

# Lower Limb Motion Estimation

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Kinematic Modelling and Estimation of the Gait using Cameras

and an IMU



Prepared by:

**Johann Hendrik Joosten**

Department of Electrical and Electronics Engineering  
University of Cape Town

Prepared for:

**Dr. Amir Patel**

Department of Electrical and Electronics Engineering  
University of Cape Town

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University of Cape Town in partial fulfilment of the academic requirements for a  
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# Terms of Reference

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## Title

Lower Limb Motion Estimation - Kinematic Modelling and Estimation of the Gait using Cameras and an IMU

## Description

Recent breakthroughs in the field of artificial intelligence has invigorated the pursuit of humanoid robots. Unfortunately, modern bipedal robots lack the elegance of motion and fluidity observed in nature. Perhaps then a modern take on the lower limb kinematics of humans could provide insight to the field of bio-inspired robotics. By using modern cameras with minimal volume and accurate sensors, data capture systems can be transferred onto the subjects in question. This methodology allows for a much larger spectrum of motion capture and can greatly improve our understanding of movement in the unconstrained real world.

## Deliverables

The following items have been identified as critical deliverables for the project: Functional harness to hold data capture equipment. Kinematic model of the human lower-limbs. Estimation and fusion algorithm to process captured data.

## Skills and Requirements

Mechanical Design, Electrical Design, Programming and Modelling.

## Area

Computer Vision, Sensors, Biomechanics and Bio-inspired Robotics.

## Declaration

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**November 7, 2017**

## Acknowledgements

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I would like to thank Dr Amir Patel for supervising this project, without whom this work would not have been possible. Also to Neil Steenkamp for helping me whenever I had questions. Lastly I would also like to thank Bradley Stocks for the foundational work he has done in this field and his efforts in documenting it.

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## Abstract

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This research aims to extend the work completed by the Mechatronics Lab at the University of Cape town that studied the use of subject borne cameras to analyse, model and estimate the kinematic motion of a cheetah tail. Image processing has progressed significantly within the last few years and studying motion with subject borne cameras allows data capture in unconstrained environments. With this improvements in sensor technology and long standing techniques of data fusion and state estimation new models for complex motion can be created.

This research proposes a methodology for understanding the bipedal motion of humans in natural environments using wearable data capture systems consisting of cameras and sensors. The system is designed using common engineering methods and a prototype constructed using limited resources.

Testing is then performed and a dataset successfully obtained. This dataset is processed and applied to a model to better quantify critical elements of the human gait using software tools.

The proposed system is novel and serves as a proof of concept that can be adapted and improved based on the availability of equipment and end user needs. The research concludes by analysing the methodology and identifying its general strengths and weaknesses, with opportunities for future listed.

# Contents

Terms of Reference . . . . .	2
Declaration . . . . .	3
Acknowledgements . . . . .	4
Abstract . . . . .	5
Glossary . . . . .	13
Symbols . . . . .	14
<b>1 Introduction</b>	<b>15</b>
1.1 Background to the Study . . . . .	15
1.2 Objectives of the Study . . . . .	16
1.3 Scope and Limitations . . . . .	17
1.4 Plan of Development . . . . .	18
<b>2 Literature Review</b>	<b>20</b>
2.1 Introduction . . . . .	20
2.2 Human Motion and Gait . . . . .	21
2.3 Computer Vision . . . . .	21
2.3.1 Computer Vision in Robotics . . . . .	22
2.3.2 New Perspectives from Animal Borne Cameras . . . . .	23

2.3.3	Human Motion Analysis Using Computer Vision . . . . .	23
2.4	Inertial Measurement Units and Sensors . . . . .	24
2.4.1	Global Position System . . . . .	25
2.4.2	Inertial Measurement Units in Robotics . . . . .	25
2.4.3	Human Motion Analysis Using Sensors . . . . .	26
2.5	Mathematical Modelling . . . . .	26
2.5.1	Mathematical Models of the Gait . . . . .	26
2.5.2	Linear Kinematics . . . . .	27
2.5.3	Rotational Matrices . . . . .	28
2.5.4	Kalman Filter and Extended Kalman Filter . . . . .	29
2.6	Natural Solutions for Robotic Shortcomings . . . . .	29
2.7	Conclusion . . . . .	30
<b>3</b>	<b>Methodology</b>	<b>32</b>
3.1	System Design . . . . .	32
3.2	Modelling the Lower Limbs . . . . .	34
3.3	Experimental Details . . . . .	35
3.4	Limitations . . . . .	35
<b>4</b>	<b>Designing the Data Capture System</b>	<b>37</b>
4.1	GoPro Hero Session Camera . . . . .	37
4.2	Camera Mount Design . . . . .	39
4.3	Smartphone Mount Design . . . . .	40
4.4	Vision Calibration . . . . .	41
4.5	Smartphone Calibration . . . . .	42

4.5.1	Accelerometer . . . . .	42
4.5.2	Gyroscope . . . . .	42
4.6	Critical Point Markers . . . . .	42
<b>5</b>	<b>Processing the Captured Data</b>	<b>44</b>
5.1	Processing the IMU Data . . . . .	44
5.1.1	Obtaining IMU Data . . . . .	45
5.1.2	Synchronizing IMU Data . . . . .	45
5.1.3	Preprocessing IMU Data . . . . .	46
5.1.4	Exporting IMU Data . . . . .	46
5.2	Processing the Video Data . . . . .	47
5.2.1	Obtaining Video Data . . . . .	47
5.2.2	Synchronizing Video Sources . . . . .	47
5.2.3	Cutting Critical Video Data . . . . .	48
5.2.4	Undistorting the Video Data . . . . .	48
5.2.5	Tracking and Exporting Marker Positions in the Frame . . . . .	49
5.3	On units . . . . .	51
5.4	On Frames of Reference . . . . .	51
<b>6</b>	<b>Data Fusion and State Estimation</b>	<b>52</b>
6.1	Prediction Equations . . . . .	53
6.2	Measurement Equations . . . . .	54
6.2.1	Euler Matrices . . . . .	54
6.2.2	Direct Cosine Matrix . . . . .	54
6.2.3	Inverse kinematics . . . . .	54

6.3	Understanding the Data Sources . . . . .	55
6.4	State Estimation . . . . .	55
6.5	Q Matrix, R Matrix and Initialization . . . . .	56
6.5.1	Defining the Q Matrix . . . . .	56
6.5.2	Defining the R Matrix . . . . .	56
6.5.3	Choosing Initial States . . . . .	57
6.5.4	Initializing the Covariance Matrix P . . . . .	57
<b>7</b>	<b>Results, Verification and Discussion</b>	<b>58</b>
7.1	Results . . . . .	58
7.1.1	System Design Results . . . . .	58
7.1.2	Model Results . . . . .	58
7.1.3	Captured and Processed Data . . . . .	59
7.1.4	EFK Results . . . . .	60
7.2	Discussion . . . . .	60
<b>8</b>	<b>Conclusions and Future Work</b>	<b>61</b>
8.1	Conclusion . . . . .	61
8.2	Future work . . . . .	61

# List of Figures

1.1 Left: Vicon motion capture system tracking the human gait (from [3]) Right: The Xsens MVN motion capture suit (from [5]) . . . . .	16
1.2 A cheetah wearing the wearable motion capture system designed by Stocks [7]	17
1.3 Flow chart outlining the report structure . . . . .	19
2.1 Pictures of modern bipedal robots Atlas (left) and Cassie (right) from [18] and [19] respectively . . . . .	21
2.2 Insight into object classification by Tesla, image from [25] . . . . .	22
2.3 Dollphins wearing dorsal mounted cameras, image from [28] . . . . .	23
2.4 Dollphins wearing dorsal mounted cameras, image from [5] . . . . .	24
2.5 Basic kinematic model to demonstrate . . . . .	28
2.6 Different bipedal and quadroped robots created by Boston Dynamics, image from [43] . . . . .	30
3.1 Diagram showing the progression and dependence of the major stages of this project . . . . .	32
3.2 Rigid beam model used to model the lower limbs of a biped . . . . .	34
4.1 3D CAD rendering of the GoPro Hero Session action camera . . . . .	37
4.2 Initial camera enclosure designed by the mechatronics lab . . . . .	39
4.3 Final dual camera enclosure designed by the author . . . . .	40
4.4 Action Mounts chest mount showing the front mounting plate . . . . .	40

4.5	stabilizer . . . . .	41
4.6	Subject wearing Green and Pink Markers to identify critical points . . . . .	43
5.1	Diagram showing the progression and dependence of the major stages of video processing in the project . . . . .	44
5.2	Androsensor Screenshots from [49] . . . . .	45
5.3	Figure demonstrating the frame of reference of the smartphone . . . . .	46
5.4	Diagram showing the progression and dependence of the major stages of video processing in the project . . . . .	47
5.5	Figure showing the user interface of SVP video editing software . . . . .	48
5.6	4 Frames from the different cameras combined . . . . .	49
5.7	Using the dltdv toolbox in MATLAB to export marker coordinates . . . . .	50
7.1	subject wearing the motion capture system . . . . .	59
7.2	. . . . .	59
7.3	. . . . .	60
7.4	iamge processing things . . . . .	60
8.1	ethics clearance . . . . .	63

# List of Tables

3.1	Known design elements of the project . . . . .	33
4.1	Possible frame rate and resolution combinations on the GPHS camera . .	38
5.1	This table shows the different headings of the output IMU file . . . . .	46
5.2	Table showing the relation between points and markers . . . . .	51
6.1	Table showing the different states of the model to be determined by the EKF . . . . .	52

# Glossary

Abbreviations listed here are used throughout the document.

- DOF - Degrees Of Freedom
- GPHS - GoPro Hero Session
- MEMS - Micro Electromechanical System
- CSV - Comma Separated Values
- 3D - Three Dimensional
- IMU - Inertial Measurement Unit
- KF - Kalman Filter
- EKF - Extended Kalman Filter
- CAD - Computer Aided Design
- SVP - Sony Vegas Pro

# Symbols

Mathematical Symbols listed here are used throughout the document.

- $\phi$  - Roll
- $\theta$  - Pitch
- $\psi$  - Yaw
- $X$  - States of the System
- $Q$  - Process Noise Matrix
- $X$  - States of the System
- $R$  - Measurement Noise Matrix

# Chapter 1

## Introduction

### 1.1 Background to the Study

Human motion capture systems are often very costly and confine the capture area to a certain confined space. These limitations prevent us from understanding bipedal motion in complex environments, knowledge that proves to be critical in the development of functional humanoid robotics. Examples of such systems can be seen in [1] where 8 cameras and stereo vision was used to recreate a 3D model of a walking person and in [2] where 10 Vicon cameras and a full body marked suit was used for the same objective.

A popular approach taken to overcome the spatial limitations inherent in camera based systems is the use of body mounted sensor networks. A commercial sensor suit developed by XSens and demonstrated in [3] can accurately recreate a 3D model of human motion using inertial sensors and data fusion. Similar work completed by Seel et al. [4] further proves the accuracy of such systems. Although the mentioned systems overcome the stated limitations; they do so at increased complexity and cost. They often lack modularity and proprietary software is difficult to adapt.

Recent work [6] completed by the Mechatronics Lab at the University of Cape Town showed data capture with both subject-borne cameras and sensors can be used to better understand unconstrained movement in a natural environment. This was based on research completed by Stocks [7] at the same laboratory. The presented work showed the successful kinematic modelling of a cheetah (*Acinonyx jubatus*) tail whilst running freely. The importance of understanding motion in the natural world is outlined in [8] and is the cornerstone of biomimicry as defined by [9].



Figure 1.1: Left: Vicon motion capture system tracking the human gait (from [3]) Right: The Xsens MVN motion capture suit (from [5])

## 1.2 Objectives of the Study

Depth imagery in the field of human motion capture has been extensively reviewed in [10], where the lack of data from complex movements in different environments is listed as a challenge. This reaffirms the difficulty stated in the previous section. Solely relying on motion sensors to understand the gait has been reviewed by [11]. Although this approach was found to be accurate for external environments it has limitation with respect to cost and sensor disturbance. From these reviews it is clear that a middle ground must exist that can combine the strengths of the approaches to provide a holistic solution.

