

1. Generate  $10^4$  random numbers between  $[0:1]$  and plot the probability distribution of these numbers in the said range.
2. Generate  $5 \times 10^4$  Gaussian random numbers and plot the probability distribution of these numbers in the range  $[-5 : 5]$ . Note that in principle the range should be  $[-\infty : \infty]$  !!
3. A Brownian particle of negligible mass is diffusing freely in a fluid medium (two dimensions). It obeys the following equation

$$\frac{d\vec{r}(x, y)}{dt} = \sqrt{D_0} \vec{\xi}(t),$$

where  $\vec{\xi}(t)$  is the random force arising due to the collision of fluid molecules and the Brownian particle, and  $D_0$  is the diffusion constant which can be set to 1.

Using Euler's method, generate the trajectory of the particle in a finite time window and plot it. For your information,  $r_x(t + \Delta t) = r_x(t) + \sqrt{D_0 \times \Delta t} G_x$ , where  $G_x$  is a Gaussian random number. Follow the same step for the  $y$ - component  $r_y$ .