ANALOG NCERT 12.8.11

EE23BTECH11046 - Poluri Hemanth*

Question: Suppose that the electric field part of an electromagnetic wave in vacuum given as
E ={(3.1N/C)cos[(1.8 rad/m)y+(5.4×10^{6}rad/s)t]}î
(a) What is the direction of propagation ?
(b) What is the wavelength ?
(c) What is the frequency ?
(d) What is the amplitude of the magnetic field part of the wave?
(e) Write an expression for the magnetic field part of the wave.

Solution:

Symbol	Values	Description
λ	3.5m	Wave length of E.M wave.
f	$0.859 \cdot 10^6 Hz$	Frequency of E.M wave.
c	$3 \cdot 10^6 m/s$	Velocity of propagation of E.M wave.
ω	$5.4 \cdot 10^6 rad/s$	Angular frequency of E..M wave.
k	$1.8 rad/m$	Wave number of E.M wave
B_o	$1.03 \cdot 10^{-6} T$	Amplitude of magnetic part of E.M wave
E_o	$3.1 N/C$	Amplitude of electric part of E.M wave.

TABLE I
PARAMETERS

(a)
As the wave is in form of cos(ky+wt) the wave is propagating along -y axis.
(b)

$$k = \frac{2\pi}{\lambda} \tag{1}$$
$$\Rightarrow 1.8 = \frac{2\pi}{\lambda} \tag{2}$$
$$\lambda = \frac{2\pi}{1.8} \tag{3}$$
$$\lambda \approx 3.5m \tag{4}$$

(c)

$$\omega = 2\pi.f \tag{5}$$
$$\Rightarrow 5.4x10^6 = 2.\pi.f \tag{6}$$
$$\Rightarrow f = 0.859 \times 10^6 Hz \tag{7}$$

(d)

$$B_o = \frac{E_o}{c} \tag{8}$$

where c is velocity of propagation of wave which is given by

$$c = \frac{\omega}{k} \tag{9}$$
$$c = \frac{5.4 \times 10^6}{1.8} \tag{10}$$
$$c = 3 \times 10^6. \tag{11}$$
$$B_o = \frac{3.1}{3 \times 10^6} \tag{12}$$
$$B_o = 1.03 \times 10^{-6} \tag{13}$$

(e)

$$\mathbf{B} = B_o cos(ky + wt)(-\hat{k}) \tag{14}$$
$$\mathbf{B} = 1.03 \times 10^{-6} T\{cos[(1.8 rad/m)y + (5.4x10^6 rad/s)t]\}(-\hat{k})$$

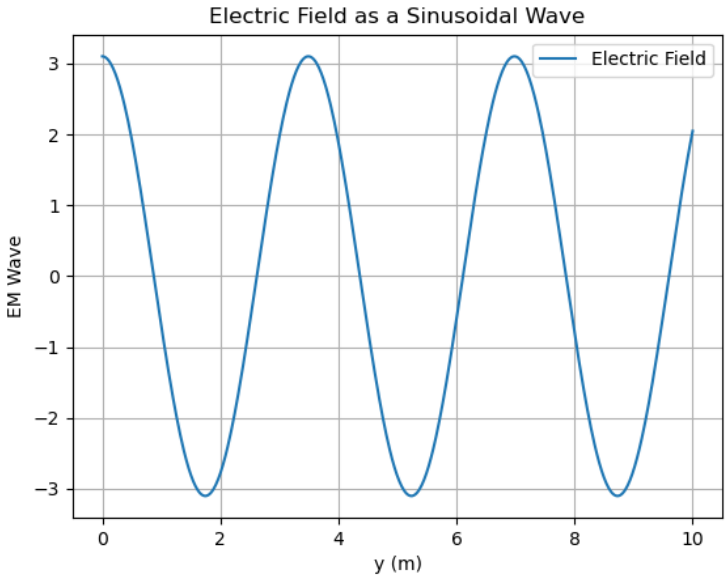

Fig. 1. Electric field part

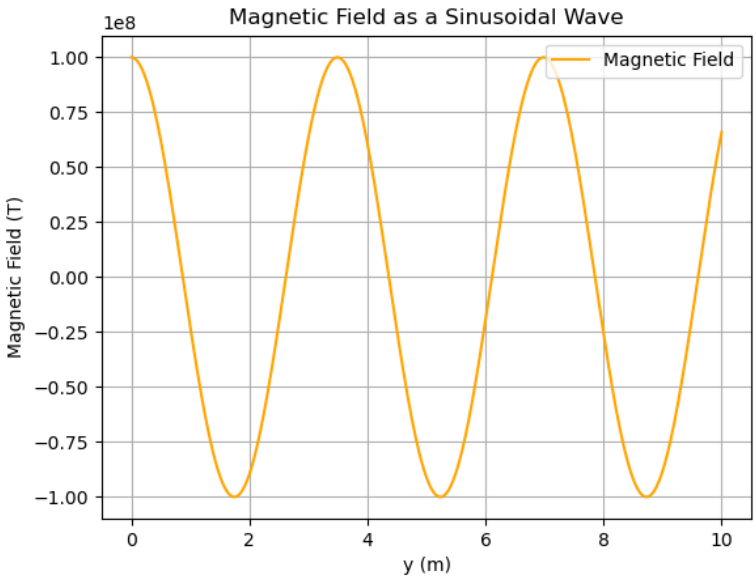

Fig. 2. Magnetic field part