This research project aims to show that subject-borne sensors, primarily a combination of cameras and IMUs, can provide researchers in the field of health sciences, biomechanics and biomimicry with extensive datasets to better understand and model the bipedal motion of humans. It builds on the foundational work presented by Stocks and Patel [7] and envisions to implement a similar system to track data points on the lower limbs of a runner. The original prototype system is shown below.

Finally this thesis will pay close attention to similarities in understanding the human gait using technologies used to control the dynamics of bipedal humanoid robots. Since these robots attempt to imitate human motion many of the key principles in the field of robotics relates directly to the bio-mechanics of humans.

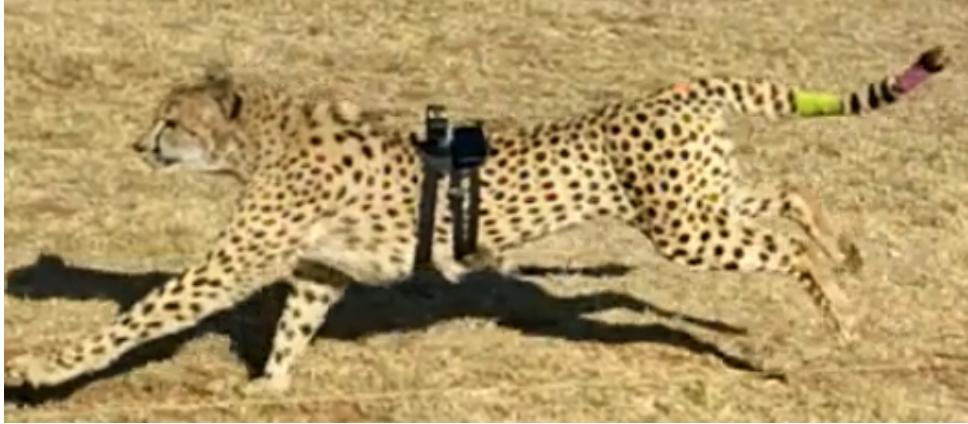


Figure 1.2: A cheetah wearing the wearable motion capture system designed by Stocks [7]

### 1.3 Scope and Limitations

The scope of this research is to model and estimate the human lower limbs during a flat ground steady state run. The motion will be estimated by determining the different joint angles as well as the motion of the runner w.r.t. the inertial frame. Joint angles are a popular method of quantization and the availability of rich datasets allow comparative analysis on the final findings of this work. This is the first logical step in the iterative design process to eventually understand movement in complex environments using wearable motion capture systems.

The availability of equipment also influenced the quality and accuracy of the system. Due to financial constraints the system was designed to use available hardware and minimize additional expenses. Although the the system designed cannot be classified as low cost, when compared to other methods of motion capture it becomes financially attractive. The components selected are also interchangeable and need not exactly match the specifications presented herein.

It should be noted that the research presented herein does not seek to push the boundaries of modern sensor technology, nor does it wish to re-imagine understood and accepted models of natural phenomena. Instead, a methodology is proposed that brings together systems from exciting disciplines of research such that richer datasets can be generated and studied. This research therefore serves as a proof of concept for a novel wearable motion capture technology.

There is another distinction to make with regard to scope of the project and that is the distinction between kinematics and dynamics. This project is aimed at understanding, modelling and estimating the kinematics of lower limbs, that is to say the movement and

motion of the lower limbs but not the forces and torques causing them. These forces are important elements of motion, but require some adoption to the proposed methodology to understand.

Furthermore this thesis will not compare different running styles or comment on their energy efficiency. Interpreting and rehabilitating the human gait is best left to medical professionals. This system may be applicable to work done in such professions, but the task of developing this system is one of engineering.

Finally a large portion of this project relies on software written for MathWorks' MATLAB [12]. This software is single purpose and serves only this thesis. The software itself is not meant to be modular or generalized, yet can serve as a guideline for research using a similar methodology. The software can be found on the accompanying disc. Some software snippets of critical importance has been added to this thesis to highlight the important aspects of implementing the various mathematical constructs. The various Dassault Systmes SOLIDWORKS [13] models are also present on the same disc. These models are also specific to this thesis and can only provide insight for adoptions.

## 1.4 Plan of Development

The following chapter contains an extensive literature review where various methods of modelling and verifying the human gait has been discussed. There are also sections dedicated to subject borne data capture, computer vision, inertial measurement units (motion sensors), humanoid robotics and mathematical modelling.

This is followed by a chapter titled methodology that presents the planning and ideation of the thesis. It serves as a link between the theoretical work presented in the literature review and the engineering approach and application detailed in the chapters that follow it. It lays out a plan and shows how engineering specifications were generated from a generally defined problem.

The final three chapters that make up the body of this report are titled "Designing the Data Capture System", "Processing the Captured Data" and "Data Fusion and State Estimation" in order of appearance. True to their title they present the processes followed to complete the major milestones of the project.

In closing a chapter is dedicated to presenting and discussing the results obtained, followed by the final chapter that draws conclusions from the presented work and makes recommendations on future work. The following flow diagram summarizes the progression

of this report.

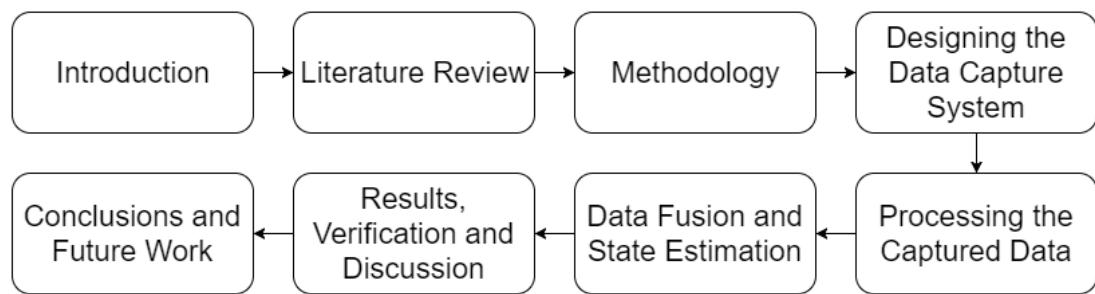


Figure 1.3: Flow chart outlining the report structure

# Chapter 2

## Literature Review

This section reviews various academic sources related to the methodology proposed. It will look at the various fields of engineering as well as bio-mechanics, biomimicry and applied mathematics to form a holistic understanding of the design space. Importantly the technologies discussed will also be related to the field of robotics as many concepts transfer easily from bipedal humans to bipedal robots.

### 2.1 Introduction

This research project brings together various disciplines of research. By combining techniques from computer vision, sensors and data fusion we can design and develop new way of capturing human gait data. Whilst the fields of biomimicry and bio-inspired robotics are relatively new, recent advances in related fields such as artificial intelligence and robotics have invigorated the pursuit of functional humanoid robotics.

Kaneko et al. described various components of humanoid robotics in [14]. Herein a fundamental element of dynamics is discussed and improvements to the robots mobility outlined as the first step in the iterative design process. The same author published work [15] relating to a functional leg module to be used for such robotic projects. These works shows that engineers have been trying to replicate the bipedal motion of humans for some time wit relatively limited success.

If we observe some of the worlds foremost attempts at bipedal robotics such as Boston Dynamics' Atlas [16] and Agility Robotics' Cassie [17] we can see that recent attempts are improving rapidly. This thesis believes that with bigger datasets of human motion in complex environments we can better design and control robotic lower limbs.

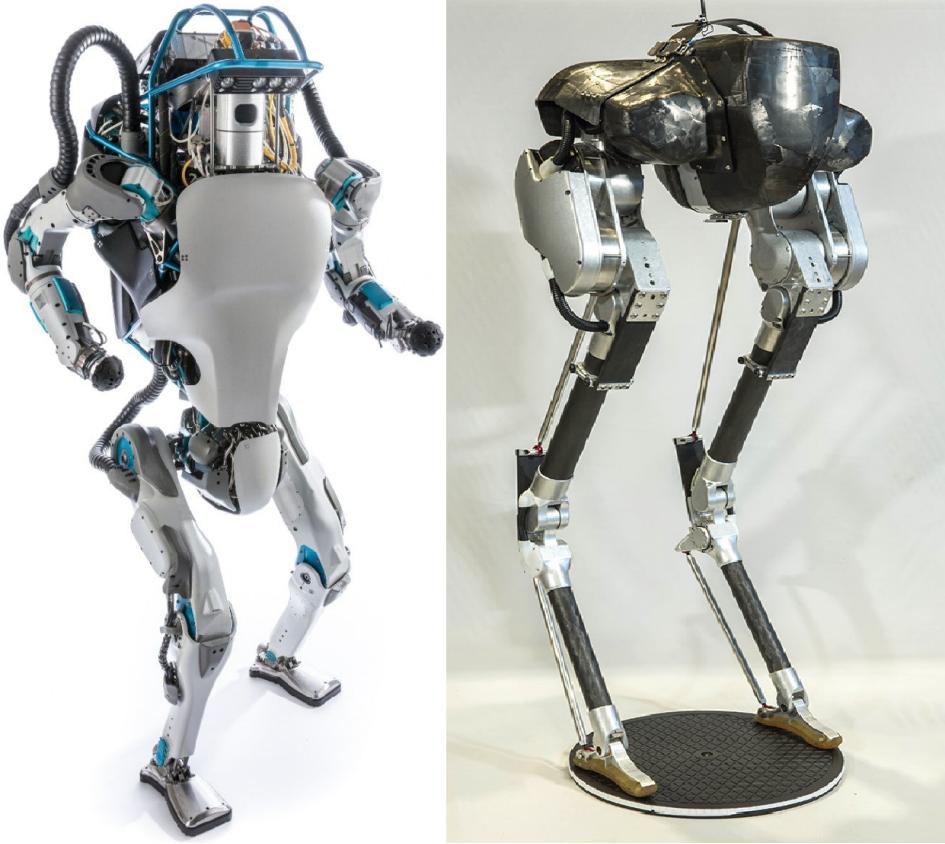


Figure 2.1: Pictures of modern bipedal robots Atlas (left) and Cassie (right) from [18] and [19] respectively

## 2.2 Human Motion and Gait

The human gait is well understood and has been studied in detail as it is a fundamental part of human mobility. It is one of the first skills developed in infancy and its importance for healthy development, as outlined by Adolph et al. [20], cannot be understated. Walking and running are also critical factors in transportation and geographical movement of people and goods in developing countries where public transport is underdeveloped and private transport not within the means of the populous. Finally walking and running as exercise has proven benefits as shown in [21] (general health) and [22] (mental health). There is thus clear evidence that the human gait has earned its right as a field of study in academia.

## 2.3 Computer Vision

While the previous section answers "why" understanding the human gait is important, the following sections will explain fields that contribute to the question of "how" the

gait is studied. The technologies and methods used to quantify it. This section titled computer vision should be interpreted within the context of this document. It will be used interchangeable with image processing as the underlying philosophies of both methodologies are algorithmic interpretation of images.

Image processing as a field was born from digital signal processing as it relates to the extraction of critical data from noisy data streams. Computer vision is the use of computational methods to achieve the same end goal; ultimately trying to emulate human vision. Image Processing has many different approaches and methodologies. These include but are not limited to feature detection, pattern recognition and classification. Modern works such as [23] and [24] have shown how neural networks perform previously mentioned tasks with unprecedented accuracy.

### 2.3.1 Computer Vision in Robotics

Recent improvements to real time image processing has allowed amazing technological breakthroughs in fields closely related to robotics. One such breakthrough is the rapid improvement of self-driving cars developed by Tesla. These vehicles use vision based technologies and real time image processing to navigate complex and changing road networks. The figure below shows how a Tesla identifies different roadside artefacts.



