

end marker \$.

$LR(1)$ items = $LR(0)$ items + lookahead

How to add lookahead with the production?

Case 1: $A \rightarrow \alpha \cdot BC, \alpha$

Suppose this is old production.

Now it precedes B, so we have to write B's production as well

$B \rightarrow \cdot D$ [1st production]

The look ahead of this production is given as we look at previous productions i.e., old whatever is after B, we find first of that value after that is look ahead of 1st production.

assume $Fist(C) = d$,

$B \rightarrow \cdot D, d$

Case 2: Now if the old production

was like $A \rightarrow \alpha \cdot B, \alpha$

here after B there's nothing

after B so lookahead is

$B \rightarrow \cdot D, \alpha$

Case 3: Assume $A \rightarrow a/b$

$A \rightarrow a, \$$

$A \rightarrow b, \$$

Steps to construct CLR parsing table:

1. Writing augmented grammar.
2. LRD collection of items to be found.
3. Defining 2 functions: goto [list of terminals] and action [list of non-terminals]

CLR Parsing.

Ex: $S \rightarrow CC$ String = dd
 $C \rightarrow CC/d$

Step 1: Write the augmented grammar and LRD items.

$S' \rightarrow S^0$

$S \rightarrow \cdot CC^1$

$C \rightarrow \cdot CC^2$

$C \rightarrow \cdot d^3$

$I_0 \rightarrow S^1 \rightarrow \cdot S, \$$

$S^1 \rightarrow \cdot CC, \$$

$\cdot C \rightarrow \cdot CC, C/d$

$C \rightarrow \cdot d, C/d$

$\text{goto}(I_0, \delta) :$

$I_1 \rightarrow S' \rightarrow S, \emptyset$

$\text{goto}(I_0, C) :$

$I_2 \rightarrow S \rightarrow C.C, \emptyset$

$C \rightarrow \cdot C.C, C/d \emptyset$

$C \rightarrow \cdot d, C/d \emptyset$

$\text{goto}(I_0, C) :$

$I_3 \rightarrow C \rightarrow C.C, C/d$

$C \rightarrow \cdot C.C, C/d$

$C \rightarrow \cdot d, C/d$

$\text{goto}(I_0, d) :$

$I_4 \rightarrow C \rightarrow d, C/d$

$\text{goto}(I_0, C) :$

$I_5 \rightarrow S \rightarrow C.C., \emptyset$

$\text{goto}(I_2, C)$

$C \rightarrow C.C, \emptyset$

$I_6 - \left\{ \begin{array}{l} C \rightarrow \cdot C.C, \emptyset \\ C \rightarrow \cdot C.C, \emptyset \end{array} \right.$

$C \rightarrow \cdot d, \emptyset$

$C \rightarrow \cdot d, \emptyset$

goto (I_2, d):

If: $c \rightarrow d, \$$

goto (I_3, c)

$I_8 \rightarrow c \rightarrow cc., \$ / d$

goto (I_3, c)

$c \rightarrow c.c, c/d$

$c \rightarrow cc., c/d$

$c \rightarrow d, c/d$

goto (I_3, d)

$c \rightarrow d, c/d \rightarrow I_4$

goto (I_6, c)

$c \rightarrow cc., \$ \rightarrow I_9$

goto (I_6, c)

$c \rightarrow c.c, \$$

$c \rightarrow cc., \$$

$c \rightarrow d, \$$

goto (I_6, d)

$c \rightarrow d, \$ \rightarrow I_f$

Step 8: Construction of CCR Parse table.

	Terminal			Nonterminals	
	Action			goto	
λ_0	c	d	\$	S	C
I_0	s_3	s_4		I_1	I_2
I_1			Accepted		
I_2	s_6	s_7			I_5
I_3	s_3	s_4			I_8
I_4	g_3	g_3			
I_5				g_1	
I_6	s_6	s_7			I_9
I_7				g_3	
I_8	g_2	g_2			
I_9	g_1	g_2	g_2		

Reduce can be find out by
seeing 'o' operator is present on last
of the grammar.

