Computational Minimalism 計算ミニマリズム

決定的であるにもかかわらず、結果が予測困難なアルゴリ ズムによる造形

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1つの点から出発する2次元セルオートマトン

2色9近傍の2次元セルオートマトンのルールは、全部で

2^(2^9)

 $13407807929942597099574024998205846127479365820592393377723561443721764030073546976 \times 801874298166903427690031858186486050853753882811946569946433649006084096$

N[2^(2^9)]

 1.34078×10^{154}

通り存在する。これは155桁の数のそこそこ大きな数である[注1]。

[注1] グーゴル数 10^{100} よりは大きいが、RSA暗号で用いられる $300 \sim 1000$ 桁の数よりは遥かに小さい。

初期条件として、最もミニマルな1つの点を考える。それでも、そこから2次元セルオートマトンのアルゴリズムによって生まれ得る造形の可能性を探索するためには、すべてのルールについての計算を実行してみなければならない。なぜなら、セルオートマトンは一般に決定的でありながら予測不可能な複雑系であり、そのすべての可能性を確率的な方法で効率良く探索することができないからだ。

汎用の数式処理/数値計算環境であるMathematica(http://www.wolfram.com/)において、セルオートマトンのルールは、一般化された「ルール番号」によって指定できる。2色9近傍2次元セルオートマトンには512通りの可能な近傍状態があり、これらの状態ひとつひとつに次のステップでの中央セルの状態を対応させることで、ルール番号を一意に得ることができる。例えば2次元セルオートマトンで最も良く知られているコンウェイのライフゲームの場合、ルールは以下のように表現できる。ここで

3121796387206642884643857416353388816364758858874716286199733047244606561418987700322611464790005 242280784132089221851121096915552864518716024960という145桁の数がライフゲームのルール番号である。

Table[Partition[IntegerDigits[i, 2, 9], 3] \rightarrow Part[IntegerDigits[3121796387206642884643857416353388816364758858874716286199733047244606561418987 \times 700322611464790005242280784132089221851121096915552864518716024960, 2, 2^9], -(1+i)], {i, 0, 2^9 - 1}]