Figure 2.2: Insight into object classification by Tesla, image from [25]

Another interesting use for computer vision in robotics is the ability to identify and classify real world objects. This allows for robotics to perform menial household tasks. Finally work completed by Taylor et al. [26] shows the importance in computer vision in robotics assisted surgery. Computer vision is an important step in automatizing robotics and due to the rapid progression in artificial intelligence, it is a field with a large potential

for growth.

### 2.3.2 New Perspectives from Animal Borne Cameras

Patel et al. [6] showed that using animal borne cameras and motion sensors, the tail kinematics of the cheetah (*Acinonyx Jubatus*) could be tracked. Patel's work was partly inspired by Kane et al. [27] where falcon (*Falco Peregrinus*) borne cameras were used to better understand airborne pursuit of prey. Giving researchers a new perspective on the behaviour of animals in the natural world.

Further work completed by Pearson et al. [28] showed that cameras mounted to dolphins (*Lagenorhynchus Obscurus*) could provide insight into their movement, social and foraging strategies. Using cameras to study ocean-life has become a popular methodology in recent time due to difficulties imposed by their environment. In essence we struggle to understand flying and swimming animals due to their complex environments. The following image shows how these devices are carried by various dolphins.



Figure 2.3: Dolphins wearing dorsal mounted cameras, image from [28]

The above research has shown the unique benefits of having cameras and sensors mounted to the subject in question.

### 2.3.3 Human Motion Analysis Using Computer Vision

From Chen et al. [10] using depth imagery to understand human motion we can see that this is a popular technique. Because imaging is a popular method in medical research imaging various human movements has a large set of well established methodologies. Naturally this has formed a foundation of using cameras to capture human movement. Companies like Vicon, Optitrack and Motion Analysis have created multiple consumer products for quantifying motion using cameras. The following image shows a typical motion capture setup using multiple cameras.

One system often used for motion capture is the Microsoft developed Kinect. [29] [30] [31] have shown positive results in modelling and quantifying the human gait using this technology. Open source software like OpenKinect allows for easy implementation and



Figure 2.4: Dollphins wearing dorsal mounted cameras, image from [5]

configuration. A drawback to this methodology is that all of these works require controlled environments due to the nature of the technology.

A thorough search for wearable system using cameras to identify critical points on the lower limbs was done, but no pre-existing research was found. It was concluded that this thesis is novel and exploring a new approach to understanding lower limb kinematics.

## 2.4 Inertial Measurement Units and Sensors

IMU's are a staple of electrical engineering as applied to dynamic systems. These sensors give us insight as to how an object is moving in space by providing data relating to orientation and acceleration of said system. These data points are created by electronically interpreting signals generated by micro-electromechanical system (MEMS). Modern smartphones have built in IMU's that are not only accurate [32], but also easy to interface with due to the open source nature of the Android operating system [33].

Generally Smartphones contain the following sensors:

- Accelerometer
- Gyroscope

- Magnetometer
- Barometer
- Temperature

**Accelerometers** provide linear acceleration data; these accelerations may be constant (eg. gravity) or changing (eg. relative motion). In smartphones they are usually based on MEMS that use various mechanical phenomena to determine motion.

**Gyroscopes** provide rotational data of the sensor relative to the inertial frame. These sensors generate angular velocity data by using .

**Magnetometers** provide information relating to the macroscopic magnetic fields in a certain area. These sensors can measure the direction, strength, or relative change of fields in three different dimensions relative to the smartphone.

**Barometers** are finely tuned atmospheric pressure sensors that can determine pressure an object is experiencing. By combining this pressure data with a well defined map of different pressure the the relative height with respect to sea-level can be calculated.

**Temperature** sensors generate local temperature data of the surrounding environment. They are important in smartphones that use lithium ion or lithium polymer batteries that can explode at high temperatures.

These sensors can be used together to better model the position, velocity and acceleration of a modern smartphone. This is easily seen when a smartphone rotates the display when held in landscape.

### 2.4.1 Global Position System

GPS (Global Position System) is a space based navigational system that uses satellites to determine a receivers absolute position on earth. This system was developed by the United States Air Force ion 1973 and made available for public use in the 1980s. It has since been improved by the addition of satellites.

### 2.4.2 Inertial Measurement Units in Robotics

IMUs are integral in the functioning of robotics. Up until very recently intelligent robotic systems had no sense of vision to provide feedback for their internal control systems.

Instead this feedback was generated by various sensors providing information about the dynamics of these systems. [15] showed the importance of feedback to control bipedal robotic lower limbs. This feedback is achieved with different electronics components including gyroscopes and accelerometers; they are preferred above potentiometers since they do not mechanically intrude on the system.

Another common application for sensors in robots is for the use of navigation. By using accurate IMU's mounted to the body of drones etc pose estimation can be used to control movement.

### **2.4.3 Human Motion Analysis Using Sensors**

Picerno completed an extensive review of motion sensor based data capture for human motion in [11].

Some new methods using interesting sensors have been developed to log human motion. [34] showed that by using highly sensitive strain sensors positioned on various joints the movement of such points of interest could be quantified. Another exotic method is the use of soft carbon nanotube capacitive sensors as in [35]. These sensors are flexible and non intrusive allowing comfortable data capture.

A low cost approach in the form of a smartphone and wrist mounted sensors was used by [36] to show alternative methods to interpret human arms movements. Finally software developments by [37] has allowed for more accurate simulations to be produced using inertial sensors. These papers are recent and shows that modern technologies and approaches to capturing motion data are being developed.

## **2.5 Mathematical Modelling**

The binding element presented in this work is the underlying mathematics. Using various mathematical tools and methods known to robotics and bio-mechanics it is possible to transform various data types in various frames of reference to a singular model.

### **2.5.1 Mathematical Models of the Gait**

Before exploring complex methods and tools used to analyze the human gait, it is important to select and understand the model they are derived from. Due to the large

amount of existing research related to the human gait some models have been well established. These models are capable of quantifying important elements of the human gait such as gait period, dynamic joint forces and neuromuscular control.

Some fundamental work complete by Zajac, Neptune and Winters will be discussed to better understand existing models.

In work completed by Zajac et al. [38] it is interesting to note the how modelling difficulties are compared to that seen in bipedal robotics. In this work he also places some important bounds on human joints. He argues that the maximum DOF (Degrees of Freedom) that any single joint can have is 6; 3 for translation and 3 for rotation. He also constrains body segments as rigid and that the internal happenings of a body segment is insignificant.

In further papers published by these authors [39] and [40] various dynamic simulations are tested against proposed methods and subject studies. These papers confirm the multi rigid segment model for studying human dynamics. Since this study is only concerned with the kinetics the assumption can be made that the model is adequate in kinematic analysis.

### 2.5.2 Linear Kinematics

By using kinematics we can quantify and understand the movement of the lower limbs. Kinematics is a branch of mechanics that fully defines the motion of a point with respect to position, velocity and acceleration (be it linear, rotational or a combination). Kinematics does not however describe the forces, torques or other variables that may affect that point. This is due to a fundamental assumption in kinematics that the point is massless.

Kinematics can be broken up into 2 main branches: *forward* and *inverse*. To illustrate the matter the following diagram is that of a basic kinematic model.

In this figure the position of point P is defined by 2 lengths, L1 and L2 with different lengths and angles from a set of shared axis. In forward kinematics we can find P if we know the angles and lengths of the different links in the system. The motion of point P can then be described by looking at how the angles and lengths of the links in the system change over time.

Inverse kinematics uses knowledge of different points in the system, such as the origin and P and the lengths of the links in the system to determine the angular offsets of each length. Since these produce a set of linear equations, the more unknowns we are faced with the more possible solutions we can generate.

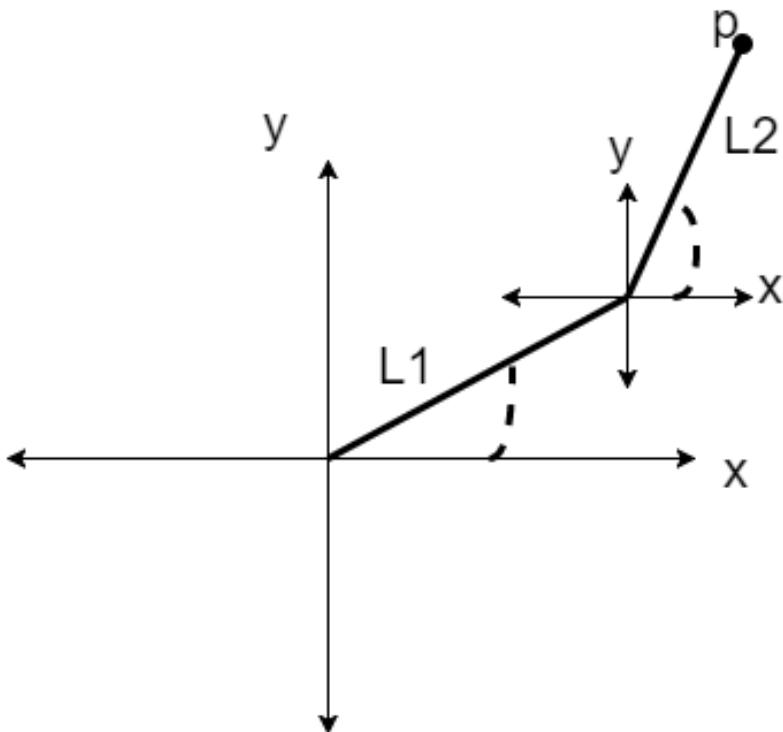


Figure 2.5: Basic kinematic model to demonstrate

As discussed in the previous section a common method of modelling the human lower limbs is to use a collection of rigid beams.

### 2.5.3 Rotational Matrices

There is an underlying difficulty in mathematically fusing various data sources and models; that of finding a common frame of reference. With the intent of using Lagrangian mechanics good definitions for the different frames are critical. This thesis will primarily use 2 different frames of reference. The inertial frame and the body frame.

The inertial frame (or world frame) can be defined in different ways as seen in [41], for the purpose of this study the NED (North East Down) definition is used. This configuration is also known as the local tangent plain and is often used in aviation.

Rotational matrices are mathematical objects that rotate vectors in three dimensional space. Since most engineering is constrained to the physical three dimensional world these matrices commonly rotate 3 dimensional vectors with a 3x3 sized matrix.

#### 2.5.4 Kalman Filter and Extended Kalman Filter

The Kalman filter is a mathematical tool used to estimate the states of a system. All measurements contain some unwanted elements of noise that produce uncertainty. Another source of uncertainty is the imprecision in the model. Simplifying assumptions disregard the minute details that when summed can have an effect on the interpretation of the data. To minimize these uncertainties it is important to filter the datasets correctly. Fortunately, estimation can be used as a form of filtering to reduce the impact of these uncertainties.

Another powerful element of the Kalman filter is its ability to fuse data from different sources to compute a more holistic picture of the underlying system. Fusion allows us to interpret sensor data within constraints of other sensors, creating a more accurate dataset. For example we can negate the drift of an accelerometer if we have absolute positional data provided by a GPS.

There is also an important distinction to be made between the KF and the EKF. To briefly explain this it should be understood that the Kalman filter was the original concept as developed by Rudolf E. Klmn and he EKF the extension of said work. The KF has an inherent limitation that it can only be applied to linear systems, whereas the EKF can be applied to non-linear system operating within a certain defined range.

The KF itself can be broken down into 2 fundamental stages of operation; a prediction stage and update stage. The prediction stage takes the known current states of the system and estimates what the measurements should be for the next time interval. The measurement stage takes in current measurements and mathematically determines the states. The states of the system are user defined parameters that can often not be directly measured.