Stack	Input string	Action
\$ 0	d d \$	Shift 4
\$ 0 d 4	d \$	Reduce $C \rightarrow d$ if we have one symbol on right side then pop 2 symbols.
\$ 0 C 2	d \$	Shift 7
\$ 0 C 2 d 7	\$	Reduce $C \rightarrow d$
\$ 0 C 2 C 5	\$	Reduce $S \rightarrow CC$
\$ 0 S 1	\$	Accepted.

3) SLR Parser:

SLR is simple LR. It is the smallest class of grammar having few numbers of states. SLR is very easy to construct and simpler to LR parsing.

Steps to construct SLR parse table:

1. Writing augmented grammar.
2. $\delta(R)^{(0)}$ Collection of items
3. Find Follow of LHS of production.
4. Defining 2 functions: goto and action.

$E_2: S \rightarrow AS/b$

$A \rightarrow SA/a$

Step 1: Writing writing Augmented Grammar

$S' \rightarrow S$

$S \rightarrow AS$

$S \rightarrow b$

$A \rightarrow SA$

$A \rightarrow a$

Step 2: Calculating Canonical collection
of LR(0) items.

$I_0 \rightarrow S' \rightarrow \cdot S^0$

$S \rightarrow \cdot AS^1$

$S \rightarrow \cdot b^2$

$A \rightarrow \cdot SA^3$

$A \rightarrow \cdot a^4$

goto(I_0, S)

$I_1 \quad S' \rightarrow \cdot S = S' \rightarrow S.$

$A \rightarrow \cdot SA = A \rightarrow S.A$

$A \rightarrow \cdot SA$

$A \rightarrow \cdot a$

(1) present
at first
then it is
final item

$2A \rightarrow \cdot b$

$S \rightarrow \cdot AS$

$S \rightarrow \cdot b$

goto(I_0 , A)

$$S \rightarrow \cdot AS = S \xrightarrow{A} A \cdot S$$

$I_0 -$

$$S \rightarrow \cdot AS$$

$$S \rightarrow \cdot b$$

$$A \rightarrow \cdot SA$$

$$A \rightarrow \cdot a$$

goto(I_0 , b)

$I_0 - S \rightarrow b \cdot$

goto(I_0 , a)

$I_0 - S \rightarrow a \cdot$

goto(I_1 , A)

I_5

$$A \rightarrow SA \cdot$$

$$A \rightarrow S \cdot A \cdot$$

$$S \rightarrow A \cdot S$$

$$S \rightarrow \cdot AS$$

$$S \rightarrow \cdot b$$

$$A \rightarrow \cdot SA$$

$$A \rightarrow \cdot a$$

goto(I_1 , S)

I_6

$$A \rightarrow \cdot SA$$

$$S \rightarrow \cdot AS$$

$$A \rightarrow \cdot SA$$

$$S \rightarrow \cdot b$$

$$A \rightarrow \cdot a$$

goto(I_1 , a);

$I_4 \rightarrow A \rightarrow a$

goto(I_1 , b)

$I_3 \rightarrow S \rightarrow b$

goto(I_2 , S);

If $S \rightarrow AS$:
 $A \rightarrow \$ \cdot A$
 $A \rightarrow \cdot SA$
 $A \rightarrow \cdot A$
 $S \rightarrow \cdot A S$
 $S \rightarrow \cdot b$

goto(I_2 , A)

$I_2 \rightarrow S \rightarrow A \cdot S$
 $S \rightarrow \cdot AS$
 $S \rightarrow \cdot b$
 $A \rightarrow \cdot SA$
 $A \rightarrow \cdot a$

goto(I_2 , a)

$A \rightarrow a \cdot - I_4$

goto(I_2 , b)