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 \{\{\{0,0,0,0\},\ \{0,0,0\},\ \{0,0,0\}\} \rightarrow 0,\ \{\{0,0,0\},\ \{0,0,0\},\ \{0,0,1\}\} \rightarrow 0, \\ \{\{0,0,0\},\ \{0,0,0\},\ \{0,1,0\}\} \rightarrow 0,\ \{\{0,0,0\},\ \{0,0,0\},\ \{1,1,1\}\} \rightarrow 0, \\ \{\{0,0,0\},\ \{0,0,0\},\ \{1,1,0\}\} \rightarrow 0,\ \{\{0,0,0\},\ \{0,0,0\},\ \{1,1,1\}\} \rightarrow 0, \\ \{\{0,0,0\},\ \{0,0,0\},\ \{1,1,0\}\} \rightarrow 0,\ \{\{0,0,0\},\ \{0,0,0\},\ \{1,1,1\}\} \rightarrow 1, \\ \{\{0,0,0\},\ \{0,0,1\},\ \{0,0,0\}\} \rightarrow 0,\ \{\{0,0,0\},\ \{0,0,1\},\ \{0,0,1\}\} \rightarrow 0, \\ \} \rightarrow 0, \\ \{\{0,0,0\},\ \{0,0,1\},\ \{0,0,0\}\} \rightarrow 0,\ \{\{0,0,0\},\ \{0,0,1\},\ \{0,0,1\}\} \rightarrow 0, \\ \} \rightarrow 0, \\ \{\{0,0,0\},\ \{0,0,1\},\ \{0,0,1\}\} \rightarrow 0, \\ \{\{0,0,0\},\ \{0,0\},\ \{0,0\},\ \{0,0\},\ \{0,0\},\ \{0,0\},\ \{0,0\},\ \{0,0\},\ \{0,0\},\ \{0,0\},\ \{0,0\},\ \{0,0\},\ \{0,0\},\ \{0,0\},\ \{0,0\},\ \{0,0\},\ \{0,0\},\ \{0,0\},\ \{0,0\},\ \{0,0\},\ \{0,0\},\ \{0,0\},\ \{0,0\},\ \{0,0\},\ \{0,0\},\ \{0,0\},\ \{0,0\},\ \{0,0\},\ \{0,0\},\ \{0,0\},\ \{0,0\},\ \{0,0\},\ \{0,0\},\ \{0,0\},\ \{0,0\},\ \{0,0\},\ \{0,0\},\ \{0,0\},\ \{0,0\},\ \{0,0\},\ \{0,0\},\ \{0,0\},\ \{0,0\},\ \{0,0\},\ \{0,0\},\ \{0,0\},\ \{0,0\},\ \{0,0\},\ \{0,0\},\ \{0,0\},\ \{0,0\},\ \{0,0\},\ \{0,0\},\ \{0,0\},\ \{0
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\{\{0, 1, 1\}, \{0, 0, 0\}, \{0, 0, 0\}\} \rightarrow 0, \{\{0, 1, 1\}, \{0, 0, 0\}, \{0, 0, 1\}\} \rightarrow 1,
\{\{0, 1, 1\}, \{0, 0, 0\}, \{0, 1, 0\}\} \rightarrow 1, \{\{0, 1, 1\}, \{0, 0, 0\}, \{0, 1, 1\}\} \rightarrow 0,
\{\{0, 1, 1\}, \{0, 0, 0\}, \{1, 0, 0\}\} \rightarrow 1, \{\{0, 1, 1\}, \{0, 0, 0\}, \{1, 0, 1\}\} \rightarrow 0,
\{\{\textbf{0, 1, 1}\},\, \{\textbf{0, 0, 0}\},\, \{\textbf{1, 1, 0}\}\} \rightarrow \textbf{0, } \{\{\textbf{0, 1, 1}\},\, \{\textbf{0, 0, 0}\},\, \{\textbf{1, 1, 1}\}\} \rightarrow \textbf{0, 0, 0}\}
\{\{\textbf{0, 1, 1}\},\, \{\textbf{0, 0, 1}\},\, \{\textbf{0, 0, 0}\}\} \rightarrow \textbf{1, } \{\{\textbf{0, 1, 1}\},\, \{\textbf{0, 0, 1}\},\, \{\textbf{0, 0, 1}\}\} \rightarrow \textbf{0, 0, 1}\}\} \rightarrow \textbf{0, 0, 1}\}
\{\{\textbf{0, 1, 1}\},\, \{\textbf{0, 0, 1}\},\, \{\textbf{0, 1, 0}\}\} \rightarrow \textbf{0,} \, \{\{\textbf{0, 1, 1}\},\, \{\textbf{0, 0, 1}\},\, \{\textbf{0, 1, 1}\}\} \rightarrow \textbf{0,} \, \{\textbf{0, 1, 1}\},\, \{\textbf{0, 1, 1}\}\}
\{\{\textbf{0, 1, 1}\},\, \{\textbf{0, 0, 1}\},\, \{\textbf{1, 0, 0}\}\} \rightarrow \textbf{0, } \{\{\textbf{0, 1, 1}\},\, \{\textbf{0, 0, 1}\},\, \{\textbf{1, 0, 1}\}\} \rightarrow \textbf{0, 1}\}
\{\{\textbf{0,1,1}\},\ \{\textbf{0,0,1}\},\ \{\textbf{1,1,0}\}\} \rightarrow \textbf{0,}\ \{\{\textbf{0,1,1}\},\ \{\textbf{0,0,1}\},\ \{\textbf{1,1,1}\}\} \rightarrow \textbf{0,}
\{\{\textbf{0,1,1}\},\,\{\textbf{0,1,0}\},\,\{\textbf{0,0,0}\}\} \rightarrow \textbf{1,}\, \{\{\textbf{0,1,1}\},\,\{\textbf{0,1,0}\},\,\{\textbf{0,0,1}\}\} \rightarrow \textbf{0,}
\{\{0, 1, 1\}, \{0, 1, 0\}, \{0, 1, 0\}\} \rightarrow 0, \{\{0, 1, 1\}, \{0, 1, 0\}, \{0, 1, 1\}\} \rightarrow 0,
\{\{\textbf{0,1,1}\},\,\{\textbf{0,1,0}\},\,\{\textbf{1,0,0}\}\}\rightarrow\textbf{0,}\,\{\{\textbf{0,1,1}\},\,\{\textbf{0,1,0}\},\,\{\textbf{1,0,1}\}\}\rightarrow\textbf{0,}
\{\{\textbf{0,1,1}\},\,\{\textbf{0,1,0}\},\,\{\textbf{1,1,0}\}\} \rightarrow \textbf{0,}\, \{\{\textbf{0,1,1}\},\,\{\textbf{0,1,0}\},\,\{\textbf{1,1,1}\}\} \rightarrow \textbf{0,}
\{\{0, 1, 1\}, \{0, 1, 1\}, \{0, 0, 0\}\} \rightarrow 0, \{\{0, 1, 1\}, \{0, 1, 1\}, \{0, 0, 1\}\} \rightarrow 0,
\{\{\textbf{0, 1, 1}\},\, \{\textbf{0, 1, 1}\},\, \{\textbf{0, 1, 0}\}\} \rightarrow \textbf{0,} \, \{\{\textbf{0, 1, 1}\},\, \{\textbf{0, 1, 1}\},\, \{\textbf{0, 1, 1}\}\} \rightarrow \textbf{0,} \, \{\{\textbf{0, 1, 1}\},\, \{\textbf{0, 1, 1}\}\},\, \{\textbf{0, 1, 1}\}\} \rightarrow \textbf{0,} \, \{\{\textbf{0, 1, 1}\},\, \{\textbf{0, 1, 1}\},\, \{\textbf{0, 1, 1}\}\} \rightarrow \textbf{0,} \, \{\{\textbf{0, 1, 1}\},\, \{\textbf{0, 1, 1}\}\},\, \{\textbf{0, 1, 1}\}\} \rightarrow \textbf{0,} \, \{\{\textbf{0, 1, 1}\},\, \{\textbf{0, 1, 1}\}\},\, \{\textbf{0, 1, 1}\}\}
\{\{0, 1, 1\}, \{0, 1, 1\}, \{1, 0, 0\}\} \rightarrow 0, \{\{0, 1, 1\}, \{0, 1, 1\}, \{1, 0, 1\}\} \rightarrow 0,
\{\{\textbf{0,1,1}\},\ \{\textbf{0,1,1}\},\ \{\textbf{1,1,0}\}\} \rightarrow \textbf{0,}\ \{\{\textbf{0,1,1}\},\ \{\textbf{0,1,1}\},\ \{\textbf{1,1,1}\}\} \rightarrow \textbf{0,}
\{\{0, 1, 1\}, \{1, 0, 0\}, \{0, 0, 0\}\} \rightarrow 1, \{\{0, 1, 1\}, \{1, 0, 0\}, \{0, 0, 1\}\} \rightarrow 0,
\{\{0, 1, 1\}, \{1, 0, 0\}, \{0, 1, 0\}\} \rightarrow 0, \{\{0, 1, 1\}, \{1, 0, 0\}, \{0, 1, 1\}\} \rightarrow 0,
\{\{0, 1, 1\}, \{1, 0, 0\}, \{1, 0, 0\}\} \rightarrow 0, \{\{0, 1, 1\}, \{1, 0, 0\}, \{1, 0, 1\}\} \rightarrow 0,
\{\{0, 1, 1\}, \{1, 0, 0\}, \{1, 1, 0\}\} \rightarrow 0, \{\{0, 1, 1\}, \{1, 0, 0\}, \{1, 1, 1\}\} \rightarrow 0,
\{\{0, 1, 1\}, \{1, 0, 1\}, \{0, 0, 0\}\} \rightarrow 0, \{\{0, 1, 1\}, \{1, 0, 1\}, \{0, 0, 1\}\} \rightarrow 0,
\{\{0, 1, 1\}, \{1, 0, 1\}, \{0, 1, 0\}\} \rightarrow 0, \{\{0, 1, 1\}, \{1, 0, 1\}, \{0, 1, 1\}\} \rightarrow 0,
\{\{0, 1, 1\}, \{1, 0, 1\}, \{1, 0, 0\}\} \rightarrow 0, \{\{0, 1, 1\}, \{1, 0, 1\}, \{1, 0, 1\}\} \rightarrow 0,
\{\{0, 1, 1\}, \{1, 0, 1\}, \{1, 1, 0\}\} \rightarrow 0, \{\{0, 1, 1\}, \{1, 0, 1\}, \{1, 1, 1\}\} \rightarrow 0,
\{\{0, 1, 1\}, \{1, 1, 0\}, \{0, 0, 0\}\} \rightarrow 0, \{\{0, 1, 1\}, \{1, 1, 0\}, \{0, 0, 1\}\} \rightarrow 0,
\{\{0, 1, 1\}, \{1, 1, 0\}, \{0, 1, 0\}\} \rightarrow 0, \{\{0, 1, 1\}, \{1, 1, 0\}, \{0, 1, 1\}\} \rightarrow 0,
\{\{0, 1, 1\}, \{1, 1, 0\}, \{1, 0, 0\}\} \rightarrow 0, \{\{0, 1, 1\}, \{1, 1, 0\}, \{1, 0, 1\}\} \rightarrow 0,
\{\{0, 1, 1\}, \{1, 1, 0\}, \{1, 1, 0\}\} \rightarrow 0, \{\{0, 1, 1\}, \{1, 1, 0\}, \{1, 1, 1\}\} \rightarrow 0,
\{\{0, 1, 1\}, \{1, 1, 1\}, \{0, 0, 0\}\} \rightarrow 0, \{\{0, 1, 1\}, \{1, 1, 1\}, \{0, 0, 1\}\} \rightarrow 0,
\{\{0, 1, 1\}, \{1, 1, 1\}, \{0, 1, 0\}\} \rightarrow 0, \{\{0, 1, 1\}, \{1, 1, 1\}, \{0, 1, 1\}\} \rightarrow 0,