### 2.6 Natural Solutions for Robotic Shortcomings

Naturally the question arises: why would we want to better understand the dynamics of animals? A persistent problem in the field of modern robotics is that of mobility; robots struggle to navigate real world surfaces and obstacles. Work by Patel et al. [42] shows how we can look towards nature for inspiration to solve this mobility problem.

As demonstrated by various prototype robots built by Boston Dynamics bipedal robots are severely limited in manoeuvrability when compared to animals. This is due to the

longest iterative design process known to man, evolution. Pictured below is a collection of bio-inspired robots build by Boston Dynamics.



Figure 2.6: Different bipedal and quadroped robots created by Boston Dynamics, image from [43]

## 2.7 Conclusion

This chapter has shown the direct parallels of technologies related to gate capture to dynamic robotic systems. With these strong parallels in mind the transferability of these systems from humans to humanoid robots is clear. In the same manner we are able to take a bio-mechanical look at the human body and treat it as a dynamics mechanical system instead of the complex bio-chemical and physiological system it really is.

This technique of abstracting systems to different domains of knowledge allows us to apply engineering methods and design to complex problem spaces. As mechanical engineers have used resistive networks to understand thermodynamics [44] and control engineers have used mechanical models and electrical models interchangeably to apply control principles [45], there is power in this methodology. Fusing different methods from different fields has proven its usefulness and this work will use this approach of horizontal thinking to create its own unique methodology.

As discussed in this chapter the importance of understanding the human gait cannot be understated. The recent breakthroughs in computer vision and neural networks has reignited a field that has potential to truly change our day to day life. The ever increasing ability of sensors technology and data capture systems allow us to quantify what we have never been able to and the underlying fundamental mathematical methods never seem to fall short.

The future of humanoid robotics sits at the overlap of computer vision, IMUs and biomimicry; add to this some form of general intelligence and the world reaches a stage of automation and transformation only imagined by authors such as Asimov and Wiener. Perhaps this work could contribute to that future.

# Chapter 3

## Methodology

To ensure the success of this project a basic plan of action was created. The following diagram shows the critical phases of the project, as interpreted from the terms of reference.

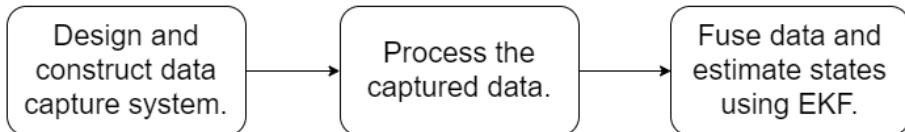


Figure 3.1: Diagram showing the progression and dependence of the major stages of this project

Due to the availability of equipment, financial limitations and time constraints various design parameters were predetermined. These known elements were central to the design process.

### 3.1 System Design

This section is dedicated to defining and understanding the specifications of the data capture system. The system itself is novel as no existing literature could be found relating to wearable motion capture systems (using cameras) for bipeds at the time of writing.

Work completed by Stocks [7] was therefore used as a starting point for the design process. The system was adapted to use 4 cameras and an IMU mounted to the torso of the subject.

The cameras will record the lower limbs of the subject while the IMU will log inertial data from the body of the subject. The video data from the cameras will provide information about the kinematics of the lower limbs with respect to the cameras while the IMU will

provide motion data of the body with respect to the inertial frame. As discussed in the previous chapter the inertial frame and the world frame are equivalent in this project.

The following equipment was provided by the Mechatronics Lab and was chosen as the main components to use in the system:

Item	Selected Equipment	From
Camera	4 GoPro Hero Session Cameras	[46]
IMU	1 Sony Xperia Z3 Compact	[47]
Chest Mount	1 Action Mount Chest Mount	[48]

Table 3.1: Known design elements of the project

The specifications of this data capture system has been defined as:

- 2 stereo housings to hold the cameras
- Chest mount to hold the cameras and IMU
- Connecting hardware to mount camera housing to the chest harness.
- Cameras must be stable during running
- IMU must be rigidly mounted to front cameras
- Cameras must capture full lower limb motion
- Harness must be comfortable during running.
- Harness must not impede natural gait of subject
- Harness must be as light as possible
- Harness must fit different size torsos
- System must be remote controlled as far as possible

These specifications ensure a system that can be used by a large demographic of people. This allows the system to be used in a variety of applications from engineering to medical science.

## 3.2 Modelling the Lower Limbs

To interpret the data and the underlying mathematics a model of the human torso and lower limbs must be created. This model consist of the lower limbs being represented as rigid links. Each leg is comprised of three different links: a thigh, calf and foot. The joints connecting the links have limited degrees of freedom to simplify the model. The ankle (serving as the joint between the foot and calf) is assumed to have a single rotational degree of freedom (pitch). The knee (serving as a joint between the calf and the thigh) has also been limited to only have a pitch element. Finally the hip (joining the thigh to the body) has been given 2 rotational degrees of freedom: pitch and yaw. This rigid model can be seen in the following figure.

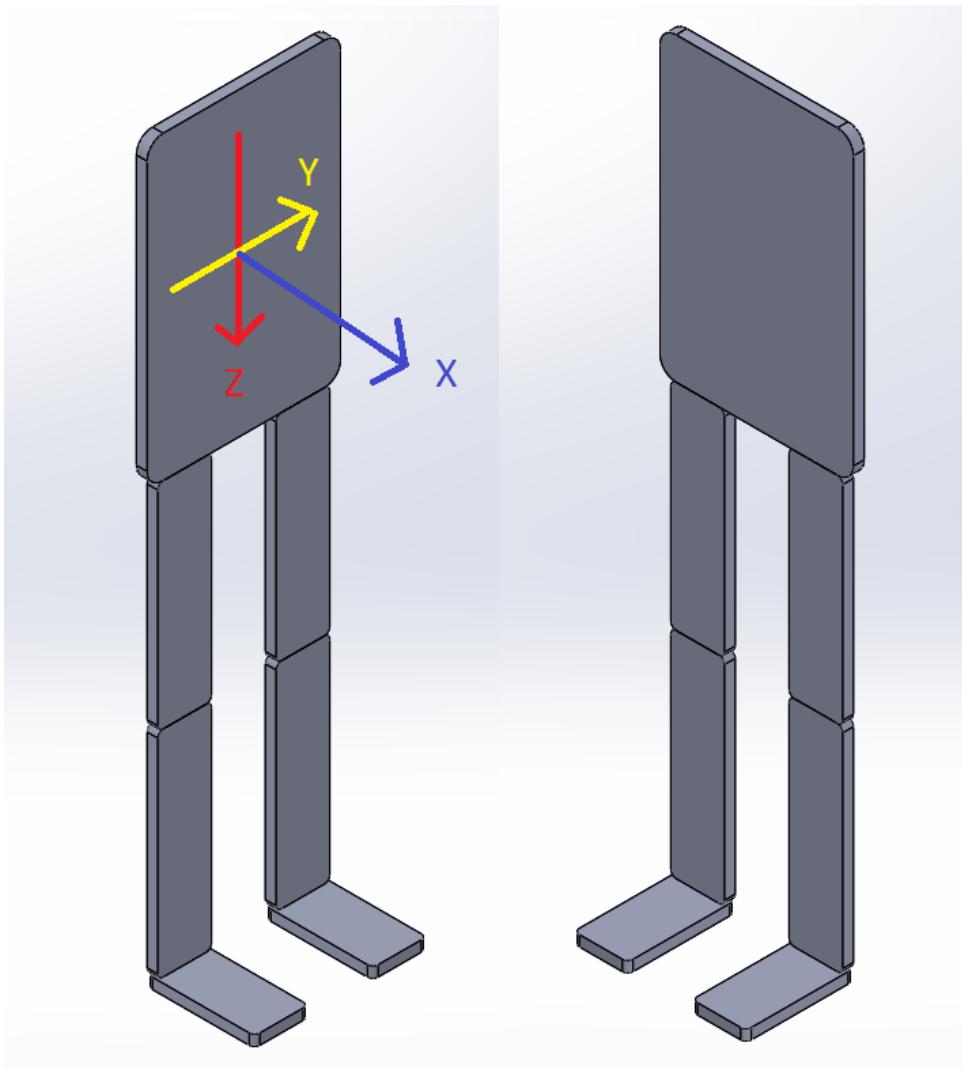


Figure 3.2: Rigid beam model used to model the lower limbs of a biped

A very important benefit to using such a model it the transferability to a robotic implementation of the lower limbs. Often robot joints are implemented using a variety of DC machines or

servomotors. by limiting the freedom of various joints we simplify the joints and reduce the amount of servomotors required to mimic the model. This allows for both cheaper and less complex bipedal robotic limbs to be constructed.

### 3.3 Experimental Details

The data was captured during a short straight road run where the runner started from a standing position and accelerated to a steady state running pace. This allowed us to capture some transients (accelerations) from the run that can be used to initialize the proposed EKF. The run lasted about 18 seconds providing us with 1800 datapoints. Test was performed 3 times and a final dataset was chosen after examining the data gathered.

### 3.4 Limitations

The scope of this research does not include runs over rough terrain as this is the logical next step after flat ground steady state running is modelled and estimated correctly. It is assumed that given robust EKF and complete image processing solution the system would be transferable for running on various terrains.

This research will also not analyse the running style, efficiency or balance of the subjects, since this thesis concerned with the engineering involved in creating a novel data capture system.

Another source of limitations is the nature of the rigid beam model. This non elastic model does not take in to account the slight compression and expansion of the limbs during running. The model also omits yaw and roll parameters about the knee and ankle as well as roll parameters about the hip; reducing the overall completeness of the model for the sake of simplicity. Finally the model assumes a rigid stationary chest that introduces some error relating the camera data.

In steady state running the chest will rotate opposite to the hips to balance the angular momentum of the runner. Since the chest swings at a rate proportional to the gait period this could be modelled as a harmonic oscillator. This idea was explored in [6] where the cheetah spine was partly modelled in this fashion with positive results. It would also be possible to interpret the rotational rates of the chest from the IMU data.

Various limitations are inherent in this project due to its novelty. These limitations

have been noted such that future work could improve upon certain elements while this foundational work serves as a point of reference.

# Chapter 4

## Designing the Data Capture System

To obtain data for the Extended Kalman Filter, a data-capture system needed to be designed. Since the data sources have been identified as multiple video streams and a 9 Degrees of freedom IMU (accelerometer, gyroscope and magnetometer) the design was centred around the following equipment. The following specifications are highly modular as any camera source and any IMU with sufficient data capture rate would suffice.

### 4.1 GoPro Hero Session Camera

Due to the availability of GoPro Hero Session cameras the wearable motion capture system was designed with these in mind. These cameras only take up a volume of  $250cm^3$  and have a square housing measuring  $6.3cm$  on all sides. The following figure presents a 3D rendered model of the camera.

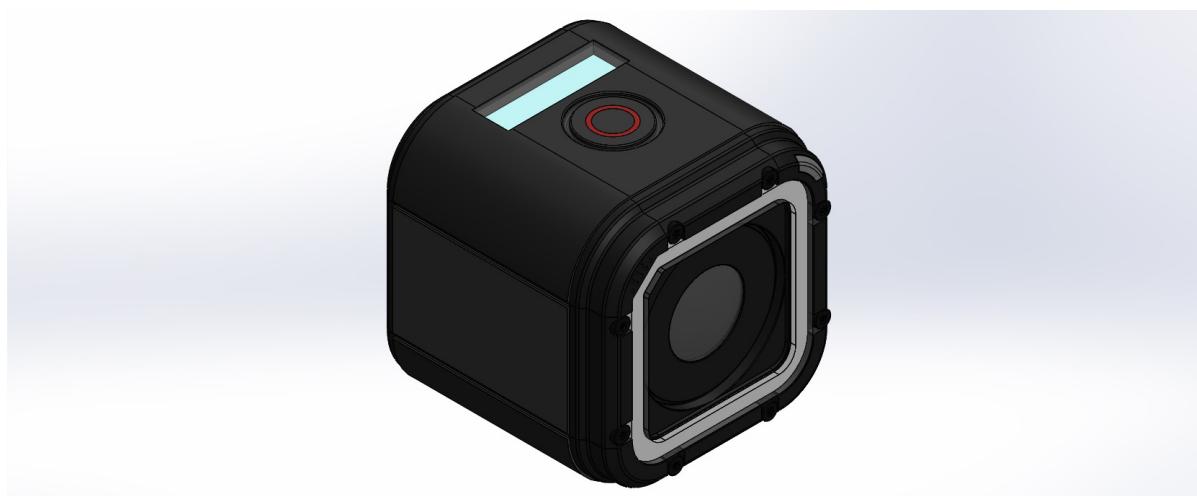


Figure 4.1: 3D CAD rendering of the GoPro Hero Session action camera

The camera can capture videos at a variety of frame rates and a variety of resolutions. These settings are limited as the software that controls the camera is proprietary. These set frame rates and resolutions are presented in the table below.