$A \cdot S \rightarrow b \cdot - I_4$

goto(I₅, S)

$$\begin{array}{l} S \rightarrow AS \\ A \rightarrow S \cdot A \\ A \rightarrow \cdot SA \\ A \rightarrow a \\ S \rightarrow \cdot AS \\ S \rightarrow \cdot b \end{array} \quad \left. \begin{array}{l} \\ \\ \\ \\ \end{array} \right\} I_5$$

goto(I₅, a)

$$A \rightarrow a \cdot \quad I_5$$

goto(I₅, b)

$$S \rightarrow b \cdot \quad I_5$$

goto(I₅, A)

$$\begin{array}{l} S \rightarrow A \cdot S \\ S \rightarrow \cdot AS \\ S \rightarrow \cdot b \\ A \rightarrow \cdot S A \\ A \rightarrow \cdot a \end{array} \quad \left. \begin{array}{l} \\ \\ \\ \end{array} \right\} I_5$$

goto(I₆, A)

$$\begin{array}{l} I_5 \quad A \rightarrow \cdot SA \\ A \rightarrow S A \cdot \quad A \rightarrow \cdot a \\ S \rightarrow A \cdot S \\ S \rightarrow \cdot AS \\ S \rightarrow \cdot b \end{array}$$

goto (I_F , S)

$$\begin{array}{l} A \rightarrow S \cdot A \\ A \rightarrow \cdot S A \\ A \rightarrow a \\ S \rightarrow \cdot A S \\ S \rightarrow b \end{array} \quad \left. \begin{array}{l} \\ \\ \\ \end{array} \right\} I_F$$

goto (I_F , a)

$$A \rightarrow a \cdot \rightarrow I_4$$

goto (I_F , b)

$$S \rightarrow b \cdot \rightarrow I_3$$

goto (I_F , A)

$$\begin{array}{l} A \rightarrow S A \cdot \\ S \rightarrow A \cdot S \end{array} \quad \left. \begin{array}{l} \\ \end{array} \right\} I_5$$

goto (I_F , S)

$$\begin{array}{l} A \rightarrow S \cdot A \\ A \rightarrow \cdot S A \\ A \rightarrow \cdot a \end{array} \quad \left. \begin{array}{l} \\ \\ \end{array} \right\} I_6$$

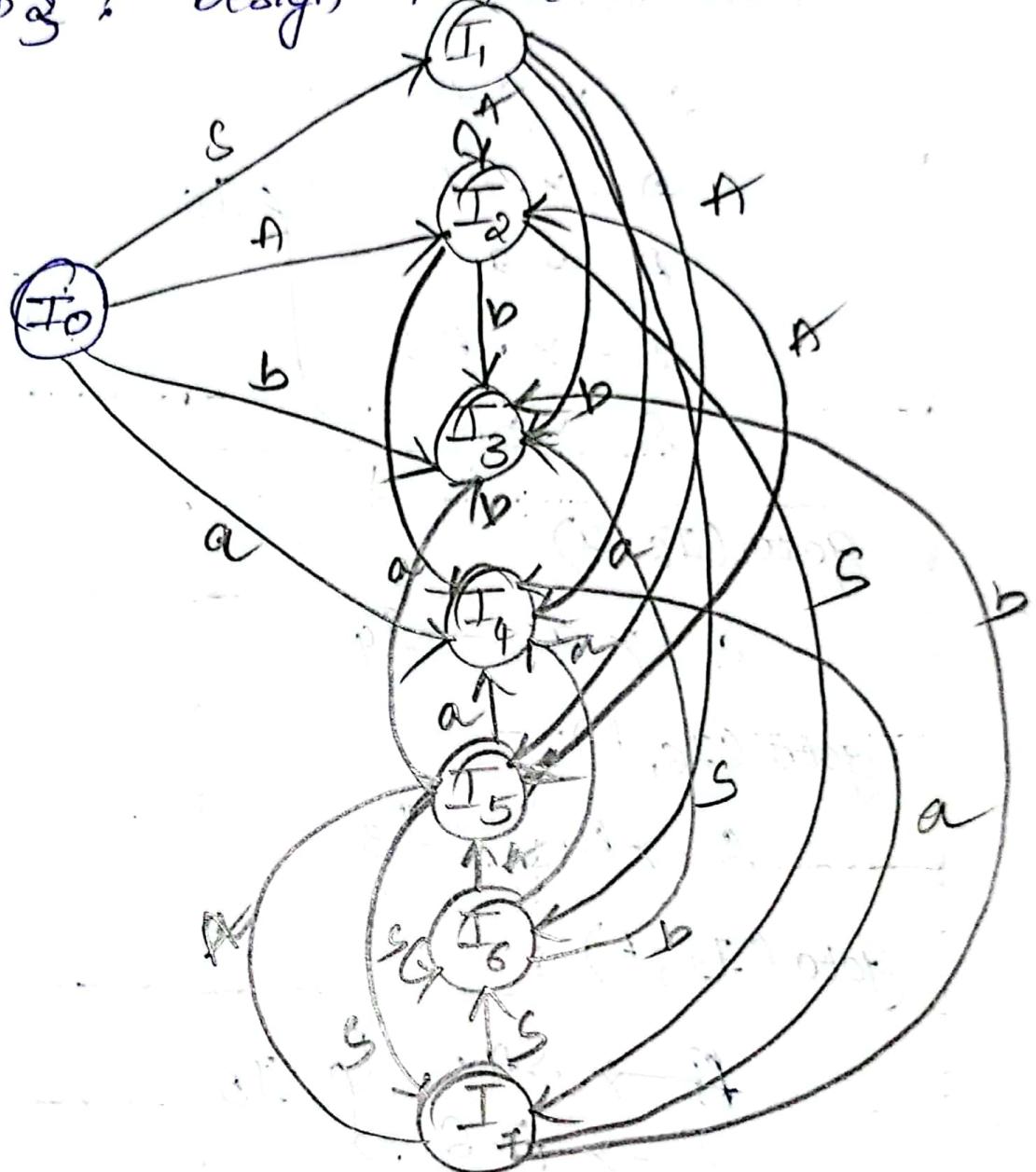
goto (I_F , a)