\{\{0, 1, 1\}, \{1, 1, 1\}, \{1, 0, 0\}\} \rightarrow 0, \{\{0, 1, 1\}, \{1, 1, 1\}, \{1, 0, 1\}\} \rightarrow 0,
\{\{0, 1, 1\}, \{1, 1, 1\}, \{1, 1, 0\}\} \rightarrow 0, \{\{0, 1, 1\}, \{1, 1, 1\}, \{1, 1, 1\}\} \rightarrow 0,
\{\{1,\,0,\,0\},\,\{0,\,0,\,0\},\,\{0,\,0,\,0\}\} \rightarrow 0,\,\{\{1,\,0,\,0\},\,\{0,\,0,\,0\},\,\{0,\,0,\,1\}\} \rightarrow 0,
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\{\{1,\,0,\,0\},\,\{0,\,0,\,0\},\,\{0,\,1,\,0\}\} \rightarrow 0,\,\{\{1,\,0,\,0\},\,\{0,\,0,\,0\},\,\{0,\,1,\,1\}\} \rightarrow 1,
\{\{1,\,0,\,0\},\,\{0,\,0,\,0\},\,\{1,\,0,\,0\}\} \rightarrow 0,\,\{\{1,\,0,\,0\},\,\{0,\,0,\,0\},\,\{1,\,0,\,1\}\} \rightarrow 1,
\{\{1,\,0,\,0\},\,\{0,\,0,\,0\},\,\{1,\,1,\,0\}\} \rightarrow 1,\,\{\{1,\,0,\,0\},\,\{0,\,0,\,0\},\,\{1,\,1,\,1\}\} \rightarrow 1,
\{\{1,\,0,\,0\},\,\{0,\,0,\,1\},\,\{0,\,0,\,0\}\} \rightarrow 0,\,\{\{1,\,0,\,0\},\,\{0,\,0,\,1\},\,\{0,\,0,\,1\}\} \rightarrow 1,
\{\{1,\ 0,\ 0\},\ \{0,\ 0,\ 1\},\ \{0,\ 1,\ 0\}\} \rightarrow 1,\ \{\{1,\ 0,\ 0\},\ \{0,\ 0,\ 1\},\ \{0,\ 1,\ 1\}\} \rightarrow 1,
\{\{1,\,0,\,0\},\,\{0,\,0,\,1\},\,\{1,\,0,\,0\}\} \rightarrow 1,\,\{\{1,\,0,\,0\},\,\{0,\,0,\,1\},\,\{1,\,0,\,1\}\} \rightarrow 1,
\{\{1,\ 0,\ 0\},\ \{0,\ 0,\ 1\},\ \{1,\ 1,\ 0\}\} \to 1,\ \{\{1,\ 0,\ 0\},\ \{0,\ 0,\ 1\},\ \{1,\ 1,\ 1\}\} \to 0,
\{\{1,\,0,\,0\},\,\{0,\,1,\,0\},\,\{0,\,0,\,0\}\} \rightarrow 0,\,\{\{1,\,0,\,0\},\,\{0,\,1,\,0\},\,\{0,\,0,\,1\}\} \rightarrow 1,
\{\{1,\ 0,\ 0\},\ \{0,\ 1,\ 0\},\ \{0,\ 1,\ 0\}\} \to 1,\ \{\{1,\ 0,\ 0\},\ \{0,\ 1,\ 0\},\ \{0,\ 1,\ 1\}\} \to 1,
\{\{1,\,0,\,0\},\,\{0,\,1,\,0\},\,\{1,\,0,\,0\}\} \rightarrow 1,\,\{\{1,\,0,\,0\},\,\{0,\,1,\,0\},\,\{1,\,0,\,1\}\} \rightarrow 1,\,\{1,\,0,\,0\},\,\{1,\,0,\,0\},\,\{1,\,0,\,0\},\,\{1,\,0,\,0\}\}
\{\{1,\,0,\,0\},\,\{0,\,1,\,0\},\,\{1,\,1,\,0\}\} \rightarrow 1,\,\{\{1,\,0,\,0\},\,\{0,\,1,\,0\},\,\{1,\,1,\,1\}\} \rightarrow 0,
\{\{1, 0, 0\}, \{0, 1, 1\}, \{0, 0, 0\}\} \rightarrow 1, \{\{1, 0, 0\}, \{0, 1, 1\}, \{0, 0, 1\}\} \rightarrow 1,
\{\{1,\ 0,\ 0\},\ \{0,\ 1,\ 1\},\ \{0,\ 1,\ 0\}\}\rightarrow 1,\ \{\{1,\ 0,\ 0\},\ \{0,\ 1,\ 1\},\ \{0,\ 1,\ 1\}\}\rightarrow 0,
\{\{1, 0, 0\}, \{0, 1, 1\}, \{1, 0, 0\}\} \rightarrow 1, \{\{1, 0, 0\}, \{0, 1, 1\}, \{1, 0, 1\}\} \rightarrow 0,
\{\{1, 0, 0\}, \{0, 1, 1\}, \{1, 1, 0\}\} \rightarrow 0, \{\{1, 0, 0\}, \{0, 1, 1\}, \{1, 1, 1\}\} \rightarrow 0,
\{\{1,\,0,\,0\},\,\{1,\,0,\,0\},\,\{0,\,0,\,0\}\} \rightarrow 0,\,\{\{1,\,0,\,0\},\,\{1,\,0,\,0\},\,\{0,\,0,\,1\}\} \rightarrow 1,
\{\{1, 0, 0\}, \{1, 0, 0\}, \{0, 1, 0\}\} \rightarrow 1, \{\{1, 0, 0\}, \{1, 0, 0\}, \{0, 1, 1\}\} \rightarrow 1,
\{\{1,\,0,\,0\},\,\{1,\,0,\,0\},\,\{1,\,0,\,0\}\} \rightarrow 1,\,\{\{1,\,0,\,0\},\,\{1,\,0,\,0\},\,\{1,\,0,\,1\}\} \rightarrow 1,
\{\{1,\,0,\,0\},\,\{1,\,0,\,0\},\,\{1,\,1,\,0\}\} \rightarrow 1,\,\{\{1,\,0,\,0\},\,\{1,\,0,\,0\},\,\{1,\,1,\,1\}\} \rightarrow 0,
\{\{1,\,0,\,0\},\,\{1,\,0,\,1\},\,\{0,\,0,\,0\}\} \rightarrow 1,\,\{\{1,\,0,\,0\},\,\{1,\,0,\,1\},\,\{0,\,0,\,1\}\} \rightarrow 1,
\{\{1,\ 0,\ 0\},\ \{1,\ 0,\ 1\},\ \{0,\ 1,\ 0\}\} \rightarrow 1,\ \{\{1,\ 0,\ 0\},\ \{1,\ 0,\ 1\},\ \{0,\ 1,\ 1\}\} \rightarrow 0,
\{\{1,\,0,\,0\},\,\{1,\,0,\,1\},\,\{1,\,0,\,0\}\} \rightarrow 1,\,\{\{1,\,0,\,0\},\,\{1,\,0,\,1\},\,\{1,\,0,\,1\}\} \rightarrow 0,
\{\{1,\ 0,\ 0\},\ \{1,\ 0,\ 1\},\ \{1,\ 1,\ 0\}\} \to 0,\ \{\{1,\ 0,\ 0\},\ \{1,\ 0,\ 1\},\ \{1,\ 1,\ 1\}\} \to 0,
\{\{1,\,0,\,0\},\,\{1,\,1,\,0\},\,\{0,\,0,\,0\}\} \rightarrow 1,\,\{\{1,\,0,\,0\},\,\{1,\,1,\,0\},\,\{0,\,0,\,1\}\} \rightarrow 1,
\{\{1\text{, 0, 0}\}\text{, }\{1\text{, 1, 0}\}\text{, }\{0\text{, 1, 0}\}\}\rightarrow1\text{, }\{\{1\text{, 0, 0}\}\text{, }\{1\text{, 1, 0}\}\text{, }\{0\text{, 1, 1}\}\}\rightarrow0\text{, }\{1\text{, 1, 0}\}\text{, }\{1\text{, 1, 0}\}\text
\{\{1,\,0,\,0\},\,\{1,\,1,\,0\},\,\{1,\,0,\,0\}\} \rightarrow 1,\,\{\{1,\,0,\,0\},\,\{1,\,1,\,0\},\,\{1,\,0,\,1\}\} \rightarrow 0,
\{\{1,\ 0,\ 0\},\ \{1,\ 1,\ 0\},\ \{1,\ 1,\ 0\}\} \rightarrow 0\text{, } \{\{1,\ 0,\ 0\},\ \{1,\ 1,\ 0\},\ \{1,\ 1,\ 1\}\} \rightarrow 0\text{, } \{\{1,\ 0,\ 0\},\ \{1,\ 1,\ 0\},\ \{1,\ 1,\ 1\}\} \rightarrow 0\text{, } \{\{1,\ 0,\ 0\},\ \{1,\ 1,\ 0\},\ \{1,\ 1,\ 1\}\} \rightarrow 0\text{, } \{\{1,\ 0,\ 0\},\ \{1,\ 1,\ 0\},\ \{1,\ 1,\ 1\}\} \rightarrow 0\text{, } \{\{1,\ 0,\ 0\},\ \{1,\ 1,\ 0\},\ \{1,\ 1,\ 1\}\} \rightarrow 0\text{, } \{\{1,\ 0,\ 0\},\ \{1,\ 1,\ 0\},\ \{1,\ 1,\ 1\}\} \rightarrow 0\text{, } \{\{1,\ 0,\ 0\},\ \{1,\ 1,\ 0\},\ \{1,\ 1,\ 1\}\} \rightarrow 0\text{, } \{\{1,\ 0,\ 0\},\ \{1,\ 1,\ 0\},\ \{1,\ 1,\ 1\}\} \rightarrow 0\text{, } \{\{1,\ 0,\ 0\},\ \{1,\ 1,\ 0\},\ \{1,\ 1,\ 1\}\} \rightarrow 0\text{, } \{\{1,\ 0,\ 0\},\ \{1,\ 1,\ 0\},\ \{1,\ 1,\ 1\}\} \rightarrow 0\text{, } \{\{1,\ 0,\ 0\},\ \{1,\ 1,\ 0\},\ \{1,\ 1,\ 1\}\} \rightarrow 0\text{, } \{\{1,\ 0,\ 0\},\ \{1,\ 1,\ 0\},\ \{1,\ 1,\ 1\}\} \rightarrow 0\text{, } \{\{1,\ 0,\ 0\},\ \{1,\ 1,\ 0\},\ \{1,\ 1,\ 1\}\} \rightarrow 0\text{, } \{\{1,\ 0,\ 0\},\ \{1,\ 1,\ 0\},\ \{1,\ 1,\ 1\}\} \rightarrow 0\text{, } \{\{1,\ 0,\ 0\},\ \{1,\ 1,\ 1,\ 0\},\ \{1,\ 1,\ 1\}\} \rightarrow 0\text{, } \{\{1,\ 0,\ 0\},\ \{1,\ 1,\ 1,\ 1\}\} \rightarrow 0\text{, } \{\{1,\ 0,\ 0\},\ \{1,\ 1,\ 1,\ 1\}\} \rightarrow 0\text{, } \{\{1,\ 0,\ 0\},\ \{1,\ 1,\ 1,\ 1\}\} \rightarrow 0\text{, } \{\{1,\ 0,\ 0\},\ \{1,\ 1,\ 1,\ 1\}\} \rightarrow 0\text{, } \{\{1,\ 0,\ 0\},\ \{1,\ 1,\ 1,\ 1\}\} \rightarrow 0\text{, } \{\{1,\ 0,\ 0\},\ \{1,\ 0,\ 0\},\ \{1,\ 0,\ 0\},\ \{1,\ 0,\ 0\}\} \rightarrow 0\text{, } \{\{1,\ 0,\ 0\},\ \{1,\ 0,\ 0\},\ \{1,\ 0,\ 0\}\} \rightarrow 0\text{, } \{\{1,\ 0,\ 0\},\ \{1,\ 0,\ 0\},\ \{1,\ 0,\ 0\}\} \rightarrow 0\text{, } \{\{1,\ 0,\ 0\},\ \{1,\ 0,\ 0\},\ \{1,\ 0,\ 0\}\} \rightarrow 0\text{, } \{\{1,\ 0,\ 0\},\ \{1,\ 0,\ 0\},\ \{1,\ 0,\ 0\}\} \rightarrow 0\text{, } \{\{1,\ 0,\ 0\},\ \{1,\ 0,\ 0\},\ \{1,\ 0,\ 0\}\} \rightarrow 0\text{, } \{\{1,\ 0,\ 0\},\ \{1,\ 0,\ 0\},\ \{1,\ 0,\ 0\}\} \rightarrow 0\text{, } \{\{1,\ 0,\ 0\},\ \{1,\ 0,\ 0\},\ \{1,\ 0,\ 0\}\} \rightarrow 0\text{, } \{\{1,\ 0,\ 0\},\ \{1,\ 0,\ 0\}\} \rightarrow 0\text{, } \{\{1,\ 0,\ 0\},\ \{1,\ 0,\ 0\}\} \rightarrow 0\text{, } \{\{1,\ 0,\ 0\},\ \{1,\ 0,\ 0\},\ \{1,\ 0,\ 0\}\} \rightarrow 0\text{, } \{\{1,\ 0,\ 0\},\ \{1,\ 0,\ 0\},\ \{1,\ 0,\ 0\}\} \rightarrow 0\text{, } \{\{1,\ 0,\ 0\},\ \{1,\ 0,\ 0\},\ \{1,\ 0,\ 0\}\} \rightarrow 0\text{, } \{\{1,\ 0,\ 0\},\ \{1,\ 0,\ 0\},\ \{1,\ 0,\ 0\}\} \rightarrow 0\text{, } \{\{1,\ 0,\ 0\},\ \{1,\ 0,\ 0\},\ \{1,\ 0,\ 0\}\} \rightarrow 0\text{, } \{\{1,\ 0,\ 0\},\ \{1,\ 0,\ 0\},\ \{1,\ 0,\ 0\}\} \rightarrow 0\text{, } \{\{1,\ 0,\ 0\},\ \{1,\ 0,\ 0\},\ \{1,\ 0,\ 0\}\} \rightarrow 0\text{, } \{\{1,\ 0,\ 0\},\ \{1,\ 0,\ 0\},\ \{1,\ 0,\ 0\}\} \rightarrow 0\text{, } \{\{1,\ 0,\ 0\},\ \{1,\ 0,\ 0\},\ \{1,\ 0,\ 0\}\} \rightarrow 0\text{, } \{\{1,\ 0,\ 0\},\ \{1,\ 0,\ 0\},\ \{1,\ 0,\ 0\}\} \rightarrow 0\text{, } \{\{1,\ 0,\ 0\},