Resolution	Frame Rates
1920 x 1440	30 fps, 25 fps
1920 x 1080	60 fps, 50 fps, 48 fps, 30 fps, 25 fps
1280 x 960	60 fps, 50 fps, 30 fps, 25 fps
1280 x 720	100 fps, 60 fps, 50 fps, 30 fps, 25 fps
848 x 480	120 fps, 100 fps

Table 4.1: Possible frame rate and resolution combinations on the GPHS camera

The relative motion of the lower limbs appeared to move rapidly and therefore the highest possible frame rate with the best resolution was chosen. The camera was configured to record at 100Hz and at a resolution of 1280 x 720 pixels. This was chosen as the quality of the 848 x 480 video was simply too low to identify the marker centres with computer algorithms.

The camera also has the ability to record using a normal lens or a wide angle lens. The field of view of the camera greatly increases with the wide angle lens but its focal length decreases proportionally. The wide lens also produces more distortion when compared to the normal lens. Due to the relatively narrow area of capture needed the camera was configured to use the normal lens as it would decrease distortion without compromising the area of interest.

Of course working with proprietary hardware there are some difficulties. One of these difficulties is created by the GoPro camera regulating its exposure automatically. In darker environments the GoPro will automatically change to low light mode, causing inconsistent light levels in videos taken in different conditions. This introduces difficulties when trying to use feature detection since the varying light levels change the relative colors of the markers.

Another difficulty is the output video files generated by the GoPro. These files have a .MP4 file extension implying that they have already been compressed. This compression causes a loss of precision opposed to the raw video data being recorded. Compression has been implemented to save memory on the GoPro's micro SD memory card. Decompressing this video data will be discussed in the following chapter.

## 4.2 Camera Mount Design

Some initial work on modelling a housing for the camera was completed by the Mechatronics Lab. This was a 2 part 3D printable enclosure with no mounting points or control access. This enclosure is pictured below.

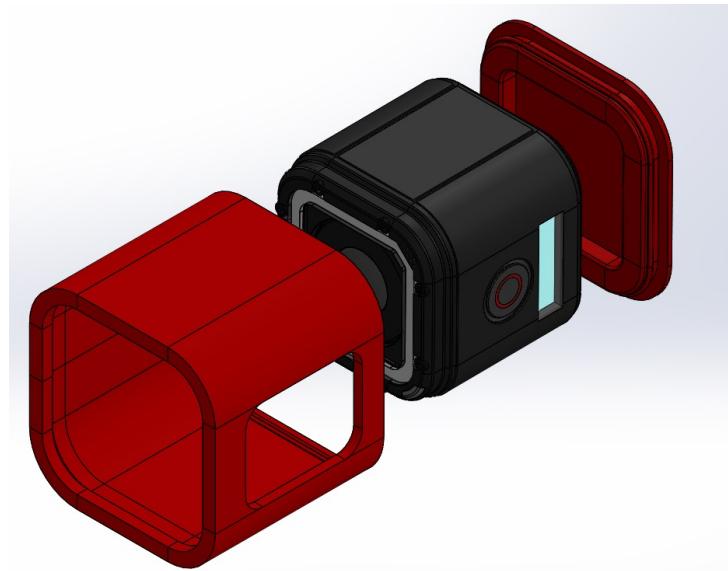


Figure 4.2: Initial camera enclosure designed by the mechatronics lab

This model was heavily modified using Dassault Systems SOLIDWORKS software to enclose 2 cameras mounted side by side. The bracket also needed a mounting point to join to the chest mount. Finally the bracket needed to be lightweight, provide access to the camera controls and not obscure the built in status screen of the cameras. The following figure shows the final dual camera bracket that was 3D printed. This bracket can be found on the accompanying CD.

This bracket was mounted to the Action Mounts Chest mount. One bracket was mounted to the front of the chest mount and using the included GoPro mounting pads the chest harness was modified to carry a bracket on the back plate as well. The back plate of the Chest Harness was relatively small and when examining the footage taken during test runs the rear camera pair was found to be very unstable. The following diagram shows the chest harness.

The need to increase the stability without hindering wearability introduced a new specification to be incorporated into the design process. The part had to comfortably fit to the back of a runner while providing a larger surface area for the camera to mount too. The part shown in the following figure was created and tested to fulfil this specification.

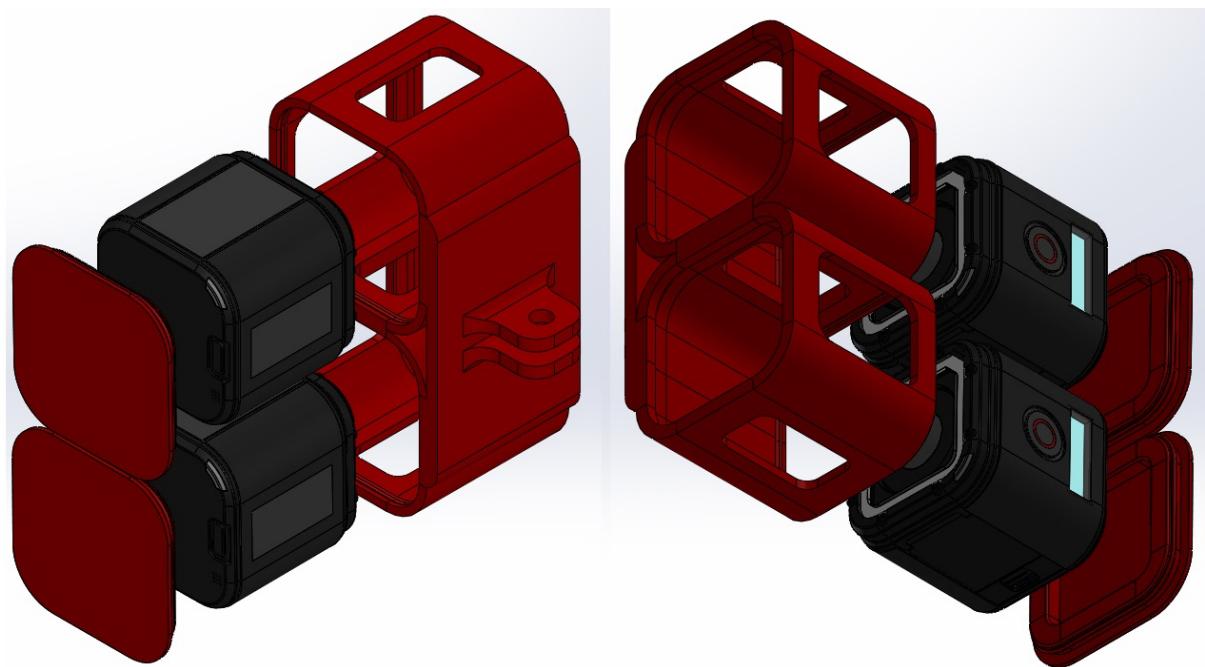


Figure 4.3: Final dual camera enclosure designed by the author



Figure 4.4: Action Mounts chest mount showing the front mounting plate

### 4.3 Smartphone Mount Design

The final design specification was to rigidly mount the smart phone to the chest of the subject

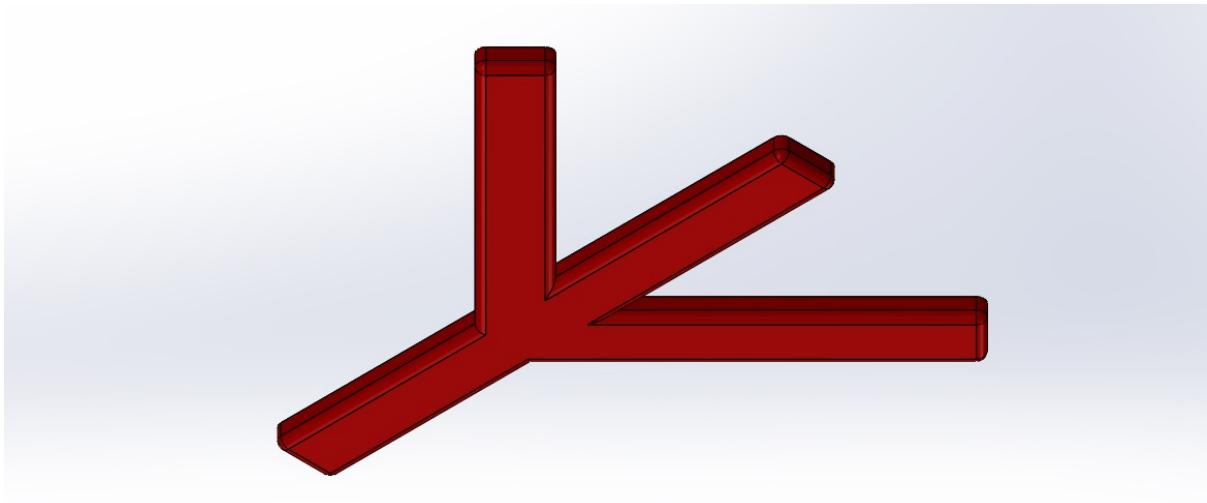


Figure 4.5: stabilizer

## 4.4 Vision Calibration

Before calibrating the stereo cameras and their singular quantifications it is important to take a step back and determine the camera matrix for each individual camera. This allows us to model the cameras mathematically and individually. This will allow us to accurately model elements such as lens distortion, principal ray offset and uncertainties accurately. The pinhole camera model is used to quantify camera parameters. In this model each point of

In order to obtain accurate positional information from the video cameras calibration was performed. MATLAB has a built in stereo camera calibration application that can calibrate a set of cameras and create an object containing all the essential parameters, including the individual camera intrinsics.

To calibrate the cameras pictures of a white and black chequerboard is fed in to the calibration application that then mathematically determines the camera parameters. In order to make this process more efficient a video of the the moving chequerboard was taken and various frames of importance extracted using a simple MATLAB script.

## 4.5 Smartphone Calibration

### 4.5.1 Accelerometer

Using the Smartphone IMU comes with several advantages and disadvantages. The phone sensors are calibrated inhouse during production of most smart phones, but as with all accelerometers the element of sensor drift is inescapable. Due to the physical nature of smartphone accelerometers there will be a drifting bias. This is usually influenced by the temperature of the of the smartphone.

An easy way to quantify and eliminate this drift is to use a stationary logging test. With the smartphone body being stationary data we would expect the only acceleration to be measured that of gravity, yet when the experiment is performed we can see non zero acceleration artefacts after the gravitational acceleration has been accounted for.

### 4.5.2 Gyroscope

Although the above mentioned inaccuracies are also present in the gyroscope, they are treated differently. This is mainly due to the fact that a gyroscope measure a rate of change whereas an accelerometer measure the rate of change of the rate of change.

Naturally...

## 4.6 Critical Point Markers

To increase the accuracy of the image processing elements of this methodology various colourful markers were used to identify critical points on the subjects lower extremities. The following picture shows the location of the markers.