$$A \rightarrow a \cdot \rightarrow I_4$$

goto (I_F , b)

$$S \rightarrow b \cdot \rightarrow I_3$$

Step 3 : Design Finite Automata



Step 4: $\text{Follow}(S) = \{b, a\}$

$\text{Follow}(A) = \{a, b\}$

$\text{Follow}(S) = \{\$, a, b\}$

$\text{Follow}(A) = \{a, b\}$

Construction of parse table.

	Action			State	
	a	b	\$	AS	AF
I ₀	S ₄	S ₃		I ₁	I ₂
I ₁	S ₄	S ₃	Accepted	I ₅	I ₅
I ₂	S ₄	S ₃		I ₇	I ₂
I ₃	g ₂	g ₂	g ₂		
I ₄	g ₄	g ₄			
I ₅	S ₄ /g ₃	S ₃ /g ₃		I ₇	I ₂
I ₆	S ₄	S ₃		I ₆	I ₅
I ₇	S ₄ /g ₁	S ₃ /g ₁	g ₁	I ₆	I ₅

Step 5: Check whether the string will accept by the parser or not.

String = abab

Stack	Tips	Action
\$ 0	abab\$	Shift 4
\$ 0a\$	bab\$	Reduce A → a
\$. 0A2	bab\$	Shift 3
\$ 0A2b3	ab\$	Reduce $S \rightarrow b$
\$ 0A2S\$	ab\$	Reduce $S \rightarrow AS$
\$ 0S1	ab\$	Shift 4
\$ 0S1a4	b\$	Reduce $A \rightarrow a$
\$ 0S1	b\$	Shift 3
\$ 0S1A5	b\$	Reduce $A \rightarrow SA$
\$ 0A2A2	b\$	Shift 3
\$ 0A2b3	\$	$S \rightarrow b$
\$ 0A2S\$	\$	Reduce $S \rightarrow AS$
\$ 0S1	\$	Accepted.

↳ LALR Parser

LALR Parser is lookahead LR parser. It is the most powerful parser which can handle large classes of grammar. The size of CLR parsing is quite large as compared to other parsing table. LALR reduces the size of this table. LALR works similar to CLR. It combines the frontier states of CLR parsing table into single state.