\{\{1,\ 0,\ 0\},\ \{1,\ 1,\ 1\},\ \{0,\ 0,\ 0\}\} \rightarrow 1,\ \{\{1,\ 0,\ 0\},\ \{1,\ 1,\ 1\},\ \{0,\ 0,\ 1\}\} \rightarrow 0,
\{\{1,\ 0,\ 0\},\ \{1,\ 1,\ 1\},\ \{0,\ 1,\ 0\}\} \rightarrow 0\,,\ \{\{1,\ 0,\ 0\},\ \{1,\ 1,\ 1\},\ \{0,\ 1,\ 1\}\} \rightarrow 0\,,
\{\{1,\,0,\,0\},\,\{1,\,1,\,1\},\,\{1,\,0,\,0\}\} \rightarrow 0,\,\{\{1,\,0,\,0\},\,\{1,\,1,\,1\},\,\{1,\,0,\,1\}\} \rightarrow 0,
\{\{1,\ 0,\ 0\},\ \{1,\ 1,\ 1\},\ \{1,\ 1,\ 0\}\} \rightarrow 0\,,\ \{\{1,\ 0,\ 0\},\ \{1,\ 1,\ 1\},\ \{1,\ 1,\ 1\}\} \rightarrow 0\,,
\{\{1,\,0,\,1\},\,\{0,\,0,\,0\},\,\{0,\,0,\,0\}\} \rightarrow 0,\,\{\{1,\,0,\,1\},\,\{0,\,0,\,0\},\,\{0,\,0,\,1\}\} \rightarrow 1,\,\{0,\,0,\,0\},\,\{0,\,0,\,0\},\,\{0,\,0,\,0\}\}
\{\{1,\ 0,\ 1\},\ \{0,\ 0,\ 0\},\ \{0,\ 1,\ 0\}\} \rightarrow 1,\ \{\{1,\ 0,\ 1\},\ \{0,\ 0,\ 0\},\ \{0,\ 1,\ 1\}\} \rightarrow 1,
\{\{1\text{, 0, 1}\}\text{, }\{0\text{, 0, 0}\}\text{, }\{1\text{, 0, 0}\}\}\rightarrow1\text{, }\{\{1\text{, 0, 1}\}\text{, }\{0\text{, 0, 0}\}\text{, }\{1\text{, 0, 1}\}\}\rightarrow1\text{, }\{0\text{, 0, 0, 0}\}\text{, }\{0\text{, 0, 0, 0}\}\text{, }\{0\text{, 0, 0, 0}\}
\{\{1\text{, 0, 1}\}\text{, }\{0\text{, 0, 0}\}\text{, }\{1\text{, 1, 0}\}\}\rightarrow1\text{, }\{\{1\text{, 0, 1}\}\text{, }\{0\text{, 0, 0}\}\text{, }\{1\text{, 1, 1}\}\}\rightarrow0\text{, }\{1\text{, 0, 1}\}\text{, }\{0\text{, 0, 0}\}\text{, }\{1\text{, 1, 1}\}\}\rightarrow0\text{, }\{1\text{, 0, 1}\}\text{, }\{0\text{, 0, 0}\}\text{, }\{1\text{, 0, 0
\{\{1\text{, 0, 1}\}\text{, }\{0\text{, 0, 1}\}\text{, }\{0\text{, 0, 0}\}\}\rightarrow1\text{, }\{\{1\text{, 0, 1}\}\text{, }\{0\text{, 0, 1}\}\text{, }\{0\text{, 0, 1}\}\}\rightarrow1\text{, }\{0\text{, 0, 1}\}\text{, }\{0\text{, 0, 1}\}\}\rightarrow1\text{, }\{0\text{, 0, 1}\}\text{, }\{0\text{, 0, 1
\{\{1,\ 0,\ 1\},\ \{0,\ 0,\ 1\},\ \{0,\ 1,\ 0\}\} \rightarrow 1,\ \{\{1,\ 0,\ 1\},\ \{0,\ 0,\ 1\},\ \{0,\ 1,\ 1\}\} \rightarrow 0,
\{\{1,\,0,\,1\},\,\{0,\,0,\,1\},\,\{1,\,0,\,0\}\} \rightarrow 1,\,\{\{1,\,0,\,1\},\,\{0,\,0,\,1\},\,\{1,\,0,\,1\}\} \rightarrow 0,
\{\{1,\ 0,\ 1\},\ \{0,\ 0,\ 1\},\ \{1,\ 1,\ 0\}\} \to 0,\ \{\{1,\ 0,\ 1\},\ \{0,\ 0,\ 1\},\ \{1,\ 1,\ 1\}\} \to 0,
\{\{1,\,0,\,1\},\,\{0,\,1,\,0\},\,\{0,\,0,\,0\}\} \rightarrow 1,\,\{\{1,\,0,\,1\},\,\{0,\,1,\,0\},\,\{0,\,0,\,1\}\} \rightarrow 1,
\{\{1, 0, 1\}, \{0, 1, 0\}, \{0, 1, 0\}\} \rightarrow 1, \{\{1, 0, 1\}, \{0, 1, 0\}, \{0, 1, 1\}\} \rightarrow 0,
\{\{1,\,0,\,1\},\,\{0,\,1,\,0\},\,\{1,\,0,\,0\}\} \rightarrow 1,\,\{\{1,\,0,\,1\},\,\{0,\,1,\,0\},\,\{1,\,0,\,1\}\} \rightarrow 0,
\{\{1, 0, 1\}, \{0, 1, 0\}, \{1, 1, 0\}\} \rightarrow 0, \{\{1, 0, 1\}, \{0, 1, 0\}, \{1, 1, 1\}\} \rightarrow 0,
\{\{1, 0, 1\}, \{0, 1, 1\}, \{0, 0, 0\}\} \rightarrow 1, \{\{1, 0, 1\}, \{0, 1, 1\}, \{0, 0, 1\}\} \rightarrow 0,
\{\{1, 0, 1\}, \{0, 1, 1\}, \{0, 1, 0\}\} \rightarrow 0, \{\{1, 0, 1\}, \{0, 1, 1\}, \{0, 1, 1\}\} \rightarrow 0,
\{\{1,\,0,\,1\},\,\{0,\,1,\,1\},\,\{1,\,0,\,0\}\} \rightarrow 0,\,\{\{1,\,0,\,1\},\,\{0,\,1,\,1\},\,\{1,\,0,\,1\}\} \rightarrow 0,
\{\{1, 0, 1\}, \{0, 1, 1\}, \{1, 1, 0\}\} \rightarrow 0, \{\{1, 0, 1\}, \{0, 1, 1\}, \{1, 1, 1\}\} \rightarrow 0,
\{\{1,\ 0,\ 1\},\ \{1,\ 0,\ 0\},\ \{0,\ 0,\ 0\}\} \rightarrow 1,\ \{\{1,\ 0,\ 1\},\ \{1,\ 0,\ 0\},\ \{0,\ 0,\ 1\}\} \rightarrow 1,
\{\{1, 0, 1\}, \{1, 0, 0\}, \{0, 1, 0\}\} \rightarrow 1, \{\{1, 0, 1\}, \{1, 0, 0\}, \{0, 1, 1\}\} \rightarrow 0,
\{\{1, 0, 1\}, \{1, 0, 0\}, \{1, 0, 0\}\} \rightarrow 1, \{\{1, 0, 1\}, \{1, 0, 0\}, \{1, 0, 1\}\} \rightarrow 0,
\{\{1,\,0,\,1\},\,\{1,\,0,\,0\},\,\{1,\,1,\,0\}\} \rightarrow 0,\,\{\{1,\,0,\,1\},\,\{1,\,0,\,0\},\,\{1,\,1,\,1\}\} \rightarrow 0,
\{\{1, 0, 1\}, \{1, 0, 1\}, \{0, 0, 0\}\} \rightarrow 1, \{\{1, 0, 1\}, \{1, 0, 1\}, \{0, 0, 1\}\} \rightarrow 0,
\{\{1, 0, 1\}, \{1, 0, 1\}, \{0, 1, 0\}\} \rightarrow 0, \{\{1, 0, 1\}, \{1, 0, 1\}, \{0, 1, 1\}\} \rightarrow 0,
\{\{1, 0, 1\}, \{1, 0, 1\}, \{1, 0, 0\}\} \rightarrow 0, \{\{1, 0, 1\}, \{1, 0, 1\}, \{1, 0, 1\}\} \rightarrow 0,
\{\{1, 0, 1\}, \{1, 0, 1\}, \{1, 1, 0\}\} \rightarrow 0, \{\{1, 0, 1\}, \{1, 0, 1\}, \{1, 1, 1\}\} \rightarrow 0,
\{\{1, 0, 1\}, \{1, 1, 0\}, \{0, 0, 0\}\} \rightarrow 1, \{\{1, 0, 1\}, \{1, 1, 0\}, \{0, 0, 1\}\} \rightarrow 0,
\{\{1,\ 0,\ 1\},\ \{1,\ 1,\ 0\},\ \{0,\ 1,\ 0\}\} \to 0,\ \{\{1,\ 0,\ 1\},\ \{1,\ 1,\ 0\},\ \{0,\ 1,\ 1\}\} \to 0,
\{\{1,\ 0,\ 1\},\ \{1,\ 1,\ 0\},\ \{1,\ 0,\ 0\}\} \to 0,\ \{\{1,\ 0,\ 1\},\ \{1,\ 1,\ 0\},\ \{1,\ 0,\ 1\}\} \to 0,
\{\{1, 0, 1\}, \{1, 1, 0\}, \{1, 1, 0\}\} \rightarrow 0, \{\{1, 0, 1\}, \{1, 1, 0\}, \{1, 1, 1\}\} \rightarrow 0,
\{\{1, 0, 1\}, \{1, 1, 1\}, \{0, 0, 0\}\} \rightarrow 0, \{\{1, 0, 1\}, \{1, 1, 1\}, \{0, 0, 1\}\} \rightarrow 0,
\{\{1, 0, 1\}, \{1, 1, 1\}, \{0, 1, 0\}\} \rightarrow 0, \{\{1, 0, 1\}, \{1, 1, 1\}, \{0, 1, 1\}\} \rightarrow 0,
\{\{1,\ 0,\ 1\},\ \{1,\ 1,\ 1\},\ \{1,\ 0,\ 0\}\} \to 0,\ \{\{1,\ 0,\ 1\},\ \{1,\ 1,\ 1\},\ \{1,\ 0,\ 1\}\} \to 0,
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\{\{1,\ 0,\ 1\},\ \{1,\ 1,\ 1\},\ \{1,\ 1,\ 0\}\} \to 0,\ \{\{1,\ 0,\ 1\},\ \{1,\ 1,\ 1\},\ \{1,\ 1,\ 1\}\} \to 0,
\{\{1, 1, 0\}, \{0, 0, 0\}, \{0, 0, 0\}\} \rightarrow 0, \{\{1, 1, 0\}, \{0, 0, 0\}, \{0, 0, 1\}\} \rightarrow 1,
\{\{1, 1, 0\}, \{0, 0, 0\}, \{0, 1, 0\}\} \rightarrow 1, \{\{1, 1, 0\}, \{0, 0, 0\}, \{0, 1, 1\}\} \rightarrow 1,
\{\{1,\,1,\,0\},\,\{0,\,0,\,0\},\,\{1,\,0,\,0\}\} \rightarrow 1,\,\{\{1,\,1,\,0\},\,\{0,\,0,\,0\},\,\{1,\,0,\,1\}\} \rightarrow 1,