From the image we can see that green markers were used to identify the toe edge of the runner in the front camera frame and pinks marker to identify the end of the thigh in the same frame. In the rear mounted camera frame pink markers were used to identify the heel of the subject and green markers to identify the centre of the calf. These markers in conjunction with the model is used to identify the lower limb orientation during the fusion stage.

These luminous green and pink markers were chosen because they are bright in most



Figure 4.6: Subject wearing Green and Pink Markers to identify critical points

lighting conditions and offer a stark contrast to both the subjects clothing and skin colour. They also contrast a typical black tar road surface where the runs were performed. This contrast makes them easy to detect using feature detection as they cause a spike in the color decomposition of the image.

# Chapter 5

## Processing the Captured Data

This chapter is dedicated to the process of extracting critical data from the video files and IMU .csv file. This process will take the raw captured data and transform it to quantified values that we can feed the Extended Kalman Filter.

### 5.1 Processing the IMU Data

The following flowcharts depicts the procedural processing of IMU data gathered from the chest mounted smartphone running the AndroSensor application. The following flow diagram shows the different steps in preprocessing.

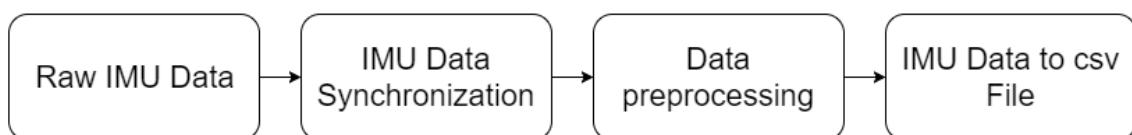


Figure 5.1: Diagram showing the progression and dependence of the major stages of video processing in the project

From the diagram we can see that our input is a large unprocessed dataset captured by the Smartphnone and logged at 100Hz. From this critical data must be extracted and synchronized with the rest of the system. The data must also undergo pre processing to simplify the implementation of the EKF.

### 5.1.1 Obtaining IMU Data

To use the smartphone as an IMU a free application "AndroSensor" [49] was installed. This application could log different parameters from all the different sensors that the smartphone contains. The application also gives the user the ability to change the output data file, log rate and what sensors are logged.

The sampling rate and logging rate of the application was configured to 100Hz as this was the maximum.

The following image is a screen shot taken from within the AndroSensor application. It shows the main screen of the application and the ability to see live plots of the active sensors.

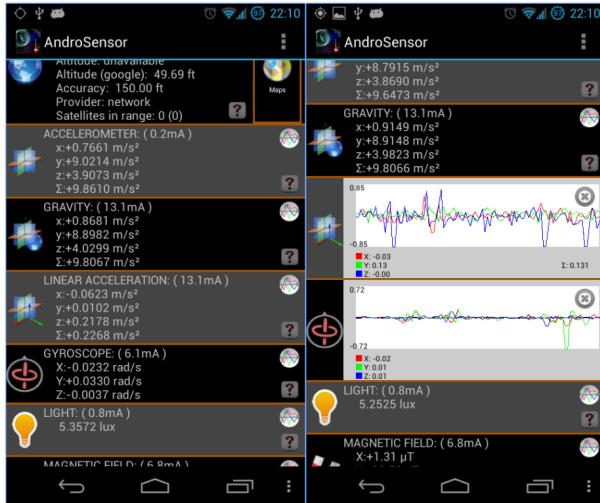


Figure 5.2: Androsensor Screenshots from [49]

The IMU data logged by the smartphone was saved as a .csv file with the first row containing the headings of various variables. These headings are summarized in the table below.

All these variables have been recorded with respect the smartphone frame of reference as shown below

### 5.1.2 Synchronizing IMU Data

The AndroSense application can record the magnitude of sound that the microphone is experiencing. Using this magnitude we can see at what sample the spike from the clap was recorded. This sample will be a common point between the IMU and the cameras and can thus be used to synchronize the different hardware elements.

	Fields
Heading	X,Y,Z
ACCELEROMETER	X,Y,Z
GRAVITY	X,Y,Z
LINEAR ACCELERATION	X,Y,Z
GYROSCOPE	X,Y,Z
MAGNETIC FIELD	X,Y,Z
ORIENTATION	X,Y,Z
ATMOSPHERIC PRESSURE	
LOCATION Latitude	
LOCATION Longitude	
LOCATION Speed	
LOCATION ORIENTATION	
VOLUME	

Table 5.1: This table shows the different headings of the output IMU file

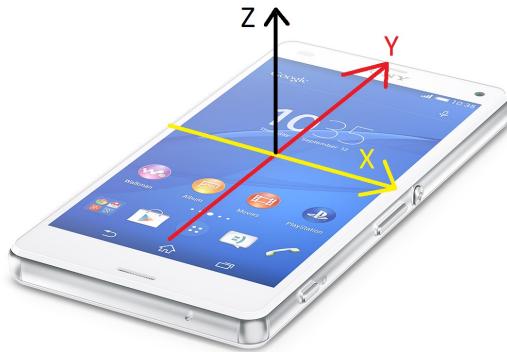


Figure 5.3: Figure demonstrating the frame of reference of the smartphone

### 5.1.3 Preprocessing IMU Data

Before we can apply the IMU data directly to the EKF we need to make some minor modifications to the data. This is critical in removing any bias from the sensors. as discussed in the Sensor calibration section.

in order to extract the linear acceleration from the data we can simply take the measure acceleration and subtract the gravitational acceleration vector

### 5.1.4 Exporting IMU Data

The IMU data was finally exported as a csv final and imported into MATLAB as different vectors. This allows for faster processing and better data processing in matlab.

## 5.2 Processing the Video Data

To once again simplify the design and implementation of the EKF it is important to pre-process the video data to a less data heavy format. The following diagram shows the process of converting a data heavy video file to a more lightweight .csv (Comma Separated Values) file whilst maintaining all critical information.

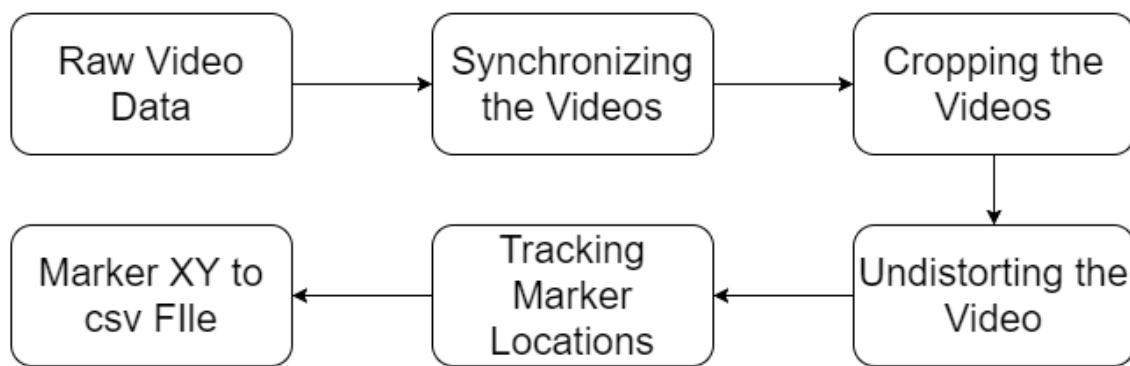


Figure 5.4: Diagram showing the progression and dependence of the major stages of video processing in the project

### 5.2.1 Obtaining Video Data

Using the chest mounted cameras detailed in the previous chapter we can generate raw video data. The GPHS cameras can be configured to record at different frame rates and resolutions as discussed in the previous chapter. The video files were stored in an .MP4 format. This meant that during recording the video was compressed and the

### 5.2.2 Synchronizing Video Sources

A typical problem faced when working with different sources of data is that of synchronization. Since this project used 4 different cameras, synchronizing the video sources are critical to generate accurate stereo vision data.

The problem of synchronization was overcome by using an audio cue to align the video data post capturing. With all systems recording, a simple hand clap can serve as a spiking audio input easily identified in the audio track of the video streams. The frame associated with this audio spike can be identified using SVP (Sony Vegas Pro) video editing software as shown in the figure below.

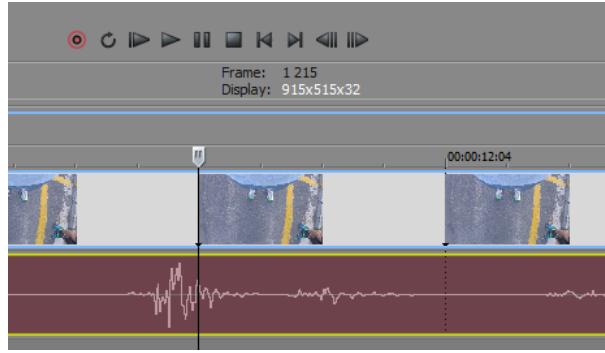


Figure 5.5: Figure showing the user interface of SVP video editing software

The red track in the above figure shows the recorded audio stream while the corresponding frames are displayed in the blue track above that. The cursor is aligned with the audio spike caused by the clap with the corresponding frame number displayed below the playback controls.

This method was repeated for every video stream such that a common starting point was generated.

### 5.2.3 Cutting Critical Video Data

With the video data synchronized the next step was to generate a subset of video demonstrating a transient period and steady state period of running. From accelerometer readings we can easily determine the gait cycle period of our subject; that is the amount of time taken between the same foot impacting the ground. These impacts are visible as spikes as seen in the accelerometer data.

### 5.2.4 Undistorting the Video Data

To generate accurate distances using stereo vision the video frames need to be undistorted.

Distortion of the frames is a result of the

To gain further understanding of undistorting video files [50] served as a reference. In this work Hartley describes various methods of undistorted images. These distortions are due to various lens effects.

### 5.2.5 Tracking and Exporting Marker Positions in the Frame

This section discusses the different methods of feature detection subdividing them into two main methodologies: automated and semi-automated. Each of these approaches offer advantages and disadvantages. To understand the approaches considered for this work it is important to visualize the input image data to the system. The following picture shows the various frames from all the cameras.



Figure 5.6: 4 Frames from the different cameras combined

The top row of images have been generated by the front mounted cameras and the bottom row by the rear mounted cameras. The left images were produced by the left cameras and the right images by the right cameras. From this image we can get a visual idea of the data our image processing system needs to manipulate.

Feature detection is a methodology in image processing that allows critical points of an image to be detected. This extracts an XY coordinate of the point of interest that can then be used to track the movement and position of object in the image. This methodology can be applied with frames with more than one point of interest as shown in this work. Multiple points of interest in multiple video sources does however increase the complexity of feature detection.

An initial approach of using automated detection was considered and three possible system were considered. Using a trained neural network, using an edge detection algorithm with a panning search algorithm and finally using a colour identifying algorithm paired

with a local search algorithm.

In theory a well trained **neural network** will provide the most robust and accurate system to identify features in varying lighting condition. It would also be the most accurate methodology for a system without the markers. This is due to the *understanding* developed by the neural network after sufficient training data is processed.

This however presents a key difficulty in setting up and training a neural network. The most important element of a neural network is the training data used to teach the. This training data needs to have annotated images with metadata fields to

A neural network therefore cannot generate training data and a method of generating training data needs to be considered in any case.

The second approach taken was that of **edge detection**. This method

The final approach considered and used was to **semi automatically** label critical point in the image using a toolbox created by Hedrick et al. [51]. This software allows for a semi automatic tracking of points of interest in the video frames. While this method is labour intensive it is arguably more accurate than the previously investigated methodologies. The following figure shows the functionality of the toolbox within MATLAB.