LR(1) Item = LR(0) Item + lookahead

Steps for constructing the LALR parsing table:

1. Writing the augmented grammar.
2. LR(1) collection of items to be found.
3. Defining 2 functions i.e. goto and action.

$$Ex: S \rightarrow d = R / R^2$$

$$d \rightarrow *R / id$$

$$R \rightarrow L$$

$$String = id = id$$

Step 1: Augmented Grammar

$$S \rightarrow S$$

$$S \rightarrow \lambda = R / R$$

$$\lambda \rightarrow *R / ?d$$

$$R \rightarrow L$$

Step 2: Calculating LR(0) items.

$$I_0 > S \rightarrow \cdot S, \$ \longrightarrow 0$$

$$S \rightarrow \cdot \lambda = R, \$ \longrightarrow 1$$

$$S \rightarrow \cdot R, \$ \longrightarrow 2$$

$$\lambda \rightarrow \cdot *R, = / \$ \longrightarrow 3$$

$$\lambda \rightarrow \cdot ?d, = / \$ \longrightarrow 4$$

$$R \rightarrow \cdot L, \$ \longrightarrow 5$$

goto(I₀, S)

$$S \rightarrow \lambda \cdot = R, \$$$

$$I_1 > S' \rightarrow S \cdot, \$$$

goto(I₀, L)

$$I_2 > S \rightarrow \lambda \cdot = R, \$$$

$$R \rightarrow L \cdot, \$$$

goto (I_0 , R)

$I_3 \rightarrow S \rightarrow R, \$$

goto (I_0 , *)

$I_4 \rightarrow L \rightarrow *R, =/\$$

$R \rightarrow \cdot L, /\$$

$L \rightarrow \cdot *R, =/\$$

$L \rightarrow \cdot id, =/\$$

goto (I_0 , id)

$I_5 \rightarrow id \rightarrow id, \$$

goto (I_2 , =)

$I_6 \rightarrow S \rightarrow L = \cdot R, \$$

$R \rightarrow \cdot L, \$$

$L \rightarrow \cdot *R, \$$

$L \rightarrow \cdot id, \$$

goto (I_4 , R)

$I_7 \rightarrow L \rightarrow *R, =/\$$

$R \not\rightarrow$

goto (I_4 , L)

$R \rightarrow L, /\$ \rightarrow I_8$

goto (I_4 , *)

$L \rightarrow *R, \$ \rightarrow I_4$

goto(I_4 , id)

$\lambda \rightarrow \text{id.}; \& \rightarrow I_5$

goto(I_6 , R)

$\delta \rightarrow \lambda = R.$, $\& \rightarrow I_9$

goto(I_6 , λ)

$R \rightarrow \lambda.$, $\& \rightarrow I_{10}$

goto(I_6 , $*$)

$\lambda \rightarrow * \cdot R,$ $\&$ } I_{10}

$R \rightarrow \cdot L,$ $\&$

$\lambda \rightarrow \cdot * R,$ $\&$

$\lambda \rightarrow \cdot \text{id},$ $\&$

goto(I_6 , id)

$\lambda \rightarrow \text{id.},$ $\& \rightarrow I_8$

goto(I_{10} , R)

$\lambda \rightarrow * R.$, $\& \rightarrow I_{11}$

goto(I_{11} , λ)

$R \rightarrow \lambda.$, $\& \rightarrow I_{10}$

goto(I_{11} , $*$)

$\lambda \rightarrow * R,$ $\& \rightarrow I_{11}$

goto (I_{11} , id)

$\alpha \rightarrow id, \$ \rightarrow T_{12}$

Combine the 8 states grammar

$I_4 \in I_{11} \rightarrow I_{411}$

$I_5 \in I_{12} \rightarrow I_{512}$

$I_7 \in I_{13} \rightarrow I_{713}$

$I_8 \in I_0 \rightarrow I_{810}$

Step 3: Construct LR parse table

	Action	*	\$	S, d	R	goto
0	S_{512}	S_{411}		1	2	3
1			Accepted			
2	S_6		g_5			
3			g_2			
411	S_{512}	S_{411}			810	T_{13}
512		g_4	g_4			
6	S_{512}	411			810	9
713		g_3	g_3			
810		g_5	g_5			
9			g_1			

Stack

\$ 0

Top Storing

id = Id \$

Action

Shift 512

\$ 0 @ Id 512

!= Id \$

Shift Reduce

L \rightarrow Id

\$ 0 R d 512

= Id \$

Shift 6

\$ 0 L 2 = 6

Id \$

Shift 512

\$ 0 L 2 = 6 Id 512

\$

Reduce 94

L \rightarrow ;

\$ 0 L 2 = 6 (8) 2

\$

Reduce 95

\$ 0 L 2 = 6 R 9

\$

Reduce 96

\$ 0 S 1

\$

Accepted.