\{\{1,\,1,\,0\},\,\{0,\,0,\,0\},\,\{1,\,1,\,0\}\} \rightarrow 1,\,\{\{1,\,1,\,0\},\,\{0,\,0,\,0\},\,\{1,\,1,\,1\}\} \rightarrow 0,
\{\{1,\ 1,\ 0\},\ \{0,\ 0,\ 1\},\ \{0,\ 0,\ 0\}\} \rightarrow 1,\ \{\{1,\ 1,\ 0\},\ \{0,\ 0,\ 1\},\ \{0,\ 0,\ 1\}\} \rightarrow 1,
\{\{1, 1, 0\}, \{0, 0, 1\}, \{0, 1, 0\}\} \rightarrow 1, \{\{1, 1, 0\}, \{0, 0, 1\}, \{0, 1, 1\}\} \rightarrow 0,
\{\{1,\ 1,\ 0\},\ \{0,\ 0,\ 1\},\ \{1,\ 0,\ 0\}\} \rightarrow 1,\ \{\{1,\ 1,\ 0\},\ \{0,\ 0,\ 1\},\ \{1,\ 0,\ 1\}\} \rightarrow 0,
\{\{1,\ 1,\ 0\},\ \{0,\ 0,\ 1\},\ \{1,\ 1,\ 0\}\} \to 0,\ \{\{1,\ 1,\ 0\},\ \{0,\ 0,\ 1\},\ \{1,\ 1,\ 1\}\} \to 0,
\{\{1,\,1,\,0\}\,,\,\{0,\,1,\,0\}\,,\,\{0,\,0,\,0\}\}\,\rightarrow\,1\,,\,\{\{1,\,1,\,0\}\,,\,\{0,\,1,\,0\}\,,\,\{0,\,0,\,1\}\}\,\rightarrow\,1\,,
\{\{1,\,1,\,0\}\,,\,\{0,\,1,\,0\}\,,\,\{0,\,1,\,0\}\}\to 1,\,\{\{1,\,1,\,0\}\,,\,\{0,\,1,\,0\}\,,\,\{0,\,1,\,1\}\}\to 0,
\{\{1, 1, 0\}, \{0, 1, 0\}, \{1, 0, 0\}\} \rightarrow 1, \{\{1, 1, 0\}, \{0, 1, 0\}, \{1, 0, 1\}\} \rightarrow 0,
\{\{1, 1, 0\}, \{0, 1, 0\}, \{1, 1, 0\}\} \rightarrow 0, \{\{1, 1, 0\}, \{0, 1, 0\}, \{1, 1, 1\}\} \rightarrow 0,
\{\{1, 1, 0\}, \{0, 1, 1\}, \{0, 0, 0\}\} \rightarrow 1, \{\{1, 1, 0\}, \{0, 1, 1\}, \{0, 0, 1\}\} \rightarrow 0,
\{\{1, 1, 0\}, \{0, 1, 1\}, \{0, 1, 0\}\} \rightarrow 0, \{\{1, 1, 0\}, \{0, 1, 1\}, \{0, 1, 1\}\} \rightarrow 0,
\{\{1,\ 1,\ 0\},\ \{0,\ 1,\ 1\},\ \{1,\ 0,\ 0\}\} \to 0,\ \{\{1,\ 1,\ 0\},\ \{0,\ 1,\ 1\},\ \{1,\ 0,\ 1\}\} \to 0,
\{\{1, 1, 0\}, \{0, 1, 1\}, \{1, 1, 0\}\} \rightarrow 0, \{\{1, 1, 0\}, \{0, 1, 1\}, \{1, 1, 1\}\} \rightarrow 0,
\{\{1, 1, 0\}, \{1, 0, 0\}, \{0, 0, 0\}\} \rightarrow 1, \{\{1, 1, 0\}, \{1, 0, 0\}, \{0, 0, 1\}\} \rightarrow 1,
\{\{1,\,1,\,0\},\,\{1,\,0,\,0\},\,\{0,\,1,\,0\}\} \rightarrow 1,\,\{\{1,\,1,\,0\},\,\{1,\,0,\,0\},\,\{0,\,1,\,1\}\} \rightarrow 0,
\{\{1,\ 1,\ 0\},\ \{1,\ 0,\ 0\},\ \{1,\ 0,\ 0\}\} \rightarrow 1,\ \{\{1,\ 1,\ 0\},\ \{1,\ 0,\ 0\},\ \{1,\ 0,\ 1\}\} \rightarrow 0,
\{\{1,\ 1,\ 0\},\ \{1,\ 0,\ 0\},\ \{1,\ 1,\ 0\}\} \to 0,\ \{\{1,\ 1,\ 0\},\ \{1,\ 0,\ 0\},\ \{1,\ 1,\ 1\}\} \to 0,
\{\{1,\ 1,\ 0\},\ \{1,\ 0,\ 1\},\ \{0,\ 0,\ 0\}\} \rightarrow 1,\ \{\{1,\ 1,\ 0\},\ \{1,\ 0,\ 1\},\ \{0,\ 0,\ 1\}\} \rightarrow 0,
\{\{1,\ 1,\ 0\},\ \{1,\ 0,\ 1\},\ \{0,\ 1,\ 0\}\} \to 0,\ \{\{1,\ 1,\ 0\},\ \{1,\ 0,\ 1\},\ \{0,\ 1,\ 1\}\} \to 0,
\{\{1,\,1,\,0\}\,,\,\{1,\,0,\,1\}\,,\,\{1,\,0,\,0\}\}\to 0\,,\,\{\{1,\,1,\,0\}\,,\,\{1,\,0,\,1\}\,,\,\{1,\,0,\,1\}\}\to 0\,,
\{\{1,\,1,\,0\}\,,\,\{1,\,0,\,1\}\,,\,\{1,\,1,\,0\}\}\to 0\,,\,\{\{1,\,1,\,0\}\,,\,\{1,\,0,\,1\}\,,\,\{1,\,1,\,1\}\}\to 0\,,
\{\{1,\,1,\,0\}\,,\,\{1,\,1,\,0\}\,,\,\{0,\,0,\,0\}\}\,\rightarrow\,1,\,\{\{1,\,1,\,0\}\,,\,\{1,\,1,\,0\}\,,\,\{0,\,0,\,1\}\}\,\rightarrow\,0\,,\,\{1,\,1,\,0\}\,,\,\{1,\,1,\,0\}\,,\,\{1,\,1,\,0\}\,,\,\{1,\,1,\,0\}\,,\,\{1,\,1,\,0\}\,,\,\{1,\,1,\,0\}\,,\,\{1,\,1,\,0\}\,,\,\{1,\,1,\,0\}\,,\,\{1,\,1,\,0\}\,,\,\{1,\,1,\,0\}\,,\,\{1,\,1,\,0\}\,,\,\{1,\,1,\,0\}\,,\,\{1,\,1,\,0\}\,,\,\{1,\,1,\,0\}\,,\,\{1,\,1,\,0\}\,,\,\{1,\,1,\,0\}\,,\,\{1,\,1,\,0\}\,,\,\{1,\,1,\,0\}\,,\,\{1,\,1,\,0\}\,,\,\{1,\,1,\,0\}\,,\,\{1,\,1,\,0\}\,,\,\{1,\,1,\,0\}\,,\,\{1,\,1,\,0\}\,,\,\{1,\,1,\,0\}\,,\,\{1,\,1,\,0\}\,,\,\{1,\,1,\,0\}\,,\,\{1,\,1,\,0\}\,,\,\{1,\,1,\,0\}\,,\,\{1,\,1,\,0\}\,,\,\{1,\,1,\,0\}\,,\,\{1,\,1,\,0\}\,,\,\{1,\,1,\,0\}\,,\,\{1,\,1,\,0\}\,,\,\{1,\,1,\,0\}\,,\,\{1,\,1,\,0\}\,,\,\{1,\,1,\,0\}\,,\,\{1,\,1,\,0\}\,,\,\{1,\,1,\,0\}\,,\,\{1,\,1,\,0\}\,,\,\{1,\,1,\,0\}\,,\,\{1,\,1,\,0\}\,,\,\{1,\,1,\,0\}\,,\,\{1,\,1,\,0\}\,,\,\{1,\,1,\,0\}\,,\,\{1,\,1,\,0\}\,,\,\{1,\,1,\,0\}\,,\,\{1,\,1,\,0\}\,,\,\{1,\,1,\,0\}\,,\,\{1,\,1,\,0\}\,,\,\{1,\,1,\,0\}\,,\,\{1,\,1,\,0\}\,,\,\{1,\,1,\,0\}\,,\,\{1,\,1,\,0\}\,,\,\{1,\,1,\,0\}\,,\,\{1,\,1,\,0\}\,,\,\{1,\,1,\,0\}\,,\,\{1,\,1,\,0\}\,,\,\{1,\,1,\,0\}\,,\,\{1,\,1,\,0\}\,,\,\{1,\,1,\,0\}\,,\,\{1,\,1,\,0\}\,,\,\{1,\,1,\,0\}\,,\,\{1,\,1,\,0\}\,,\,\{1,\,1,\,0\}\,,\,\{1,\,1,\,0\}\,,\,\{1,\,1,\,0\}\,,\,\{1,\,1,\,0\}\,,\,\{1,\,1,\,0\}\,,\,\{1,\,1,\,0\}\,,\,\{1,\,1,\,0\}\,,\,\{1,\,1,\,0\}\,,\,\{1,\,1,\,0\}\,,\,\{1,\,1,\,0\}\,,\,\{1,\,1,\,0\}\,,\,\{1,\,1,\,0\}\,,\,\{1,\,1,\,0\}\,,\,\{1,\,1,\,0\}\,,\,\{1,\,1,\,0\}\,,\,\{1,\,1,\,0\}\,,\,\{1,\,1,\,0\}\,,\,\{1,\,1,\,0\}\,,\,\{1,\,1,\,0\}\,,\,\{1,\,1,\,0\}\,,\,\{1,\,1,\,0\}\,,\,\{1,\,1,\,0\}\,,\,\{1,\,1,\,0\}\,,\,\{1,\,1,\,0\}\,,\,\{1,\,1,\,0\}\,,\,\{1,\,1,\,0\}\,,\,\{1,\,1,\,0\}\,,\,\{1,\,1,\,0\}\,,\,\{1,\,1,\,0\}\,,\,\{1,\,1,\,0\}\,,\,\{1,\,1,\,0\}\,,\,\{1,\,1,\,0\}\,,\,\{1,\,1,\,0\}\,,\,\{1,\,1,\,0\}\,,\,\{1,\,1,\,0\}\,,\,\{1,\,1,\,0\}\,,\,\{1,\,1,\,0\}\,,\,\{1,\,1,\,0\}\,,\,\{1,\,1,\,0\}\,,\,\{1,\,1,\,0\}\,,\,\{1,\,1,\,0\}\,,\,\{1,\,1,\,0\}\,,\,\{1,\,1,\,0\}\,,\,\{1,\,1,\,0\}\,,\,\{1,\,1,\,0\}\,,\,\{1,\,1,\,0\}\,,\,\{1,\,1,\,0\}\,,\,\{1,\,1,\,0\}\,,\,\{1,\,1,\,0\}\,,\,\{1,\,1,\,0\}\,,\,\{1,\,1,\,0\}\,,\,\{1,\,1,\,0\}\,,\,\{1,\,1,\,0\}\,,\,\{1,\,1,\,0\}\,,\,\{1,\,1,\,0\}\,,\,\{1,\,1,\,0\}\,,\,\{1,\,1,\,0\}\,,\,\{1,\,1,\,0\}\,,\,\{1,\,1,\,0\}\,,\,\{1,\,1,\,0\}\,,\,\{1,\,1,\,0\}\,,\,\{1,\,1,\,0\}\,,\,\{1,\,1,\,0\}\,,\,\{1,\,1,\,0\}\,,\,\{1,\,1,\,0\}\,,\,\{1,\,1,\,0\}\,,\,\{1,\,1,\,0\}\,,\,\{1,\,1,\,0\}\,,\,\{1,\,1,\,0\}\,,\,\{1,\,1,\,0\}\,,\,\{1,\,1,\,0\}\,,\,\{1,\,1,\,0\}\,,\,\{1,\,1,\,0\}\,,\,\{1,\,1,\,0\}\,,\,\{1,\,1,\,0\}\,,\,\{1,\,1,\,0\}\,,\,\{1,\,1,\,0\}\,,\,\{1,\,1,\,0\}\,,\,\{1,\,1,\,0\}\,,\,\{1,\,1,\,0\}\,,\,\{1,\,1,\,0\}\,,\,\{1,\,1,\,0\}\,,\,\{1,\,1,\,0\}\,,\,\{1,\,1,\,0\}\,,\,\{1,\,1,\,0\}\,,\,\{1,\,1,\,0\}\,,\,\{1,\,1,\,0\}\,,\,\{1,\,1,\,0\}\,,\,\{1,\,1,\,0\}\,,\,\{1,\,1,\,0\}\,,\,\{1,\,1,\,0\}\,,\,\{1,\,1,\,0\}\,,\,\{1,\,1,\,0\}\,,\,\{1,\,1,\,0\}\,,\,\{1,\,1,\,0\}\,,\,\{1,\,1,\,0\}\,,\,\{1,\,1,\,0\}\,,\,\{1,\,1,\,0\}\,,\,\{1,\,1,\,0\}\,,\,\{1,\,1,\,0\}\,,\,\{1,\,1
\{\{1\text{, }1\text{, }0\}\text{, }\{1\text{, }1\text{, }0\}\text{, }\{0\text{, }1\text{, }0\}\} \rightarrow 0\text{, }\{\{1\text{, }1\text{, }0\}\text{, }\{1\text{, }1\text{, }0\}\text{, }\{0\text{, }1\text{, }1\}\} \rightarrow 0\text{, }\{1\text{, }1\text{, }0\}\text{, }\{1\text{, }1\text{, 
\{\{1,\,1,\,0\}\,,\,\{1,\,1,\,0\}\,,\,\{1,\,0,\,0\}\}\to 0\,,\,\{\{1,\,1,\,0\}\,,\,\{1,\,1,\,0\}\,,\,\{1,\,0,\,1\}\}\to 0\,,
