VERIFICATION OF BOOLEAN THEOREMS

EXP.NO.: 2

AIM:

To study and verify the Boolean theorems using logic gates.

COMPONENTS REQUIRED:

| S.No. | Apparatus | Specifications | Quantity |
|-------|------------------|------------------|----------|
| 1. | IC Trainer kit | | 1 no |
| 2. | Logic gate IC's | IC 7404, IC 7408 | 1no each |
| 3. | Logic gate IC's | IC 7402, IC 7486 | 1no each |
| 4. | Connecting wires | | 1 set |

Theorems:

- 1. Idempotent laws:
 - a) x + x = x
 - **b**) $x \cdot x = x$
- 2. Identity law:

$$x + 1 = x$$

3. Null law:

$$x.0 = x$$

4. Involution law (or) double negation law:

$$(x')' = x$$

5. Associative law:

$$x + (y + z) = (x + y) + z$$

 $x \cdot (y \cdot z) = (x \cdot y) \cdot z$

6. Demorgan's law:

$$(x + y)' = x' \cdot y'$$

 $(x \cdot y)' = x' + y'$

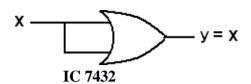
7. Adsorption theorem:

$$x + (x.y) = x$$

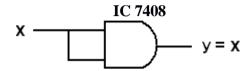
$$x.(x+y) = x$$

1. Idempotence laws:

a)
$$x + x = x$$

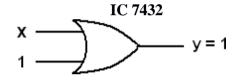


b)
$$x. x = x$$



2. Identity law:

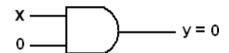
$$x + 1 = 1$$



3. Null law:

$$x.0 = 0$$

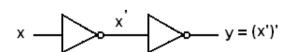
IC 7408



4. Involution law (or) double negation law:

$$(x')' = x$$

IC 7404 IC 7404



TRUTH TABLE

| x + x = x |
|-----------|
| 0 |
| 1 |
| |

| x | <i>x</i> . <i>x</i> |
|---|---------------------|
| | =x |
| 0 | 0 |

| X | x + 1 = |
|---|---------|
| 0 | 1 |
| 1 | 1 |

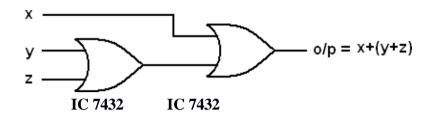
| | 0 |
|---|------|
| X | x. 0 |
| | = 0 |
| 0 | 0 |

| х | <i>x</i> ′ | (x')' $= x$ |
|---|------------|-------------|
| 0 | 1 | 0 |

5. Associative law:

a)
$$x + (y + z) = (x + y) + z$$

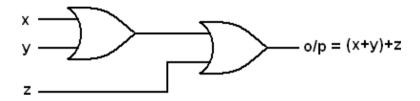
L.H.S



| x | y | Z | y + z | x+ (y+z) | $\begin{vmatrix} x \\ + y \end{vmatrix}$ | (x + y) +z |
|---|---|---|----------|-------------|--|------------------|
| 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| 0 | 0 | 1 | 1 | 1 | 0 | 1 |
| 0 | 1 | 0 | 1 | 1 | 1 | 1 |
| 0 | 1 | 1 | 1 | 1 | 1 | 1 |
| 1 | 0 | 0 | 0 | 1 | 1 | 1 |
| 1 | 0 | 1 | 1 | 1 | 1 | 1 |
| 1 | 1 | 0 | 1 | 1 | 1 | 1 |
| 1 | 1 | 1 | 1 | 1 | 1 | 1 |