Ex: S \rightarrow CC

C \rightarrow aC/b

Storing % bb

Ex: E \rightarrow E + T / T

T \rightarrow T * F / F

Storing % id \$ id \$ id \$

F \rightarrow (E) / Id



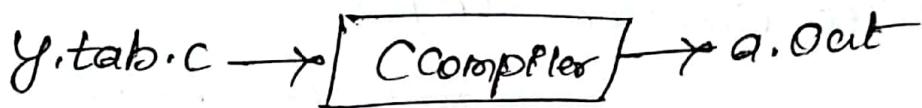
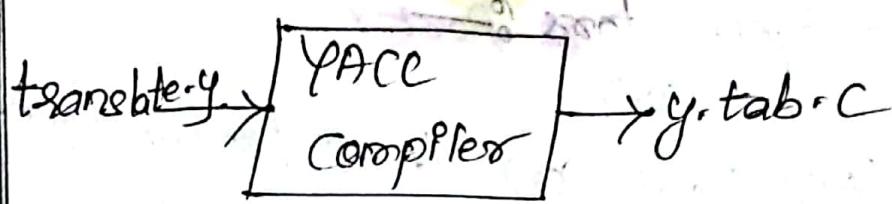
VI) Parser Generators :-

(or)

YACC Tool (or) YACC Parser Generators
(Yet Another Compiler Compiler)

1. YACC provides a tool to produce a parser for a given grammar.
2. YACC is a program designed to compile a LR(0) grammar.
3. It is used to produce the source code of the syntactic analyzer of the language produced by LR(0) grammar.
4. The Input of YACC is the rule (or) grammar and the output is a program.

It is a tool to produce a parser. It accepts input from lexical analyzer(tokens) and produce parsers. It is also called as parser generators.



Structure of YACC tool.

YACC program generally contains

3 sections.

1. declarations
2. translation rules
3. Auxiliary functions.

The Declaration Part:

There are two sections in the declarations part of YACC programs;
in the first section, we put ordinary C declarations, delimited by % and %., and in second section contains only include statement that causes the C preprocessor to include the standard header file <ctype.h>.

The translation Rules Part:

In this part the YACC Specification after the first %Y part, we put the translation rules. Each rules contains of a grammar production and the associated semantic actions.

$\langle \text{heads} \rangle \rightarrow \langle \text{body}_1 \rangle / \langle \text{body}_2 \rangle / \dots / \langle \text{body}_n \rangle$

would be written as in YACC

$\langle \text{heads} \rangle : \langle \text{body}_1 \rangle \{ \langle \text{semantic action} \rangle \}$

$/ \langle \text{body}_2 \rangle \{ \langle \text{semantic action} \rangle \}$

⋮

$/ \langle \text{body}_n \rangle \{ \langle \text{semantic action} \rangle \}$

Ex: $E \rightarrow E + T / T$

expr: expr '+' term { \$1 = \$1 + \$3; }

| term

⋮

The Auxiliary functions :

It is mainly used to define C functions `ypylex()` will be written in auxiliary functions.

YACC Program of Simple Desk Calculator

$E \rightarrow E + T / T$

$T \rightarrow T * F / F$

$F \rightarrow (E) / id$

→ translate.y

1. #

~~#include <ctype.h>~~ — ctype stands
for conversion.

2. #

3. token DIGIT

4. %

line : expr 'n' { printf("%d\n", \$1) }

expr : expr '+' term { \$\$ = \$\$ + \$3 }

| term ;

term : term '*' factor { \$\$ = \$\$ * \$3 }

| factor ;

factor : '(' expr ')' { \$\$ = \$2 }

| DIGIT ;

5. % — lexical analyzer

yylemlc()

{ int c ;

c = getchar();

if (c.isdigit())

{
 yylval = c - '0';

getchar();

}