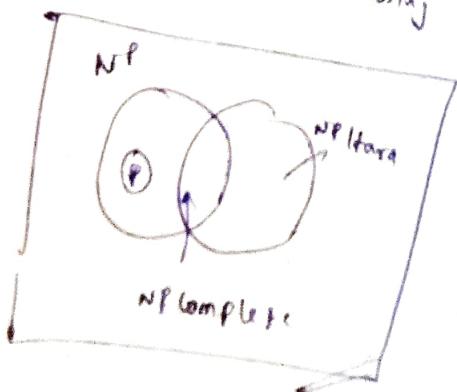
(a) NP is a set of problems for which problem instances where the answer is yes . two types :

NP Hard & <sup>NP</sup>Complete

NP Hard : All problems in NP are polynomial time reducible

NP Complete : If language is NP and is polynomially reducible

NP class contains problems that can't be solved in polynomial time using deterministic algorithms.



$$P \subset NP$$

$$\begin{aligned} & \text{Sat is in } P \\ & \text{if } P = N \end{aligned}$$

8)

Heap is a specialized tree-based data structure which is complete tree satisfying heap property.

Heaps can be implemented as an array, with each element representing a  $\text{ith}$  node of the heap.

Various types of Heap: Binary Heap, Radix Heap, etc..

Application of Heaps are:

Heap sort, Priority Queue, k-way Merge.

- (i) In a Max Heap, for any given node  $C$ , if  $P$  is parent node of  $C$ , then key of  $P \geq$  key of  $C$ .
- (ii) In min heap, the key of  $P \leq$  key of  $C$ .
- (iii) Node at top of heap is Root Node.

All the Answers in this Answer Book have been in my own handwriting. Nobody helped me in writing the answers.

25/06/21