1

NCERT DISCRETE 11.9.2.15

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If $\frac{a^n+b^n}{a^{n-1}+b^{n-1}}$ is A.M between According to Cauchy's Residue Theorm: then find value of n. For a v(n) such that **Question:** and **Solution:**

| S/No | Symbol | Values | Description |
|---------|--------------|--------------|-------------------------------------|
| 1 | <i>x</i> (0) | а | First term of A.P |
| 2 | x(1) | <u>a+b</u> 2 | A.M of first and third terms of A.P |
| 3 | x(2) | b | Third term of A.P |
| TABLE I | | | |

PARAMETERS

 $y(n) = \frac{1}{2\pi j} \oint Y(Z) dz$ (12) = $\sum_{i=1}^{N} RES(Y, a_k)$ [N is no of poles of Y(Z)] (13)

where

We represent a, b, A.M of those two in an A.P The general term of A.P used is x(n) = a + nd. where

 $RES(Y, a_k) = \frac{1}{(m-1)!} \lim_{z \to a_k} \frac{d^{m-1}}{dz^{m-1}} [Y(Z) \cdot (z - a_k)^m]$ (14)

From (8)

$$d = \frac{b-a}{k+1} \{k \text{ is no of A.M's inserted between } a, b\}$$

 $\Rightarrow x(1) = a + d$

 $x(1) = \lim_{z \to 1} \frac{a}{1 - z^{-1}} (z - 1) + \lim_{z \to 1} \frac{1}{1!} \frac{d}{dz} \left(\frac{d \cdot z^{-1}}{(1 - z^{-1})^2} (z - 1)^2 \right)$

(16)

(17)

$$d = \frac{b-a}{2}$$

$$(2) \Rightarrow x(1)$$

$$x(0) = a$$

$$x(1) = A.M$$

(6)

(9)

$$x(2) = b$$

$$x(1) = \frac{a+b}{2}$$

x(2) = b

From (6)

$$x(1) = \frac{x(0)^n + x(2)^n}{x(0)^{n-1} + x(2)^{n-1}}$$

$$\frac{x(0)^n + x(2)^n}{x(0)^{n-1} + x(2)^{n-1}} = \frac{x(0) + x(2)}{2}$$
 (18)

Convolution of x(n) with u(n) and their Z transform.

$$\Rightarrow x(0)^{n} + x(2)^{n} = x(2)x(0)^{n-1} + x(0)x(2)^{n-1}$$
(19)

$$x(n) * u(n) \stackrel{\mathcal{Z}}{\longleftrightarrow} X(Z)$$
 (7)

$$\Rightarrow x(0)^{n-1}(x(0) - x(2)) = x(2)^{n-1}(x(0) - x(2))$$
 (20)

$$X(Z) = \frac{a}{1 - z^{-1}} + \frac{dz^{-1}}{(1 - z^{-1})^2}$$
 (8)

$$\Rightarrow n \begin{cases} = 1 & \text{if } a \neq b \\ \in R & \text{if } a = b \end{cases}$$
 (21)

From contour integration method

$$x(n) = \frac{1}{2\pi i} \oint X(Z) z^{n-1} dz \tag{10}$$

$$\Rightarrow x(1) = \frac{1}{2\pi j} \oint X(Z) \, dz \tag{11}$$

solution of n using 3d plot

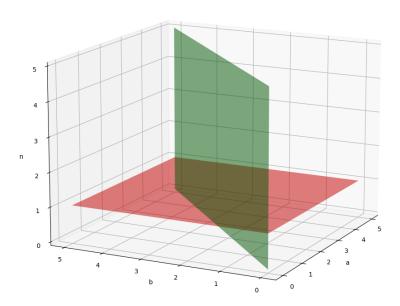


Fig. 1. Plot of n in planes