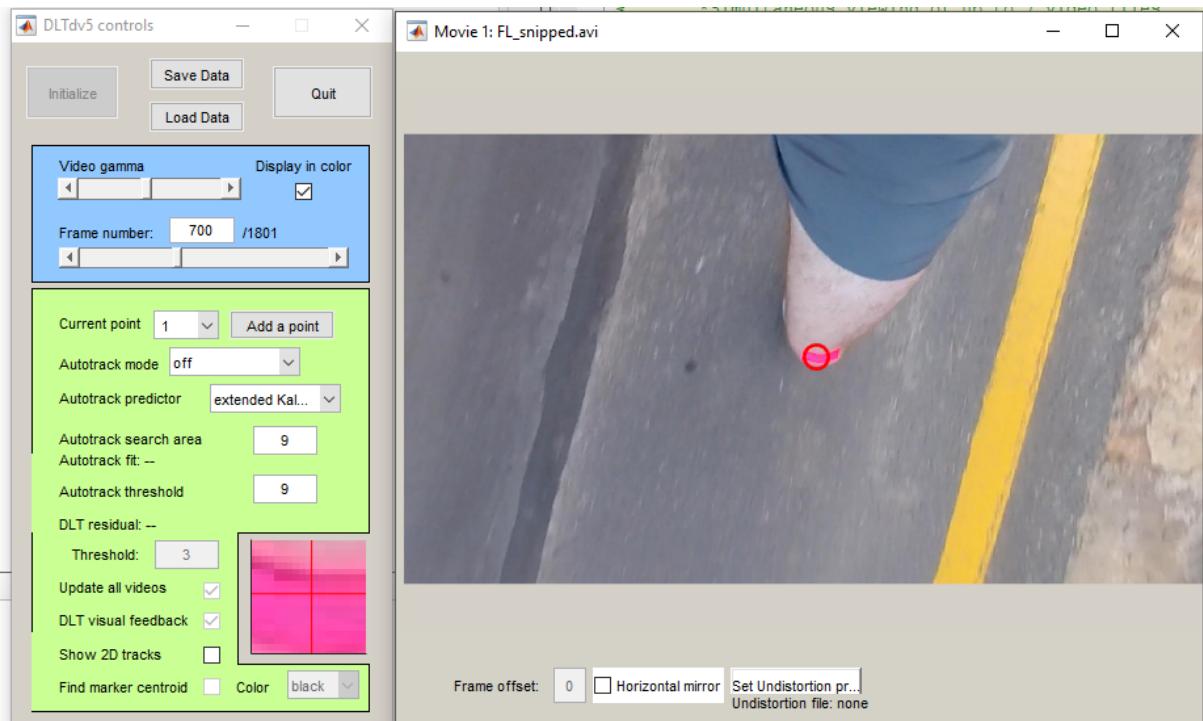


Figure 5.7: Using the dltdv toolbox in MATLAB to export marker coordinates

By using this toolbox we can generate a dataset of  $(x, y)$  pixel coordinates by identifying the different markers on each frame and assigning their corresponding points to them.

The following tables shows the markers and their corresponding point.

Front Cameras	
Point 1	Right Knee
Point 2	Left Knee
Point 3	Right Foot
Point 4	Left Foot
Rear Cameras	
Point 1	Right Calf
Point 2	Left Calf
Point 3	Right Heel
Point 4	Left Heel

Table 5.2: Table showing the relation between points and markers

### 5.3 On units

In order to assure consistency between the different sources of data considering a general set of units is of critical importance. It was decided to implement the system using SI units such that all lengths was given in meters and all angles in radians.

gyroscope was logged as radians per second,

accelerometer was logged as meters per second .

imgae data was recorded as m

### 5.4 On Frames of Reference

we need to developed some commonalities among the various sensors and their individual frames of reference. The body frame

# Chapter 6

## Data Fusion and State Estimation

This chapter is dedicated to explaining the mathematical methods and models used to fuse data generated by the cameras and IMU.

A good starting point for this chapter would be to define the states of interest of our system. These states are predicted by EKF using various measurements relating directly and indirectly to them. The following tables specifies the parameters used to symbolize the states of the system.

State	Description
$x_{body}$	x Position of body w.r.t. the inertial frame
$y_{body}$	y Position of body w.r.t. the inertial frame
$z_{body}$	z Position of body w.r.t. the inertial frame
$\phi_{body}$	Roll of body w.r.t. the inertial frame
$\theta_{body}$	Pitch of body w.r.t. the inertial frame
$\psi_{body}$	Yaw of body w.r.t. the inertial frame
$\theta_{LH}$	Pitch of left thigh w.r.t. left hip
$\psi_{LH}$	Yaw of left thigh w.r.t. left hip
$\theta_{LK}$	Pitch of left calf w.r.t. left knee
$\theta_{LA}$	Pitch of left foot w.r.t. left ankle
$\theta_{RH}$	Pitch of right thigh w.r.t. right hip
$\psi_{RH}$	Yaw of right thigh w.r.t. right hip
$\theta_{RK}$	Pitch of the right calf w.r.t. right knee
$\theta_{RA}$	Pitch of the right foot w.r.t. the right ankle

Table 6.1: Table showing the different states of the model to be determined by the EKF

Our system is not only concerned with these positional and angular elements, but also how they change over time. These rates where defined as the derivative of the states with respect to time. The first derivative serving as velocity and angular velocity, while the second derivative serving as acceleration and angular acceleration. Here the vector  $x$

serves as a element of our state vector  $X$ .

$$\mathbf{x} = [x_{body} \ y_{body} \ z_{body} \ \phi_{body} \ \theta_{body} \ \psi_{body} \ \theta_{LH} \ \psi_{LH} \ \theta_{LK} \ \theta_{LA} \ \theta_{RH} \ \psi_{RH} \ \theta_{RK} \ \theta_{RA}]$$

The vector  $x$  contains 14 elements.

$$\mathbf{X} = [\mathbf{x} \ \dot{\mathbf{x}} \ \ddot{\mathbf{x}}]$$

From this it is clear that our state vector  $X$  contains 42 elements.

## 6.1 Prediction Equations

The fundamental assumption made when deriving the prediction equations for our states was that the acceleration (both linear and angular) was constant between sampling intervals. It would therefore stand that for the positional states of the filter ( $x_{body}$   $y_{body}$   $z_{body}$ ) and the angular states ( $\theta_{body}$  ...  $\theta_{RA}$ ) could be predicted using:

$$\begin{aligned}\ddot{p}_{k+1} &= \ddot{p}_k + \sigma_{\ddot{p}}^2 \\ \dot{p}_{k+1} &= \dot{p}_k + \ddot{p}_k T + \sigma_{\dot{p}}^2 \\ p_{k+1} &= p_k + \dot{p}_k T + \sigma_p^2\end{aligned}$$

for the positional states and:

$$\begin{aligned}\ddot{\alpha}_{k+1} &= \ddot{\alpha}_k + \sigma_{\ddot{\alpha}}^2 \\ \dot{\alpha}_{k+1} &= \dot{\alpha}_k + \ddot{\alpha}_k T + \sigma_{\dot{\alpha}}^2 \\ \alpha_{k+1} &= \alpha_k + \dot{\alpha}_k T + \sigma_\alpha^2\end{aligned}$$

for the angular states.

These prediction equations where created in MATLAB using symbolic functions. The sigma associated each equations takes into account the prediction uncertainties contained in the Q matrix. By adjusting these values we can increase the filter performance. This is discussed further in a later section.

## 6.2 Measurement Equations

The measurement equations for the lower limbs were generated using inverse kinematics. This requires a model

### 6.2.1 Euler Matrices

The following matrices are the rotational matrices for rotating a point in 3D space along a certain axis.

$$Roll(\phi) = \begin{bmatrix} 1 & 0 & 0 \\ 0 & \cos \phi & -\sin \phi \\ 0 & \sin \phi & \cos \phi \end{bmatrix}$$

$$Pitch(\theta) = \begin{bmatrix} \cos \theta & 0 & \sin \theta \\ 0 & 1 & 0 \\ -\sin \theta & 0 & \cos \theta \end{bmatrix}$$

$$Yaw(\psi) = \begin{bmatrix} \cos \psi & -\sin \psi & 0 \\ \sin \psi & \cos \psi & 0 \\ 0 & 0 & 1 \end{bmatrix}$$

### 6.2.2 Direct Cosine Matrix

### 6.2.3 Inverse kinematics

front

right knee

$$p1xyz = bodyY + bodyZ + R1 * Thigh$$

left knee

$$p2xyz = bodyY + bodyZ + R1 * Thigh$$

right foot

$$p3xyz = bodyY + bodyZ + R1 * Thigh + R2 * Calf + R3 * Foot$$

left foot

$$p4xyz = bodyY + bodyZ + R1 * Thigh + R2 * Calf + R3 * Foot$$

**back**

right calf

$$p1xyz = bodyY + bodyZ + R1 * Thigh + R2 * 0.5 * Calf$$

left calf

$$p2xyz = bodyY + bodyZ + R1 * Thigh + R2 * 0.5 * Calf$$

right heel

$$p2xyz = bodyY + bodyZ + R1 * Thigh + R2 * Calf$$

left heel

$$p2xyz = bodyY + bodyZ + R1 * Thigh + R2 * Calf$$

## 6.3 Understanding the Data Sources

It is important to understand the different parameters that mathematically quantify cameras. These parameters can be divided into *extrinsic* and *intrinsic*. Extrinsic camera variables related to the cameras position in the inertial frame and the direction the camera is facing. These can be summarized by the extrinsic camera matrix

$$[R | \mathbf{t}] = \left[ \begin{array}{ccc|c} r_{1,1} & r_{1,2} & r_{1,3} & t_1 \\ r_{2,1} & r_{2,2} & r_{2,3} & t_2 \\ r_{3,1} & r_{3,2} & r_{3,3} & t_3 \end{array} \right]$$

## 6.4 State Estimation

This section will mathematically explain the Kalman filter and its implementation in this project.

Process equation of the kalam filter. from states to emasurements

$$X_{k+1} = FX_k + w_k$$

our state, contained in the vector  $X$  can be estimated by applying the process matrix  $F$  to our current known state. the term  $w$  is the noise variable that accounts for process noise.

Measurement equations from measurements to states.

$$Y_k = H_k X_k + v_k$$

$w$  will be contained int he matrix  $Q$

while  $v$  will be contained in the matrix  $R$

linearizing nonlinear system we get the EKF

## 6.5 Q Matrix, R Matrix and Initialization

This section will discuss the final components of the EKF namely the  $Q$  matrix containing the various process noise variations,  $R$  matrix containing the various measurement noise variances and the initial state values.

### 6.5.1 Defining the Q Matrix

From the above equations we can see that the  $Q$  matrix must have dimensions of  $n * n$ , where  $n$  in this equation is the total amount of states. As previously defined in this section our filter operates over 42 states, giving  $Q$  a size of  $42 * 42$ . All the variance parameters will be contained on the diagonal of the matrix with all other entries being zero.

To find the initial values for these uncertainties the the derivative of the various accelerations where taken. The maximum element from that set was selected as the uncertainty parameter.

### 6.5.2 Defining the R Matrix

The  $R$  matrix relates to the measurement variables and must therefore have size of  $m*m$ , where  $m$  is the amount of inputs the EKF. These are elements of the sensors themselves

and can be found by researching the relative data sheets for the smartphone IMU. As for the cameras a relatively large uncertainty of about 5 pixels was assumed.

### 6.5.3 Choosing Initial States

The subject was stationary during the initial stages of the run. This allows us to initialize our state vector with all states initially zero. The filter will therefore track the transience and steady state estimation of a running subject, giving insight into the filters performance under different conditions.

### 6.5.4 Initializing the Covariance Matrix P

following on from the previous section zeroing the initial states of the system allows us to have a relatively small initial covariance matrix due to the relative certainty we have that the states are truly zero.

# **Chapter 7**

## **Results, Verification and Discussion**

This chapter is dedicated to discussing the results generated and their verification.

### **7.1 Results**

The project had various critical phases that were completed. The following phases and their results have been documented below.

#### **7.1.1 System Design Results**

The data capture system was designed to meet the specifications

pictured below is a subject wearing the data capture system. The subject confirmed the comfort of the data capture system due to the

#### **7.1.2 Model Results**

The model proved sufficient

talk about how the model would also allow the sensor to be used for subjects with prosthesis and allow for better understanding of disabled persons.