\{\{1,\,1,\,0\}\,,\,\{1,\,1,\,0\}\,,\,\{1,\,1,\,0\}\}\to 0\,,\,\{\{1,\,1,\,0\}\,,\,\{1,\,1,\,0\}\,,\,\{1,\,1,\,1\}\}\to 0\,,
\{\{1,\,1,\,0\}\,,\,\{1,\,1,\,1\}\,,\,\{0,\,0,\,0\}\}\,\rightarrow\,0\,,\,\{\{1,\,1,\,0\}\,,\,\{1,\,1,\,1\}\,,\,\{0,\,0,\,1\}\}\,\rightarrow\,0\,,\,\{1,\,1,\,1,\,1\}\,,\,\{0,\,0,\,1\}\}\,\rightarrow\,0\,,\,\{1,\,1,\,1,\,1\}\,,\,\{0,\,0,\,1\}\}\,\rightarrow\,0\,,\,\{1,\,1,\,1,\,1\}\,,\,\{0,\,0,\,1\}\}\,\rightarrow\,0\,,\,\{1,\,1,\,1,\,1\}\,,\,\{0,\,0,\,1\}\}\,\rightarrow\,0\,,\,\{1,\,1,\,1,\,1\}\,,\,\{0,\,0,\,1\}\}\,\rightarrow\,0\,,\,\{1,\,1,\,1,\,1\}\,,\,\{0,\,0,\,1\}\}\,\rightarrow\,0\,,\,\{1,\,1,\,1,\,1\}\,,\,\{0,\,0,\,1\}\}\,\rightarrow\,0\,,\,\{1,\,1,\,1,\,1\}\,,\,\{0,\,0,\,1\}\}\,\rightarrow\,0\,,\,\{1,\,1,\,1,\,1\}\,,\,\{0,\,0,\,1\}\}\,\rightarrow\,0\,,\,\{1,\,1,\,1,\,1\}\,,\,\{0,\,0,\,1\}\}\,\rightarrow\,0\,,\,\{1,\,1,\,1,\,1\}\,,\,\{0,\,0,\,1\}\}\,\rightarrow\,0\,,\,\{1,\,1,\,1,\,1\}\,,\,\{0,\,0,\,1\}\}\,\rightarrow\,0\,,\,\{1,\,1,\,1,\,1\}\,,\,\{0,\,0,\,1\}\}\,\rightarrow\,0\,,\,\{1,\,1,\,1,\,1\}\,,\,\{0,\,0,\,1\}\}\,\rightarrow\,0\,,\,\{1,\,1,\,1,\,1\}\,,\,\{0,\,0,\,1\}\}\,\rightarrow\,0\,,\,\{1,\,1,\,1,\,1\}\,,\,\{0,\,0,\,1\}\}\,\rightarrow\,0\,,\,\{1,\,1,\,1,\,1\}\,,\,\{0,\,0,\,1\}\}\,\rightarrow\,0\,,\,\{1,\,1,\,1,\,1\}\,,\,\{0,\,0,\,1\}\}\,\rightarrow\,0\,,\,\{1,\,1,\,1,\,1\}\,,\,\{0,\,0,\,1\}\}\,\rightarrow\,0\,,\,\{1,\,1,\,1,\,1\}\,,\,\{0,\,0,\,1\}\}\,\rightarrow\,0\,,\,\{1,\,1,\,1,\,1\}\,,\,\{0,\,0,\,1\}\}\,\rightarrow\,0\,,\,\{1,\,1,\,1,\,1\}\,,\,\{0,\,0,\,1\}\}\,\rightarrow\,0\,,\,\{1,\,1,\,1,\,1\}\,,\,\{0,\,0,\,1\}\}\,\rightarrow\,0\,,\,\{1,\,1,\,1,\,1\}\,,\,\{0,\,0,\,1\}\}\,\rightarrow\,0\,,\,\{1,\,1,\,1,\,1\}\,,\,\{0,\,0,\,1\}\,,\,\{1,\,1,\,1\}\,,\,\{0,\,0,\,1\}\,,\,\{1,\,1,\,1\}\,,\,\{1,\,1,\,1\}\,,\,\{1,\,1,\,1\}\,,\,\{1,\,1,\,1\}\,,\,\{1,\,1,\,1\}\,,\,\{1,\,1,\,1\}\,,\,\{1,\,1,\,1\}\,,\,\{1,\,1,\,1\}\,,\,\{1,\,1,\,1\}\,,\,\{1,\,1,\,1\}\,,\,\{1,\,1,\,1\}\,,\,\{1,\,1,\,1\}\,,\,\{1,\,1,\,1\}\,,\,\{1,\,1,\,1\}\,,\,\{1,\,1,\,1\}\,,\,\{1,\,1,\,1\}\,,\,\{1,\,1,\,1\}\,,\,\{1,\,1,\,1\}\,,\,\{1,\,1,\,1\}\,,\,\{1,\,1,\,1\}\,,\,\{1,\,1,\,1\}\,,\,\{1,\,1,\,1\}\,,\,\{1,\,1,\,1\}\,,\,\{1,\,1,\,1\}\,,\,\{1,\,1,\,1\}\,,\,\{1,\,1,\,1\}\,,\,\{1,\,1,\,1\}\,,\,\{1,\,1,\,1\}\,,\,\{1,\,1,\,1\}\,,\,\{1,\,1,\,1\}\,,\,\{1,\,1,\,1\}\,,\,\{1,\,1,\,1\}\,,\,\{1,\,1,\,1\}\,,\,\{1,\,1,\,1\}\,,\,\{1,\,1,\,1\}\,,\,\{1,\,1,\,1\}\,,\,\{1,\,1,\,1\}\,,\,\{1,\,1,\,1\}\,,\,\{1,\,1,\,1\}\,,\,\{1,\,1,\,1\}\,,\,\{1,\,1,\,1\}\,,\,\{1,\,1,\,1\}\,,\,\{1,\,1,\,1\}\,,\,\{1,\,1,\,1\}\,,\,\{1,\,1,\,1\}\,,\,\{1,\,1,\,1\}\,,\,\{1,\,1,\,1\}\,,\,\{1,\,1,\,1\}\,,\,\{1,\,1,\,1\}\,,\,\{1,\,1,\,1\}\,,\,\{1,\,1,\,1\}\,,\,\{1,\,1,\,1\}\,,\,\{1,\,1,\,1\}\,,\,\{1,\,1,\,1\}\,,\,\{1,\,1,\,1\}\,,\,\{1,\,1,\,1\}\,,\,\{1,\,1,\,1\}\,,\,\{1,\,1,\,1\}\,,\,\{1,\,1,\,1\}\,,\,\{1,\,1,\,1\}\,,\,\{1,\,1,\,1\}\,,\,\{1,\,1,\,1\}\,,\,\{1,\,1,\,1\}\,,\,\{1,\,1,\,1\}\,,\,\{1,\,1,\,1\}\,,\,\{1,\,1,\,1\}\,,\,\{1,\,1,\,1\}\,,\,\{1,\,1,\,1\}\,,\,\{1,\,1,\,1\}\,,\,\{1,\,1,\,1\}\,,\,\{1,\,1,\,1\}\,,\,\{1,\,1,\,1\}\,,\,\{1,\,1,\,1\}\,,\,\{1,\,1,\,1\}\,,\,\{1,\,1,\,1\}\,,\,\{1,\,1,\,1\}\,,\,\{1,\,1,\,1\}\,,\,\{1,\,1,\,1\}\,,\,\{1,\,1,\,1\}\,,\,\{1,\,1,\,1\}\,,\,\{1,\,1,\,1\}\,,\,\{1,\,1,\,1\}\,,\,\{1,\,1,\,1\}\,,\,\{1,\,1,\,1\}\,,\,\{1,\,1,\,1\}\,,\,\{1,\,1,\,1\}\,,\,\{1,\,1,\,1\}\,,\,\{1,\,1,\,1\}\,,\,\{1,\,1,\,1\}\,,\,\{1,\,1,\,1\}\,,\,\{1,\,1,\,1\}\,,\,\{1,\,1,\,1\}\,,\,\{1,\,1,\,1\}\,,\,\{1,\,1,\,1\}\,,\,\{1,\,1,\,1\}\,,\,\{
\{\{1,\,1,\,0\}\,,\,\{1,\,1,\,1\}\,,\,\{0,\,1,\,0\}\}\to 0\,,\,\{\{1,\,1,\,0\}\,,\,\{1,\,1,\,1\}\,,\,\{0,\,1,\,1\}\}\to 0\,,
\{\{1,\,1,\,0\}\,,\,\{1,\,1,\,1\}\,,\,\{1,\,0,\,0\}\} \rightarrow 0\,,\,\{\{1,\,1,\,0\}\,,\,\{1,\,1,\,1\}\,,\,\{1,\,0,\,1\}\} \rightarrow 0\,,
\{\{1,\,1,\,0\}\,,\,\{1,\,1,\,1\}\,,\,\{1,\,1,\,0\}\}\to 0\,,\,\{\{1,\,1,\,0\}\,,\,\{1,\,1,\,1\}\,,\,\{1,\,1,\,1\}\}\to 0\,,
\{\{1,\ 1,\ 1\},\ \{0,\ 0,\ 0\},\ \{0,\ 0,\ 0\}\} \rightarrow 1,\ \{\{1,\ 1,\ 1\},\ \{0,\ 0,\ 0\},\ \{0,\ 0,\ 1\}\} \rightarrow 1,
\{\{1,\ 1,\ 1\},\ \{0,\ 0,\ 0\},\ \{0,\ 1,\ 0\}\}\rightarrow 1,\ \{\{1,\ 1,\ 1\},\ \{0,\ 0,\ 0\},\ \{0,\ 1,\ 1\}\}\rightarrow 0,
\{\{1,\ 1,\ 1\},\ \{0,\ 0,\ 0\},\ \{1,\ 0,\ 0\}\} \rightarrow 1,\ \{\{1,\ 1,\ 1\},\ \{0,\ 0,\ 0\},\ \{1,\ 0,\ 1\}\} \rightarrow 0,
\{\{1,\,1,\,1\}\,,\,\{0,\,0,\,0\}\,,\,\{1,\,1,\,0\}\}\to 0\,,\,\{\{1,\,1,\,1\}\,,\,\{0,\,0,\,0\}\,,\,\{1,\,1,\,1\}\}\to 0\,,
\{\{1,\,1,\,1\}\,,\,\{0,\,0,\,1\}\,,\,\{0,\,0,\,0\}\}\,\rightarrow\,1\,,\,\{\{1,\,1,\,1\}\,,\,\{0,\,0,\,1\}\,,\,\{0,\,0,\,1\}\}\,\rightarrow\,0\,,
\{\{1,\,1,\,1\}\,,\,\{0,\,0,\,1\}\,,\,\{0,\,1,\,0\}\}\to 0\,,\,\{\{1,\,1,\,1\}\,,\,\{0,\,0,\,1\}\,,\,\{0,\,1,\,1\}\}\to 0\,,
\{\{\textbf{1, 1, 1}\}\text{, }\{\textbf{0, 0, 1}\}\text{, }\{\textbf{1, 0, 0}\}\}\rightarrow \textbf{0, }\{\{\textbf{1, 1, 1}\}\text{, }\{\textbf{0, 0, 1}\}\text{, }\{\textbf{1, 0, 1}\}\}\rightarrow \textbf{0, }\{\textbf{1, 1, 1}\}\text{, }\{\textbf{0, 0, 1}\}\text{, }\{\textbf{1, 0, 1}\}\}\rightarrow \textbf{0, }\{\textbf{1, 1, 1}\}\text{, }\{\textbf{1, 0, 0, 1}\}\text{, }\{\textbf{1, 0, 0, 1}\}\}\rightarrow \textbf{0, }\{\textbf{1, 1, 1}\}\text{, }\{\textbf{1, 0, 0, 1}\}\text{, }\{\textbf{1, 0, 0, 1}\}\}\rightarrow \textbf{0, }\{\textbf{1, 0, 0, 1}\}\text{, }\{\textbf{1, 0, 0, 1}\}
\{\{1,\ 1,\ 1\}\,,\ \{0\ ,\ 0\ ,\ 1\}\,,\ \{1\ ,\ 1\ ,\ 0\}\}\,\to\,0\,,\ \{\{1\ ,\ 1\ ,\ 1\}\,,\ \{0\ ,\ 0\ ,\ 1\}\,,\ \{1\ ,\ 1\ ,\ 1\}\}\,\to\,0\,,
\{\{1, 1, 1\}, \{0, 1, 0\}, \{0, 0, 0\}\} \rightarrow 1, \{\{1, 1, 1\}, \{0, 1, 0\}, \{0, 0, 1\}\} \rightarrow 0,
\{\{1,\ 1,\ 1\}\,,\ \{0,\ 1,\ 0\}\,,\ \{0,\ 1,\ 0\}\}\to 0\,,\ \{\{1,\ 1,\ 1\}\,,\ \{0,\ 1,\ 0\}\,,\ \{0,\ 1,\ 1\}\}\to 0\,,
\{\{1, 1, 1\}, \{0, 1, 0\}, \{1, 0, 0\}\} \rightarrow 0, \{\{1, 1, 1\}, \{0, 1, 0\}, \{1, 0, 1\}\} \rightarrow 0,
