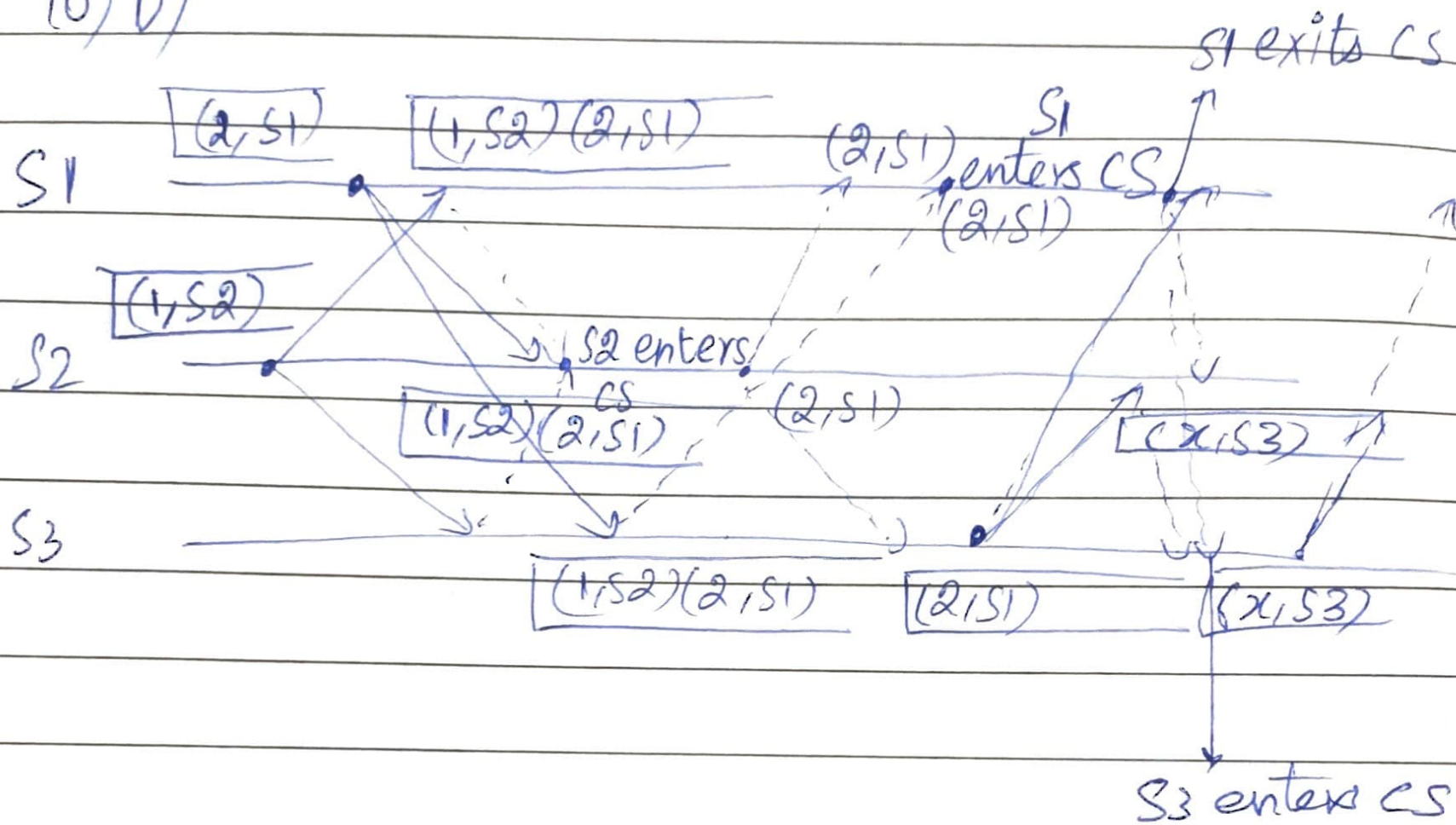


10) b)



How CS will be executed:

A site S_i will enter CS if

- i) S_i receives request with timestamps larger than itself
- ii) S_i 's request is at the top of request-queue.

So

S_2 will execute when S_1 's request timestamp is greater.

It already satisfies L2 because S_1, S_2 are the first ones wanting to execute the CS.

⇒ Once S_2 is done it will send release msg to other two sites.

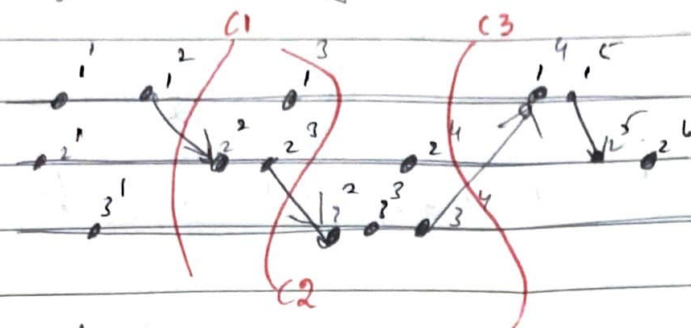
Even in this case, S_1 has requested CS before S_3 , so timestamp of S_1 is smaller ⇒ S_2 is executed

Finally after S_1 is done, it sends RELEASE msg. S_3 gets to enter the CS.

Order of execution

S_2, S_1, S_3

6. (ij)



a) Causal dependencies

$$e_1^1 \rightarrow e_3^3, e_3^3 \rightarrow e_2^6, e_3^1 \rightarrow e_2^6$$

$$e_1^3 \rightarrow e_2^6, e_1^1 \rightarrow e_2^4$$

Causal Precedence:

$$\forall e_i^x, \forall e_j^y \in H,$$

$$e_i^x \rightarrow e_j^y \Leftrightarrow$$

$$\left\{ \begin{array}{l} e_i^x \rightarrow e_j^y \text{ via } (i=j) \wedge (x < y) \\ e_i^x \rightarrow \text{msg } e_j^y \end{array} \right.$$

$$e_i^x \rightarrow \text{msg } e_j^y$$

$$\exists e_k^z \in H; e_i^x \rightarrow e_k^z \wedge e_k^z \rightarrow e_j^y$$

causal precedence:

all 5 satisfies, all 4 messages, events within same process

Concurrent relations

$$e_1^3 \parallel e_3^3, e_2^4 \parallel e_3^1, e_2^4 \parallel e_3^3$$

$$e_2^4 \parallel e_1^5, e_2^4 \parallel e_1^4, e_1^1 \parallel e_2^1,$$

$$e_1^1 \parallel e_3^1, e_2^1 \parallel e_3^1, e_1^3 \parallel e_2^3$$

b) Consistent global state

$$\left\{ \begin{array}{l} e_1^1, e_2^3, e_3^3 \\ \text{or} \\ e_2^4, e_3^3 \end{array} \right\} \quad \begin{array}{l} \text{Send } \checkmark \\ \text{Recr } \checkmark \end{array}$$

Sample global state

$$\{ LS_1^2, LS_2^3, LS_3^2 \}$$

$$\{ LS_1^2, LS_2^3, LS_3^3 \}$$

$$\{ LS_1^5, LS_2^6, LS_3^4 \} \quad \{ LS_1^5, LS_2^5, LS_3^4 \}$$

So for causal precedence, all 5 causal dependencies satisfy third condition.

By first condition: all events within a process

By second condition: all events \rightarrow msg
satisfy causal precedence.