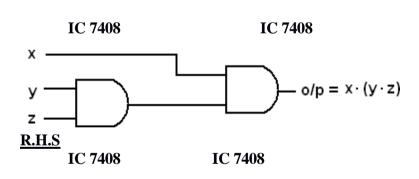
<u>**R.H.S**</u>

IC 7432 IC 7432

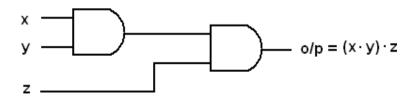


b)
$$x.(y.z) = (x.y).z$$

L.H.S



| _ | | | | | | | |
|---|---|---|---|------|------------|------------|------------|
| | x | у | Z | y. z | <i>x</i> . | <i>x.y</i> | (x. y) |
| | | | | | (y.z) | | . Z |
| | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| | 0 | 0 | 1 | 0 | 0 | 0 | 0 |
| | 0 | 1 | 0 | 0 | 0 | 0 | 0 |
| | 0 | 1 | 1 | 1 | 0 | 0 | 0 |
| | 1 | 0 | 0 | 0 | 0 | 0 | 0 |
| | 1 | 0 | 1 | 0 | 0 | 0 | 0 |
| | 1 | 1 | 0 | 0 | 0 | 1 | 0 |
| | 1 | 1 | 1 | 1 | 1 | 1 | 1 |
| | | | | | L | | |



6. Demorgan's law:

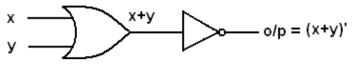
a)
$$(x + y)' = x'.y'$$

L.H.Ś

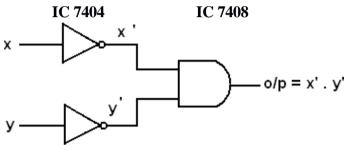
IC 7432

IC 7404

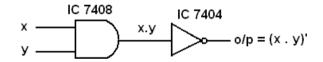
| х | Y | x + y | (x + y) ' | <i>x</i> ′ | y ' | x'. y' |
|---|---|-------|-----------|------------|------------|--------|
| 0 | 0 | 0 | 1 | 1 | 1 | 1 |
| 0 | 1 | 1 | 0 | 1 | 0 | 0 |
| 1 | 0 | 1 | 0 | 0 | 1 | 0 |
| 1 | 1 | 1 | 0 | 0 | 0 | 0 |







b)
$$(x.y)' = x' + y'$$



<u>L.H.S</u>

| x | Y | x.y | (x.y) ' | x' | y' | x'+y' |
|---|---|-----|---------|----|----|-------|
| 0 | 0 | 0 | 1 | 1 | 1 | 1 |
| 0 | 1 | 0 | 1 | 1 | 0 | 1 |
| 1 | 0 | 0 | 1 | 0 | 1 | 1 |
| 1 | 1 | 1 | 0 | 0 | 0 | 0 |

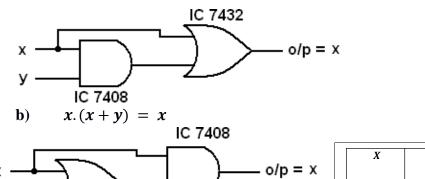
R.H.S

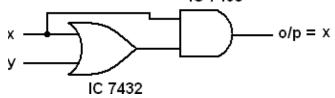
| x — C 7404 | IC 7432 |
|------------|-------------|
| yy ' | o/p = x'+y' |

7. Adsorption theorem:

a)
$$x + (x, y) = x$$

| X | у | <i>x</i> . <i>y</i> | $\begin{array}{c} x + (x. y) \\ = x \end{array}$ |
|---|---|---------------------|--|
| 0 | 0 | 0 | 0 |
| 0 | 1 | 0 | 0 |
| 1 | 0 | 0 | 1 |





| X | у | x + y | $\begin{array}{c c} x. (x + y) \\ = x \end{array}$ |
|---|---|----------|--|
| 0 | 0 | 0 | 0 |
| 0 | 1 | 1 | 0 |
| 1 | 0 | 1 | 1 |
| 1 | 1 | 1 | 1 |

Procedure:

- 1. Connections are made as per the circuit diagram for each of the theorems.
- 2. Switch on the IC trainer kit.
- 3. Apply logic inputs 0 or 1 to input variables
- 4. Verify the truth table by observing the output indicators for all the theorems.

Result:

Thus, the Boolean theorems and Laws are studied and verified using logic gates.