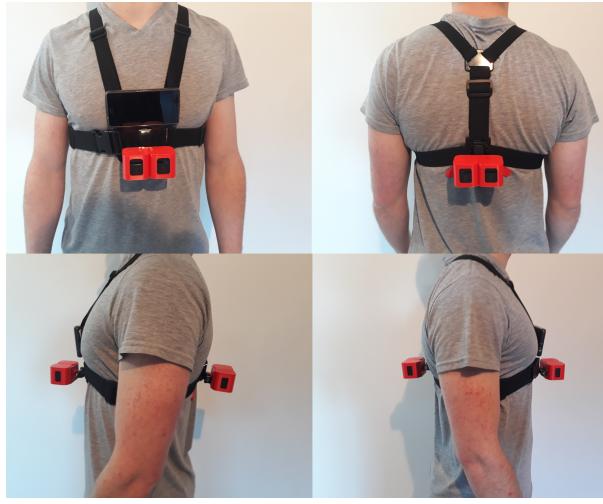


Figure 7.1: subject wearing the motion capture system

### 7.1.3 Captured and Processed Data

The following is a graph of the accelerometer in the z-body frame against time. From

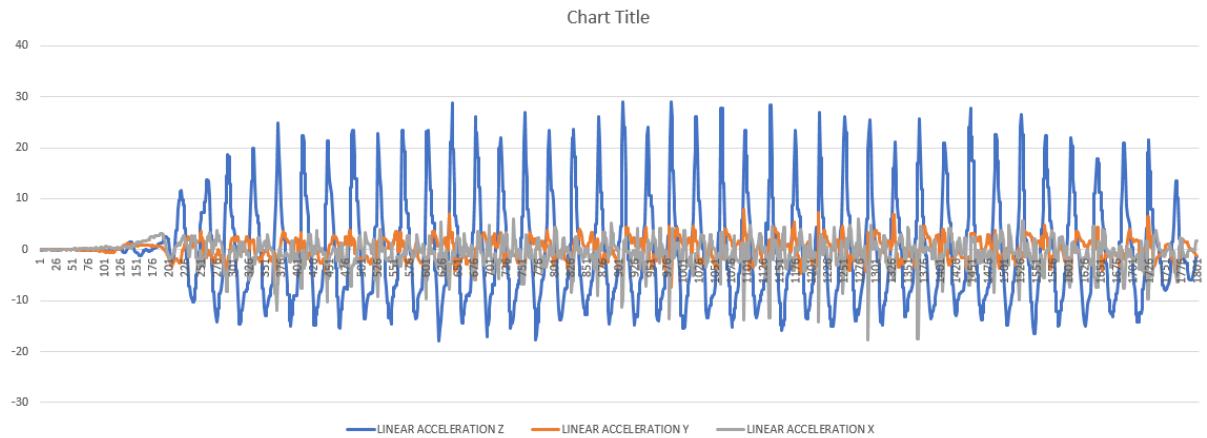


Figure 7.2

this graph it it the rythmic motion of running is easy to see. a spike of close to 4g seen at the moment of impact and a maximum acceleration of around 1 g as the subject reaches maximum height.

after image processing

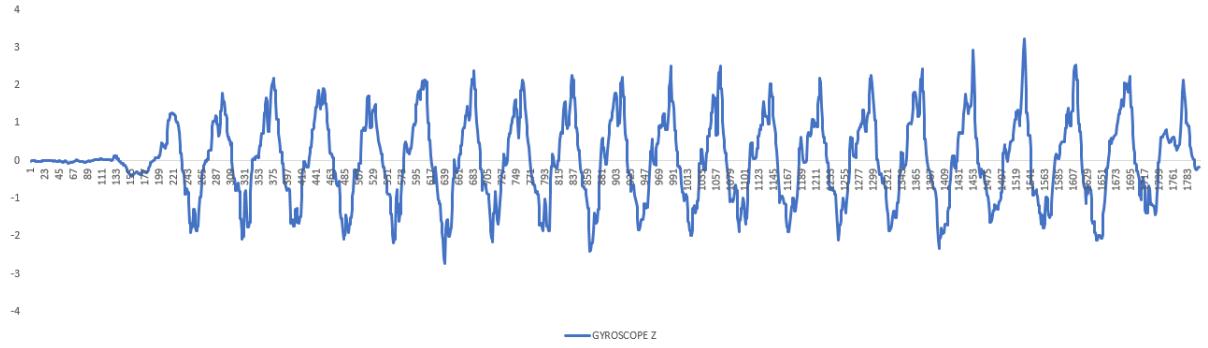


Figure 7.3

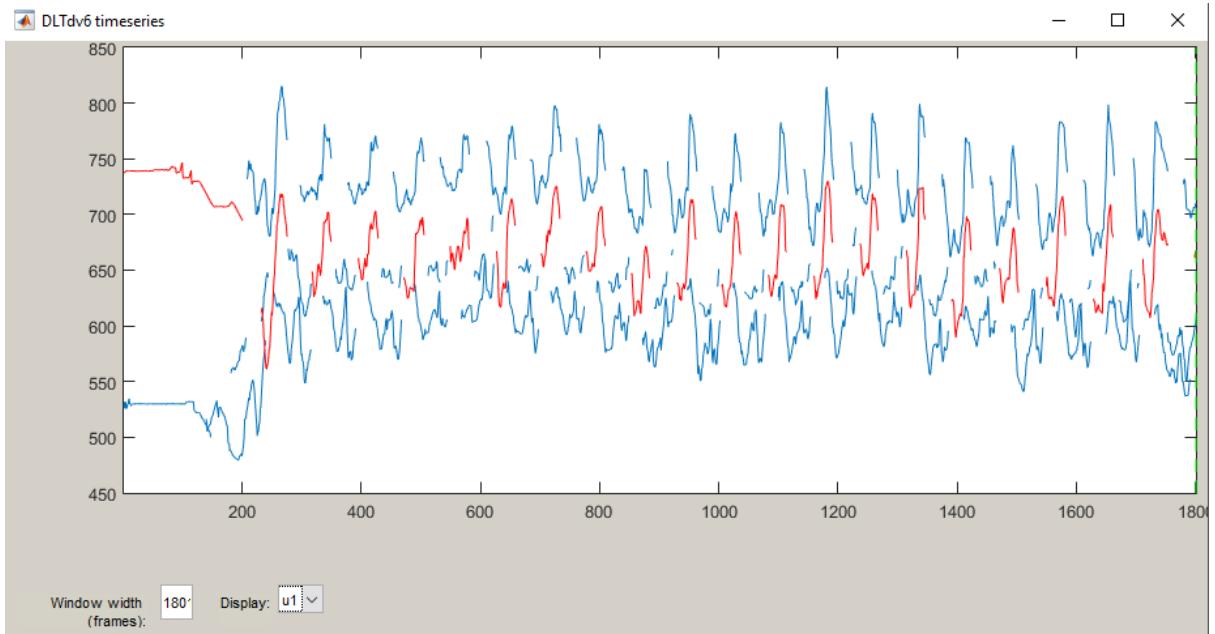


Figure 7.4: iamge processing things

#### 7.1.4 EFK Results

## 7.2 Discussion

subject borne cameras are have shown their viability.

# Chapter 8

## Conclusions and Future Work

This chapter is dedicated to drawing conclusions based on results found and make recommendation on future iterations of this project. Since the underlying methodology is quite novel this system should serve as the foundational step to a fully automated motion capture system.

### 8.1 Conclusion

The aim of this project was threefold: design a novel wearable data capture system using cameras and sensors to record various parameters of a running bipedal subject, develop a kinematic model to interpret the gathered data points, and design an estimation algorithm to process the captured data. These goals were achieved within certain constraints as discussed in the results section

Due to the relatively small dataset used in this project it serves as a proof of concept and a foundational work that can be iteratively improved.

### 8.2 Future work

The system was originally designed with four cameras due to the availability of equipment and the assumption that stereo vision would be implemented. From this a set of front and rear mounted cameras would be necessary. Originally there was an intention to reduce the total amount of cameras.

The iterative design would have followed the following mapping. Initially using 4 cameras

and an smartphone as a sensor. reducing the system to two cameras (one mounted to the back of the runner and one mounted to the chest of the runner) and a smartphone as a sensor. The next iteration would use the the smartphone camera at the front and a single camera at the back whilst using the smartphone as a sensor as well. This system greatly reduces the cost of the original design philosophy, even given that a powerful and modern smartphone would be used. The final iteration would use only the smartphone at the front as a single camera and sensor. For this method to work the estimation algorithm would need to better understand the periodic motion of the human gait and the model would need to increase in complexity.

Due to the labour intensive approach taken to image processing a further avenue for improvement is the automation of feature detection. The progression would start from the current implementation of markers and use a semi-automatic toolbox to identify critical points on the image. Next computer algorithms should be created to automate the image processing with markers. This could allow for much longer runs and larger datasets to be studied, introducing elements such as fatigue and other running modifiers. The next iterative step would be to remove the markers from the runner such that the setup time of the system is reduces. This is a difficult problem to solve using classical image processing as the variables relating to the runner and the environment are not constant. Perhaps a neural network can be trained to identify the different elements of the lower limbs.

These improvements would decrease the overall cost of the system and optimize the process substantially. This decrease in hardware does imply that the complexity of the underlying algorithms and models would increase. This trade-off can be considered for future work.

Finally the results obtained have not been verified. An experiment to verify these results was designed, where external cameras would generate three dimensional position data of the markers. This can be compared to the data generated from the EKF as applied to the wearable motion capture system.

Application for Approval of Ethics in Research (EiR) Projects  
 Faculty of Engineering and the Built Environment, University of Cape Town

## APPLICATION FORM

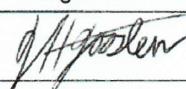
**Please Note:**

Any person planning to undertake research in the Faculty of Engineering and the Built Environment (EBE) at the University of Cape Town is required to complete this form **before** collecting or analysing data. The objective of submitting this application *prior* to embarking on research is to ensure that the highest ethical standards in research, conducted under the auspices of the EBE Faculty, are met. Please ensure that you have read, and understood the **EBE Ethics in Research Handbook**(available from the UCT EBE, Research Ethics website) prior to completing this application form: <http://www.ebe.uct.ac.za/usr/ebe/research/ethics.pdf>

<b>APPLICANT'S DETAILS</b>			
Name of principal researcher, student or external applicant		Johann Hendrik Joosten	
Department		Electrical and Electronics Engineering	
Preferred email address of applicant:		joostenhendrik@gmail.com	
If a Student	Your Degree: e.g., MSc, PhD, etc.,	B.Sc(Eng) Mechatronics	
	Name of Supervisor (if supervised):	Dr. Amir Patel	
If this is a researchcontract, indicate the source of funding/sponsorship		-	
Project Title		Modelling the Kinematics of the Human Lower-Limbs using Cameras and an IMU	

**I hereby undertake to carry out my research in such a way that:**

- there is no apparent legal objection to the nature or the method of research; and
- the research will not compromise staff or students or the other responsibilities of the University;
- the stated objective will be achieved, and the findings will have a high degree of validity;
- limitations and alternative interpretations will be considered;
- the findings could be subject to peer review and publicly available; and
- I will comply with the conventions of copyright and avoid any practice that would constitute plagiarism.

SIGNED BY	Full name	Signature	Date
Principal Researcher/ Student/External applicant	Johann Hendrik Joosten		22/08

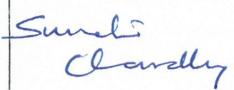
APPLICATION APPROVED BY	Full name	Signature	Date
Supervisor (where applicable)	Amir Patel		22/08/2017
HOD (or delegated nominee)  Final authority for all applicants who have answered NO to all questions in Section1; and for all Undergraduate research (Including Honours).	S. CHOWDHURY		11/10/17

Figure 8.1: ethics clearance

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