\{\{1,\ 1,\ 1\},\ \{0,\ 1,\ 0\},\ \{1,\ 1,\ 0\}\} \rightarrow 0\text{, } \{\{1,\ 1,\ 1\},\ \{0,\ 1,\ 0\},\ \{1,\ 1,\ 1\}\} \rightarrow 0\text{, } \{\{1,\ 1,\ 1\},\ \{0,\ 1,\ 0\},\ \{1,\ 1,\ 1\}\} \rightarrow 0\text{, } \{\{1,\ 1,\ 1\},\ \{0,\ 1,\ 0\},\ \{1,\ 1,\ 1\}\} \rightarrow 0\text{, } \{\{1,\ 1,\ 1\},\ \{1,\ 1,\ 1\}\} \rightarrow 0\text{, } \{\{1,\ 1,\ 1\},\ \{1,\ 1,\ 1\}\} \rightarrow 0\text{, } \{\{1,\ 1,\ 1\},\ \{1,\ 1,\ 1\}\} \rightarrow 0\text{, } \{\{1,\ 1,\ 1\},\ \{1,\ 1,\ 1\}\} \rightarrow 0\text{, } \{\{1,\ 1,\ 1\},\ \{1,\ 1,\ 1\}\} \rightarrow 0\text{, } \{\{1,\ 1,\ 1\},\ \{1,\ 1,\ 1\}\} \rightarrow 0\text{, } \{\{1,\ 1,\ 1\},\ \{1,\ 1,\ 1\}\} \rightarrow 0\text{, } \{\{1,\ 1,\ 1\},\ \{1,\ 1,\ 1\}\} \rightarrow 0\text{, } \{\{1,\ 1,\ 1\},\ \{1,\ 1,\ 1\}\} \rightarrow 0\text{, } \{\{1,\ 1,\ 1\},\ \{1,\ 1,\ 1\}\} \rightarrow 0\text{, } \{\{1,\ 1,\ 1\},\ \{1,\ 1,\ 1\}\} \rightarrow 0\text{, } \{\{1,\ 1,\ 1\},\ \{1,\ 1,\ 1\}\} \rightarrow 0\text{, } \{\{1,\ 1,\ 1\},\ \{1,\ 1,\ 1\}\} \rightarrow 0\text{, } \{\{1,\ 1,\ 1\},\ \{1,\ 1,\ 1\}\} \rightarrow 0\text{, } \{\{1,\ 1,\ 1\},\ \{1,\ 1,\ 1\}\} \rightarrow 0\text{, } \{\{1,\ 1,\ 1\},\ \{1,\ 1,\ 1\}\} \rightarrow 0\text{, } \{\{1,\ 1,\ 1,\ 1\}\} \rightarrow 0\text{, } \{\{1,\ 1,\ 1\}\} \rightarrow 0\text{, } \{\{1,\ 1,\ 
\{\{1, 1, 1\}, \{0, 1, 1\}, \{0, 0, 0\}\} \rightarrow 0, \{\{1, 1, 1\}, \{0, 1, 1\}, \{0, 0, 1\}\} \rightarrow 0, \{\{1, 1, 1\}, \{0, 1, 1\}, \{0, 1, 1\}\} \rightarrow 0, \{\{1, 1, 1\}, \{0, 1, 1\}, \{0, 1, 1\}\} \rightarrow 0, \{\{1, 1, 1\}, \{0, 1, 1\}, \{0, 1, 1\}\} \rightarrow 0, \{\{1, 1, 1\}, \{0, 1, 1\}, \{0, 1, 1\}\} \rightarrow 0, \{\{1, 1, 1\}, \{0, 1, 1\}, \{0, 1, 1\}\} \rightarrow 0, \{\{1, 1, 1\}, \{0, 1, 1\}, \{0, 1, 1\}\} \rightarrow 0, \{\{1, 1, 1\}, \{0, 1, 1\}, \{0, 1, 1\}\} \rightarrow 0, \{\{1, 1, 1\}, \{0, 1, 1\}, \{0, 1, 1\}\} \rightarrow 0, \{\{1, 1, 1\}, \{1, 1\}, \{1, 1\}, \{1, 1\}, \{1, 1\}, \{1, 1\}, \{1, 1\}, \{1, 1\}, \{1, 1\}, \{1, 1\}, \{1, 1\}, \{1, 1\}, \{1, 1\}, \{1, 1\}, \{1, 1\}, \{1, 1\}, \{1, 1\}, \{1, 1\}, \{1, 1\}, \{1, 1\}, \{1, 1\}, \{1, 1\}, \{1, 1\}, \{1, 1\}, \{1, 1\}, \{1, 1\}, \{1, 1\}, \{1, 1\}, \{1, 1\}, \{1, 1\}, \{1, 1\}, \{1, 1\}, \{1, 1\}, \{1, 1\}, \{1, 1\}, \{1, 1\}, \{1, 1\}, \{1, 1\}, \{1, 1\}, \{1, 1\}, \{1, 1\}, \{1, 1\}, \{1, 1\}, \{1, 1\}, \{1, 1\}, \{1, 1\}, \{1, 1\}, \{1, 1\}, \{1, 1\}, \{1, 1\}, \{1, 1\}, \{1, 1\}, \{1, 1\}, \{1, 1\}, \{1, 1\}, \{1, 1\}, \{1, 1\}, \{1, 1\}, \{1, 1\}, \{1, 1\}, \{1, 1\}, \{1, 1\}, \{1, 1\}, \{1, 1\}, \{1, 1\}, \{1, 1\}, \{1, 1\}, \{1, 1\}, \{1, 1\}, \{1, 1\}, \{1, 1\}, \{1, 1\}, \{1, 1\}, \{1, 1\}, \{1, 1\}, \{1, 1\}, \{1, 1\}, \{1, 1\}, \{1, 1\}, \{1, 1\}, \{1, 1\}, \{1, 1\}, \{1, 1\}, \{1, 1\}, \{1, 1\}, \{1, 1\}, \{1, 1\}, \{1, 1\}, \{1, 1\}, \{1, 1\}, \{1, 1\}, \{1, 1\}, \{1, 1\}, \{1, 1\}, \{1, 1\}, \{1, 1\}, \{1, 1\}, \{1, 1\}, \{1, 1\}, \{1, 1\}, \{1, 1\}, \{1, 1\}, \{1, 1\}, \{1, 1\}, \{1, 1\}, \{1, 1\}, \{1, 1\}, \{1, 1\}, \{1, 1\}, \{1, 1\}, \{1, 1\}, \{1, 1\}, \{1, 1\}, \{1, 1\}, \{1, 1\}, \{1, 1\}, \{1, 1\}, \{1, 1\}, \{1, 1\}, \{1, 1\}, \{1, 1\}, \{1, 1\}, \{1, 1\}, \{1, 1\}, \{1, 1\}, \{1, 1\}, \{1, 1\}, \{1, 1\}, \{1, 1\}, \{1, 1\}, \{1, 1\}, \{1, 1\}, \{1, 1\}, \{1, 1\}, \{1, 1\}, \{1, 1\}, \{1, 1\}, \{1, 1\}, \{1, 1\}, \{1, 1\}, \{1, 1\}, \{1, 1\}, \{1, 1\}, \{1, 1\}, \{1, 1\}, \{1, 1\}, \{1, 1\}, \{1, 1\}, \{1, 1\}, \{1, 1\}, \{1, 1\}, \{1, 1\}, \{1, 1\}, \{1, 1\}, \{1, 1\}, \{1, 1\}, \{1, 1\}, \{1, 1\}, \{1, 1\}, \{1, 1\}, \{1, 1\}, \{1, 1\}, \{1, 1\}, \{1, 1\}, \{1, 1\}, \{1, 1\}, \{1, 1\}, \{1, 1\}, \{1, 1\}, \{1, 1\}, \{1, 1\}, \{1, 1\}, \{1, 1\}, \{1, 1\}, \{1, 1\}, \{1, 1\}, \{1, 1\}, \{1, 1\}, \{1, 1\}, \{1, 1\}, \{1, 1\}, \{1, 1\}, \{1, 1\}, \{1, 1\}, \{1, 1\}, \{1, 1\}, \{1, 1\}, \{1, 1\}, \{1, 1\}, \{1, 1\}, \{1, 1\}, \{1, 1\}, \{1, 1\}, \{1, 1\}, \{1, 1\}, \{1, 1\}, \{1, 1\}, \{1, 1\}, \{1, 1\}, \{1, 1\}, \{1, 1\}, \{1, 1\}, \{1, 1\}, \{1, 1\}, \{1, 1\}, \{1, 1\}, \{1
\{\{1, 1, 1\}, \{0, 1, 1\}, \{0, 1, 0\}\} \rightarrow 0, \{\{1, 1, 1\}, \{0, 1, 1\}, \{0, 1, 1\}\} \rightarrow 0,
\{\{1,\ 1,\ 1\},\ \{0,\ 1,\ 1\},\ \{1,\ 0,\ 0\}\} \to 0,\ \{\{1,\ 1,\ 1\},\ \{0,\ 1,\ 1\},\ \{1,\ 0,\ 1\}\} \to 0,
\{\{1, 1, 1\}, \{0, 1, 1\}, \{1, 1, 0\}\} \rightarrow 0, \{\{1, 1, 1\}, \{0, 1, 1\}, \{1, 1, 1\}\} \rightarrow 0,
\{\{1, 1, 1\}, \{1, 0, 0\}, \{0, 0, 0\}\} \rightarrow 1, \{\{1, 1, 1\}, \{1, 0, 0\}, \{0, 0, 1\}\} \rightarrow 0,
\{\{1, 1, 1\}, \{1, 0, 0\}, \{0, 1, 0\}\} \rightarrow 0, \{\{1, 1, 1\}, \{1, 0, 0\}, \{0, 1, 1\}\} \rightarrow 0,
\{\{1, 1, 1\}, \{1, 0, 0\}, \{1, 0, 0\}\} \rightarrow 0, \{\{1, 1, 1\}, \{1, 0, 0\}, \{1, 0, 1\}\} \rightarrow 0,
\{\{1, 1, 1\}, \{1, 0, 0\}, \{1, 1, 0\}\} \rightarrow 0, \{\{1, 1, 1\}, \{1, 0, 0\}, \{1, 1, 1\}\} \rightarrow 0,
\{\{1,\ 1,\ 1\},\ \{1,\ 0,\ 1\},\ \{0,\ 0,\ 0\}\} \to 0,\ \{\{1,\ 1,\ 1\},\ \{1,\ 0,\ 1\},\ \{0,\ 0,\ 1\}\} \to 0,
\{\{1,\ 1,\ 1\},\ \{1,\ 0,\ 1\},\ \{0,\ 1,\ 0\}\} \to 0,\ \{\{1,\ 1,\ 1\},\ \{1,\ 0,\ 1\},\ \{0,\ 1,\ 1\}\} \to 0,
\{\{1,\ 1,\ 1\},\ \{1,\ 0,\ 1\},\ \{1,\ 0,\ 0\}\} \to 0\,,\ \{\{1,\ 1,\ 1\},\ \{1,\ 0,\ 1\},\ \{1,\ 0,\ 1\}\} \to 0\,,
\{\{1, 1, 1\}, \{1, 0, 1\}, \{1, 1, 0\}\} \rightarrow 0, \{\{1, 1, 1\}, \{1, 0, 1\}, \{1, 1, 1\}\} \rightarrow 0,
\{\{1, 1, 1\}, \{1, 1, 0\}, \{0, 0, 0\}\} \rightarrow 0, \{\{1, 1, 1\}, \{1, 1, 0\}, \{0, 0, 1\}\} \rightarrow 0,
\{\{1,\ 1,\ 1\},\ \{1,\ 1,\ 0\},\ \{0,\ 1,\ 0\}\} \to 0,\ \{\{1,\ 1,\ 1\},\ \{1,\ 1,\ 0\},\ \{0,\ 1,\ 1\}\} \to 0,
\{\{1, 1, 1\}, \{1, 1, 0\}, \{1, 0, 0\}\} \rightarrow 0, \{\{1, 1, 1\}, \{1, 1, 0\}, \{1, 0, 1\}\} \rightarrow 0,
\{\{1,\ 1,\ 1\},\ \{1,\ 1,\ 0\},\ \{1,\ 1,\ 0\}\} \to 0,\ \{\{1,\ 1,\ 1\},\ \{1,\ 1,\ 0\},\ \{1,\ 1,\ 1\}\} \to 0,
\{\{1,\ 1,\ 1\},\ \{1,\ 1,\ 1\},\ \{0,\ 0,\ 0\}\} \to 0,\ \{\{1,\ 1,\ 1\},\ \{1,\ 1,\ 1\},\ \{0,\ 0,\ 1\}\} \to 0,
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 \{\{1, 1, 1\}, \{1, 1, 1\}, \{0, 1, 0\}\} \rightarrow 0, \{\{1, 1, 1\}, \{1, 1, 1\}, \{0, 1, 1\}\} \rightarrow 0, \\ \{\{1, 1, 1\}, \{1, 1, 1\}, \{1, 0, 0\}\} \rightarrow 0, \{\{1, 1, 1\}, \{1, 1, 1\}, \{1, 0, 1\}\} \rightarrow 0, \\ \{\{1, 1, 1\}, \{1, 1, 1\}, \{1, 1, 0\}\} \rightarrow 0, \{\{1, 1, 1\}, \{1, 1, 1\}, \{1, 1, 1\}\} \rightarrow 0\}
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Mathematicaの作者であるスティーブン・ウルフラムは、256通りのルールがある3近傍2色の1次元セルオートマトンの挙動をしらみつぶしに計算し、そこから4つのクラスを導いた。しかし2色9近傍2次元セルオートマトンの場合、ルールの数が多いので、完全なしらみつぶしによる方法は困難である。そこでまず上記のライフゲームのルールを出発点に、その近傍のルールを少しずつしらみつぶしに計算してみることで、ミニマルな初期条件と決定的なアルゴリズムから生み出される、予測不可能な造形の可能性を発見的に[注2]探求した。

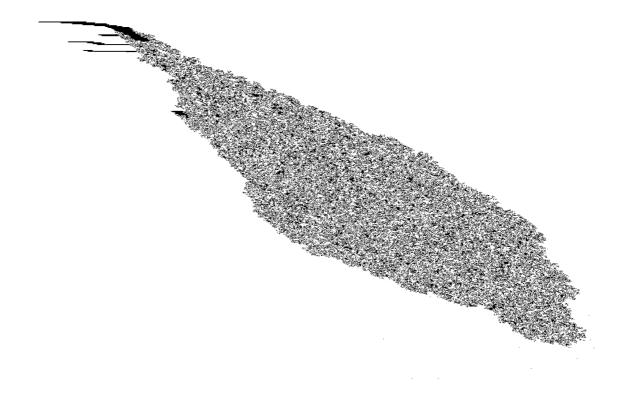
[注2] 実際には「発見した」というよりもむしろ「出会った」という方が近い。ただし 決定的であるということは、計算を行わなずとも、すべてが事前に存在している、ということでもある。

例えば、

3121796387206642884643857416353388816364758858874716286199733047244606561418987700322611464790005 242280784132089221851121096915552864518716024029という、ライフゲームと下3桁の数のみが異なるルール番号のルールを用いた場合、1つの点だけを出発点としても、4096ステップの計算後には、以下のような1965×1964ドットのグリッド上に拡がる形態が生成される。内部は斑状であり、境界は不規則かつ不定形であり、多数の小片が飛散している。

ArrayPlot[First[CellularAutomaton[

2, $\{1, 1\}\}$, $\{\{\{1\}\}\}$, $0\}$, 4096, -1]], Frame \rightarrow False]



ミニマリズムとアルゴリズム

こうした、ミニマルな初期条件と決定的な反復アルゴリズムによる造形は、1960年代の初頭に、素材の組み合せとその構造に関する事実を全面に出すことで、対象そのものに対する関心とそれを知覚体験する行為にフォーカスを当てたミニマリズム美術を、自然と思い起こさせる。初期値としてのドットは、デジタル表現における最も基本的な素材であり、セルオートマトンのアルゴリズムは、そこから構造や形態を自律的に生成する。

ミニマリズムの代表的な作家のひとりであるドナルド・ジャッドは、鉄やアルミ、ガラスといった物質的な具体性を持つ工業用素材と規則的・反復的な形態を用いることで、作品にイリュージョンやメタファーの入り込む余地をなくした。そのことは、アルゴリズムを明確に記述したプログラムとそれを正確に実行する計算を素材とするアルゴリズム・アートにおいても同様である。ミニマリストの中にはメル・ボックナーのように、順列集合、フィボナッチ数列、回転や逆順のような数学的操作をデッサンやレリーフで直接表現したアーティストもいた。

ミニマル・アートのシンプルな幾何学的表象は、そこにフィジカルな物質性や空間性を介在させることで、鑑賞者から対象に関するマキシマムな知覚や解釈を引きだした。本作品においても、シンプルなアルゴリズムによって生み出された人間の主観や偶然性を廃した形態が内包する予測不可能な複雑性が、その表象を知覚し解釈すること自体にフォーカスを当てる。こうしたアルゴリズムの計算によるミニマリスティックなアプローチを「Computational Minimalism (計算ミニマリズム)」と呼ぶことができるだろう。その中核にあるのは、単純なシステムから複雑な形態を生成する「Complex Simplicity (複雑な単純性)」である。そこではミニマリズム同様に、作品を作る過程は重視されない。コンセプトの実体としてのアルゴリズムだけが重要なのであり、プロセスとしてのアルゴリズムはただ、プログラムとして明晰に記述され、ハードウェアによって正確かつ高速に実行されれば良い。

計算する宇宙

1941年に、世界初のプログラム制御式コンピュータ「Zuse Z3」を完全動作させた、ドイツ人技術者のコンラッド・ツーゼは、1969年(コンウェイのライフゲームが登場する70年以前)に「Rechnender Raum (Calculating Space 計算する宇宙)」という論文を出版した。これは宇宙全体がいわばセルオートマトンのような、離散化されたグリッド上の計算から生れていると考えるものであり、「人間によるものであれ、自然界のものであれ、すべての現象はコンピュテーションの産物である」と考えるウルフラムの著書(思想)『A New Kind of Science』の起源ともなる重要なテキストである。ツーゼはその論文で、古典物理学、量子物理学、そして計算する空間(デジタル物理学)の3つを比較し論じているが、今日までツーゼの理論に反する物理現象は見つかっていない。

同様に、MITやボストン大学の教授職を歴任したエドワード・フレドキンも「デジタル物理学」、今では「デジタル哲学」として、ツーゼ同様に宇宙は巨大なセル・オートマトンであり、私たちが見たり感じたりしているのはそこから生れる情報である、と強く主張した。

アイシュタインの重力理論(相対性理論)と物質の究極の姿を探る量子論を結ぶことを目指した、最新の「ループ量子重力」理論は、従来のニュートン力学や量子力学が前提としてきた連続的な時間や空間を背景としていない。時空はスピンという素粒子が持っている属性のネットワーク(スピン・ネットワーク)から二次的に生み出されるものであり、宇宙はスピンというノードとそのリンクによる抽象的なネットワークに還元することができると主張する。この理論は同時に、時間と空間をどんどん細かく分割していくと、ついには分割不可能なサイズに到達することを予測しており、それは時間も空間も究極にはデジタルであることを意味している。ツーゼやフレドキン、そしてウルフラムが主張するように、宇宙の基本的構造は本当にアルゴリズミックに計算される巨大なセルオートマトンのようなものなのかもしれない。だとすればそれは、宇宙の縮図であり、部分であり、本性でもあるといえるのだ。

計算する宇宙におけるアートは一体どのようなものになるだろう。決定的な世界では、計算を行わなくとも すべてが事前に存在しており、自由意志も単なる幻想に過ぎないとすれば、多くの計算の中から、私がこの 数少ない結果と出会い選択したということが、そこでは一体どういう意味を持つのだろう。あるいはアート には、可能性の総体としてのランダム性、確率性が必要不可欠なのか。アルゴリズム・アートは、そうした 宇宙と計算に関する本質的な問いかけを提起する。

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